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Finite Mixture Models

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### **OUTLINE**

- ► Introduction
- ► Data Preprocessing
- ► GMM
- ► Conclusion

# INTRODUCTION OF FINAL PROJECT

Traditional basketball has as few as three or as many as five positions.

- Guard (1.Point Guard, 2.Shooting Guard)
- Forward (3.Small Forward, 4.Power Forward)
- Center (5.Center)

Positional restrictions are gradually fading in modern basketball, and an increasing number of players are filling multiple roles.

- Dual Guard (1+2), Swing Man (2+3), Stretch Forward (3+4), etc...

We try to subdivide player types for each position using clustering methods, rather than simply limiting to existing roles.

#### Data

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#### 2021-2022 season NBA player stats

- ► Basketball-Reference.com
  - Player stats for per game, also advanced indices (ex. VORP).
  - There are so many indices, we should select the variables or reduce the dimensions.



Specific indices might be classified as follows.

Offense: FG%, 3P%, 2P%, eFG%, AST, PTS, TS%, USG%

► Deffence : PF, TRB%, STL%, BLK%, TOV%

► Contributuon : PER, WS%48, BPM, VORP

### **D**ATA

Naturally, the indicators do not reveal everything about the player.



(a) Stephen Curry -All time 3-points shooter



**(b)** Russel Westbrook - Triple-double machine

#### Data

Naturally, the indicators do not reveal everything about the player.

- ► The indices is not overwhelming in Stephen Curry's case, but the attack unfolds through the space created by Curry leading the defense.
- ▶ Russel Westbrook was named MVP of the season and had a triple-double in the 2016-2017 season, but he later changed the method of counting VORP indicators.
- ► Kawhi Leonard is the league's best swingman and has twice been named Final MVP, but he also takes care of himself during the regular season.

### VARIABLE FILTERING

The variables were pre-filtered, with a focus on "ratio statistics".

- ▶ Because all of the contribution indicators are ratio statistics, uniformity was achieved through filtering.
- ► Furthermore, the ratio is generally regarded as more significant.
- ▶ Of course, using more diverse variables is beneficial, but it was removed because the ratio and cumulative statistics move in similar directions when the dimension is reduced.

### NA IMPUTATION

NA was found in the data representing current ratio statistics and was replaced with 0.

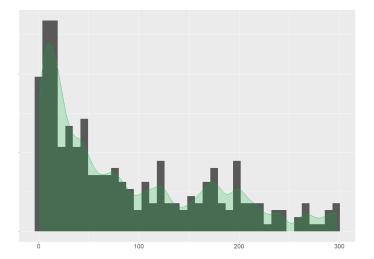
- ► In the case of the center, there have been instances where players with greater influence under the goal.
- ► For example DeAndre Jordan, two-times rebound leaders, do not throw three points and thus cannot calculate the success rate.
  - It is reasonable to replace it with zero in this case.

Furthermore, it was critical to limit the number of samples suitable for analysis.

- ▶ Players traded to other teams during the season were added together.
- ▶ Because garbage members are unimportant in the analysis, the analysis target was set at 200 minutes of playing time (less than 3 minutes on average in the season).
- ► Raising the playing time standard reduced the number of observations, while lowering the standard increased the influence of outliers.

Then, 
$$n = 450$$
,  $p = 17$ .

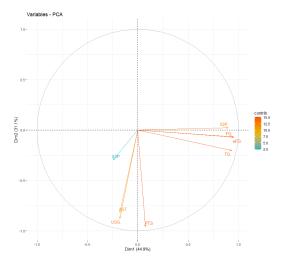
# TREAT GARBAGE MEMBERS

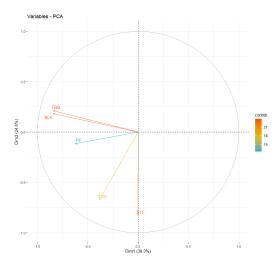


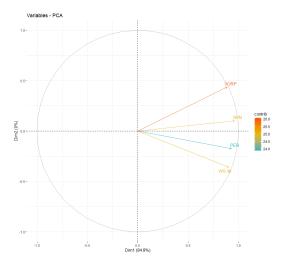
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Because "p = 17" and "n = 556" are currently used, the number of variables must be reduced for proper clustering.

- ► Using prior knowledge, the indicator's information can be classified as attack, defense, or contribution.
- ▶ Dimensionality reduction is accomplished using PCA with two offense, defence indices and one contribution index, taking into account the number of each index.
  - Offense: FG%, 3P%, 2P%, eFG%, AST, PTS, TS%, USG.
  - Defence: PF, TRB%, STL, BLK, TOV.
  - Contribution: PER, WS%48, BPM, VORP.





