

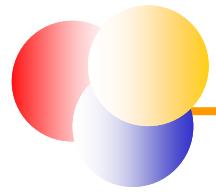


# Software Metrics

## Lecture 2

# Measurement Theory

Yuming Zhou



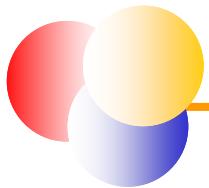
# What is Measurement?

- **Measurement** is the process by which *numbers* or *symbols* are assigned to *attributes* of *entities* in the real world in such a way as to ascribe them according to *defined rules*

$$entity = \left\{ \begin{array}{ll} attribute_1 & (value_{11}, value_{12}, \dots) \\ attribute_2 & (value_{21}, value_{22}, \dots) \\ \dots & \dots \\ attribute_n & (value_{n1}, value_{n2}, \dots) \end{array} \right\}$$



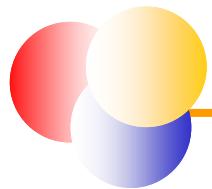
# What are Metrics and Software Metrics?



- **Metrics** are standards (i.e., commonly accepted scales) that define measurable attributes of entities, their units and their scopes
- **Software metrics** are metrics that are used to quantify:
  - Software product
  - Software development resources
  - Software development process



# Why Use Software Metrics?



- We use them to derive a basis for estimation
- To track project progress
- To determine complexity
- To help us to understand when we have achieved a desired state of software quality
- To analyze our defects

They help us to understand, control  
and improve software!!!



# 什么是一个“好”的软件度量

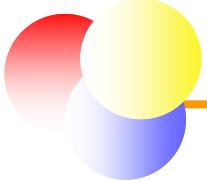
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- A. Meneely, et al. [Validating software metrics: a spectrum of philosophies](#). ACM TOSEM 2012
- L. Briand, et al. [Property-based software engineering measurement](#). IEEE TSE 1996
- B. Kitchenham, et al. [Towards a framework for software measurement validation](#). IEEE TSE 1995
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# 什么是一个“好”的软件度量





# Contents

- ▶ **The Process of Measurement**
- ▶ **Measurement Scales**
- ▶ **Scale Types**
- ▶ **Meaningfulness in Measurement**



