

Name Nan Tang

Please answer the following questions:

1. If  $X$  has density  $f(x) = \theta e^{-\theta x}$ ,  $x > 0$ , what is  $E(X)$ ?

$$X \sim \text{Exp}(\theta), \quad x > 0.$$

$$E(X) = \frac{1}{\theta}$$

2. What does it mean to say that  $(-0.25, 0.25)$  is a 95% confidence interval for a parameter  $\theta$ ?

That means we are 95% confident that the true population mean is captured in the interval  $(-0.25, 0.25)$ .

In other words, 95% of the time, when we calculate the confidence interval in this way, true mean will be within  $(-0.25, 0.25)$ .

3. What is the difference between drawing a sample with and without replacement?

Let  $M$  be number of success within a total number of  $N$

$P = \frac{M}{N}$  if draw with replacement, i.e.  $p$  is constant.

If draw without replace,  $M$  decreases by 1 after each draw and  $N$  decreases by 1 after each successful draw.  $P$  is quite different between each draw time.

4. Consider the times of large earthquakes in the Puget Sound region. What distribution would you suggest the time between earthquakes should have?

I think the span of time between two earthquake  $T$  is an exponential distribution, since poisson distribution is often used to describe events like earthquake that occur rarely.