

Monte Carlo Simulation

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Lab No: **05**

Ques.1) (a)

-> Samples are being generated for $N(0,1)$ using Box-Muller and Marsgalia-Bray methods for 100 and 10000 values. The mean and variance observed :

Mean:

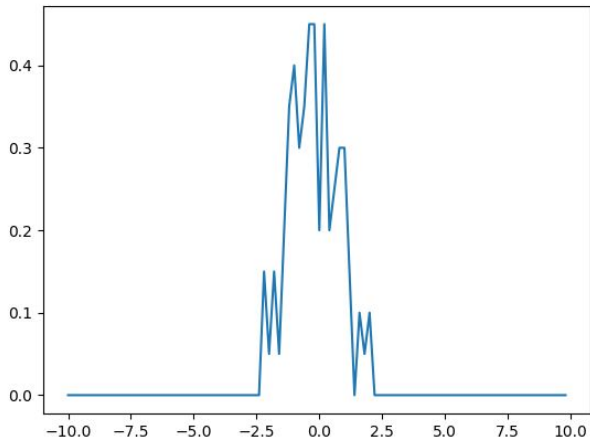
Method	100 values	10000 values
Box-Muller	-0.128	-0.013
Marsgalia-Bray	-0.036	-0.005

Variance:

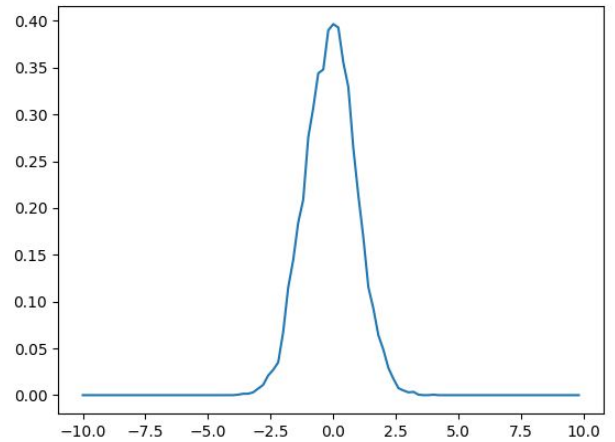
Method	100 values	10000 values
Box-Muller	0.94	1.007
Marsgalia-Bray	0.98	1.0129

Ques.1) (b)

-> For **Box-Muller**:

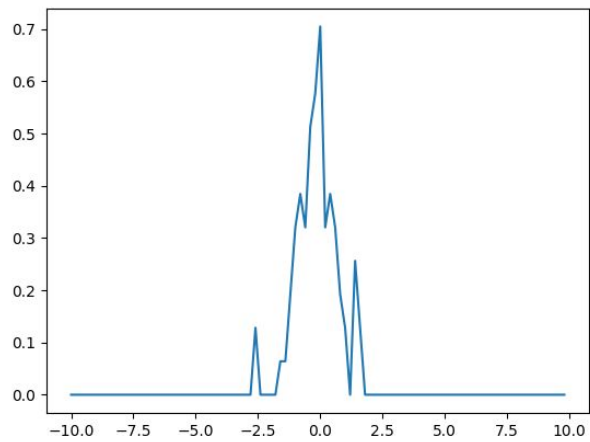


No of iterations = 100

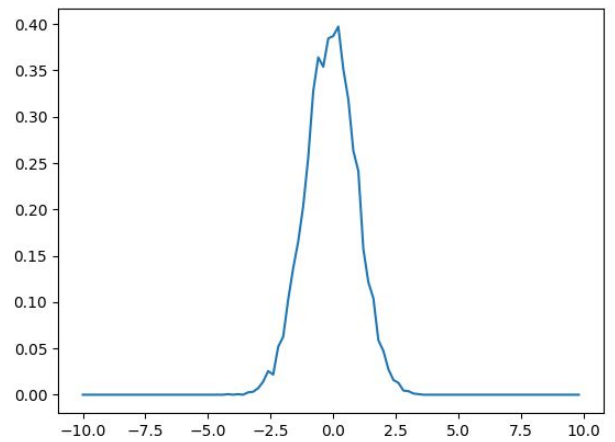


No of iterations = 10000

-> For **Marsaglia-Bray**:



