

	One random variable, X		Two joint random variables (X, Y)	
	Discrete	Continuous	Discrete	Continuous
Probability mass/density function defined for	pmf: $p_X(x)$ $= P(X = x)$ all x with $p_X(x) > 0$	pdf: $f_X(x)$ $(P(X = x) \equiv 0)$ $-\infty < x < \infty$	$p_{X,Y}(x, y)$ $= P(X = x, Y = y)$	$f_{X,Y}(x, y)$ $-\infty < x < \infty, -\infty < y < \infty$
Probability $P(X \in A)$ Note:	$\sum_{x \in A} p_X(x)$ $p_X(x) \geq 0$ $\sum_x p_X(x) = 1$	$\int_{x \in A} f_X(x) dx$ $f_X(x) \geq 0$ $\int_x f_X(x) dx = 1$	$\sum \sum_{(x,y) \in A} p_{X,Y}(x, y)$ $p_{X,Y}(x, y) \geq 0$ $\sum_x \sum_y p_{X,Y}(x, y) = 1$	$\int \int_{(x,y) \in A} f_{X,Y}(x, y) dx dy$ $f_{X,Y}(x, y) \geq 0$ $\int_x \int_y f_{X,Y}(x, y) dx dy = 1$
Cumulative distrib. func. cdf, $F_X(x) = P(X \leq x)$	$F_X(x) = \sum_{z \leq x} p_X(z) \quad F_X(x) = \int_{-\infty}^x f_X(z) dz$		$F_{X,Y}(x, y) = P(X \leq x, Y \leq y)$ $\sum_{z \leq x, w \leq y} p_{X,Y}(z, w) \quad \int_{z=-\infty}^x \int_{w=-\infty}^y f_{X,Y}(z, w) dz dw$	
Result:	$P(a < X \leq b) = F_X(b) - F_X(a)$		$P(a_1 < X \leq a_2, b_1 < Y \leq b_2) =$ $F_{X,Y}(a_2, b_2) - F_{X,Y}(a_1, b_2) - F_{X,Y}(a_2, b_1) + F_{X,Y}(a_1, b_1)$	
From cdf to pdf	$f_X(x) = \frac{d}{dx} F_X(x)$		$f_{X,Y}(x, y) = \frac{\partial^2}{\partial x \partial y} F_{X,Y}(x, y)$	
Marginal pmf/pdf			$p_X(x) = \sum_y p_{X,Y}(x, y)$ $p_Y(y) = \sum_x p_{X,Y}(x, y)$	$f_X(x) = \int_y f_{X,Y}(x, y) dy$ $f_Y(y) = \int_x f_{X,Y}(x, y) dx$
Expectation $E(X)$ Result: $E(g(X))$	$\sum_x x p_X(x)$ $\sum_x g(x) p_X(x)$	$\int_{-\infty}^{\infty} x f_X(x) dx$ $\int_{-\infty}^{\infty} g(x) f_X(x) dx$	$\sum_x \sum_y g(x, y) p_{X,Y}(x, y) \quad \int_x \int_y g(x, y) f_{X,Y}(x, y) dx dy$	
Consequence:	$E(g_1(X) + g_2(X)) = E(g_1(X)) + E(g_2(X))$		$E(g_1(X) + g_2(Y)) = E(g_1(X)) + E(g_2(Y))$	