

```
import numpy as np

def taylor_sin(x, n=5):
    """Compute the Taylor expansion of sin(x) around x=0 up to order n."""
    res = 0
    for i in range(n):
        res += ((-1)**i / np.math.factorial(2*i + 1)) * x**(2*i + 1)
    return res

# Generate a dataset of input-output pairs
X_train = np.linspace(-np.pi, np.pi, 1000)
y_train = np.array([taylor_sin(x) for x in X_train])

n_steps = 10

def prepare_data(X, y, n_steps):
    X_seq, y_seq = [], []
    for i in range(len(X) - n_steps):
        X_seq.append(X[i:i+n_steps])
        y_seq.append(y[i:i+n_steps])
    return np.array(X_seq), np.array(y_seq)

# Prepare the training data
X_train_seq, y_train_seq = prepare_data(X_train, y_train, n_steps)

from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import LSTM, Dense

# Define the LSTM model
model = Sequential([
    LSTM(64, activation='relu', input_shape=(n_steps, 1)),
    Dense(1)
])

# Compile the model
model.compile(optimizer='adam', loss='mse')

# Train the model
model.fit(X_train_seq, y_train_seq, epochs=100, batch_size=32)
```

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Epoch 92/100
31/31 [=====] - 0s 8ms/step - loss: 1.6771e-04
Epoch 93/100
31/31 [=====] - 0s 9ms/step - loss: 1.6797e-04
Epoch 94/100
31/31 [=====] - 0s 8ms/step - loss: 1.6177e-04
Epoch 95/100
31/31 [=====] - 0s 9ms/step - loss: 1.6259e-04
Epoch 96/100
31/31 [=====] - 0s 8ms/step - loss: 1.6502e-04
Epoch 97/100
31/31 [=====] - 0s 9ms/step - loss: 1.7203e-04
Epoch 98/100
31/31 [=====] - 0s 9ms/step - loss: 2.0976e-04
Epoch 99/100
31/31 [=====] - 0s 8ms/step - loss: 1.9172e-04
Epoch 100/100
31/31 [=====] - 0s 9ms/step - loss: 1.8402e-04
<keras.callbacks.History at 0x7fb4ccd85220>

```

```
import matplotlib.pyplot as plt
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```
# Generate predictions
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```
X_test = np.linspace(-np.pi, np.pi, 100)
```

```
y_test = np.array([taylor_sin(x) for x in X_test])
```

```
X_test_seq, y_test_seq = prepare_data(X_test, y_test, n_steps)
```

```
y_pred_seq = model.predict(X_test_seq)
```

```
# Plot the results
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plt.plot(X_test, y_test, label='Ground Truth')
```

```
plt.plot(X_test[n_steps:], y_pred_seq[:, -1], label='Predictions')
```

```
plt.legend()
```

```
plt.show()
```

```
3/3 [=====] - 0s 8ms/step
```