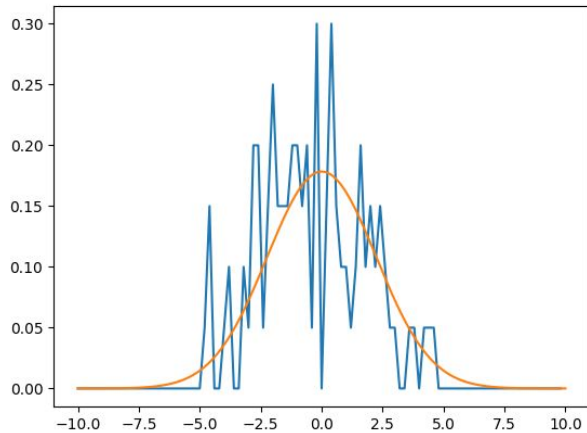
No of iterations = 100



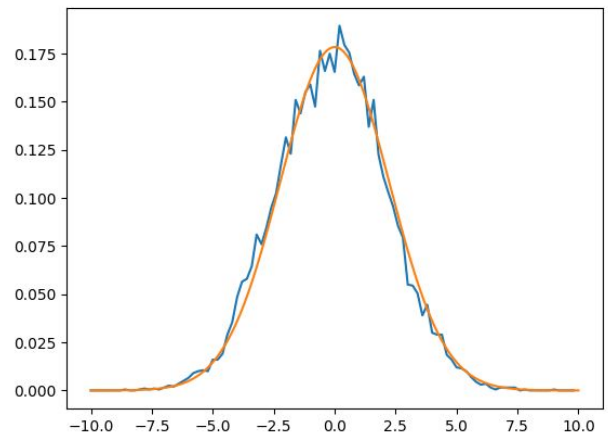
No of iterations = 10000

Ques.1) (c)

-> Box-Muller for $N(0,5)$:

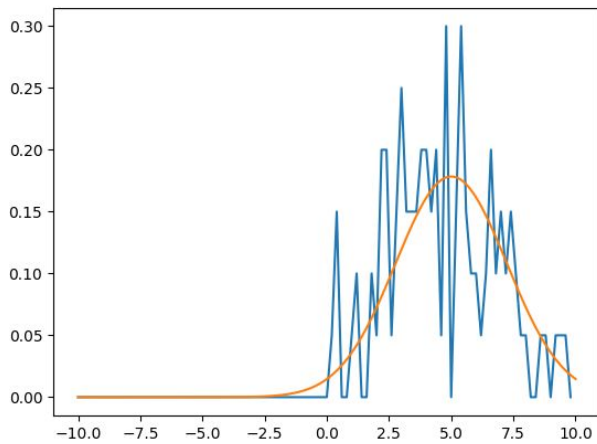


No of iterations = 100

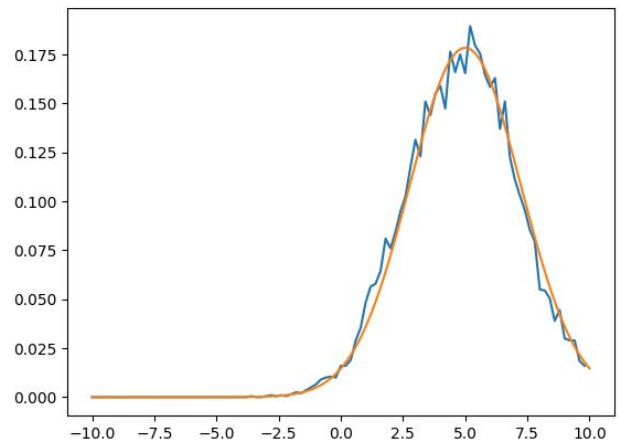


No of iterations = 10000

-> Box-Muller for $N(5,5)$:



