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R20 H.T.No. CMR INSTITUTE OF TECHNOLOGY: HYDERABAD

II - B. Tech. - I - Semester End Examinations - February - 2023

Discrete Mathematics & Graph Theory

[Time: 3 Hours]

(CSE, CSD, CSM, AID, AIM)

[Max. Marks: 70]

Note: 1. This question paper contains two parts A and B.

 Fart A is compulsory which carries 20 marks. Answer all questions in Part A.
 Part B consists of 5 Units. Answer any one full question from each unit. Each question carries 10 marks and may have in the part of marks and may have i, ii, iii as sub questions.

4. Illustrate your answers with NEAT sketches wherever necessary.

 $10 \times 2M = 20 M$

	PART-A			- 40	
S.No	Question	BTL	со	PO	
1	Find the duals of the following	1	1	1,2,12	
2	i) p→(q∧r) ii)pv(rvq) Explain logical NAND	2	1	1,2,12	
3	Define types of Quantifiers	1	2	1,2,12	
4	What are Free and Bounded variables with examples	1	2	1,2,12	
5	Let A and B be two finite sets such that $n(A) = 20$, $n(B) = 28$ and $n(A \cup B) = 36$, find $n(A \cap B)$.	1	3	1,2,12	
6	Let $f(x)=x+2$, $g(x)=x-2$ and $h(x)=3x$ for $x \in \mathbb{R}$, where \mathbb{R} is the set of real numbers. Find $g \circ f$, $f \circ g$	1	3	1,2,12	
7	Define sum rule and product rule.	1	4	1,2,12	
8	In how many different ways can a committee of 5 teachers and four students be selected from 9 teachers and 15 students	1	4	1,2,12	
9	Prove Handshaking Lemma with example	5	5	1,2,12	
0	Explain about planar graph and complete graph with examples	2	5	1,2,1	

PART-B

 $5 \times 10M = 50 M$

i. List all the connectives using truth tables Show that $\sim (p \leftrightarrow q) \equiv (p \lor q) \land \sim (p \land q)$ using truth	4	2	1	1,2,12
OR				
 i. Show that (~p ∧ (~q∧r)) v(q∧r)v(p∧r) = r without using truth table ii a)Change (p ↓ q) in terms of ↑ only 	2	5	1	1,2,12
 b)Change (p ↑ q) in terms of ↓ only i. Show that ~P is a valid inference from the premises ~(P∧~Q),~QvR,~R ii. Construct the PDNF of the following given formula 	2	3	2	1,2,17
	 ii. Show that ~(p↔q) ≡(p v q) ∧~(p∧q) using truth table ii. Show that (~p ∧ (~q∧r)) v(q∧r)v(p∧r) ≡ r without using truth table iii. a)Change (p ↓ q) in terms of ↑ only b)Change (p ↑ q) in terms of ↓ only ii. Show that ~P is a valid inference from the premises 	 ii. Show that ~(p↔q) ≡(p v q) ∧~(p∧q) using truth table ii. Show that (~p ∧ (~q∧r)) v(q∧r)v(p∧r) ≡ r without using truth table ii. a)Change (p ↓ q) in terms of ↑ only b)Change (p ↑ q) in terms of ↓ only i. Show that ~P is a valid inference from the premises 	 ii. Show that ~(p↔q) ≡(p v q) ∧~(p∧q) using truth table ii. Show that (~p ∧ (~q∧r)) v(q∧r)v(p∧r) ≡ r without using truth table iii. a)Change (p ↓ q) in terms of ↑ only b)Change (p ↑ q) in terms of ↓ only iii. Show that ~P is a valid inference from the premises 	 ii. Show that ~(p ↔ q) ≡(p v q) ∧~(p∧q) using truth table ii. Show that (~p ∧ (~q∧r)) v(q∧r)v(p∧r) ≡ r without using truth table iii. a)Change (p ↓ q) in terms of ↑ only b)Change (p ↑ q) in terms of ↓ only i. Show that ~P is a valid inference from the premises

