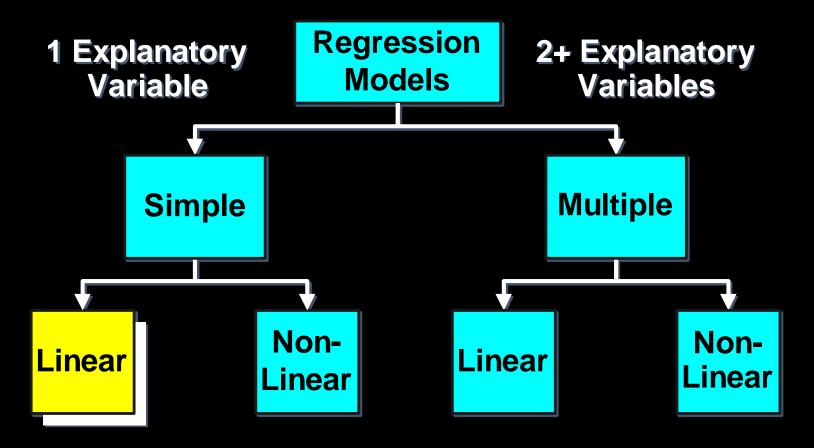
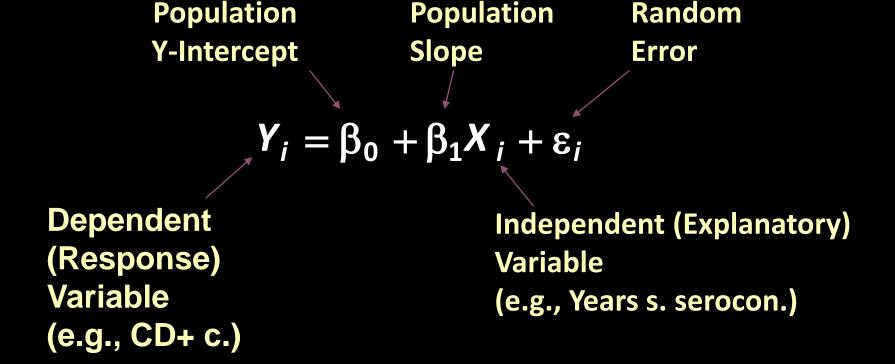
Linear Regression Model

Types of Regression Models

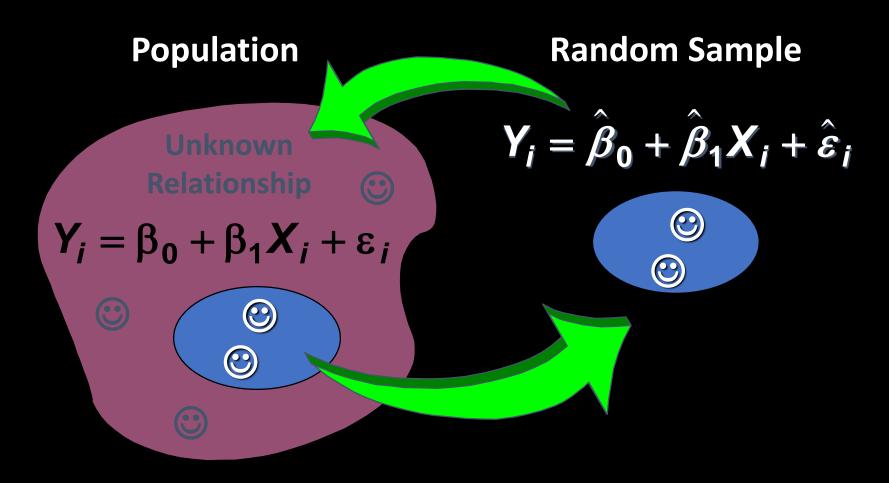


Linear Regression Model

 1. Relationship Between Variables Is a Linear Function



Population & Sample Regression Models



Estimating Parameters: Least Squares Method

Coefficient Equations

Prediction equation

$$\hat{\mathbf{y}}_i = \hat{\beta}_0 + \hat{\beta}_1 x_i$$

Sample slope

$$\hat{\beta}_1 = \frac{SS_{xy}}{SS_{xx}} = \frac{\sum (x_i - \overline{x})(y_i - \overline{y})}{\sum (x_i - \overline{x})^2}$$

Sample Y - intercept

$$\hat{\beta}_0 = \overline{y} - \hat{\beta}_1 \overline{x}$$

Parameter Estimation Example

 Obstetrics: What is the relationship between Mother's Estriol level & Birthweight using the following data?

Estriol	Birthweight (g/1000)		
(mg/24h)			
1	1		
2	1		
3	2		
4	2		
5	4		

Parameter Estimation Solution Table

Xi	Yi	X_i^2	Y_i^2	X_iY_i
1	1	1	1	1
2	1	4	1	2
3	2	9	4	6
4	2	16	4	8
5	4	25	16	20
15	10	55	26	37

Parameter Estimation Solution

$$\hat{\beta}_{1} = \frac{\sum_{i=1}^{n} X_{i} Y_{i} - \frac{\left(\sum_{i=1}^{n} X_{i}\right) \left(\sum_{i=1}^{n} Y_{i}\right)}{n}}{\sum_{i=1}^{n} X_{i}^{2} - \frac{\left(\sum_{i=1}^{n} X_{i}\right)^{2}}{n}} = \frac{37 - \frac{(15)(10)}{5}}{55 - \frac{(15)^{2}}{5}} = 0.70$$

$$\hat{\beta}_0 = \overline{Y} - \hat{\beta}_1 \overline{X} = 2 - (0.70)(3) = -0.10$$