



i) Gaussian:  $\begin{bmatrix} y^{(pr)} \\ z^{(pr)} \\ x^{(pr)} \end{bmatrix}$

$\Rightarrow E = \begin{bmatrix} \mu_p \\ \mu_r \\ \underbrace{\mu_p + \mu_r}_{\mu_p + \mu_r} \end{bmatrix}$

$Cov(y, z) = 0$  (indep.)

$Cov(x, x) = Var(\underbrace{y^{(pr)} + z^{(pr)}}_{\mu_p + \mu_r} + \epsilon^{(pr)})$   
 $= \sigma_p^2 + \tau_r^2 + \sigma^2$   
 (all indep.)

$Cov(x, y) = Cov(y + z + \epsilon, y)$   
 $= \sigma_p^2$

$Cov(x, z) = Cov(y + z + \epsilon, z)$   
 $= \tau_r^2$

$\Rightarrow \Sigma = \begin{bmatrix} y & z & x \\ y & \sigma_p^2 & 0 & \sigma_p^2 \\ z & 0 & \tau_r^2 & \tau_r^2 \\ x & \sigma_p^2 & \tau_r^2 & \sigma_p^2 + \tau_r^2 + \sigma^2 \end{bmatrix}$