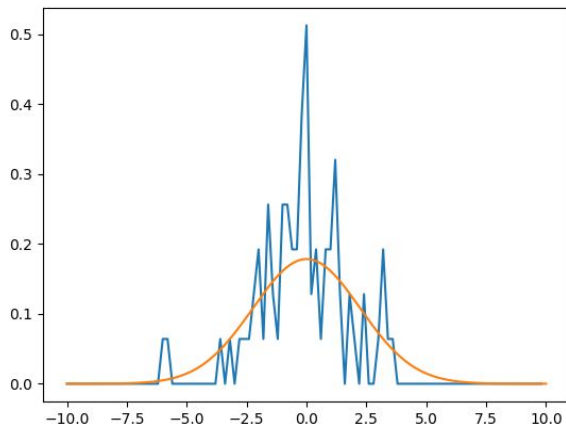
No of iterations = 100



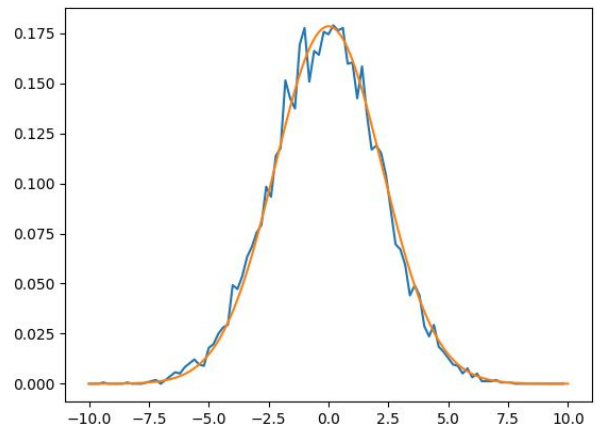
No of iterations = 10000

-> The orange lines represent the actual distribution curve according to the formula of Normal distribution and the blue lines represent the observed one.

-> Marsgalia-Bray for $N(0,5)$:

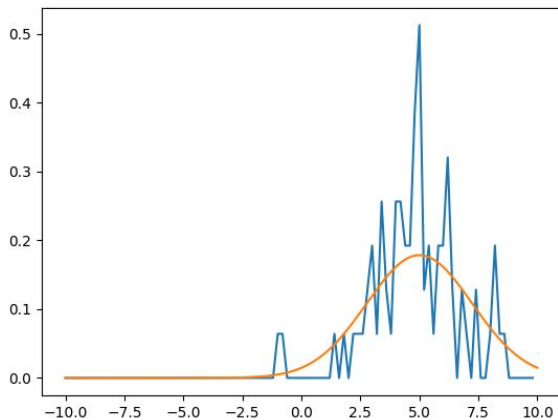


No of iterations = 100

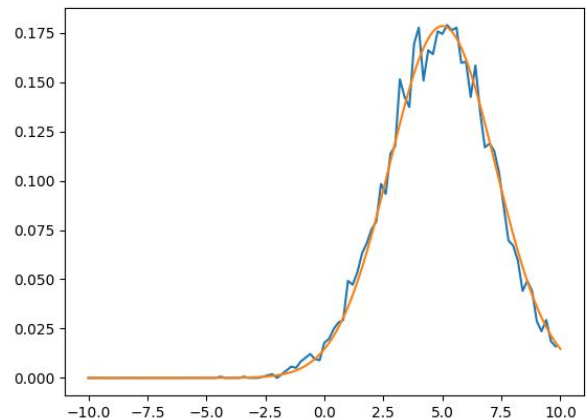


No of iterations = 10000

-> Marsgalia-Bray for $N(5,5)$:



No of iterations = 100



No of iterations = 10000

-> The orange lines represent the actual distribution curve according to the formula of Normal distribution and the blue lines represent the observed one.

-> It can be concluded from both the above methods that generated distribution converges to the actual distribution according to the formula on increasing the number of iterations in the process.

Ques.2)

-> The time of executions in the above methods are:

Method	100 values	10000 values
Box-Muller	0.000177	0.018710
Marsaglia-Bray	0.0001467	0.019892

```
naman-ubuntu@naman:~/Desktop/Monte_Lab5$ python3 180123029_NamanGoyal_a.py
Mean generated for 100 values is -0.12843280738574303
Variance generated for 100 values is 0.9363486343921261
Time of execution for 100 values is 0.0001766681671142578
Mean generated for 10000 values is -0.012292695595812704
Variance generated for 10000 values is 1.007429959144274
The time of execution for 10000 values is 0.01871013641357422
naman-ubuntu@naman:~/Desktop/Monte_Lab5$ |
```

```
naman-ubuntu@naman:~/Desktop/Monte_Lab5$ python3 180123029_NamanGoyal_b.py
Mean generated for 100 values is -0.03635027010377276
Variance generated for 100 values is 0.6845029390132865
Time of execution for 100 values is 0.00014662742614746094
Proportion of Values Rejected for 100 samples = 0.22
Mean generated for 10000 values is -0.005834580943937106
Variance generated for 10000 values is 1.0129621631803947
The time of execution for 10000 values is 0.01989269256591797
Proportion of Values Rejected for 10000 samples = 0.2174
naman-ubuntu@naman:~/Desktop/Monte_Lab5$ |
```

Ques.3)

-> From the above 2 figs., we can see that the **Proportion of Values Rejected for Marsaglia-Bray** for the 2 samples :

- 1.) For 100 values :: **0.22**
- 2.) For 10000 values :: **0.2174**

-> The values are **very close to 1 - $\pi/4 = 0.214601$.**

-> So they observed are values are **comparable** to the above-given value.
