Mass Transfer

Spring 2018

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http://www.jamescannon.net/teaching/mass-transfer

http://raw.githubusercontent.com/NanoScaleDesign/MassTransfer/master/mass_transfer.pdf

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Chapter 0

Course information

0.1 This course

This is the Spring 2018 Mass Transfer graduate course at Kyushu University.

0.1.1 What you need to do

- Borrow the book "Principles of Heat and Mass Transfer", 7th Edition, by Incropera et. al. from the Mechanical Engineering Office on the 4th floor of West 4. The course will be based on that book and you will need to refer to it in class.
- Prepare a challenge-log in the form of a workbook or folder where you can clearly write the calculations you perform to solve each challenge. This will be used in the final assessment and will be occasionally reviewed by the teacher.
- Submit a weekly feedback form by **8am on Monday** before class at https://goo.gl/forms/slmT8LNxM10vtlSs2.
- Please bring a wifi-capable internet device to class, as well as headphones if you need to access online components of the course during class. If you let me know in advance, I can lend computers and provide power extension cables for those who require them (limited number).

0.1.2 How this works

- This booklet forms part of an active-learning segment in the course. The learning is self-directed in contrast to the traditional lecture-style model.
- Learning is guided through solving a series of challenges combined with instant feedback about the correctness of your answer.
- Traditional lectures are replaced by discussion time. Here, you are encouraged to discuss any issues with your peers, teacher and any teaching assistants. You can also learn from explaining concepts to your peers.
- Discussion-time is from 10:30 to 12:00 on Mondays at room Engineering-2.
- Peer discussion is encouraged, however, if you have help to solve a challenge, always make sure you do understand the details yourself. You will need to be able to do this in an exam environment. The questions on the exam will be similar in nature to the challenges.
- Every challenge in the book typically contains a **Challenge** with suggested **Resources** which you are recommended to utilise in order to solve the challenge. **Solutions** will be given. Occasionally the teacher will provide extra **Comments** to help guide your thinking.
- For deep understanding, it is recommended to study the suggested resources beyond the minimum required to complete the challenge.
- The challenge document has many pages and is continuously being developed. Therefore it is advised to view the document on an electronic device rather than print it. The date on the front page denotes the version of the document. You will be notified when the document is updated.
- A target challenge will be set each week. This will set the pace of the course and define the examinable material. It's ok if you can't quite reach the target challenge for a given week, but you should be careful not to fall behind, since the date of the exam cannot be delayed.

0.1.3 Assessment

In order to prove to outside parties that you have learned something from the course, we must perform summative assessments. You will receive a weighted score based on:

- \bullet Challenge-log (10%) final state at the end of the course, showing your calculations for all the challenges in the course.
- Coursework (20%)
- Final exam (70%)

 $\label{eq:final score} Final\ score = MAX(Weighted\ score,\ Final\ exam)$

0.2 Timetable

	Discussion	Target	Note
1	28 May	-	
2	4 June	2.7	
3	11 June	2.13	
4	18 June		
5	25 June		
6	2 July		
-	23 July	-	Final exam

0.3 Hash-generation

Some solutions to challenges are encrypted using MD5 hashes. In order to check your solution, you need to generate its MD5 hash and compare it to that provided. MD5 hashes can be generated at the following sites:

- Wolfram alpha: (For example: md5 hash of "q1.00") http://www.wolframalpha.com/input/?i= md5+hash+of+%22q1.00%22
- www.md5hashgenerator.com

Since MD5 hashes are very sensitive to even single-digit variation, you must enter the solution *exactly*. This means maintaining a sufficient level of accuracy when developing your solution, and then entering the solution according to the format suggested by the question. Some special input methods:

Solution	Input
5×10^{-476}	5.00e-476
5.0009×10^{-476}	5.00e-476
$-\infty$	-infinity (never "infinite")
2π	6.28
i	$\operatorname{im}(1)$
2i	$\operatorname{im}(2)$
1+2i	re(1)im(2)
-0.0002548 i	im(-2.55e-4)
1/i = i/-1 = -i	im(-1)
$e^{i2\pi} \left[= \cos(2\pi) + i\sin(2\pi) = 1 + i0 = 1 \right]$	1.00
$e^{i\pi/3} = \cos(\pi/3) + i\sin(\pi/3) = 0.5 + i0.87$	re(0.50)im(0.87)
Choices in order A, B, C, D	abcd

The first 6 digits of the MD5 sum should match the first 6 digits of the given solution.

