

String

1 KMP

1.1 Fail

```
// input: 0-based, output: 1-based
auto getFail (const std::string& s) {
    int n = s.size();
    std::vector<int> fail(n + 1);
    for (int i = 1, j = 0; i < n; ++i) {
        while (j && s[i] != s[j]) j = fail[j];
        fail[i + 1] = j += (s[i] == s[j]);
    }
    return fail;
}
```

1.2 Trans

```
// input: 0-based, output: 1-based
auto getTrans(const std::string& s) {
    int n = s.size();
    auto fail = getFail(s);

    std::vector<int> trans(n + 1);
    for (int i = 1, j = 0; i < n; ++i) {
        while (j && s[i] != s[j]) j = fail[j];
        j += s[i] == s[j];
        while (2 * j > i + 1) j = fail[j];
        trans[i + 1] = j;
    }
    return trans;
}
```

1.3 occurrence

```
// input: 0-based, output: 0-based
auto occurrence(const std::string& s, const std::string& t) {
    int n = s.size(), m = t.size();
    auto fail = getFail(t);

    std::vector<int> occur;
    for (int i = 0, j = 0; i < n; ++i) {
        while (j && s[i] != t[j]) j = fail[j];
        j += s[i] == t[j];
        if (j == m) {
            occur.push_back(i - m + 1);
            j = fail[j];
        }
    }
    return occur;
}
```

2 Manacher

2.1

```
// input: 0-based, idx(s[i]) = 2i
std::vector<int> Manacher(const std::string& t) {
    std::string s = "#";
    for (auto& ch : t) {
        s += '$', s += ch;
    } s += '$';

    int n = s.size() - 1;
    std::vector<int> d(n + 1);
    for (int i = 1, j = 1; i <= n; ++i) {
        d[i] = i < j + d[j] ? std::min(d[2 * j - i], j + d[j] - i) : 1;
        while (i + d[i] <= n && i - d[i] >= 1 && s[i - d[i]] == s[i + d[i]]) ++d[i];
        if (i + d[i] > j + d[j]) j = i;
    }

    return d;
}
```

2.2

题意：找最长的子串满足存在一个字符串 S 使得该子串可以被表示成 $S+\bar{S}+S+\bar{S}$ 。显然一个字符串只有 $O(n)$ 个本质不同的回文串，暴力 check 即可

```
// input: 0-based, idx(s[i]) = 2i
int Manacher(const std::string& t) {
    std::string s = "#";
    for (auto& ch : t) {
        s += '$', s += ch;
    } s += '$';

    int n = s.size() - 1, ans = 0;
    std::vector<int> d(n + 1);
    for (int i = 1, j = 1; i <= n; ++i) {
        d[i] = i < j + d[j] ? std::min(d[2 * j - i], j + d[j] - i) : 1;
        while (i + d[i] <= n && i - d[i] >= 1 && s[i - d[i]] == s[i + d[i]]) ++d[i];
        if (i + d[i] > j + d[j]) {
            if (s[i] == '$') {
                for (int k = j + d[j]; k < i + d[i]; ++k) {
                    if (s[k] == '$') continue;
                    int l = (2 * i - k) >> 1, r = k >> 1;
                    if ((r - l + 1) % 4 != 0) continue;
                    int x = i >> 1;
                    if (d[l + x] - 1 >= (r - l + 1) / 2) {
                        ans = std::max(ans, r - l + 1);
                    }
                }
            }
            j = i;
        }
    }

    return ans;
}
```

3 Z Function

```
// input: 0-based, output: 0-based
auto ZFunction(const std::string& s) {
    int n = s.size();
    std::vector<int> z(n + 1);
    z[0] = n;
    for (int i = 1, j = 1; i < n; ++i) {
        z[i] = std::max(0, std::min(j + z[j] - i, z[i - j]));
        while (i + z[i] < n && s[i + z[i]] == s[z[i]]) z[i]++;
        if (i + z[i] > j + z[j]) j = i;
    }
    return z;
}
```