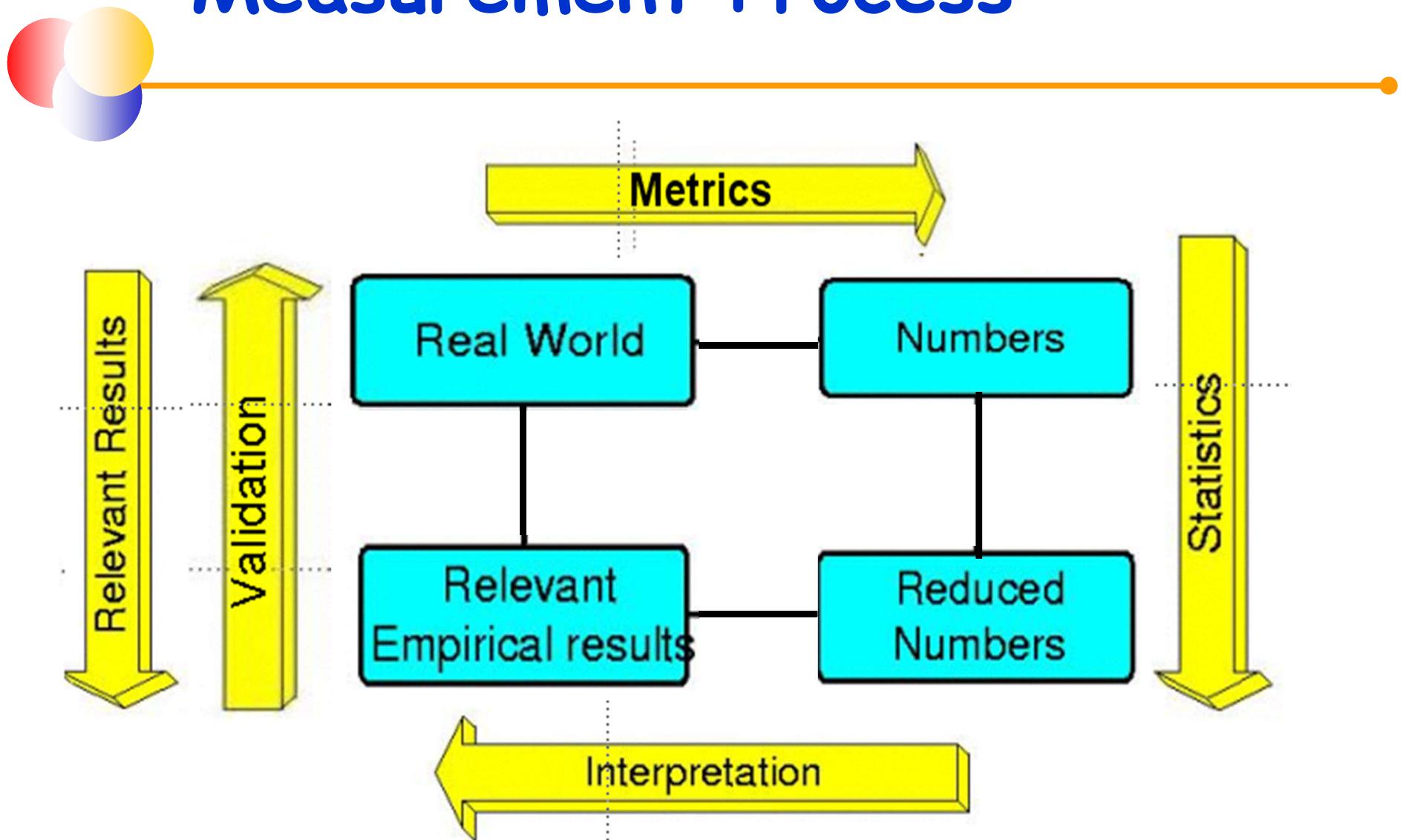
# Section 1

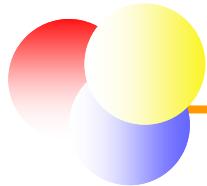
## The Process of Measurement

- 
- **Measurement Process**
  - **Key Problems**
  - **Key Stages of Measurement**

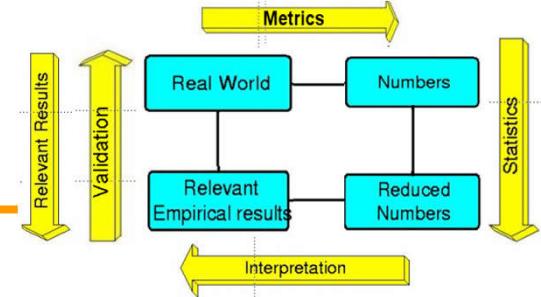


# Measurement Process



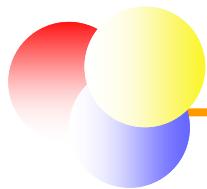


# Key Problems

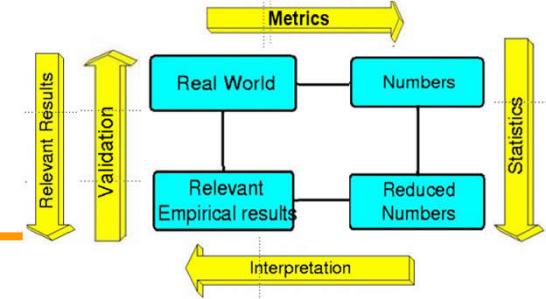


- **How much must we know about an attribute before it is reasonable to consider measuring it?** For example, do we know enough about “size” of Web sites to be able to measure it? Or “complexity” of programs?
- **What meaningful operations can we perform on metrics?** For example, does it make sense to calculate the average productivity for a group of developers, or the average quality of a set of Web sites?



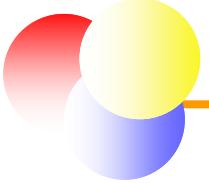


# Key Problems (cont.)



- **Using measurement, what meaning statements can we make about an attribute and the entities that posses it?** For example, is it meaningful to talk about doubling a design's quality? If not, how do we compare different designs?
- **How do we know if we have really measured the attribute we wanted to measure?** For example, does the count of the number of “broken links” found on a Web site during integration testing measure the quality of the site? If not, what does the count tell us?





