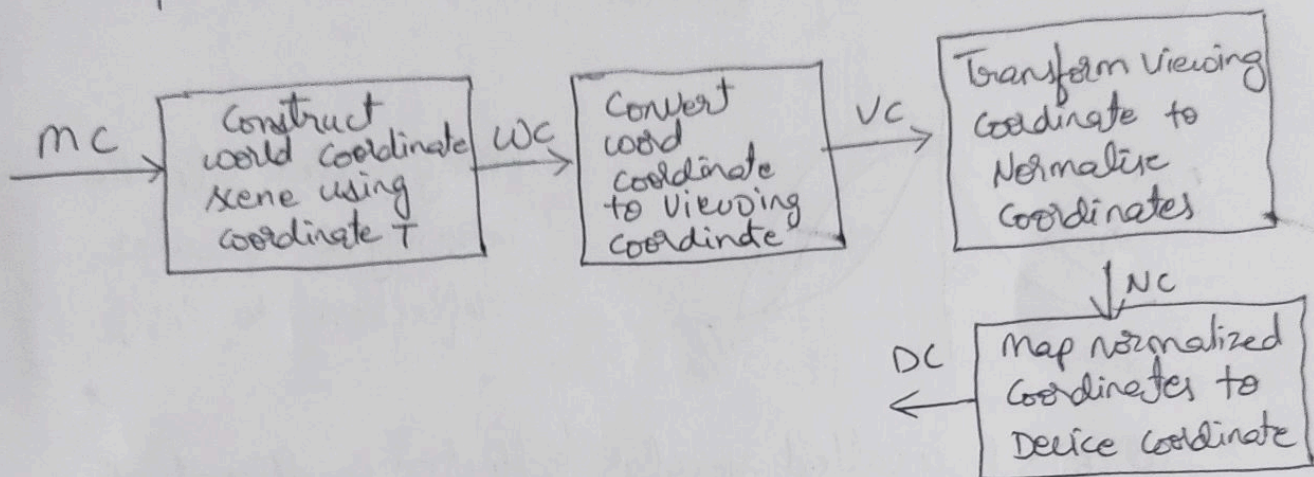


CGV ASSIGNMENT

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- ① Build a 2D viewing transformation pipeline & also explain OPEN GL 2D viewing functions



A section of 2D scene that is selected for display is called a clipping window because all parts of scene outside the selected section are "clipped off".

Depending upon graphics library, the viewport is defined in normalized coordinates (or) screen co-ordinates. At the final step of viewing transformation the contents of viewport are transferred to portions within the display window.

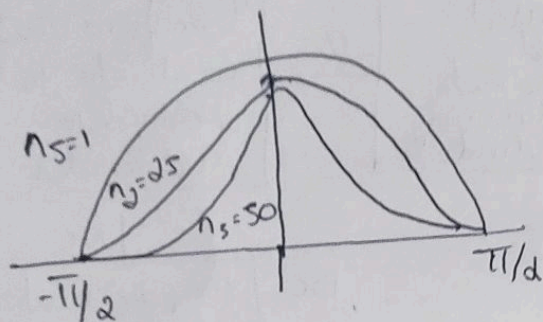
The OpenGL 2D viewing function in OpenGL projection mode. Before we should start a viewport to OpenGL.

```
glMatrixMode(GL_PROJECTION);
```

```
glViewport(xmin, ymin, Vpwidth, Vpheight);
```


2. Build phong lighting model with equations

Phong reflection is a empirical mode of local illumination. It describes the way of surface reflects light as a diffuse reflection of rough surfaces with the specular reflection of shining reflection



Phong model sets the intensity of specular reflection to $\cos^n \phi$

$0 \leq \omega(\theta) \leq 1$ is called specular reflection co-efficient of light direction & viewing direction

```
glutInitWindowPosition(xTopLeft, yTopLeft);  
glutInitWindowSize(dwidth, dheight);  
glutCreateWindow("Title of Window");
```

3. Apply homogenous co-ordinates for translation, rotation and scaling via matrix representation.

→ A standard technique for accomplish 2D (or) 3D Transformation is to expand each two-dimensional coordinate

$$\text{where } \Rightarrow x = \frac{x_h}{h}, \quad y = \frac{y_h}{h}$$

Translation

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$P' = T(t_x, t_y) \cdot P$$

Scaling

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} s_x & 0 & 0 \\ 0 & s_y & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix} \cdot P' = (s_x, s_y) \cdot P$$

$$\text{Rotation} - \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$P' = R(\theta) \cdot P$$

