

Homework # 9 (due Mon Mar 11, at the beginning of our class meeting)

We plan to grade your HW#9 papers quickly & return them to you Wednesday for you to review as you prepare for our final exam Fri Mar 15.

1. Assume you have $X_1, \dots, X_m \sim \text{iid Normal}(\mu_X, \sigma_X^2)$ and $Y_1, \dots, Y_n \sim \text{iid Normal}(\mu_Y, \sigma_Y^2)$, X 's and Y 's independent.

(a) Derive the formula for a level $1-\alpha$ confidence interval for the ratio of the 2 variances. Justify each step of your derivation. You will need to identify suitable summary statistics to use, the sampling distribution for their ratio, or for a simple function of their ratio, write a suitable probability statement that can be manipulated to find the endpoints of a confidence interval.

(b) Derive the formula for a level $1-\alpha$ confidence interval for the ratio of the 2 standard deviations.

(c) Use your result in (b), and the data from the last pages of our Confidence Intervals lecture notes (on Guardiola seeds) to construct the relevant 90% confidence intervals. Then give suitable statements interpreting your results in words (not formulae). Those statements should include "90%", "Guardiola seeds", "variance" and/or "variances", "confident" and/or "confidence".

From our textbook:

Pages 309-310/

Problem 5.3.3: Read the set-up for problem 5.3.3. Explore the data. Do you find evidence or reason to support or refute the normality assumption? Clearly state and justify your conclusion.

Problem 5.3.6: Clearly show how you derived your answers.

Page 377/ 6.4.4:

- (a) Derive the statistical hypothesis test for this problem, clearly show & justify how you derived your solution.
- (b) Show how one derives the critical (rejection) region for this hypothesis test.
- (c) How does your answer to (b) compare to the level 95% confidence interval for μ ?
Comment on whether/why this comparison is/not surprising.

Pp 378-379/ 6.4.10, 6.4.11, 6.4.14, 6.4.21