4 Suffix Array

要学会使用 sa, rk, height 数组，多观察性质，转化成 sa, rk, height 能做的

```
// input: 0-based, output: 1-based
auto SuffixArray(const std::string& s) {
    int n = s.size();
    std::vector<int> sa(n + 1), rk(n + 1);
    std::iota(sa.begin() + 1, sa.end(), 1);
    std::sort(sa.begin() + 1, sa.end(), [&](int x, int y) {
        return s[x - 1] < s[y - 1];
    });

    rk[sa[1]] = 1;
    for (int i = 1; i < n; ++i) {
        rk[sa[i + 1]] = rk[sa[i]] + (s[sa[i + 1] - 1] != s[sa[i] - 1]);
    }

    std::vector<int> tmp(n + 1), cnt(n + 1);
    for (int k = 1; rk[sa[n]] != n; k <= 1) {
        for (int i = n - k + 1, j = 1; i <= n; ++i, ++j) {
            tmp[j] = i;
        }
        for (int i = 1, j = k; i <= n; ++i) {
            if (sa[i] <= k) continue;
            tmp[++j] = sa[i] - k;
        }

        for (int i = 1; i <= n; ++i) {
            cnt[rk[i]]++;
        }
        for (int i = 1; i < rk[sa[n]]; ++i) {
            cnt[i + 1] += cnt[i];
        }
        for (int i = n; i >= 1; --i) {
            sa[cnt[rk[tmp[i]]]--] = tmp[i];
        }

        std::swap(rk, tmp);
        rk[sa[1]] = 1, cnt[tmp[sa[n]]] = 0;
        for (int i = 1; i < n; ++i) {
            cnt[tmp[sa[i]]] = 0;
        }
    }
}
```

```

        rk[sa[i + 1]] = rk[sa[i]] + (
            tmp[sa[i + 1]] != tmp[sa[i]] ||
            sa[i] + k - 1 == n ||
            tmp[sa[i + 1] + k] != tmp[sa[i] + k]
        );
    }
}

std::vector<int> height(n + 1);
for (int i = 1, lcp = 0; i <= n; ++i) {
    if (rk[i] == 1) continue;
    if (lcp != 0) lcp--;
    while (
        i + lcp <= n &&
        sa[rk[i] - 1] + lcp <= n &&
        s[i + lcp - 1] == s[sa[rk[i] - 1] + lcp - 1]
    ) ++lcp;
    height[rk[i]] = lcp;
}

return std::tuple {
    std::move(sa),
    std::move(rk),
    std::move(height)
};
}

```

4.1 求 Longest Common Substring

```

int n = s.size(), m = t.size();
auto [sa, rk, height] = SuffixArray(s + '$' + t);

std::array<int, 3> ans { 0, 0, 0 };
for (int i = 1; i <= n + m; ++i) {
    int x = sa[i], y = sa[i + 1];
    int len = height[i + 1];
    if (len <= ans[0]) continue;
    if (x <= n && y >= n + 2) {
        ans = { len, x - 1, y - n - 2 };
    }
    if (y <= n && x >= n + 2) {
        ans = { len, y - 1, x - n - 2 };
    }
}
}

```

5 Suffix Automaton

// Node: 1-based "" 为 1 号节点

```

struct SAM {
    static constexpr int N = 26;
    struct Node {
        int len;
        int link;
        std::array<int, N> next;
        Node() : len(), link(), next() {}
    };
};

```

```

i64 substr;
std::vector<Node> t;

SAM (int n = 0) {
    t.reserve(n);
    t.assign(2, Node());
    t[0].next.fill(1);
    t[0].len = -1;
    substr = 0;
}

int newNode() {
    t.push_back();
    return t.size() - 1;
}

int extend(int p, int c) {
    int cur = newNode();
    t[cur].len = t[p].len + 1;

    while (t[p].next[c] == 0) {
        t[p].next[c] = cur;
        p = t[p].link;
    }

    int q = t[p].next[c];
    if (t[q].len == t[p].len + 1) {
        t[cur].link = q;
    } else {
        int r = newNode();
        t[r].len = t[p].len + 1;
        t[r].link = t[q].link;
        t[r].next = t[q].next;
        t[q].link = r;
        while (t[p].next[c] == q) {
            t[p].next[c] = r;
            p = t[p].link;
        }
        t[cur].link = r;
    }

    substr += t[cur].len - t[t[cur].link].len;
    return cur;
}

int len(int p)          const {return t[p].len; }
int link(int p)         const {return t[p].link; }
int next(int p, int x)  const {return t[p].next[x]; }
int size()              const {return t.size(); }
i64 count ()            const {return substr; }

```

```
// [ SAM 节点的个数 (不含空节点), 后缀树 ]
auto getTree() {
    int n = t.size();
    std::vector<std::vector<int>> adj(n);
    for (int i = 2; i < n; ++i) {
        adj[t[i].link].push_back(i);
    }
    return std::pair { n - 1, std::move(adj) };
}
};
```