# How to Answer These Problems

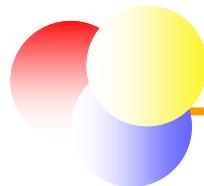
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To answer these questions, we must establish  
the basics of a theory of measurement

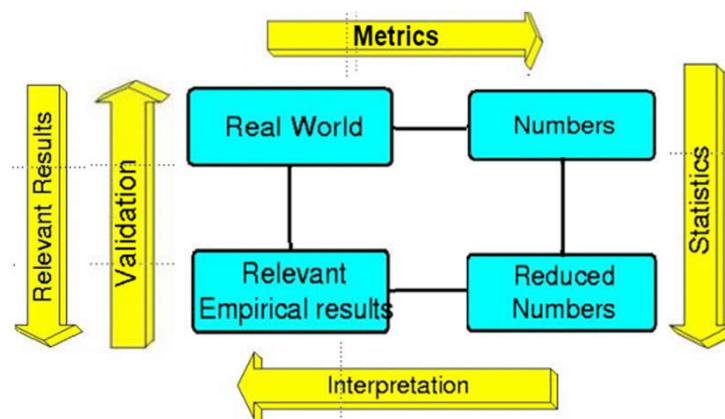
- Measurement Theory
  - Tells us the rules to be applied
- Why Rules?
  - to be consistent in our measurement
  - to provide a basis for interpreting data
- The measurement theory we'll use is the Representational Theory of Measurement



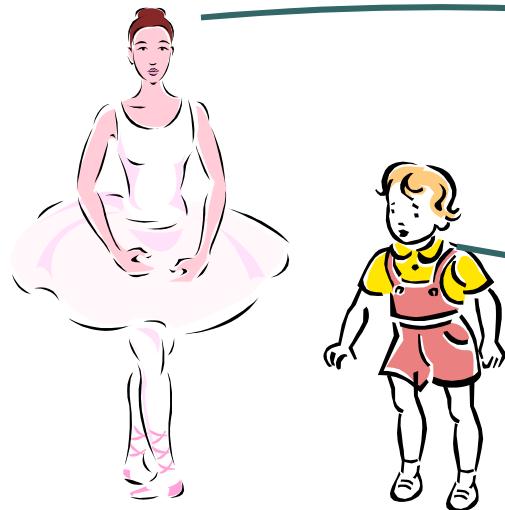
# Representation Condition



- Require a metric  $m$ 
  - Must map the attributes of the entities into numbers
  - Numerical relations of the data **preserve** empirical relations



# Real World



Mary taller than Tom

# Number System

$m$

90

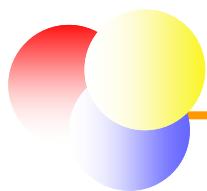
175

$m(\text{Mary}) > m(\text{Tom})$

**$m$  satisfy representation condition**

$x$  taller than  $y \iff m(x) > m(y)$





# Example 1 /1

Peoples: Frankie, Mary, Tom

Relations:

R1:  $x$  is taller than  $y \Rightarrow (x, y) \in R1$

R2:  $x$  is tall  $\Rightarrow x \in R2$

R3: both  $x$  and  $y$  are not higher than  $z$ , but  
 $x$  is higher than  $z$  if sitting on  $y$ 's  
shoulder  $\Rightarrow (x, y, z) \in R3$



