



Hierarchical Clustering



Hierarchical Clustering

- It is time to explore another clustering method!
- Hierarchical clustering is very common in biology and lends itself nicely to visualizing clusters.
- It can also help the user decide on an appropriate number of clusters.



Hierarchical Clustering

- Section Overview:
 - Theory and Intuition of Hierarchical Clustering
 - Coding Example of Hierarchical Clustering



Hierarchical Clustering

Theory and Intuition



Hierarchical Clustering

- Like most clustering algorithms, Hierarchical Clustering simply relies on measuring which data points are most “similar” to other data points.
- “Similarity” is defined by choosing a distance metric.



Hierarchical Clustering

- ***So why use Hierarchical Clustering?***
 - Easy to understand and visualize.
 - Helps users decide how many clusters to choose.
 - Not necessary to choose cluster amount **before** running the algorithm.



Hierarchical Clustering

- ***So why use Hierarchical Clustering?***
 - Divides points into ***potential*** clusters:
 - Agglomerative Approach:
 - Each point begins as its own cluster, then clusters are joined.
 - Divisive Approach:
 - All points begin in the same cluster, then clusters are split.



Hierarchical Clustering

- Hierarchical Clustering
 - Divides points into ***potential*** clusters:

N1

N2

N3

N4

N5

N6



Hierarchical Clustering

- Hierarchical Clustering
 - Agglomerative:

|

N1

|

N2

|

N3

|

N4

|

N5

|

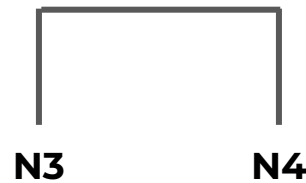
N6





Hierarchical Clustering

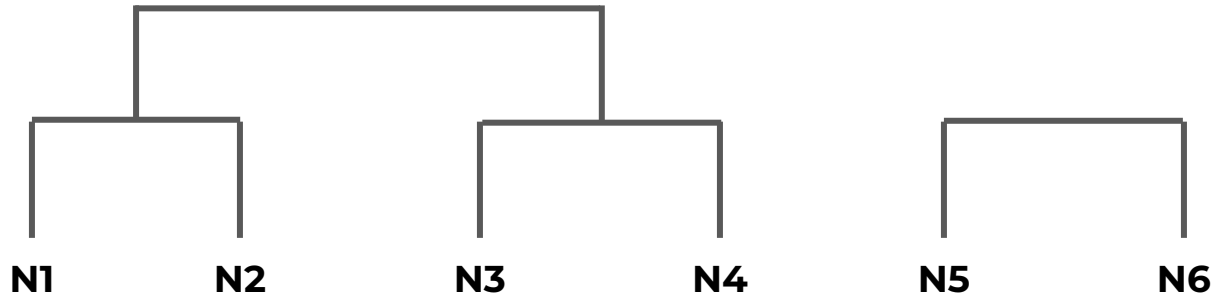
- Hierarchical Clustering
 - Agglomerative:





Hierarchical Clustering

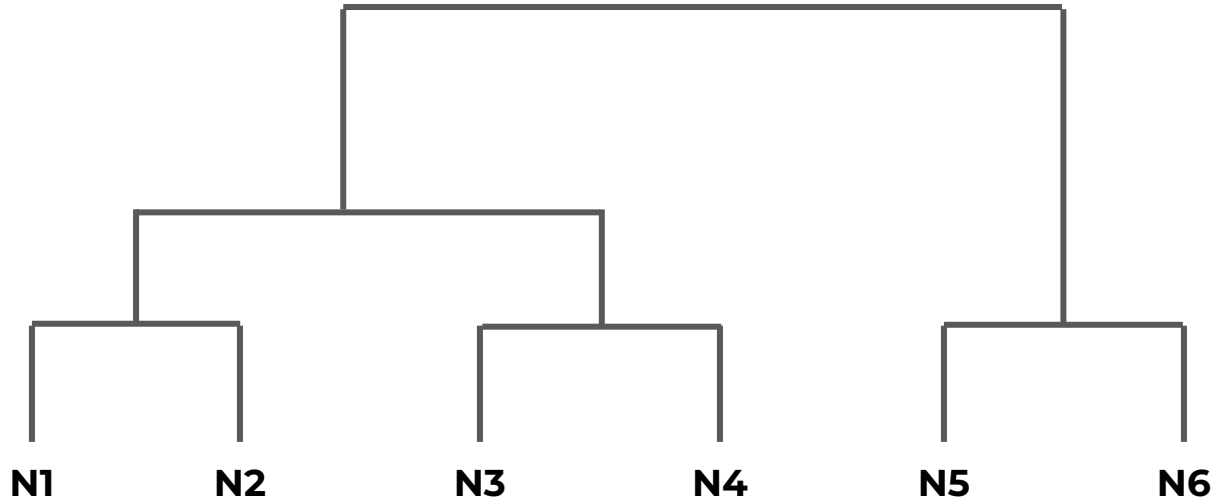
- Hierarchical Clustering
 - Agglomerative:





Hierarchical Clustering

- Hierarchical Clustering
 - Agglomerative:





Hierarchical Clustering

- Opposite of the Agglomerative approach is a **Divisive** approach, which starts with all points belonging to the same cluster, and then begins divisions to separate out clusters.



