

Output:



Input: leaf set $L = \{1, 2, 3, 4, 5\}$
Triplet set:



level One (1) $\forall x_1 \in L, x_2 \in L$ (even $x_1 = x_2$) compute $SN(\{x_1, x_2\})$

$$\boxed{x_1=1, x_2=2}$$

$$X = \{1\} \quad Z = \{2\}$$

$$\bullet z=2 \rightarrow a=1 \quad L \setminus (X \cup Z) = \{3, 4, 5\}$$

$$SN(\{1, 2\}) = \{1, 2\}$$

$$\begin{array}{c} \cancel{1 \in 2} \quad \cancel{2 \in 1} \end{array} \Rightarrow X = \{1, 2\} \quad Z = \emptyset$$

Note $SN\{x, x\} = \{x\}$ (Proof of lemma 7)

$$SN(1,1) = 1$$

$$SN(2,2) = 2$$

$$SN(3,3) = 3$$

$$SN(4,4) = 4$$

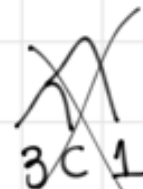
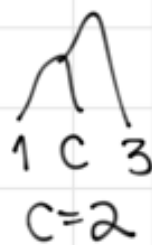
$$SN(5,5) = 5$$

$$\rightarrow SN(1,2) = \{1,2\}$$

$$\boxed{X_1=1, X_2=3}$$

$$X = \{1\} \quad Z = \{3\}$$

$$\bullet z=3 \rightarrow a=1$$



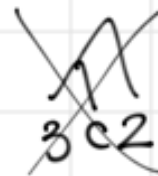
$$c=2 \Rightarrow Z = \{2,3\}$$

$$X = \{1,3\} \quad Z = \{2\}$$

$$\bullet z=2 \rightarrow a=3$$



$$a=1$$



$$\Rightarrow SN(1,3) = \{1,2,3\}$$

$$X = \{1,2,3\} \quad Z = \emptyset$$

continue ∇ SU

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level one (2) $SN = SN_{11}, SN_{22}, SN_{33}, SN_{44}, SN_{55},$
 $SN_{12}, SN_{13}, SN_{14}, SN_{15}, SN_{23},$
 $SN_{24}, SN_{25}, SN_{34}, SN_{35}, SN_{45}$
 $q=15$

not all!
 Need to be
 the set of
 "maximal SN"

- $SN(x,y) = L \Rightarrow$ trivial
- $SN(x,y)$ maximal if
 - nontrivial
 - not a proper subset of any nontrivial $SN(y_1, y_2)$

trivial
 or
 proper subset
 of a nontrivial SN \Rightarrow not maximal

levelOne(3) $\forall SN_i$; if $|SN_i| \geq 3 \Rightarrow Ni = \text{levelOne}(J|SN_i)$
 if $|SN_i| < 3 \Rightarrow Ni =$  or 