

Assignment 1

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vector

Abstract—This document contains the solution to find the coordinates of the points of section, given the line joining points is divided into four equal parts.

Download all python codes from

<https://github.com/NamrataMishra97/Assignment-1-EE5600>

and latex codes from

<https://www.overleaf.com/project/613635b77e317673c499deca>

Problem

Vector-2, Example-1, Question-20

The line joining the points $(-6,8)$ and $(8,-6)$ is divided into four equal parts; Find the coordinates of the points of section.

Solution:

We will be using matrix approach for calculating the coordinates of the points of section which is divided into four equal parts.

Let us consider $\mathbf{x1}$ and $\mathbf{y1}$ are points on a line which divides the line in the ratio of 3:1. Given that,

$$\begin{bmatrix} \mathbf{x1} \\ \mathbf{y1} \end{bmatrix} = \frac{1}{4} \begin{bmatrix} -6 & 8 \\ 8 & -6 \end{bmatrix} \begin{bmatrix} 3 \\ 1 \end{bmatrix} \quad (0.0.1)$$

Solving above matrix we get the coordinate points

$$\begin{bmatrix} \mathbf{x1} \\ \mathbf{y1} \end{bmatrix} = \begin{bmatrix} -10/4 \\ 18/4 \end{bmatrix} = \begin{bmatrix} -5/2 \\ 9/2 \end{bmatrix} \quad (0.0.2)$$

Let us consider another points $\mathbf{x2}$ and $\mathbf{y2}$ on a line which divides the line in the ratio of 1:1.

$$\begin{bmatrix} \mathbf{x2} \\ \mathbf{y2} \end{bmatrix} = \frac{1}{2} \begin{bmatrix} -6 & 8 \\ 8 & -6 \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix} \quad (0.0.3)$$

Solving above matrix we get the coordinate points

$$\begin{bmatrix} \mathbf{x2} \\ \mathbf{y2} \end{bmatrix} = \begin{bmatrix} 2/2 \\ 2/2 \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \end{bmatrix} \quad (0.0.4)$$

Let us consider another points $\mathbf{x3}$ and $\mathbf{y3}$ on a line which divides the line in the ratio of 1:3

$$\begin{bmatrix} \mathbf{x3} \\ \mathbf{y3} \end{bmatrix} = \frac{1}{4} \begin{bmatrix} -6 & 8 \\ 8 & -6 \end{bmatrix} \begin{bmatrix} 1 \\ 3 \end{bmatrix} \quad (0.0.5)$$

Solving above matrix we get coordinate points

$$\begin{bmatrix} \mathbf{x3} \\ \mathbf{y3} \end{bmatrix} = \begin{bmatrix} 18/4 \\ -10/4 \end{bmatrix} = \begin{bmatrix} 9/2 \\ -5/2 \end{bmatrix} \quad (0.0.6)$$

Result

Plot of coordinate of the points obtained from Python code is shown below.

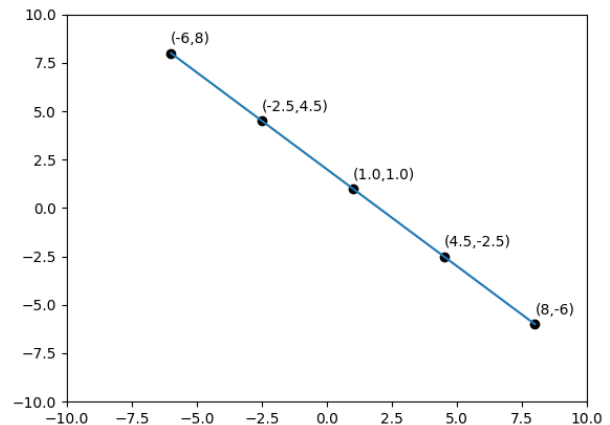


Fig. 0: Plot of coordinate of the point which divides the line into four parts

Conclusion

The points $(\mathbf{x1y1})$, $(\mathbf{x2y2})$, $(\mathbf{x3y3})$ divides the lines into four parts in ratio (3:1) (1:1) (1:3). The points $(\mathbf{x1y1}) = (-2.5, 4.5)$, $(\mathbf{x2y2}) = (1, 1)$, $(\mathbf{x3y3}) = (4.5, -2.5)$