Name: ID:
S; Marzban 10 +14 wrong-answer penalty answer without explanation
e single most important advantage pairwise t-tests? makes fewer assumptions. is no advantage.
e population, and another random all of the appropriate tests for the
t-test an F test in an RCBD
ng two models: Model 1 has more
ween SSE1 and SSE2.
lving two treatment factors ($y =$ cal randomization distribution
the intercept) $-1 \qquad \qquad \qquad 2^{k-2}$
mal qqlot of the effects to identify .
of
effect ge
ij

Stat 421, Test 2, Fall, Nov. 16, 2016

ONLY a half-size "cheat sheet" is allo

Multiple choice: Circle all the correct answers; there is For rest, SHOW answer & work; NO CREDIT for correct a

Points

1

1

1

1

1

In testing the equality of three population means, what is the of performing the ANOVA F-test as compared to performing 3 p

The F-test makes less Type 1 error.

The F-test

The F-test is more convenient to code.

There

You make a random sample of 100 observations of y from one sample of 50 observations of y from another population. Circle equality of means.

unpaired, pooled t-test

unpaired, Welch t-test

paired

For a given data set involving multiple factors, consider fitti terms than model 2. Then (circle the correct answer)

SSE1 < SSE2

SSE1 > SSE2

SSE1 = SSE2

There is no specific relation bety

4. In performing the randomization test in a full model invo A+B+AB) which of the following is/are correct? The empiric

of SSA can be used to test the effect of A

of SSB can be used to test the effect of B

of SSAB can be used to test the interaction effect AB

of SSE can be used to test if any of the effects are nonzero.

5. In a 2^k design/model, how many effects are there (excluding 2^k

6. In 2^k design/models, Daniel's conjecture (about using a norr significant effects) is useful when the number of effects is large small small or large.

 $\frac{1}{7}$. Consider a problem involving a response Y observed at each 3 levels of factor A. The data are shown in the adjacent figure. The black (red) boxplot denotes the data collected on day 1 (2).

a) Without doing any tests, does it appear that factor A has an on the response? Explain in 1 sentence.

6 1

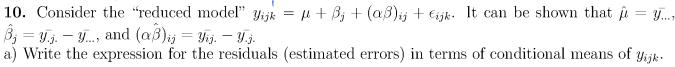
b) If you were to run a test with the model $y_{ij} = \mu + \alpha_i + \epsilon_{ii}$ what kind of p-value would you expect to get? Circle: Small/Lar

c) If you were to run a test with the model $y_{ij} = \mu + \alpha_i + \beta_j + \epsilon$ with β corresponding to the Day factor, what kind of p-value would you expect to get? Circle: Small/Large

Consider data collected from a completely randomized factorial design involving three 4-level factors. A research group uses a full factorial model of the data and finds that factor A is highly significant. A different research group decides to use a model based on an LSD. Is it possible that they will find factor A to be non-significant? Yes/No AND provide some explanation.



Suppose you have collected data according to an LSD involving three p-level factors. Give an argument in terms of the number of observations and the number of parameters in a model (or equivalently in terms of the df of SS terms), to explain what will happen if you try to fit the following model to the data: $y_{ijk} = \mu + \alpha_i + \beta_j + \gamma_k + (\alpha \beta)_{ij} + \epsilon_{ijk}$





esto, P.3 (as an example)

b) Note (do not prove) that the estimate of β_j is the same as that of the full model $y_{ijk} = \mu + \alpha_i + \alpha_j$ $\beta_j + (\alpha \beta)_{ij} + \epsilon_{ijk}$. Also recall (do not prove) that the estimate of the residuals in the full model is $y_{ijk} - y_{ij}$. Show that $SSAB_{reduced} = SSA_{full} + SSAB_{full}$

Hint: use the anova decomposition for the two models; DO NOT use the formulas for parameter estimates in the formulas for SS because it will be very time consuming.

11./Consider the model $y_{ijk} = \mu + (\alpha \beta)_{ij} + \epsilon_{ijk}$, i = 1 - a, j = 1 - b, k = 1 - n. Starting from the expression for SSE, take appropriate derivatives, impose appropriate constraints, and find the estimates for the parameters μ , and $(\alpha \beta)_{ij}$.

And found that the estimates of the parameters $(\alpha_i, \beta_j, \cdots)$ depend on the choice of the constraints. However, you also found out that certain combinations of parameter estimates are unaffected by the choice of the constraint. Such combinations are called uniquely estimable functions. Here, consider the additive model $y_{ij} = \mu + \alpha_i + \beta_j + \epsilon_{ij}$, for whom the least-squares normal equations are given below. Show that any zero-sum contrast $\Gamma = \sum_i c_i \mu_i$, is a uniquely estimable function, where $\mu_i = \mu + \alpha_i$ are the treatment means. Hint1: If some combination of parameters can be written in terms of the data (y), then it is uniquely estimable. Hint2: It's sufficient to look at only one of the least squares equations (for convenience, I have left out the symbols): $\bar{y}_{..} - \mu - \bar{\alpha}_{.} - \bar{\beta}_{.} = 0$ $\bar{y}_{..} - \mu - \bar{\alpha}_{.} - \bar{\beta}_{.} = 0$

~ 2 white 13. Consider a 2^1 design/model with a treatment factor A, with n replications. Show that SSA, as defined by $\sum_{ij} (\bar{y_{i.}} - \bar{y_{..}})^2$, is equal to $\frac{1}{2n} (\text{contrast}_A)^2$.

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