Chapter 1

Hash practise

1.1 Hash practise: Integer

X = 46.3847Form: Integer.

Place the indicated letter in front of the number. Example: aX where X=46 is entered as a46

hash of aX = e77fac

1.2 Hash practise: Decimal

X = 49

Form: Two decimal places.

Place the indicated letter in front of the number. Example: aX where X=46.00 is entered as a46.00

hash of bX = 82c9e7

1.3 Hash practise: String

X = abcdef Form: String.

Place the indicated letter in front of the number. Example: aX where X = abc is entered as aabc

and cX = 990ba0

1.4 Hash practise: Scientific form

X = 500,765.99

Form: Scientific notation with the mantissa in standard form to 2 decimal place and the exponent in

integer form.

Place the indicated letter in front of the number.

Example: aX where $X = 4 \times 10^{-3}$ is entered as a4.00e-3

and A = be8a0d

Chapter 2

Diffusion

2.1 Definition of Mass Transfer

Resources

• Chapter 14, introduction

Challenge

Add the points of the following conditions which constitute diffusive mass-transfer

1 point: Evaporation of water vapour into the air

2 points: Water being pumped through a pipe

4 points: Dissolving of sugar into tea

8 points: Aeration of waste-water

16 points: Motion of air around a room due to the presence of a fan

Solution

X = Your solutionForm: Integer.

Place the indicated letter in front of the number. Example: aX where X=46 is entered as a46

 $Hash\ of\ aX=d16142$

2.2 Diffusion in the long time limit

Resources

• Book: 14.1.1 to 14.1.2

• Video: https://www.youtube.com/watch?v=-FLv0uxLrDI

Challenge

Consider a box of volume $1\,\mathrm{m}^3$. The box contains 1 mole of gas. At time t=0, all the gas molecules in the left 1/4 of the box are labeled A. As time goes to $t=\infty$, what will the density of the molecules labeled A be in the right half of the box? Note that there is only 1 species of gas in the box.

Solution

(Units: Moles / m^3)

X = Your solution

Form: Decimal to 2 decimal places.

Place the indicated letter in front of the number. Example: aX where X = 46.00 is entered as a46.00

Hash of bX = e1f90a

2.3 Definitions of quantities I

Resources

• Book: 14.1.1 to 14.1.2

• Video: https://www.youtube.com/watch?v=-FLvOuxLrDI

Challenge

Assuming air is made up exclusively of oxygen and nitrogen with their partial pressures in the ratio 0.21:0.79, what are their mass-fractions?

Solutions

Oxygen: 0.233 Nitrogen: 0.767

2.4 Definitions of quantities II

Resources

• Book: 14.1.1 to 14.1.2

• Video: https://www.youtube.com/watch?v=-FLvOuxLrDI

Challenge

Japan imports substantial amounts of LNG which is a mixture of the following gases:

Liquid	Mol %
Methane	93.5
Ethane	4.6
Propane	1.2
Carbon dioxide	0.7

The masses of Methane, Ethane, Propane and Carbon Dioxide are 16, 30, 44 and 44 g/mol respectively.

Assuming ideal gases, calculate the following:

- 1. The mole-fraction of ethane
- 2. The mass-fraction of ethane
- 3. The average molecular mass of the mixture
- 4. The mass-density of the gas when heated to 207 K under a total pressure of 1.4×10^5 Pa
- 5. The partial pressure of the methane when the total pressure is $1.4 \times 10^5 \,\mathrm{Pa}$

Solutions

1.

X = Your solution

Form: Decimal to 3 decimal places.

Place the indicated letter in front of the number. Example: aX where X = 46.000 is entered as a46.000

Hash of cX = bf4ce8

2.

