Data Structure Homework 2

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Question 1 (a)

Please show the content in the representation for a polynomial ADT
by storing the two polynomials in the same array.

$a(x) = 4x^6 + 2x^3 + 2x^2 + 3 \;\; b(x) = 100x^{80} - 2x^3 + 5x^2$

Answer

	start A			end A	start B		end B
index	0	1	2	3	4	5	6
coef	4	2	2	3	100	-2	5
expon	6	3	2	0	80	3	2

Question 1 (b)

How many times of the switch instruction within the while loop will be executed by using the padd() function to add the above two polynomials a(x) and b(x)? Please explain your answer.

Answer

According to the padd() function in the picture,
we can see that it will keep attaching the highest exponents which hasn't been attached between $a(x)$ and $b(x)$.

We can see the switch 0 :
It will attach both $a(x)$ and $b(x)$ if the highest exponents of $a(x)$ and $b(x)$ is same.

On the other hand, if the highesting exponents of $a(x)$ and $b(x)$ is different, it will attach the higher one.

We can see that how the while loop end is when one of the $f(x)$ is completely attached to new matrix.

Therefore, the total execute time will depends on the amounts of terms in $D(x)$ ($D(x) = a(x) + b(x)$)
which $\geq max(smallest_{exponent}a(x), smallest_{exponent}b(x))$

The remaining terms will be execute after the while loop.

For example :

if $a(x) = 4x^3 + 2x^2 + x$, $b(x) = 3x^3 + 3x^2 + 3$ then the
$max(smallest_{exponent}a(x), smallest_{exponent}b(x))$ will be 1 since the smallest exponent of $a(x) = 1$, $b(x) = 0$

According to my conclusion above, the total execute time will be the amounts of exponents which ≥ 1 The amounts of exponents which ≥ 1 is 3

Question 2 (a)

i	row_terms[i]	starting_row position
0	1	0
1	2	1
2	3	3
3	2	6

result array
B(T)

	row	col	val
b(t)[0]	4	7	8
b(t)[1]	0	2	2
b(t)[2]	1	0	1
b(t)[3]	1	5	1
b(t)[4]	2	2	-1
b(t)[5]	2	5	2
b(t)[6]	2	6	1
b(t)[7]	3	0	1
b(t)[8]	3	2	1

Question 2 (b)

result

	row	col	val
arr[0]	5	4	10
arr[1]	0	1	1
arr[2]	0	3	1
arr[3]	1	0	2
arr[4]	1	1	-1
arr[5]	1	2	-3
arr[6]	1	3	1
arr[7]	3	0	8
arr[8]	3	2	-2
arr[9]	3	3	4
arr[10]	4	2	4

Question 2(c)

Initially, row_begin is set to be 1. Before row_begin is assigned a new value, how many times of the instruction “i = row_begin;” is executed for the given example?

4 times. Since there are four columns in B which has nonzero elements.

If the matrix A is a m * n matrix and matrix B is a n * k matrix, how many times of the instruction “i = row_begin;” is executed?

Since the question does not imply "Before row_begin in assigned a new value", therefore, the answer = numbers of rows in A which has nonzero element * number of cols in B which has nonzero element.

Question 2(d)

How many times of the instruction “row_begin = i;” is executed for the given example?

4 times. Since there are four rows in A which has nonzero elements.

If the matrix A is a m * n matrix and matrix B is a n * k matrix, how many times of the instruction “row_begin= i;” is executed?

The number of rows in A which has nonzero elements. So $max = m, min = 0$