Frankie

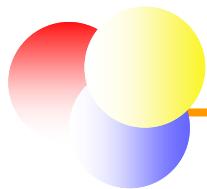


Mary



Tom





# Example 1 /2

$R_1 = \{(Frankie, Mary), (Frankie, Tom), (Mary, Tom)\}$



Frankie

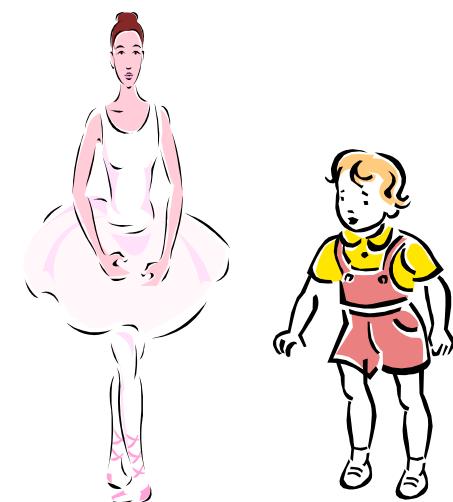


Mary

Frankie



Tom

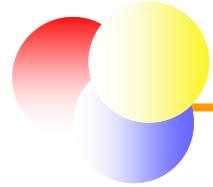


Frankie



Tom





# Example 1 /3

$R_2 = \{\text{Frankie, Mary}\}$

$R_3 = \{(\text{Tom, Mary, Frankie}), (\text{Mary, Tom, Frankie})\}$



# Representation Condition

---

$$x \text{ taller than } y \iff m(x) > m(y)$$

$$x \text{ is tall} \iff m(x) > 170$$

both x and y are not higher than z, but x is higher than z if sitting on y's shoulder