X = Your solution

Form: Decimal to 3 decimal places.

Place the indicated letter in front of the number. Example: aX where X = 46.000 is entered as a 46.000

Hash of dX = d34e49

3. (Units: g/mol)

X = Your solution

Form: Decimal to 2 decimal places.

Place the indicated letter in front of the number. Example: aX where X=46.00 is entered as a46.00

Hash of eX = 6b58f1

4.

 $1397 \, \mathrm{kg} \, \mathrm{m}^{-3}$

5. (Units: kPa) X = Your solutionForm: Integer.

Place the indicated letter in front of the number. Example: aX where X=46 is entered as a46

 $Hash\ of\ fX=4d1d94$

2.5 Mass diffusivity

Resources

 \bullet Book: 14.1.3 - 14.1.4, Table A-8

Challenge

Estimate the mass diffusivity of the following gases in air at $350~\mathrm{K}$ and $1~\mathrm{atm}$ pressure:

- 1. Ammonia
- 2. Hydrogen

Solutions

- 1. $3.6 \times 10^{-5} \,\mathrm{m}^2 \,\mathrm{s}^{-1}$
- 2. $5.2 \times 10^{-5} \,\mathrm{m}^2 \,\mathrm{s}^{-1}$

2.6 Cases of diffusion

Resources

• Book: 14.1.3 - 14.1.4

Challenge

Considering air as a mixture of two gases $(O_2 \text{ and } N_2)$, situated in a closed, cylindrical container with its axis vertical and with opposite ends maintained at different temperatures. Assume the total pressure of the air is uniform throughout the container.

Consider each of the following conditions:

- A) The bottom surface is colder than the top surface
- B) The top surface is colder than the bottom surface
- 1. Add the points for the following true statements:
- 1 point There is motion of the air in case (A)
- 2 points There is no motion of the air in case (A)
- 4 points There is motion of the air in case (B)
- 8 points There is no motion of the air in case (B)
- 16 points There is diffusive mass transfer inside the cylinder in case (A)
- 32 points There is no diffusive mass transfer inside the cylinder in case (A)
- **64 points** There is diffusive mass transfer inside the cylinder in case (B)
- 128 points There is no diffusive mass transfer inside the cylinder in case (B)
- 2. Explain your reasoning

Solutions

1.

X = Your solutionForm: Integer.

Place the indicated letter in front of the number. Example: aX where X=46 is entered as a46

Hash of gX = 389975

2.

Please compare your answer with your partner in class.

2.7 Diffusion coefficient equivalency

Resources

• Video: https://www.youtube.com/watch?v=NTlR18NyqAE

${\bf Challenge}$

Prove that in a binary mixture, the diffusion coefficient of gas "A" in "B" is the same as the diffusion coefficient of gas "B" in "A" (ie, $D_{AB} = D_{BA}$).

2.8 Column evaporation derivation

Resources

• Book 14.2

Challenge

Starting from basic knowledge of absolute flux in terms of both diffusion and advection:

$$N_A'' = -CD_{AB}\Delta x_A + x_A N_A'' \tag{2.1}$$

show that evaporation in a stationary column (figure 14.2 in the book) can be given by

$$N_A'' = \frac{CD_{AB}}{L} ln\left(\frac{1 - x_{A,L}}{1 - x_{A,0}}\right)$$
 (2.2)

where $x_{A,L}$ and $x_{A,0}$ are the molar fractions at the top and bottom the column, respectively.

Solution

Compare your answer with your partner

2.9 Saturated water vapour pressure

Resources

- http://www.chemguide.co.uk/physical/phaseeqia/vapourpress.html
- https://sciencing.com/water-vapor-pressure-vs-humidity-19402.html

Challenge

- 1) Write a few sentences briefly explaining what is meant by "Saturated Vapour Pressure" and how it is related to "Relative humidity".
- 2) Considering an air-water interface at equilibration, if the relative humidity is 50% and the saturated water density is $0.02 \,\mathrm{kmol}\,\mathrm{m}^{-3}$, what is the density of water vapour near the interface? In addition to a numerical answer, explain in a few words the reasoning behind your answer.
- **3)** Under the same conditions as part (2), what is the mole-fraction of water vapour above the surface? In addition to a numerical answer, explain in a few words the reasoning behind your answer.
- 4) Considering the saturation pressure of water is 0.03 atm, what is the mole-fraction of water vapour in the air at 1 atm?

