

DAA Hand On -3

function $x = f(n)$

$x = 1$

for $i = 1 : n$

for $j = 1 : n$

$x = x + 1;$

- 1) find the runtime of the algorithm mathematically
Ans let us count the number of basic operations in terms of the output size "n"

This algorithm contains nested loops

and the inner loop of the nested loop contains the operation

$x = x + 1$

↓

it is executed $n \times n$ times

$$\therefore \text{runtime } T(n) = 1 + \sum_{i=1}^n \sum_{j=1}^n 1$$

$$T(n) = 1 + \sum_{i=1}^n \left(\sum_{j=1}^n 1 \right)$$

\therefore inner summation \rightarrow Constant

$$T(n) = 1 + \sum_{i=1}^n n$$

$$= 1 + n \sum_{i=1}^n 1$$

$$\therefore \sum_{i=1}^n 1 \Rightarrow n$$

$$T(n) = 1 + n(n)$$

$$T(n) = 1 + n^2$$

Runtime of given algorithm is $O(n^2)$