	a) P v($\sim p \rightarrow (q \ v(\sim q \rightarrow r)))$ b) $[p \rightarrow (q \land r)] \land [\sim p \rightarrow (\sim q \land \sim r)]$				
	$0) [p \rightarrow (q \land r)] \land [\sim p \rightarrow (\sim q \land \sim \gamma)]$ OR				
12	\mathbf{p}	3	2	2	1,2,12
12	b) Build PDNF for (pvr) \(\lambda\) (pv~q)				
	ii. a) Using Rule CP show that $p \rightarrow (q \rightarrow r)$, $q \rightarrow (r \rightarrow s)$				
	b)Show that (x) $[P(x) \rightarrow Q(x)] \land (x) [Q(x) \rightarrow R(x)] \rightarrow (x) [p(x) \rightarrow R(x)]$			3	1,2,12
13		2	1	3	1,2,12
	ii. Let R={(1,2),(3,4),(2,2)} S={(4,2),(2,5),(3,1),(1,3)} find ROS,SOR,RO(SOR),(ROS)OR,ROR,SOS,ROROR.		1		
	OR				1 2 12
13.H	relation on X Find Transitive closure R +	1	5	3	1,2,12
	ii. Determine whether the following posets are lattices are not a)($\{1,2,3,4,5\}$, /) and b)($\{1,2,4,8,16\}$, /)				121
14.A		1		4	1,2,12
	b) How many arrangements are there for the words				
	'TALLAHASSEE so that no two A's should be adjacent?				
	ii. Explain pigeon hole principle with example				
	OR				
14.B	i. Find n if	1		4	1,2,1
	a)P (n,2)=72				
	b) $P(n,4)=42P(n,2)$ c) 2P				
	(n,2)+50=P(2n, 2)				
	ii. a) Among 20 members of a team, there are 2 wicket keepers and				
	5 howlers. In how many ways can eleven persons can be chosen to				
	include only one wicket keeper and atleast 3 bowlers.?				
	b)Suppose there are many red socks, many white socks and many				
	blue socks in a box what is the least number of socks that one				
	should take out from the box to be sure of getting a matching pair?				
	should take out from the box to be sure of getting a material grant				
.A	i. Define DFS and BFS algorithms and mention the steps	1	,	2 5	1,2,
	followed in defining algorithm.				
j	ii. Show that if a planar graph is Self dual then $ E =2 V -2$				
	OR				
	. Construct bipartite graph K3,4 and prove that K3,4 graph does not ave a Hamiltonian cycle	ot 3		1 5	1,2,
1 4	i. Select an example of a graph which is Hamiltonian but not Euler	ia			

CMR INSTITUTE OF TECHNOLOGY: HYDERABAD UGC AUTONOMOUS

 $II-B.Tech.-I-Semester\ Supply\ Examinations-February-2024$ Discrete Mathematics & Graph Theory (Common to CSE, CSD, CSM, AID, AIM)

[Max. Marks: 70] [Time: 3 Hours]

This question paper contains two parts A and B.

2. Part A is compulsory which carries 20 marks. Answer all questions in Part A.

3. Part B consists of 5 Units. Answer any one full question from each unit. Each question carries 10 marks and may have i, ii, iii as sub questions.

4. Illustrate your answers with NEAT sketches wherever necessary.

PART-A

 $10 \times 2M = 20 M$

S.No	Question	Blooms Taxonomy Level	со	PO
1	Explain about converse, inverse and contra positive of the conditional statement	2	1	1,2
2	Construct the truth table for $\neg p \leftrightarrow (q \land r)$	3	1	1,2
3	Define predicate and predicate logic?	1	2	1,2
4	Analyze and symbolize the following statements: a) all men are good b) no men are good	2	2	1,2
5	Find the sets A & B given that $A - B = \{1,2,4\} B - A = \{7,8\}$ and A U B = $\{1,2,4,5,7,8,9\}$.	1	3	1,2
6	What is set inclusion and exclusion?	1	3	1,2
7	In how many ways can 8 distinguishable balls be put in to 5 distinguishable boxes if anybox can contain more than one ball?	1	4	1,2
3	In how many different ways can a committee of 5 teachers and four students be selected from 9 teachers and 15 students	1	4	1,3
	What is complete graph?Construct K ₅	1		5 1,
	Define about walk,trail,path,cicuit,cycle?	1		5 1.

PART-B

 $5 \times 10M = 50 M$

	i. Show that $\neg (p \ V \ (\neg p \ \Lambda \ q))$ and $(\neg p \ \Lambda \ \neg q)$ are logically equivalent	2	5	1	1,2
11.A	ii. Prove the principle of Duality for the following				
	$(\neg p \lor q) \Rightarrow (\neg p \lor (\neg p \lor q)) \Leftrightarrow (\neg p \lor q)$				
	b) $(p \lor q) \land (\neg p \land (\neg p \land q)) \Leftrightarrow (\neg p \land q)$ OR				