Solution

1)

Compare your answer with your partner.

2)

(Units: $kmol m^{-3}$) X = Your solution

Form: Decimal to 2 decimal places.

Place the indicated letter in front of the number. Example: aX where X=46.00 is entered as a46.00

Hash of aX = 9bb791

Compare your reasoning with your partner.

3)

X = Your solution

Form: Decimal to 2 decimal places.

Place the indicated letter in front of the number. Example: aX where X = 46.00 is entered as a46.00

Hash of bX = 06ac46

Compare your reasoning with your partner.

4)

X = Your solution

Form: Decimal to 2 decimal places.

Place the indicated letter in front of the number. Example: aX where X=46.00 is entered as a46.00

Hash of cX = f2a860

2.10 Evaporation through a pore

Resources

 \bullet Book 14.2

Challenge

In your challenge log, work through example 14.2 (you do not need to include the "comments" part in your challenge log).

2.11 Evaporation pan

Resources

• Book 14.2, Table A-8

Challenge

Evaporation pans like the one shown are used to measure the rate of evaporation of water in a local area.



(image: Bidgee, Wikipedia)

An evaporation pan is placed in a location with an ambient air temperature of $298\,\mathrm{K}$ and relative humidity of 25%. The pan contains water at the same temperature as the surrounding air. The pan has a diameter of $20\,\mathrm{cm}$ and height of $160\,\mathrm{mm}$, and it starts half-full of water.

- 1. Assuming only diffusive mass transport, what is the initial evaporation rate?
- 2. Including the effects of advection, what is the initial evaporation rate?

(The saturation pressure of water at 298 K is 0.035 31 bar, and its specific volume at an atmospheric pressure of 1 atm is $39.13\,\mathrm{m}^3\,\mathrm{kg}^{-1}$.)

Solution

- 1. $1.087 \times 10^{-8} \,\mathrm{kmol}\,\mathrm{s}^{-1}$
- 2. $1.116 \times 10^{-8} \,\mathrm{kmol}\,\mathrm{s}^{-1}$

2.12 Stationary Medium

Resources

• Video: https://www.youtube.com/watch?v=F0deXOH_YEM

Challenge

- 1. Briefly explain what is meant by a stationary medium.
- 2. Considering a stationary medium of 3 species "A", "B" and "C" with equal molar concentration, if the flux of species "A" is $2 \,\mathrm{kmol}\,\mathrm{m}^{-2}\,\mathrm{s}^{-1}$ and "B" is $-8 \,\mathrm{kmol}\,\mathrm{m}^{-2}\,\mathrm{s}^{-1}$, what is the flux of species "C"?
- 3. Considering a binary system of atoms "A" and "B" with concentration $5\,\mathrm{kmol}\,\mathrm{m}^{-3}$ and $10\,\mathrm{kmol}\,\mathrm{m}^{-3}$ respectively, if the molar velocity of species "A" is $2\,\mathrm{m}\,\mathrm{s}^{-1}$, what is the molar velocity of species "B"?

Solutions

1.

Please compare your answer with your partner.

2.

(Units: $kmol m^{-2}$) X = Your solutionForm: Integer.

Place the indicated letter in front of the number. Example: aX where X=46 is entered as a46

Hash of gX = 4a4314

3.

(Units: $m s^{-1}$) X = Your solution

Form: Decimal to 2 decimal places.

Place the indicated letter in front of the number. Example: aX where X=46.00 is entered as a46.00

 $Hash\ of\ hX=5ba818$

2.13 Stationary Medium Approximation

Resources

• Book 14.3

Challenge

In a few sentences, describe what is meant by the stationary medium approximation. Give at least one real-world example each of case where the stationary medium approximation would and would-not be appropriate.

Solution

Compare your answer with your partner