

$$\begin{aligned}
b_2^{\text{MHK}} &= \frac{\sum_{i=1}^n (p_i - \bar{p})(\omega_i - \bar{\omega})}{\sum_{i=1}^n (\omega_i - \bar{\omega})^2} = \frac{\sum_{i=1}^n ([\beta_1 + \beta_2 \omega_i + u_{pi}] - [\beta_1 + \beta_2 \bar{\omega} + \bar{u}_p])(\omega_i - \bar{\omega})}{\sum_{i=1}^n (\omega_i - \bar{\omega})^2} = \\
&= \frac{\sum_{i=1}^n (\beta_2 (\omega_i - \bar{\omega})(\omega_i - \bar{\omega}) + (u_{pi} - \bar{u}_p)(\omega_i - \bar{\omega}))}{\sum_{i=1}^n (\omega_i - \bar{\omega})^2} = \beta_2 + \frac{\sum_{i=1}^n (u_{pi} - \bar{u}_p)(\omega_i - \bar{\omega})}{\sum_{i=1}^n (\omega_i - \bar{\omega})^2}.
\end{aligned}
\tag{\Upsilon}$$