Hierarchical Clustering

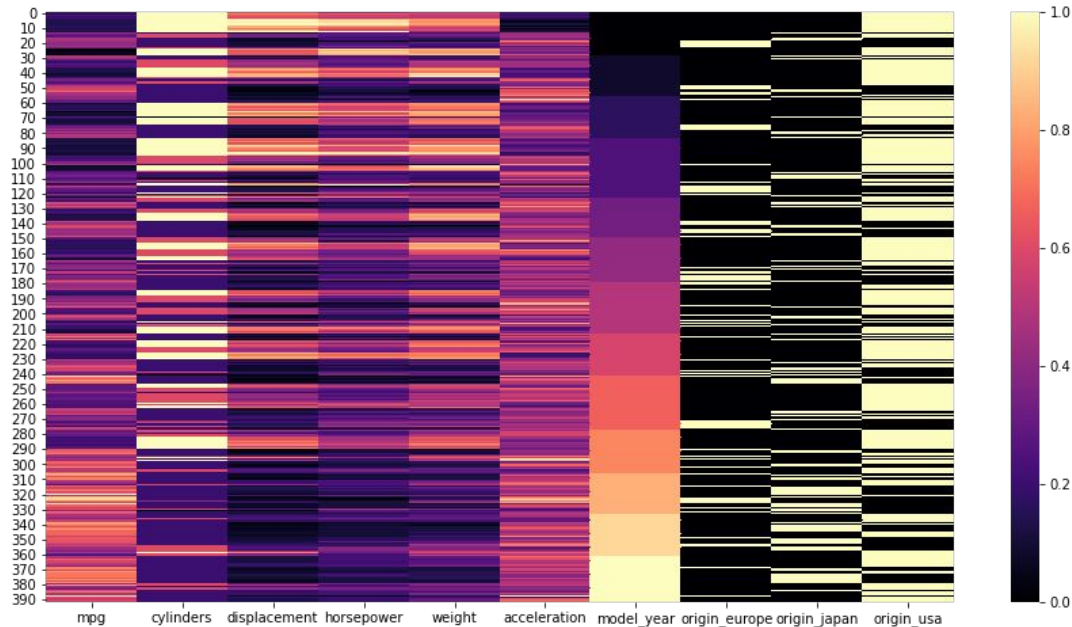
- ***Hierarchical Clustering Process***

- Compare data points to find most similar data points to each other.
- Merge these to create a cluster.
- Compare clusters to find most similar clusters and merge again.
- Repeat until all points in a single cluster.



Hierarchical Clustering

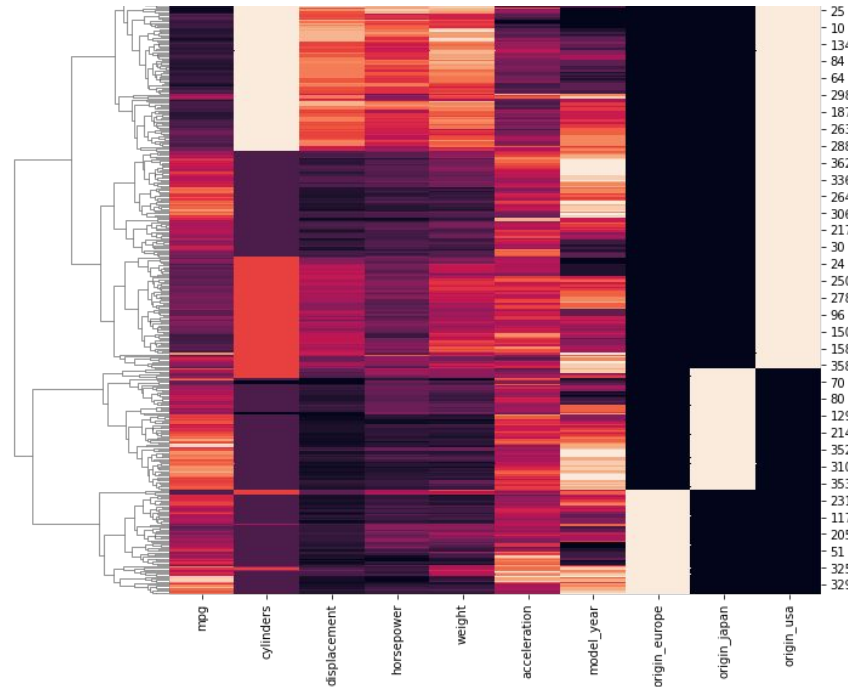
- ***Hierarchical Clustering Process***





Hierarchical Clustering

- Hierarchical Clustering Process***





Hierarchical Clustering

- There are a few key topics we still need to understand for Hierarchical Clustering:
 - Similarity Metric
 - Dendrogram
 - Linkage Matrix



