

$$y \cdot \frac{1}{g(k^T x)} - (1-y) \cdot \frac{1}{1-g(k^T x)} \cdot \frac{dg(k^T x)}{dk}$$

$$\frac{d}{dk_j} \ell(k) = (y - h(x)) x_j = y \cdot x_j - h(x) \cdot x_j = y \cdot x_j - g(k^T x) x_j$$

$$\Rightarrow \frac{d}{dk_j^2} \ell(k) = - \frac{d}{dk_j} (g(k^T x) x_j)$$

$$(x, y) \begin{pmatrix} a & b \\ c & d \end{pmatrix}$$

$$= -x_j^2 \cdot \frac{d}{dk_j} g(k^T x) = -x_j^2 \cdot \frac{1}{1+e^{-k^T x}} = -x_j^2 \cdot \frac{e^{-k^T x}}{(1+e^{-k^T x})^2}$$

$$f(g(x))' = f'(g(x)) \cdot g'(x)$$

$$\frac{d}{dk_j} = -g(k^T x)(1-g(k^T x)) \cdot x_j \cdot x_j$$

$$+ \frac{1}{(1+e^{-k^T x})^2} \cdot e^{-k^T x} \cdot x \cdot x_j$$

$$H = - \sum_{i=1}^m \overbrace{h(x^{(i)}) (1-h(x^{(i)}))}^{>0} \cdot \underbrace{x^{(i)} x^{(i)T}}_{\leq 1}$$

$$= g(k^T x)(1-g(k^T x)) \cdot (-x_j)$$

$$= -x_j^2 \cdot x_j^2 \cdot g(k^T x)(1-g(k^T x))$$

$$\Rightarrow - \sum_{k=1}^m x^{(k)} \cdot x^{(k)T}$$

$$\Rightarrow - \sum_{i=1}^n \sum_{j=1}^n \sum_{k=1}^m x_i^{(k)} x_j^{(k)} z_i z_j \in \mathbb{R}^{m \times n \times n} \geq 0 \Rightarrow \leq 0$$

$$(x^T z)^2 \geq 0 \quad \text{b.c. } 1^2$$

$$x^T z \quad x^T z$$

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$$\sum_i a_{ij} x_i z_j = \sum_j x_j z_j \quad \rightarrow \text{distrib.}$$

$$\sum_{i=1}^{10} x_i \sum_{j=1}^{10} z_j$$

$$x + z$$

$$(a + b)(x + z)$$

$$= ax + az + bx + bz$$