Tutorial sheet -1

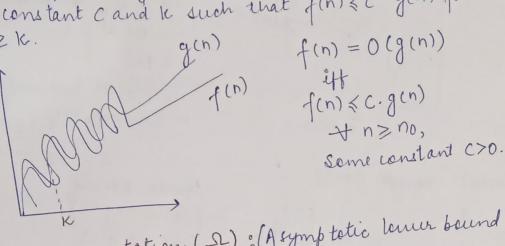
Sol 1: - Asymptotic Notation :-

→ These notations are used to tell the complexity of an algorithm when the input is very large.

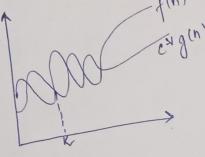
→ It describes the algorithm effect ency and performance in a meaningful way. It describes the schaviour of time or space complexity for large instance characteristics. space complexity for large instance characteristics.

· The asymptotic notation of an algorithm is classified into Etheric ento 5 types:

(i) Big Oh notation (0) : (Asymptotic upper Bound) The function f(n) = O(g(n)), if and only if there exist a + ne constant C and k such that f(n) < C* g(n) for all n

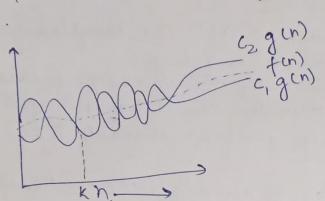


(i') Big Omega notation (SL): (A symptotic lower bound) The punction $f(n) = \Omega(g(n))$, iff there exists a +ue constant c and k such that $f(n) \ge c * g(n)$ for all $n, n \ge k$.



 $f(n) = \Omega g(n)$ iff f(n) > c.g(n) + n≥no & some const C>0.

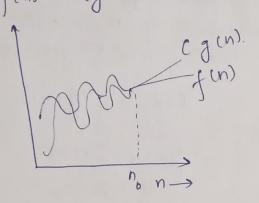
(iii) Big theta notation (0): (Asymptotic tight bound) The function f(n) = O(g(n)), iff there exists a the constant C1, C2 & K such that C1 & g(n) < f(n) < C2 & g(n) for all n, f(n) = O(g(n))



$$f(n) = O(g(n))$$

 $c,g(n) \le f(n) \le c_2 \circ g(n)$
 $+ n \ge \max(n, n_2)$

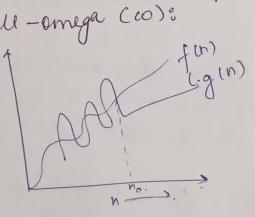
(iv) Small-oh (0):- 0 gives us upper bound. f(n) = 0 (g(n)).



$$f(n) < Cg(n)$$

 $+ n > n_0 & + c > 0$
 $n = O(n^2)$
 $n < 1 n^2$
 $2 n^2$
 $0 \le n^2$
 $n < 0.001 n^2 n_0$

(V) Small-omega (co):



former bound

$$f(n) = \omega g(n)$$

$$f(n) > c.g(n)$$

$$A n > n_0 & A C > 0$$

$$n^2 = \omega(n)$$

Time complexity for a loop means no. of times loop has

-> For the above loop, the loop will run for the following values of 1:î | 1 | 2 | 4 | 8 | 16 | 32 | ... | 2 k value 2° 2' 2² 23 24 25 ... n e=1,2,4,8,16,32,...,2k this means & times ie 2k=n K log 2 = log n $K = \log n \left(\log_2 2 = 1 \right)$ i. T. C = O(lag n) Bol3:- T(n) = (3T(n-1), n>0. By forward substitution, T(n) = 3T(n-1)T(0) = 1 T(1) = 3T(1-1)= 3 7 (0) T(2) = 3T(2-1)= 3*3 = 32 T(3) = 3T(3-1)=3T(2)= $3^{1}3^{2}=3^{3}$. $T(n) = 3^n.$

$$\frac{1}{100} = \frac{1}{100} = \frac{1}$$

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Si=Si-j+i
The value of "increases by one for each iteration. The
 value contained in's' at the ith iteration is the
Sum of the first 'i' + we integers. If k is the total no.
  of iterations taken by any program then while loop
   ter minates if : 1+2+3+...+k
       = |K(k+1)|2] > n
       40, k=0(\sqrt{n})
60. T. C = O (5n)
Sol6: uoid function (int n)
           int i, count = 0;
            for (i=1; $\delta(=n;i++) 0(n)

count++;
    Time complexity: O(n).
 Sol7:- void function (int n)
             int i, i, k, went = 0;
             for ( i = n/2 ; i <= n; i++)
               for(j=1;j(=n;j=j*2)
                                           O (logn)
                  for(k=1; k<=n; k=k*2) o(log n)
                      count ++;
         J. C = log n * log n = O(nlog2n)
          T. C = O (n log2 n)
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Sol8: - function (int n)
           if (n==1)
            return;
                                 O(n) times
           for (t=1 ton)
                                 o(n) times
              for ( = 1 ton)
                 { printf(" "") ")
         function (n-3);
  Time complexity: O(n2) ans.
sol9:- uoid function (int n)

§ for (i=1 to n) §

O(n)
           for (i=1) j < = n, j = j+1) O(n)
               printf(" * ");
    f.c = O(n) * O(n) = O(n^2)
       T. C = O(n2)
 80110: nk is O(ch) aus.
     n^k = O(c^n)
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