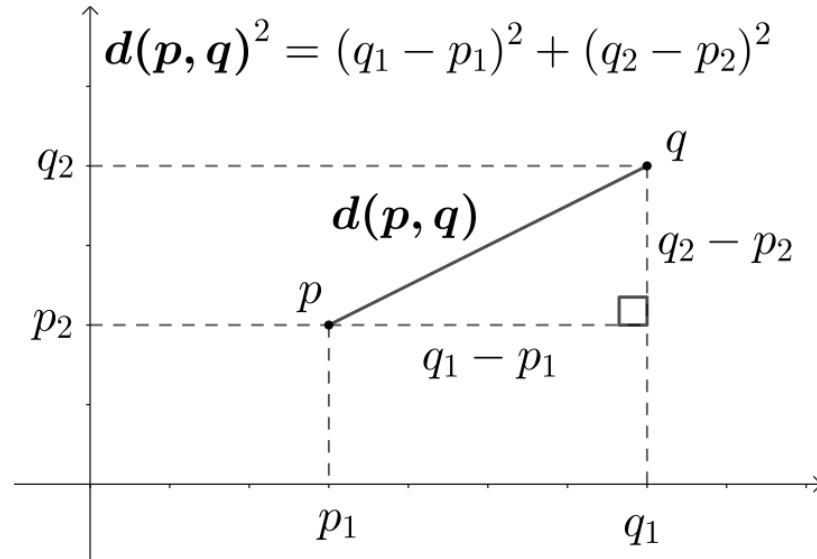
Hierarchical Clustering

- Similarity Metric
 - Measures distance between two points.
 - Many options:
 - Euclidean Distance
 - Manhattan
 - Cosine
 - and many more...



Hierarchical Clustering

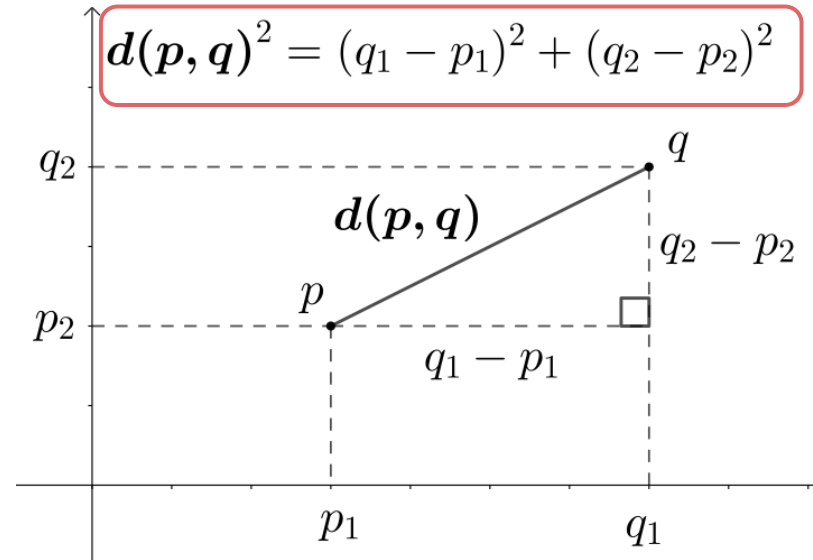
- Similarity Metric
 - Default choice is Euclidean





Hierarchical Clustering

- Similarity Metric
 - Default choice is Euclidean





Hierarchical Clustering

- Similarity Metric
 - Each dimension would be a feature
 - For **n** data points and **p** features:
 - $D^2 = (x_{11} - x_{12})^2 + \dots + (x_{n-1p-1} - x_{np})^2$



Hierarchical Clustering

- Similarity Metric
 - Each dimension would be a feature
 - For **n** data points and **p** features:
 - $D^2 = (x_{11} - x_{12})^2 + \dots + (x_{n-1p-1} - x_{np})^2$
 - Using MinMaxScaler we can scale all features to be between 0 and 1.
 - This allows for maximum distance between a feature to be 1.