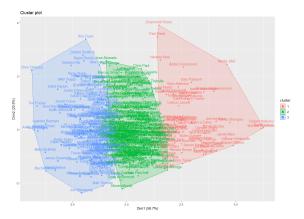


The dimensionally reduced variables have the following meaning.

- ► "Offense 1" index represent main ball handlers and scorers.
- ► "Offense 2" index indicate the effectiveness of an attack.
- ► "Defence 1" index indicates a height advantage.
- ► "Defence 2" index represent defensive power while the ball is in play.
- "Overall contribution" index show how much this player contributes to the victory.

### **EDA**

This is the outcome of clustering all data, regardless of position.



We will proceed with clustering by dividing by position because we cannot get new information.



### **GMM**

The analysis logic is summarized before performing clustering with GMM.

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- 1. The analysis is started with each position for center, forward and guard.
- 2. Within the covariance structure of the variables used, a model is chosen.
- 3. The best model is chosen by comparing the silhouette values of the selected models for each variable.

### SILHOUETTE VALUES

The silhouette value is a quantitative measure of how well the clustering was done.

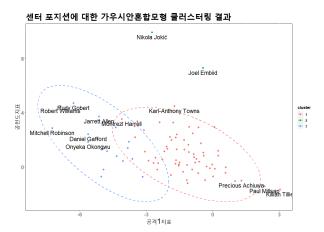
► Calculate the cohesiveness of each observation in a cluster and its distance from other cluster observations.

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- This is aggregated by taking the mean of all observations.
- ► The "Rand Index" is appropriate in a simulation scenario where the correct answer is known, but it cannot be calculated if the correct answer is unknown.
- ▶ If the silhouette value is 0.5 or higher, it is considered successful; if it is 0.25 to 0.5, it is considered meaningful in some degree.

# **CENTER - GMM**

For center, the silhouette value is 0.42 with 3 clusters in EEE covariance structure by using "Offense 1" & "Overall contribution".



### CENTER - GMM

Center athletes are classified into three types.

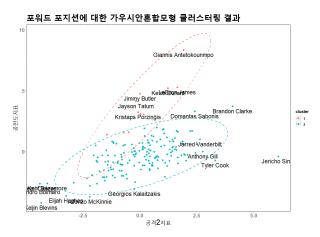
- 1. The offensive center, such as the Karl-Anthony Towns, is the first type.
  - Even if their contribution to victory is minor, it is a center type who can supplement the team's insufficient offense.

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- 2. The MVP-class center is the second type.
  - They can not only play the center position, but also shoot and coordinate games.
- 3. A defensive center, such as Rudy Gobert, is the third type.
  - Rudy Gobert is the defender of the year, and players with excellent under-the-goal control, such as Gobert, can be described as such.

## FORWARD - GMM

For Forward, the silhouette value is 0.46 with 2 clusters in EVV covariance structure by using "Offense 2" & "Overall contribution".



### FORWARD - GMM

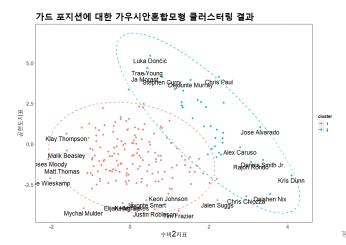
Forward athletes are classified into two types.

- 1. The first type is the "superstar."
  - These are players who can take high efficiency in attack and lead it to victory.
  - Small forward players such as LeBron James and Kevin Durant have dominated NBA Finals MVP over the last decade.
- 2. A "non-superstar" player is the second type.
  - It has more ball possession time than superstar players in comparison.

Overall, superstar players chose the cluster, and these two aspects appeared even when other variables were used.

#### Guard - GMM

For Guard, the silhouette value is 0.36 with 2 clusters in EVE covariance structure by using "Defence 1,2" & "Overall contribution".



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Guard athletes are classified into two types.

- 1. The first type of player is the "Catch and Shooter."
  - He's the type of player who, like Klay Thompson, doesn't take many possession but can play shooting guard for the team.
- 2. The second type is more difficult to understand.
  - To begin with, he is an ace guard, like Luka Doncic, Chris paul, and Stephen Curry, who lead the overall attack as "main ball handlers."
  - Then there's Alex Caruso, a role player who contributes to the team through excellent defense rather than scoring.

In the case of guards, the analysis process reveals that the clustering results were not well produced.

### CONCLUSION

I'll discuss the limitations and improvements I noticed during the analysis.

- ► First, it was difficult to effectively use various variables.
  - It was more natural to interpret the "PC" variables based on prior knowledge of the players rather than proceeding with the interpretation while looking at the reduced variables.
- ► Second, rather than the actual player types, some players influenced the outcome of clustering.
  - This phenomenon occurred because "Hero Ball" is possible depending on the superstar's personal competence in the case of basketball.
  - Because more clusters are desired, the Bayesian nonparametric method "DPMM" may be more appropriate in this case.