11 1					
11.1	, find the truth value of the following: a) $(p \leftrightarrow r) \land (-q \rightarrow s)$	1	5	1	1,2
	b)[$\neg (p \land q) \lor \neg r$] $\lor [(q \leftrightarrow \neg p) \rightarrow (r \lor \neg s)]$ ii. Prove that $(\neg P \land (\neg Q \land P)) \lor (Q \land P) \lor (P \land P) \leftrightarrow P$				
	ii. Prove that $(\neg P \land (\neg Q \land R)) \lor (Q \land R) \lor (P \land R) \Leftrightarrow R$.				
12.A	i Constant				
12.A	$P \rightarrow ((P \rightarrow Q) \land \neg(\neg Q \lor \neg P)).$	6	2	2	1,2
	ii. Show that $S \vee R$ is tautologically implied by $(P \vee Q) \wedge (P \rightarrow R) \wedge (Q \rightarrow S)$.				
	OR				
12.B	i. Using the indirect method of proof, show that	2	5	2	1,2
	$P \to Q, Q \to R, \neg (P \land R), P \lor R \Rightarrow R.$				
	ii. Prove by induction 1.2.3+2.3.4+3.4.5++ $n(n+1)(n+2) = \frac{1}{4}$				
	$n(n+1)(n+2)(n+3)$, for all $n \in N$				
13.A	i. In a class of 106 students, each student studies at least one of the	1	5	3	1,2
	three subjects Maths, Physics and Chemistry. 48 of them study Maths, 51 studies Physics and 53 Chemistry. 16 studies Maths and Physics, 17				
	study Maths and Chemistry and 18 study Physics and Chemistry. Find				
	1) the number of students who exactly study two subjects				
	ii) The number of students who study all the three subjects?				
	iii)The number of students who exactly study one subjects?				
	Iv) The number of students who study Physics and Maths but not				
	Chemistry? ii. What is an Equivalence Relation. Let X={1,2,3,4} and				
	R= $\{(1,1),(1,4),(4,1),(4,4),(2,2),(2,3),(3,2),(3,3)\}$. Prove that R is an				
	equivalence relation				
	OR				
2 D	i. Let $f: R \rightarrow R$ and $g: R \rightarrow R$, where R is the set of real numbers. Find	5	3	3	1,2
3.B	fog and gof, where $f(x) = x^2-2$ and $g(x) = x+4$. Determine whether				1,2
	these functions are injective, surjective, and bijective.				
	ii.a) Select an example of a relation that is neither reflexive nor				
	irreflexive				
	b)Select an example of a relation that is irreflexive and transitive				
4.A	i. There are four bus lines between A and B and three bus lines	100		4	1,2
	between B and C.In how many ways can a man travel				
	a)by bus from A to C via B?				
	b) round trip by bus from A to C via B?				
	c) round trip by bus from A to C via B if he does not want to use a				
	bus line more than once?				
	ii. A certain question paper contains two parts A and B each containing 4				
	questions. How many different ways a student can answer 5 questions				
	by selecting atleast 2 questions from each part?				

OR					
14.B	 i. Prove the following identities: (a)C(n+1,r)=C(n,r-1)+C(n,r) (b)C(m+n,2)-C(m,2)-C(n,2)=mn ii. Determine the coefficient of (a)xyz² in the expansion of (2x-y-z)⁴ (b)a²b³c²d⁵ in the expansion of (a+2b-3c+2d+5)¹6 	5	4	1,2	

15.A	 i. Find the chromatic number for the following graph ii. a)Define graph and types of graphs with examples b)Is there a simple graph with the degree sequence {1,1,3,3,3,4,6,7} 	1		5	1,2
	OR				
15.B	i. Without constructing graph .Prove that the graph whose adjacency matrix is given by $X = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$ ii. Select an example of a graph which is Hamiltonian but not Eulerian and vice versa	5	3	5	1,2

Code	No.:	ESC-210
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CMR INSTITUTE OF TECHNOLOGY: HYDERABAD UGC AUTONOMOUS

II – B.Tech. – I Semester Supply Examinations– February – 2024 Discrete Mathematics (CSE)

[Time: 3 Hours]

[Max. Marks: 70]

Notes 1 Th

1. This question paper contains two parts A and B.

- 2. Part A is compulsory which carries 20 marks. Answer all questions in Part A.
- 3. Part B consists of 5 Units. Answer any one full question from each unit. Each question carries 10 marks and may have i, ii, iii as sub questions.
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PART-A

 $10 \times 2M = 20 M$

S.No	Question	Blooms Taxonomy Level	со	PO
1	Define Well-formed formula.	L2	1	1,2,3
2	Write the converse of the statement: "If John is a human then he is mortal"	L2	1	1,2,3
3	Define Predicate and Give an example.	L2	2	1,2,3
4	State Principal disjunctive normal form.	L2	2	1,2,3
5	State Principle of inclusion and exclusion.	L2	3	1,2,3
6	Define a Poset.	L2	3	1,2,3
7	In how many ways can 5 children arrange themselves in a ring?	L2	4	1,2,3
8	State sum rule.	L2	4	1,2,3
9	Define Euler's circuit.	L2	5	1,2,3
10	Define a planar graph and give one example.	L2	5	1,2,3