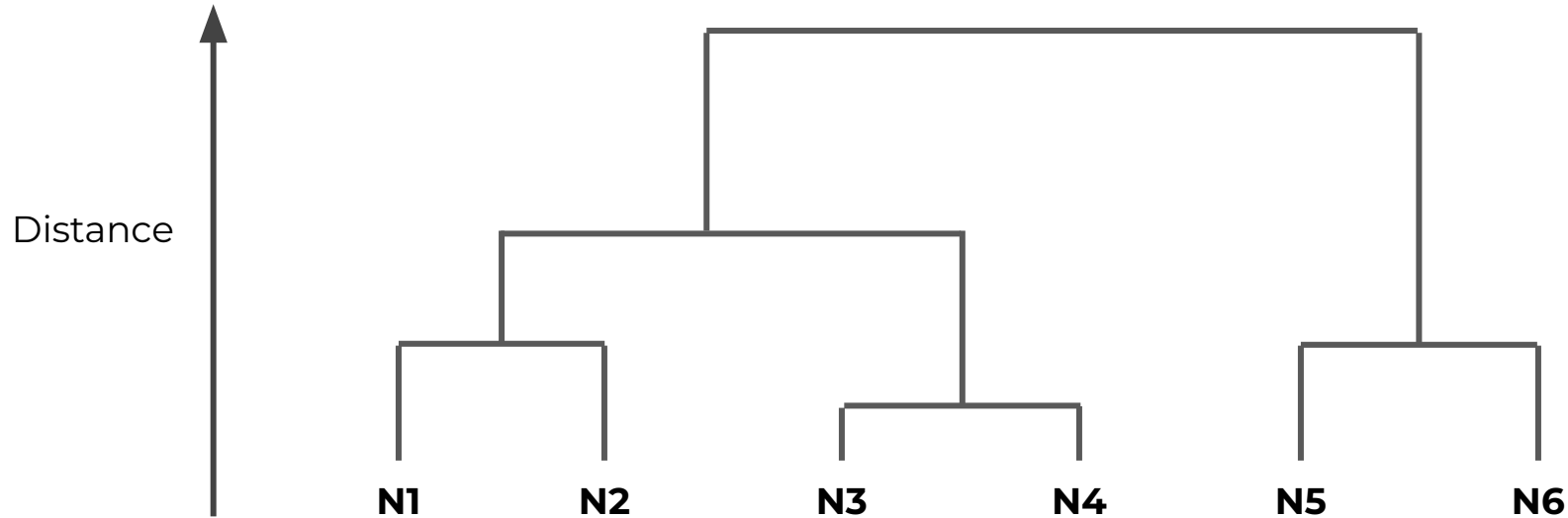
Hierarchical Clustering

- Dendrogram:
 - Plot displaying all potential clusters.
 - Very computationally expensive to compute and display for larger data sets.
 - Very useful for deciding on number of clusters.



Hierarchical Clustering

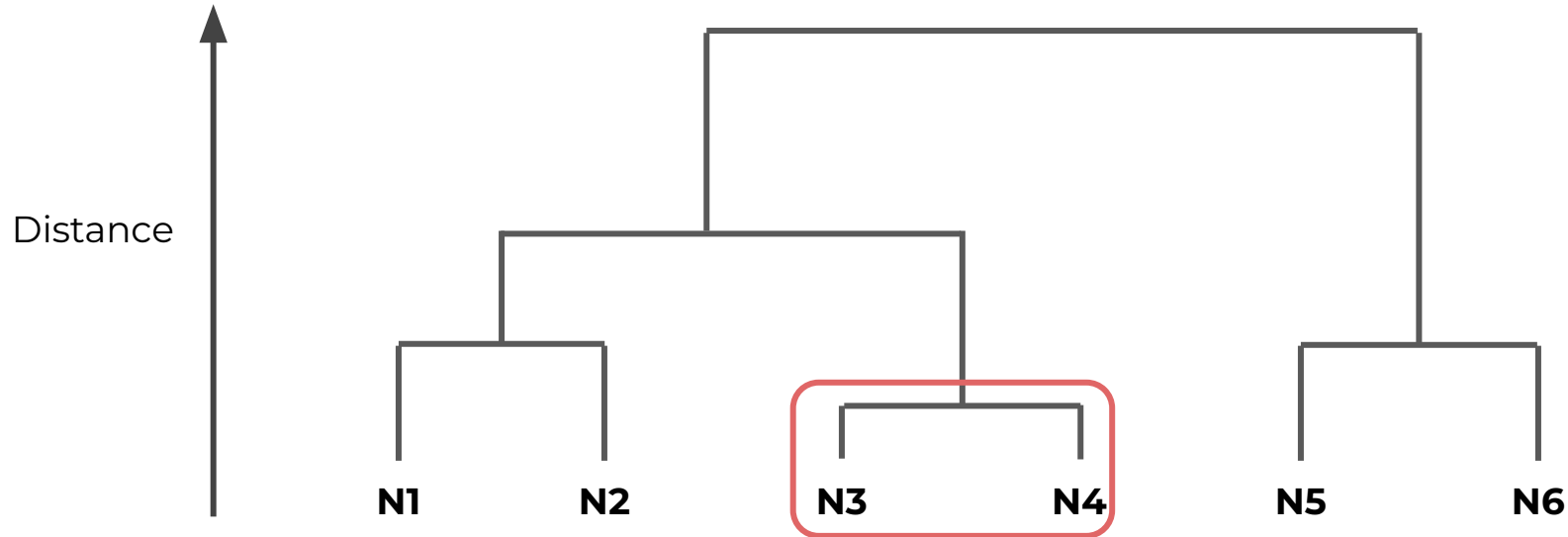
- Dendrogram:





Hierarchical Clustering

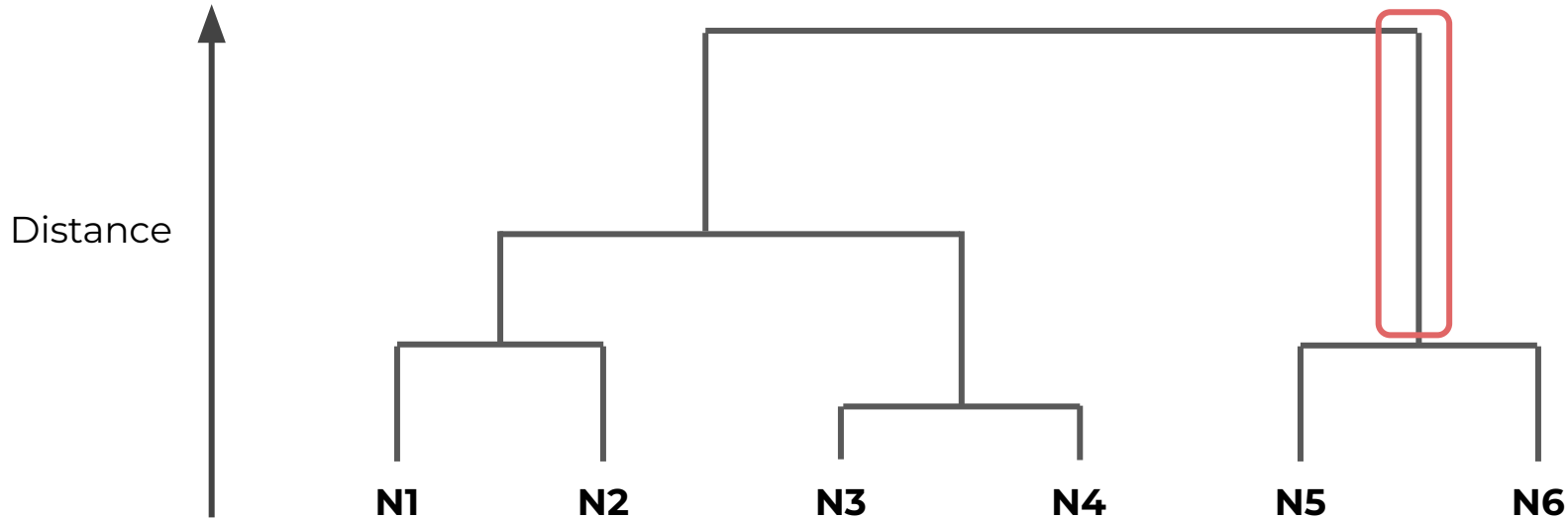
- Dendrogram:





Hierarchical Clustering

- Dendrogram:

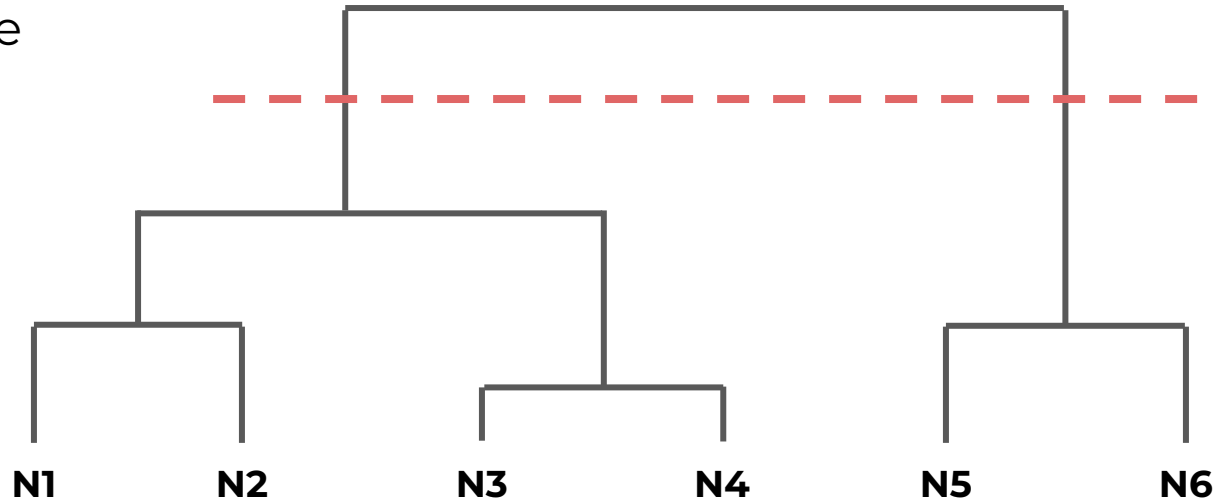




Hierarchical Clustering

- Dendrogram:

“Slice” to decide
cluster count

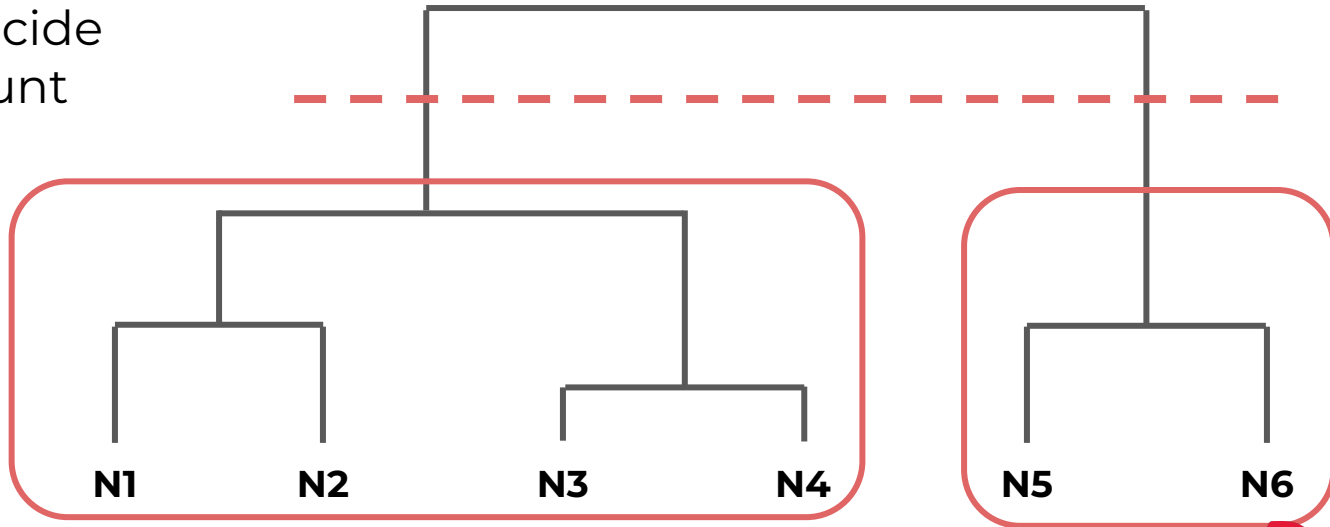




Hierarchical Clustering

- Dendrogram:

“Slice” to decide
cluster count

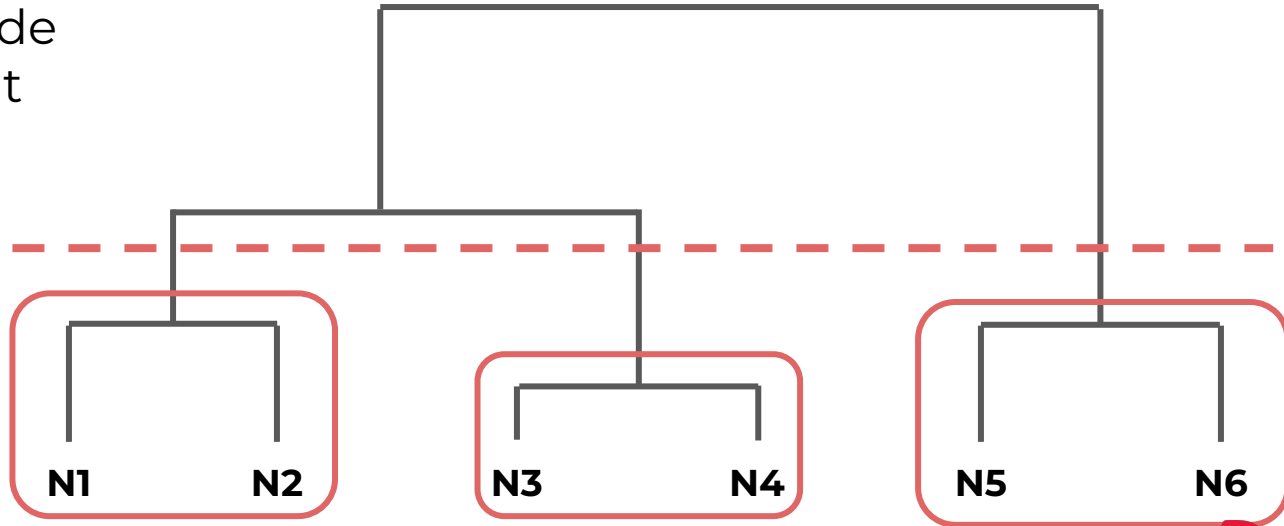




Hierarchical Clustering

- Dendrogram:

“Slice” to decide
cluster count





Hierarchical Clustering

- Linkage
 - How do we measure distance from a point to an entire cluster?
 - How do we measure distance from a cluster to another cluster?