5.1 弦论

计算 k th 子串, $t == 1$ 时多次出现需要多次计算

```
int n = s.size();
SAM sam(n);
vector<int> p(n + 1);
p[0] = 1;
for (int i = 0; i < n; ++i) {
    p[i + 1] = sam.extend(p[i], s[i] - 'a');
}

auto [m, adj] = sam.getTree();
vector<i64> siz(m + 1);
if (t == 1) { // 考虑 endpos.size()
    for (int i = 1; i <= n; ++i) {
        siz[p[i]]++;
    }
    auto dfs = [&](auto &&dfs, int u) -> void {
        for (auto v : adj[u]) {
            dfs(dfs, v);
            siz[u] += siz[v];
        }
    }; dfs(dfs, 1);
} else { // 否则一个集合只算一次
    for (int i = 1; i <= m; ++i) {
        siz[i] = 1;
    }
}
siz[1] = 0;

vector<int> deg(m + 1);
adj.assign(m + 1, {});
for (int u = 1; u <= m; ++u) {
    for (int ch = 0; ch < 26; ++ch) {
        int v = sam.next(u, ch);
        if (v == 0) continue;
        adj[v].push_back(u);
        deg[u]++;
    }
}

i64 substr = 0;
vector<i64> dp = siz;
```

```

for (int u = 2; u <= m; ++u) {
    substr += (sam.len(u) - sam.len(sam.link(u))) * siz[u];
}
if (substr < k) {
    cout << "-1\n";
    return;
}

queue<int> que;
for (int u = 1; u <= m; ++u) {
    if (deg[u] == 0) {
        que.push(u);
    }
}
while (!que.empty()) {
    int u = que.front();
    que.pop();
    for (auto v : adj[u]) {
        dp[v] += dp[u];
        if (--deg[v] == 0) {
            que.push(v);
        }
    }
}

int u = 1;
string ans;
while (k > siz[u]) {
    ans.push_back('$');
    k -= siz[u];
    for (int ch = 0; ch < 26; ++ch) {
        int v = sam.next(u, ch);
        if (v == 0) continue;
        ans.back() = 'a' + ch;
        if (k > dp[v]) {
            k -= dp[v];
        } else break;
    }
    u = sam.next(u, ans.back() - 'a');
}
cout << ans << "\n";

```

6 Palindromic Automaton

```

// odd root: 1
// even root: 0
struct PAM {
    static constexpr int N = 26;
    struct Node {
        int len, fail;
        std::array<int, N> next;
        Node() : len(0), fail(0), next{} {}
    };
    int cur;
    std::vector<int> s;

```

```

std::vector<Node> t;
PAM(int n = 0) {
    s.reserve(n);
    t.reserve(n + 2);
    t.assign(2, Node());
    t[t[0].fail = 1].len = -1;
}

int newNode() {
    t.emplace_back();
    return t.size() - 1;
}

int append(int p, int ch) {
    int n = s.size();
    s.push_back(ch);

    auto get = [&](int p) {
        while (n - t[p].len - 1 < 0 || ch != s[n - t[p].len - 1]) {
            p = t[p].fail;
        }
        return p;
    };

    p = get(p);
    if (t[p].next[ch] == 0) {
        int cur = newNode();
        t[cur].len = t[p].len + 2;
        t[p].next[ch] = cur;
        if (t[cur].len != 1) {
            t[cur].fail = t[get(t[p].fail)].next[ch];
        }
    }

    return t[p].next[ch];
}

int len(int p)          const { return t[p].len; }
int fail(int p)         const { return t[p].fail; }
int next(int p, int x)  const { return t[p].next[x]; }
int size()              const { return t.size(); }
};

```

7 Aho Corasick Automaton

```

// 记得 work
// 树根 "" 为 1 号节点
// adj 为失配树的子节点
struct ACAM {
    static constexpr int N = 26;
    struct Node {
        int len, fail;
        std::vector<int> adj;
        std::array<int, N> next;
        Node() : len(0), fail(0), adj{}, next{} {}
    };
};

```



```

std::vector<Node> t;

ACAM (int n = 0) {
    t.reserve(n);
    t.assign(2, Node());
    t[0].next.fill(1);
    t[0].len = -1;
    t[0].adj.push_back(1);
}

int newNode() {
    t.emplace_back();
    return t.size() - 1;
}

int insert(const std::string& s) {
    int p = 1;
    for (auto c : s) {
        int x = c - 'a';
        if (t[p].next[x] == 0) {
            t[p].next[x] = newNode();
            t[t[p].next[x]].len = t[p].len + 1;
        }
        p = t[p].next[x];
    }
    return p;
}

void work() {
    std::queue<int> q;
    q.push(1);

    while (!q.empty()) {
        int u = q.front();
        q.pop();

        for (int i = 0; i < N; i++) {
            if (t[u].next[i] == 0) {
                t[u].next[i] = t[t[u].fail].next[i];
            } else {
                t[t[u].next[i]].fail = t[t[u].fail].next[i];
                t[t[t[u].fail].next[i]].adj.push_back(t[u].next[i]);
                q.push(t[u].next[i]);
            }
        }
    }
}

int len(int p)                const { return t[p].len; }
int fail(int p)               const { return t[p].fail; }
const std::vector<int>& adj(int p) const { return t[p].adj; }
int next(int p, int x)        const { return t[p].next[x]; }
int size()                    const { return t.size(); }
};

```