PART-B

5 X 10M = 50 M

11.A	i. Construct a truth table for the statement $(p \lor q) \land (p \to q)$.	L3	1	1,2,3
	ii. Show that $\neg (p \leftrightarrow q) \Leftrightarrow (p \land \neg q) \lor (\neg p \land q)$.	L3	1	1,2,3
	OR			1
11.B	 i. Using the statements; R: Mark is Rich, H: Mark is happy Write the following statements in symbolic form: (i) Mark is poor but happy (ii) Mark is rich or unhappy (iii) Mark is neither rich or poor (iv) Mark is poor or he is both rich and unhappy. 	L3	1	1,2,3
	ii. Construct a truth table for the statement $(Q \to P) \land (\neg P \land Q)$.	L3	1	1,2,3

2.A	Obtain the principal disjunctive and conjunctive normal forms of	1.3	2	1001
	the following formulas. $P \lor (\neg P \to (Q \lor (\neg Q \to R)))$.		2	1,2,3
2.B	OR		and the same	Printed and the second second
12.B	Symbolize the following argument and check for its validity: Every living thing is a plant or an animal. Ravi's dog is alive and it is not a plant. All animals have hearts.	L3	2	1,2,3
13.A	Hence, Ravi's dog has a heart. If there are 200 faculty members that speak French, 50 that speak Russian, 100 that speak Spanish, 20 that speak French and Russian, 60 that speak French and Spanish, 35 that speak Russian and Spanish, while only 10 speak French, Russian, and Spanish, (i)how many speak either French or Russian or Spanish? (ii) How many speak French and Russian but not Spanish.		3	1,2,3
	OR			
13.B	Let $X = \{1, 2, 3, 4\}$ and $R = \{(x, y) : x > y\}$. Draw the graph of R and also give its matrix.	L3	3	1,2,3
14.A	Find the number of non- negative integral solutions of the equation $x_1 + x_2 + x_3 + x_4 + x_5 = 20$, where $x_1 \ge 3$, $x_2 \ge 2$, $x_3 \ge 4$, $x_4 \ge 6$, and, $x_5 \ge 0$?	L3	4	1,2,3
	OR			
14.B	i. A farmer buys 3 cows, 8 pigs, and 12 goats from a man who has 9 cows, 25 pigs, and 75 goats. How many choices does the farmer have	L3	4	1,2,3
	ii. How many committees of 5 or more can be chosen from 9 people's	2 L3	4	1,2,3
15.A	Define Isomorphism in Graphs. Check whether the following graphs G_1 and G_2 are Isomorphic?	L3	5	1,2,3
	OR			
	Show that a complete bipartite graph $K_{m,n}$ is planar if and only if	L3	5	1,2

Code No.: 20-ESC-208

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11.B L Show that ((PvQ) A -(-PA(-Qv-R)))v(-PA-Q)v(-PA-R)#1

OR

12.17

Use Demorgans laws to find the negation of each statement

a) I want a car and worth a cycle

 c) I've fallen and I can't get up. b) My cat stays outside or it makes a mess d)You study or you don't get a good grade

tautology without using truthtable

CMR INSTITUTE OF TECHNOLOGY: HYDERABAD UGC ALTONOMOUS

II - B.Tech. - I - Semester Supply Examinations- AUG - 2023 Discrete Mathematics & Graph Theory

(Common to CSE, CSD, CSM, AID & AIM) Max. Marks: 70]

Time: 3 Hours

Note: This question paper contains two parts A and B

Part A is compulsory which carries 20 marks. Answer all questions in Part A

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S.No	Question	Blooms Taxonomy Level
-	Which of the following formulas are well-formed:	
	a) $(p \rightarrow q)$ b) $p \rightarrow (\neg p \lor q)$ c) $(p \rightarrow q) \rightarrow \land q$ d) $\neg (p \lor q)$	
2	Explain tautology and contradiction with examples	
	Simplify the disjunctive normal form of $PA(P\rightarrow Q)$	
4	Apply the contra positive of the statement. If n is a multiple of 12, then it is a multiple of 4.	
LA.	Design the Hasse diagram for $\{1,2,3,6\}$ at b if and only if a divides b.	
4	Define a)onto function b)one to one function	
1	Define permutations and combinations	
30	In how many ways can 8 distinguishable balls be put in to 5 distinguishable hoxes if anybox can contain more than one ball?	
٠	Define planar graph and non planar graphs with example	-
10	How many vertices does a regular graph of degree 4 with 10 edges?	-