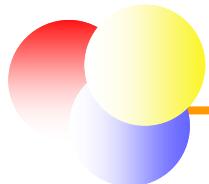


$$m(x) < m(z)$$

$$m(y) < m(z)$$

$$0.8m(x) + 0.7m(y) > m(z)$$

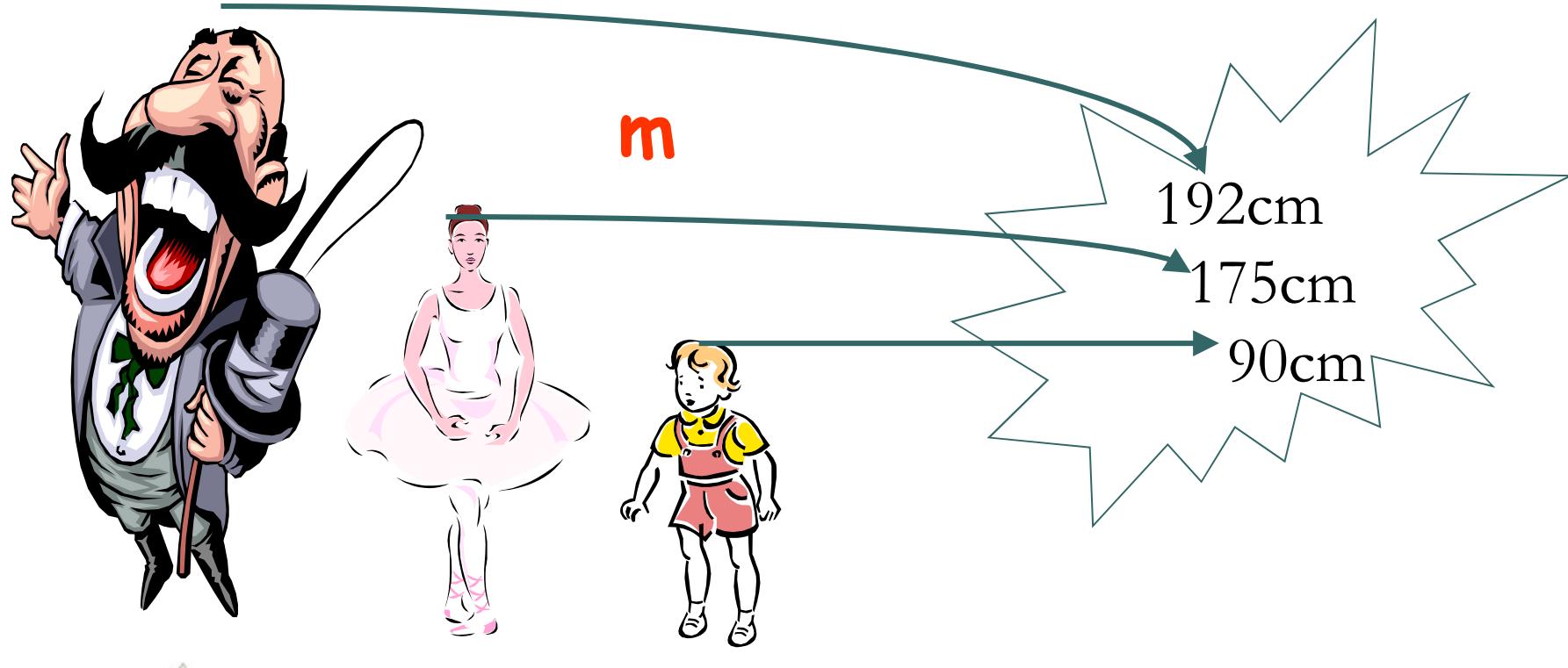




# Example 1 /4

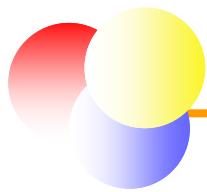
## Measuring

$$m(\text{Frankie}) = 192\text{cm}$$
$$m(\text{Mary}) = 175\text{cm}$$
$$m(\text{Tom}) = 90\text{cm}$$



Tom

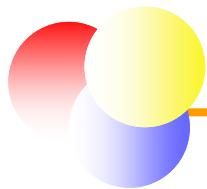




# M satisfy representation condition?

- Entities: {Frankie, Mary, Tom}
  - Attribute: Height
  - Empirical Relations: {R1, R2, R3}
- 
- Values: {192cm, 175cm, 90cm}
  - Numerical relation:
    - S1:  $m(\text{Frankie}) > m(\text{Mary})$ ,  $m(\text{Frankie}) > m(\text{Tom})$ ,  
 $m(\text{Mary}) > m(\text{Tom})$
    - S2:  $m(\text{Frankie}) > 170\text{cm}$ ,  $m(\text{Mary}) > 170\text{cm}$
    - S3:  $0.8*m(\text{Mary}) + 0.7*m(\text{Tom}) > m(\text{Frankie})$  . .  
 $0.8*m(\text{Tom}) + 0.7*m(\text{Mary}) > m(\text{Frankie})$  . . 20



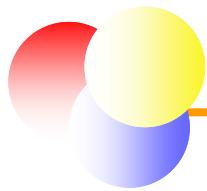


# Key Stages of Measurement

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- 1) Identify **attribute** for some real world entity
- 2) Identify **empirical relations** for attribute
- 3) Identify **numerical relations** corresponding to each empirical relation
- 4) Define **the model** for the mapping from real world entities to numbers
- 5) Check that numerical relations **preserve** and are preserved by empirical relations

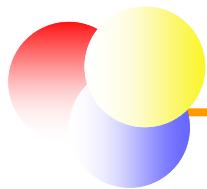




# How to Identify Empirical Relations

- The way we perceive the real world compare the attributes of entities, not assignment numbers to them
- The arity of empirical relations may be unary, binary, or others.
  - “is taller than” -----binary
  - “is tall” -----unary
  - “x is higher than z if sitting on y’s shoulder” -----ternary





# Surveys: Program functionality

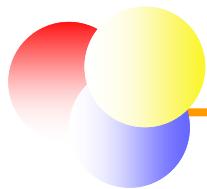
	A	B	C	D
A	----	80	10	80
B	20	----	5	50
C	90	95	----	96
D	20	50	4	----

More functionality

(x,y) excess 60%

(C, A), (C,B), (C,D), (A, B), (A, D)    transitive

Obtain a preliminary understanding of relations by surveys



# Example 2 /1

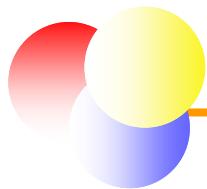
## Ranking 4 software products based on user preferences

- Identify attribute: ranking the products (entities) A, B, C and D based on user preferences
- Identify empirical relations: represented by the table

	A	B	C	D
A	-	80	10	80
B	20	-	5	50
C	90	95	-	96
D	20	50	4	-

(A,B) = 80 means %80 of the users preferred product A to B





## Example 2 /2

	A	B	C	D
A	-	80	10	80
B	20	-	5	50
C	90	95	-	96
D	20	50	4	-

value greater than 60.  
of users prefer A  
than B.