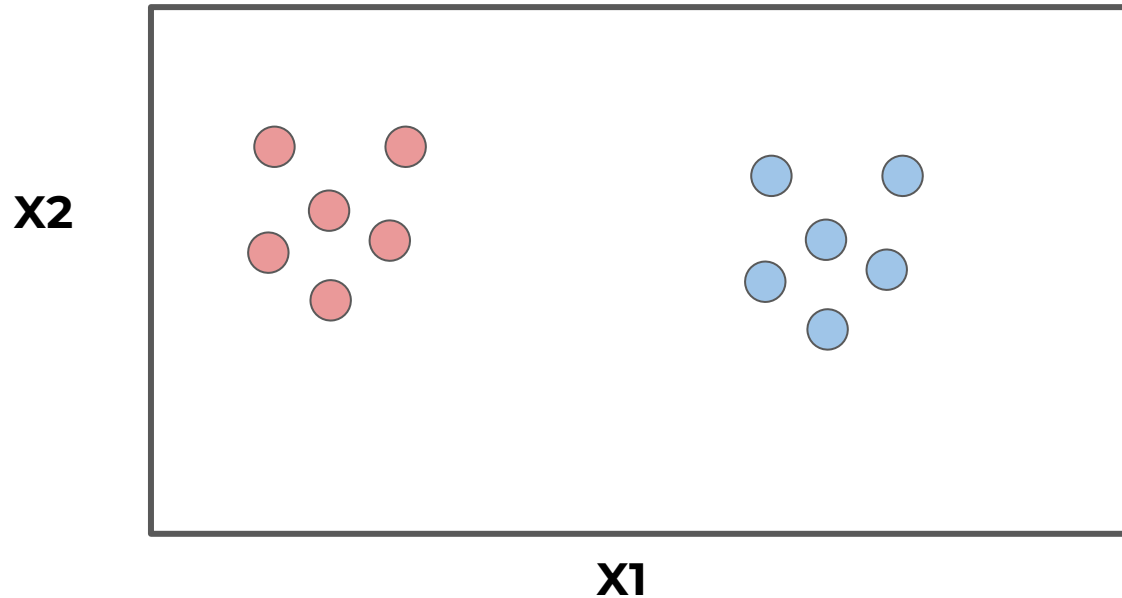
Hierarchical Clustering

- Linkage
 - Once two or more points are together and we want to continue agglomerative clustering to join clusters, we need to decide on a **linkage** parameter.