12.B 12.A i. Construct the principal disjunctive normal form of Show that the following premises are inconsistent ii. Show that S VR is tautologically implied by (P $VQMP \rightarrow RMQ \rightarrow S$) liable for penalty, he will go bankrupt. If the bank will loan him money, he will not go bankrupt. As a matter of fact, the contract is P+((P+Q) 1-QV-P))+ valid, and the bank will loan him money. If the contract is valid, then John is liable for penalty. If John is (a) P_{\wedge} $(P \rightarrow Q)$; (b) $\neg (P \vee Q) \rightarrow (P \wedge Q)$ ii. Simplify conjunctive normal forms of o. á. 12 = 1,2,12 1,2,12

	13.8						13.4
ii. What is an Compatibility Relation ?Let X={ball bed dog let.egg} and R={(x,y)x,y\u00e1X} and xRy if x and y contain some common letter} Prove that R has Compatibility relation	13.B L Let $f(x) = x + 2$, $g(x) = x - 2$ and $h(x) = 3x$ for $x \in R$, where R is the set of real numbers. Find $g * f$, $f * g$, $f * f$, $g * g$, $f * h$, $h * g$. $h * f$ and $f * h * g$.	OR	2 2 3 5 5	diagram is lattice or not	30, 530 = (1.2, 3, 5, 6, 10, 15, 30)?Examine whether the given hasse	divisible by any of 2, 3? II. Let n be a positive integer and $5n$ be the set of all divisors of n if $n =$	i. How many natural numbers n s 1000 are not
	and and			traces and the terms and terminal to the			west
							ě.
	(_a)		and the second second				6
Service and the service and th	12						1,2,12

11.A Liffustrate all laws of logically equivalence formulas with proofs ii. Find the negations of the following statements.

~

1,2,12

PART-B

 $5 \times 10M = 50 M$

a) Ian will take a job in industry or go to graduate school

c) If the processor is fast then the printer is slow b) lames will bicycle or run tomorrow

The second of th	15.B		V.51		-	-
61 02 03	OR 15.B i. Which of the following graphs are isomorphic?	ii. Develop path matrix by using warshall's algorithm for the 0100 of 010 following matrix $A^{\#}$ 0011 1101 1100	i. Discuss about Konigsberg Bridge Problem?	II. a) If 8 people P. Q. R. S. T. U. V and W are seated around a round fable how many different circular arrangements are possible. If table how many different circular arrangements are possible of carrangements are considered the same when one can be obtained from the other by rotation? from the other by rotation? b) If 8 people P. Q. R. S. T. U. V and W are seated around a round table if P.Q.R and S are males and T.U.V and W are females, in how many arrangements do the sexes alternate.	i. How many solutions are there to the equation $x_1 + x_2 + x_3 - x_4 + x_3 = 16 \text{ where each } x_i > = 2$	i. illustrate pigeon hole principle with example? OR
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					4	
	<u>ي</u>		N			-
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CMR INSTITUTE OF TECHNOLOGY: HYDERABAD UGC AUTONOMOUS

H - B.Tech. - I -Semester Supply Examinations - AUG - 2023
Discrete Mathematics

[Time: 3 Hours]

[Max. Marks: 70]

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SVO	o Question	Blooms
		Level
Aires	Explain tautology with an example	S
2	Discuss law of duality with an example	-
w	Explain normal forms	^
	COUNTY TRANSPORTED	J
40	Discuss proof by contradiction	-
S	List out the basic operations on sets	-
6	Define bijective function with an example	
7	Explain pigeon hole principle with an example	S
0*6	Find the minimum number of students in a class to be sure that three of them are born in the same month.	44
9	Discuss planer graphs in detail	-
0	Define chromatic number.	3

PART-B

 $5 \times 10M = 50 M$

			Heatandon se	ii. Discuss in details about the importance of predicate calculus	
1,2,3	5 4 1 1.23	44	5	II B i. Show that R is logically equivalent to $P \rightarrow Q$, $Q \rightarrow R$, and P.	2
			-	OR	
ONO AMBRICA	K OL CENTRAL SCO		E-97 LTDA SERVIÇAN	ii. Discuss duality principle. Write the duality of (A \cap B) \cup C	
1,2,3		42	race a	II.A 1. Obtain DNF and CNF for the following Statements. P^(P-Q) 1 4 1 1,2,3	>