$$p(x) > p(y)$$

If  $p(x) > p(y)$  and  $p(y) > p(z)$

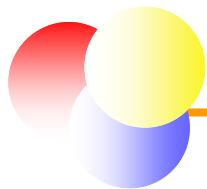
Then  $p(x) > p(z)$

**Valid pairs (C,A), (C,B), (C,D), (A,B) and (A,D)**

### ■ Verification:

- No conflict between the data collected and the model





## Example 2 /3

- Verification fails if the data was collected as shown here because
  - $M(B,C) > 60\% \text{ then } p(B) > p(C)$
  - $M(C,A) > 60\% \text{ then } p(C) > p(A)$
  - $M(A,B) > 60\% \text{ then } p(A) > p(B)$

	A	B	C	D
A	-	80	10	80
B	20	-	95	50
C	90	5	-	96
D	20	50	4	-

- There is a conflict between the real and formal model and the model must be revised

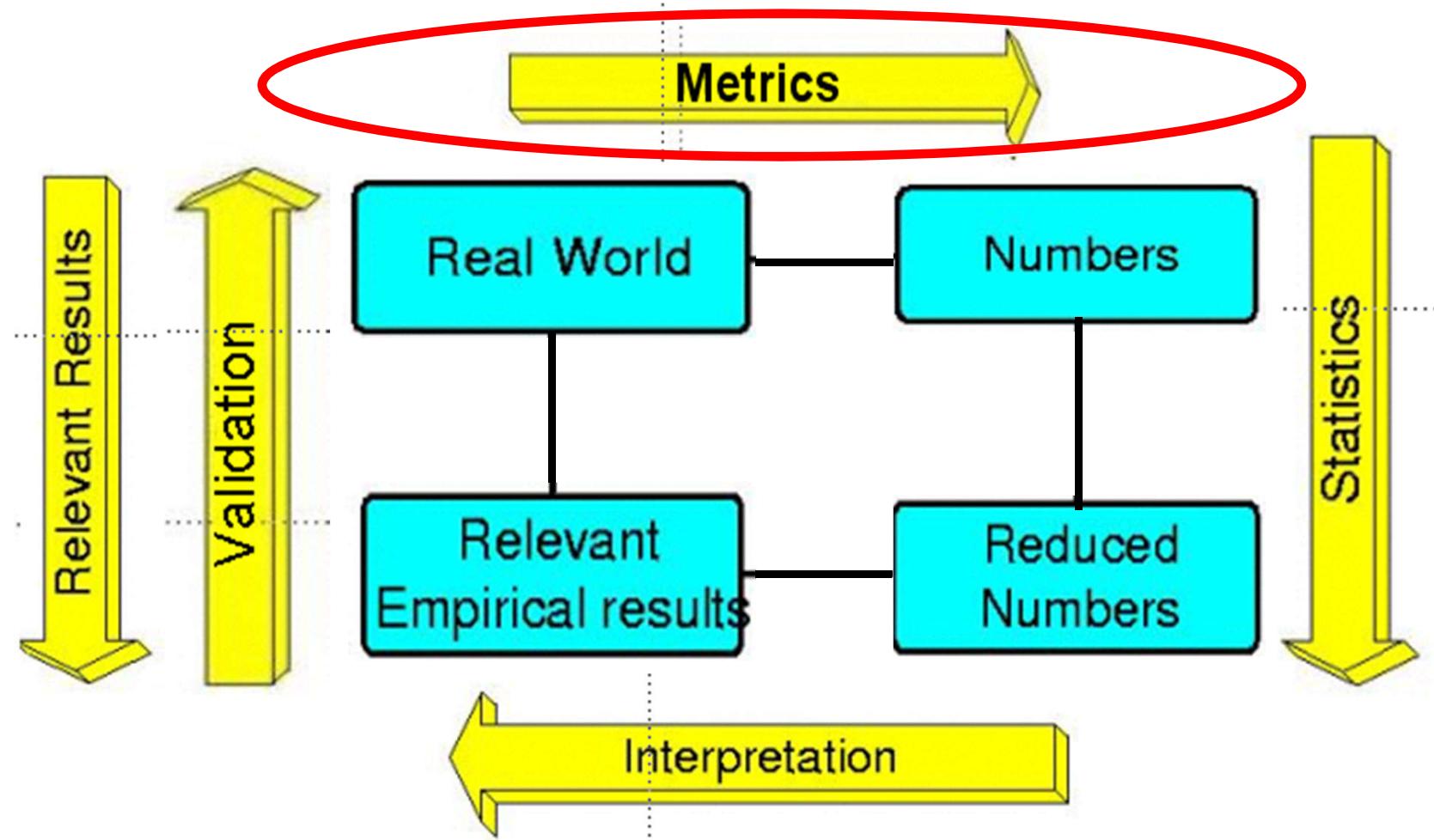


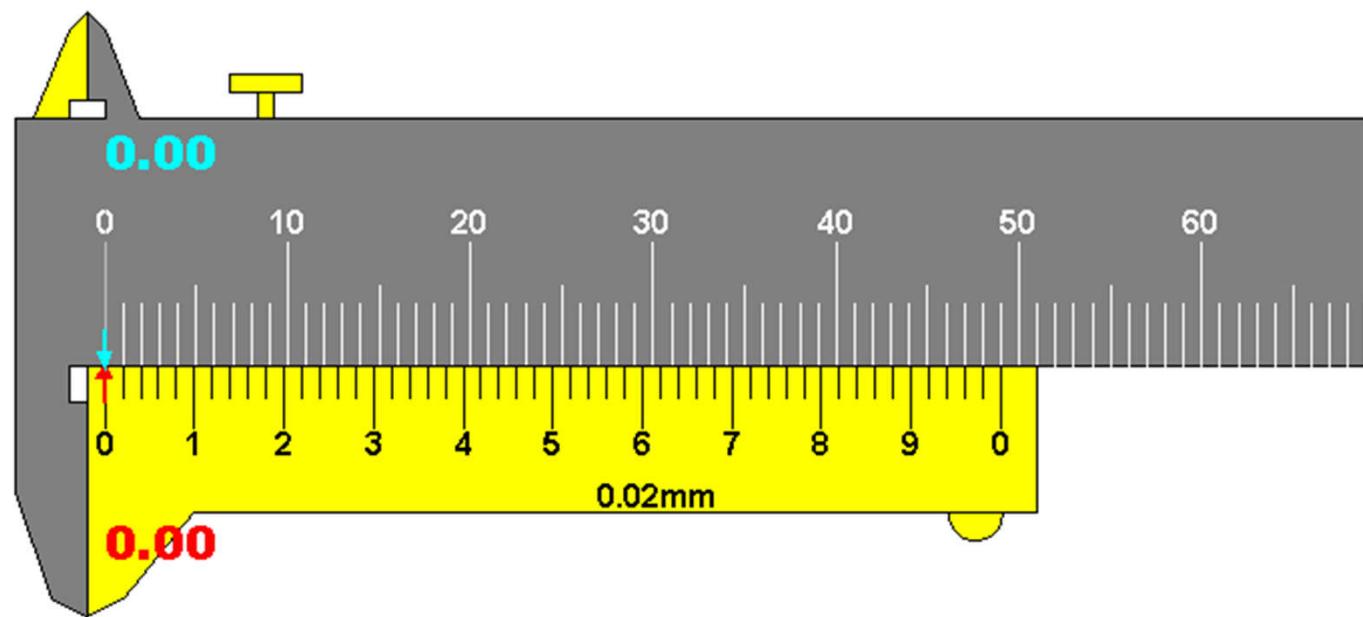
## Section 2

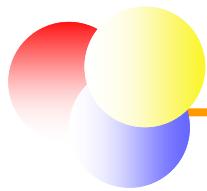
# Measurement Scales

- 
- Empirical Relational Systems
  - Numerical Relational Systems
  - Representational Condition
  - Scales









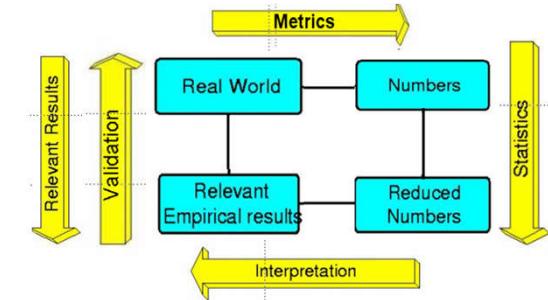
# Empirical Relational System

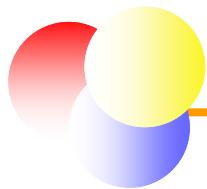
$$ERS = \langle E, \mathcal{R}, O \rangle$$