Hierarchical Clustering

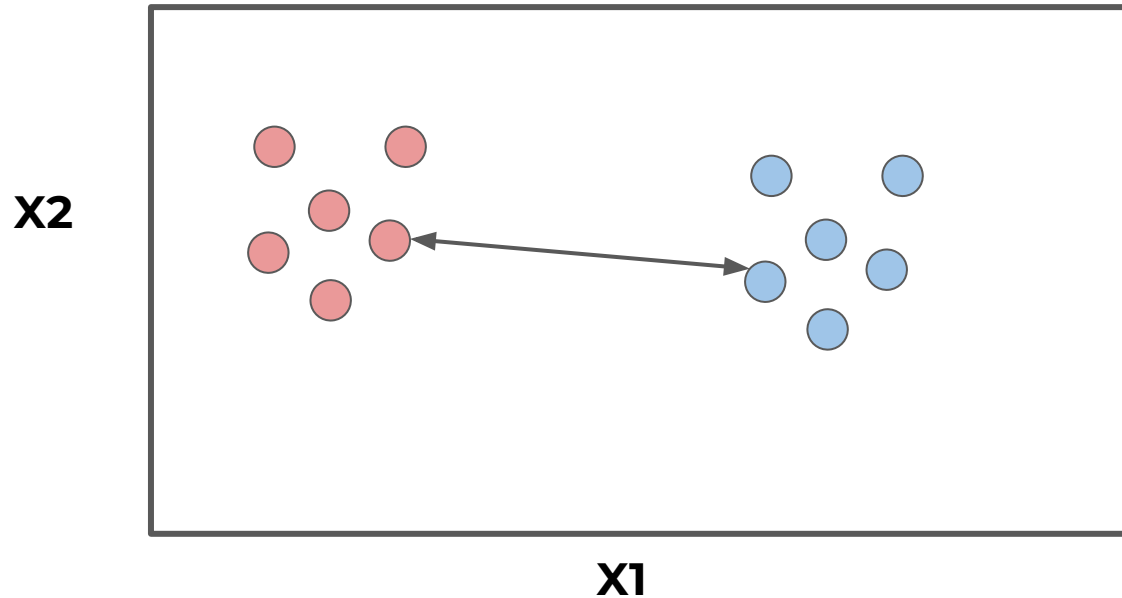
- Linkage





Hierarchical Clustering

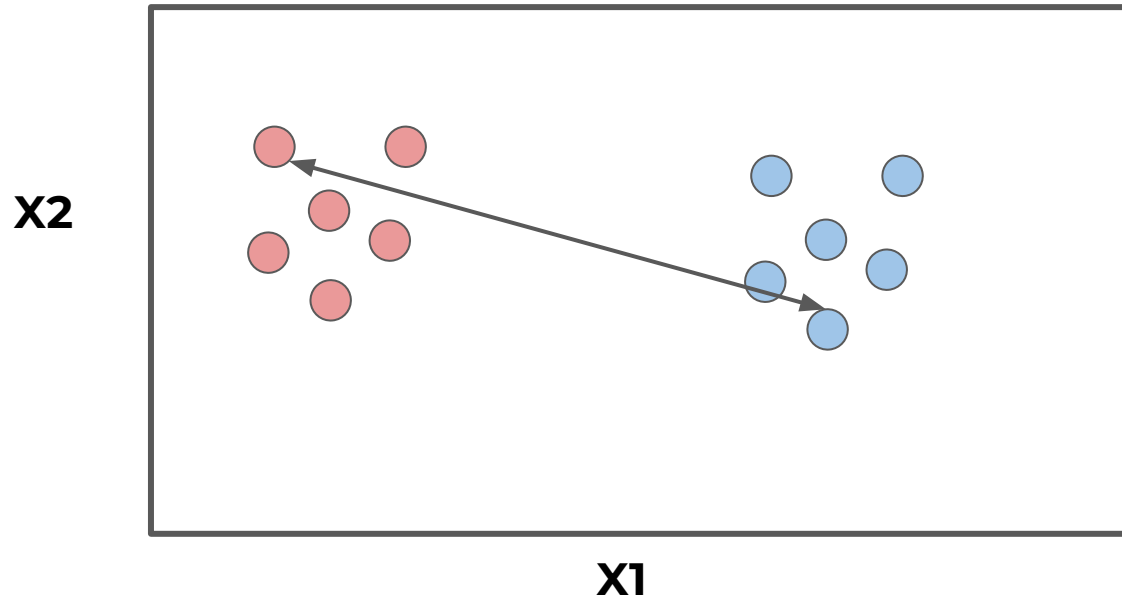
- Linkage





Hierarchical Clustering

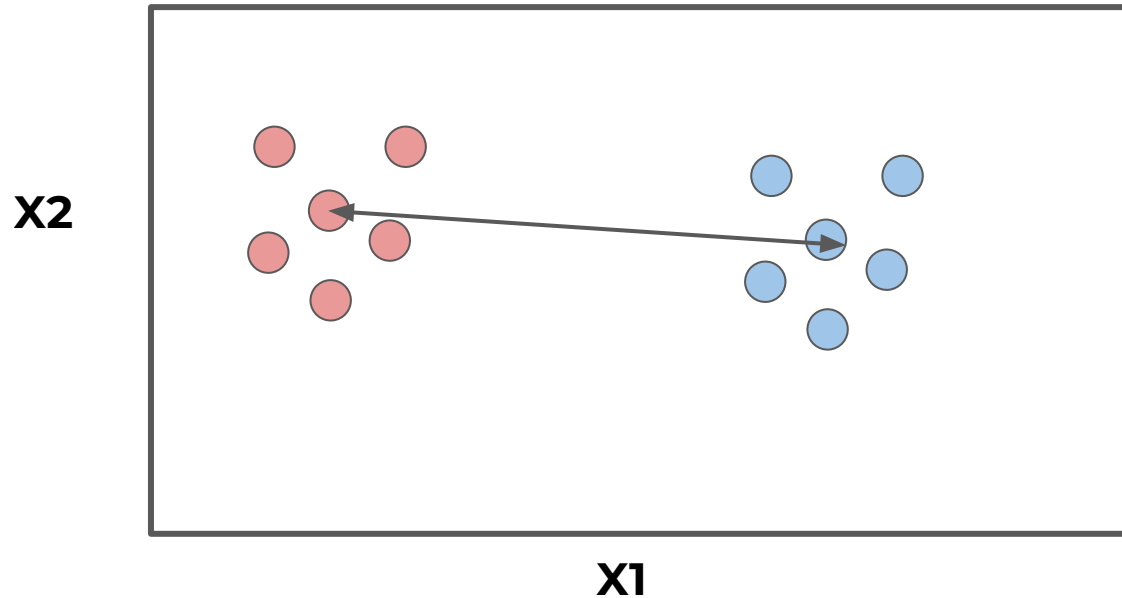
- Linkage





Hierarchical Clustering

- Linkage

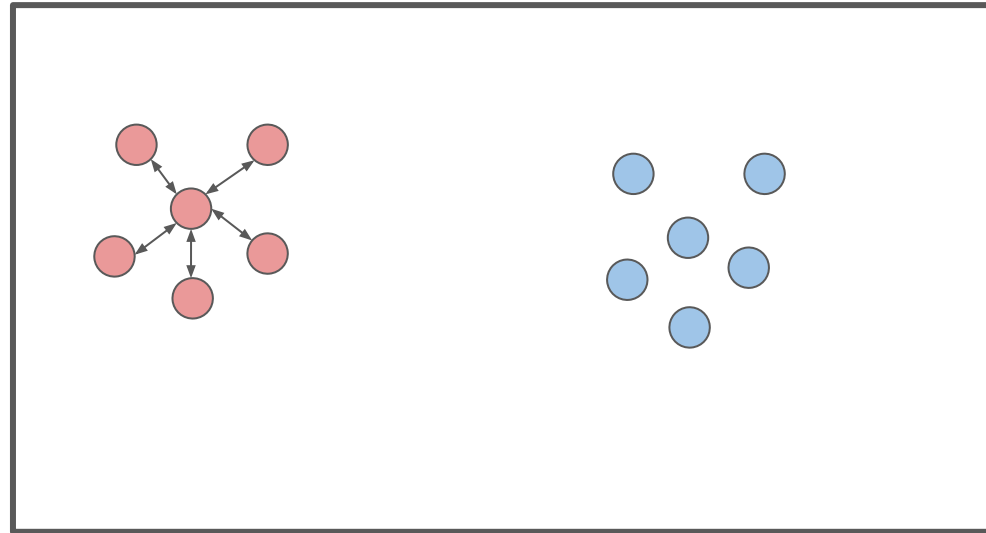




Hierarchical Clustering

- Linkage

X2



X1



Hierarchical Clustering

- Linkage
 - Criterion determining which distance to use between sets of observation.
 - Algorithm will merge pairs of clusters that minimizes the criterion.



Hierarchical Clustering

- Linkage:
 - **Ward:** minimizes variance of clusters being merged.
 - **Average:** uses average distances between two sets.
 - **Minimum** or **Maximum** distances between all observations of the two sets.