Shortest Path Algorithms: Taxonomy and Advance in Research

my summary

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1 Introduction

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1.1 Overview

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1.2 Restatement of the Problem

Second Problem "momentum's role in the match" means the level of momentum affects the future scores of the match. The coach may subscribe to the idea that each point is an independent event and governed by probability. In this view, consecutive success and momentum changes (swings) are seen as more random than influenced by previous events. To judge this autocorrelation and to use our model, we

• perform autocorrelation test on momentum, and perform correlation test between current momentum and future scores.

1.3 Our Work

• develop a model to

2 Notations and asssumptions

2.1 Notations

To access a certain field in a point, we simply use the field name stated in the given dictionary as index, i.e. for a point point, we use $point_{ace}$ to denote the binary variable that shows whether player hits an ace ball in the point.

2.2 Assumptions

To simplify the problem, we made the following assumptions:

- **Assumption 1:** The px_unf_err column of the data only counts those unforced errors that occurred when the player was hitting in baseline.
 - **Justification:** Usually when a player is at net, the point will end in a few strikes, and there's little probability that the player will hit an unforced error within that few strikes. What's more, the px_net_point and px_net_point_won columns of the data can predominantly reflect the player's ability at net, therefore reducing the impact of counting the unforced errors while at net.
- **Assumption 2:** The current performance on a certain aspect of a player can be reflected by the player's 3 latest shots of that aspect.
 - E.g. P_{ace} can be reflected by the proportion of aces in the 3 latest serves of the player, P_{win} can

Symbols	Description
player	the current player we are considering (e.g. while calculating momentum)
$point_i$	the i^{th} point of the match, a vector consists of fields stated in the given dictionary
cur	the current index of the point, i.e. the match is currently at the cur^{th} point
H_i	denotes the set $\{point_{cur}, point_{cur-1}, \dots, point_{cur-i+1}\}$
S_i	the set of latest <i>i</i> points where <i>player</i> serves
R_i	the set of latest i points where $player$ returns
P_{ace}	current probability of hitting an ace by player
P_{df}	current probability of double-faulting by player
P_{1st}	current first serve goal rate by player
P_{fw}	current probability of <i>player</i> winning a served point within 3 rallies
rd	current return depth of player
P_{win}	current probability of hitting a winner by player
P_{net}	current net win rate of player
dist	player's running distance on the point
P_{unf}	current probability of hitting an unforced error by player
scored	whether <i>player</i> scored the current point
diff	the score diffrence for <i>player</i> in the current game (by number of points)
<u>M</u>	the current momentum of player after a point

be reflected by the proportion of winners in the 3 latest **shots** of the player, rd can be reflected by the return depth of the 3 latest **returns** of the player, etc.

Justification: The current performance of a player consists of the average performance and the status of the player at the moment, which can be comprehensively reflected in the player's performance on recent shots. For convenience, we specified that the 3 latest shots can reflect the player's current performance.

3 Momentum Evaluation Model

To determine which player is performing better at a specific time, we create a indicator "Momentum" to give a quantitative and overall evaluation.

Definition 3.1. *Niche width is the range of resources that a species can use.*

Niche width is an indicator [1]

3.1 Model Overview

3.2 Data Processing and Normalization

In order to quantify the factors used in our model, based on our assumptions, we calculate them using the following formulae:

$$P_{ace} = \frac{\sum_{p \in S_3} p_{ace}}{3} \tag{1}$$

$$P_{df} = -\frac{\sum_{p \in S_3} p_{double_fault}}{3} \tag{2}$$

$$P_{1st} = \frac{\sum_{p \in S_3} [p_{serve_no} = 1]}{3} \tag{3}$$

$$P_{fw} = \frac{\sum_{p \in S_3} [p_{rally_count} \le 3][p_{point_victor} = player]}{3}$$
 (4)

$$\sum_{p \in R_3} \begin{cases} 0, & p_{return_depth} = ND \\ 1, & p_{return_depth} = D \\ -1, & p_{return_depth} = NA \end{cases}$$

$$rd = \frac{1}{3}$$
(5)

$$P_{win} = \frac{\sum_{p \in H_3} p_{winner}}{3} \tag{6}$$

$$P_{net} = \frac{\sum_{p \in H_3} p_{net_pt_won}}{\sum_{p \in H_3} p_{net_pt}}$$
 (7)

$$dist = \begin{cases} 0, & point_{cur,distance_run} < 5\\ -1, & point_{cur,distance_run} > 45\\ \frac{5 - point_{cur,distance_run}}{40}, & otherwise \end{cases}$$
(8)

$$P_{unf} = -\frac{\sum_{p \in H_3} p_{unf_err}}{3} \tag{9}$$

$$scored = [point_{cur,point_victor} = player]$$
 (10)

$$diff = \frac{\sum_{p \in point} [p_{set_no} = point_{cur,set_no}][p_{game_no} = point_{cur,game_no}](2[p_{point_victor} = player] - 1)}{\min\{3, \sum_{p \in point} [p_{set_no} = point_{cur,set_no}][p_{game_no} = point_{cur,game_no}]\}}$$
(11)

In order to normalize the data processed, we convert the original data to limit them in [-1, 1]. For those factors that negatively influence the momentum, such as P_{df} , we made sure it's in [-1, 0]. For those factors that positively influence the momentum, such as P_{win} , we made sure it's in [0, 1]. For those factors that influence the momentum in both ways, such as diff, we made sure it's in [-1, 1].

3.3 Visualization and Analysis

In figure 1, when the red line is above the blue line, it means that the player is performing better than the opponent.

In figure 2, we minus the opponent's momentum from the player's momentum to get the difference. And the difference indicates how much better the player is performing than the opponent.

3.4 momentum autocorrelation and correlation with runs of success

to

Algorithm 1 An algorithm with caption

```
Require: n \ge 0
Ensure: y = x^n
y \leftarrow 1
X \leftarrow x
N \leftarrow n
while N \ne 0 do
if N is even then
X \leftarrow X \times X
N \leftarrow \frac{N}{2}
else if N is odd then
y \leftarrow y \times X
N \leftarrow N - 1
end if
end while
```

momentum autocorrelation

correlation with runs of success To give a quantitative evaluation of "future scores", we calculate points gain in future multiple points, and calculate difference between the two players, this indicates how much better the player is performing than the opponent.

4 Robustness Analysis

5 Strength and Weaknesses

5.1 Strengths

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5.2 Weaknesses

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References

[1] Alice Axford, Bob Birkin, Charlie Copper, and Danny Dannford. Demostration of bibliography items. *Journal of Texperts*, 36(7):114–120, Mar 2013.

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B report on Use of AI

1.

OpenAI ChatGPT (Feb 2,2024 version, ChatGPT3.5)

Query1: "swings in play and runs of success by one player are random" can this sentence to be interpreted as swings in play and runs of success by one player are independent?

Output: Yes, the sentence "swings in play and runs of success by one player are random" can be interpreted as suggesting that swings in play and runs of success by one player are independent of each other. In statistical terms, independence means that the occurrence or outcome of one event does not influence the occurrence or outcome of another.

In the context of tennis, this would imply that the fluctuations in the dynamics of the match (swings in play) and a player's success streaks (runs of success) are not connected or dependent on each other. Each event is considered random and not influenced by the occurrence of the other.