A Difference between raster scan display and random display

Random scan

- It has high resolution
- It is more expensive
- Easier to modify
- Solid pattern tough to fill
- Refresh rate depends on resolution
- Beam penetration technology comes under it

Raster scan

- It is low resolution
- It is less expensive
- Modification is tough
- Easy to fill solid pattern
- Does not depend on pictures
- Shadow mask technology comes under it

⑤ Demonstrate OpenGL function for display window management using GLUT

→ We perform the GLUT initialization

glutInit(&argc, argv)

Next, we can state that display window is to be created on screen

glutCreateWindow("AN Example")

The following function call paints the line segment

glutDisplayFunc (line-segment);

The function must be last one in program. It puts the scene in infinite loops that

glutMainLoop();

⑥ OpenGL Visibility functions

→ a) open GL polygon culling functions

Backface removal with function

glEnable (GL_CULL_FACE);

glCullFace (mode);

Disable with

glDisable (GL_CULL_FACE);

glutInitDisplayMode (GLUT_SINGLE | GLUT_DEPTH)

④ Route several curves that we discussed w/ perspective projection transformation coordinates.

$$x_p = x \left[\frac{z_{prp} - z_{vp}}{z_{prp} - z} \right] + x_{prp} \left[\frac{z_{vp} - z}{z_{prp} - z} \right]$$

$$y_p = y \left[\frac{z_{prp} - z_{vp}}{z_{prp} - z} \right] + y_{prp} \left[\frac{z_{vp} - z}{z_{prp} - z} \right]$$

Case 1

① Projection reference point is limited along x-view axis:

$$x_{prp} = y_{prp} = 0 ; \quad x_p = x \left[\frac{z_{prp} - z_{vp}}{z_{prp} - z} \right] ; \quad y_p = y \left[\frac{z_{prp} - z_{vp}}{z_{prp} - z} \right]$$

② when projection reference point is at co-ordinate origin

$$(x_{prp}, y_{prp}, z_{prp}) = (0, 0, 0)$$

$$x_p = x \left(\frac{z_{vp}}{z} \right) ; \quad y_p = y \left(\frac{z_{vp}}{z} \right)$$

③ If view plane is un plane:

$$z_{vp} = 0 ; \quad x_p = x \left[\frac{z_{prp}}{z_{prp} - z} \right] - x_{prp} \left[\frac{z}{z_{prp} - z} \right] \quad y_p = \left[y \right] \left[\frac{z_{vp}}{z_{prp} - z} \right]$$

④ If view plane is in un plane and definition on -

$$x_{prp} = y_{prp} = z_{vp} = 0 ; \quad x_p = x \left[\frac{z_{prp}}{z_{prp} - z} \right] - x_{prp} \left[\frac{z}{z_{prp} - z} \right]$$

$$y_p = \left[y \right] \left[\frac{z_{prp}}{z_{prp} - z} \right] - y_{prp} \left[\frac{z}{z_{prp} - z} \right]$$

⑤ Explain Bezier curve equation along with equation along with properties.

Solⁿ Generated by French engineer Pierre Bezier for use in design. It can be fitted to any number of control points.

Equation: $P_k = (x_k, y_k, z_k)$ P_k = generally $(n+1)$ control point

Position P_k = Position vector that describes path

$$P(y) = \sum_{k=0}^n P_k \cdot B_k \in \Sigma_{n,n}(Y) \quad B \in \Sigma_{n,n}(Y) \quad C_{n,k} \quad u^k (1-u)^{n-k}$$

is Bezier polynomial.

② Explain Normalization transformation for orthogonal projectors
 we assume that orthogonal projection into volume to
 mapped into symmetric normalization cube with left-handed
 reference frame. Also Z-co-ordinate position for handed
 reference frame

$$\text{Matrix, norm} = \begin{bmatrix} \frac{2}{X_{\max} - X_{\min}} & 0 & 0 & \frac{X_{\min} + X_{\max}}{X_{\max} - X_{\min}} \\ 0 & \frac{2}{Y_{\max} - Y_{\min}} & 0 & -\frac{Y_{\max} + Y_{\min}}{Y_{\max} - Y_{\min}} \\ 0 & 0 & \frac{-2}{Z_{\min} - Z_{\max}} & \frac{Z_{\min} + Z_{\max}}{Z_{\min} - Z_{\max}} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$