Where

- $E$  is a set of entities
- $\mathcal{R}$  is a set of empirical relations  $R_i$   
 $R_i$  has an arity  $n_i$ , i.e.,  $R_i \subseteq E^{n_i}$
- $O$  is a set of binary operations among entities  
each binary operation  $o_j$  is function

$$o_j : E \times E \rightarrow E$$





# Some Examples

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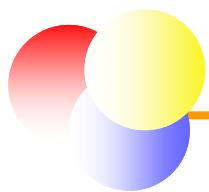
- The size of programs

$ERS = \langle \{program\}, \{\text{longer\_than}\}, \{\oplus\} \rangle$

- The criticality of software failures

$ERS = \langle \{software\ failures\}, \{\text{syntactic, semantic, system\_crash}\} \rangle$





# Numerical Relation Systems

$$NRS = \langle V, \mathfrak{I}, P \rangle$$

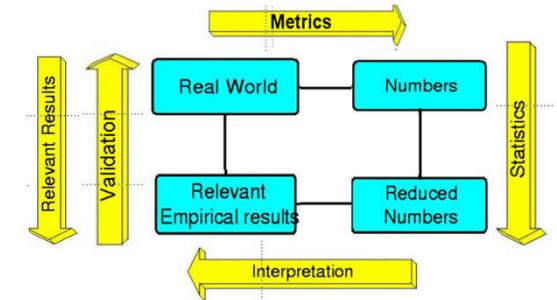
where

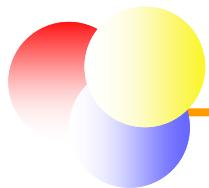
- $V$  is a set of values
- $\mathfrak{I}$  is a set of numerical relations

$S_i$  has the same arity  $n_i$  of the empirical  $R_i$ , i.e.,  $S_i \subseteq E^{\text{ni}}$

- $P$  is a set of binary operations among values
  - each binary operation  $\bullet_j$  is function

$$\bullet_j : V \times V \rightarrow V$$

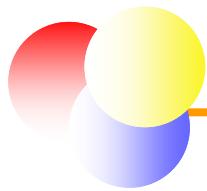




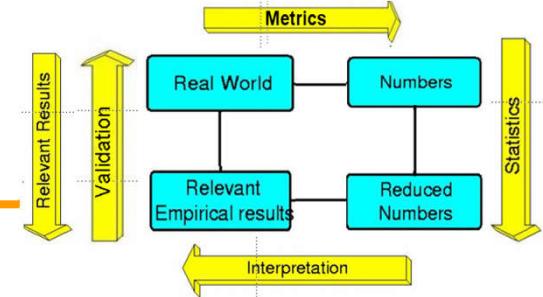
# Some Examples

- $NRS = \langle \{real\}, \{\rangle\}, \{+\} \rangle$
- $NRS = \langle \{Nature\}, \{\rangle\}, \{-\} \rangle$
- $NRS = \langle \{all\ strings\}, \{\rangle\}, \{\oplus\} \rangle$





# Metric



- **Metric:**

$$m : E \rightarrow V$$

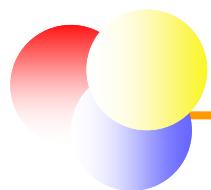
a **function** that associates a value with each entity

- **Notice:**

establishes **a link** between the set of entities and the set of values, **regardless of the relations and operations** in the empirical and numerical relational system



# Representation Condition



## ■ Representation condition

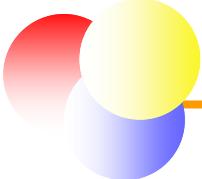
$$\forall i \in 1..n, \forall e_1, \dots, e_n \in E, \forall R_i \in \mathcal{R}, \forall S_i \in \mathfrak{I}$$

$$R_i(e_1, \dots, e_n) \Leftrightarrow S_i(m(e_1), \dots, m(e_n))$$

$$\forall j \in 1..m \quad \forall e_1, e_2 \in E$$

$$m(e_1 o_j e_2) = m(e_1) \bullet_j m(e_2)$$



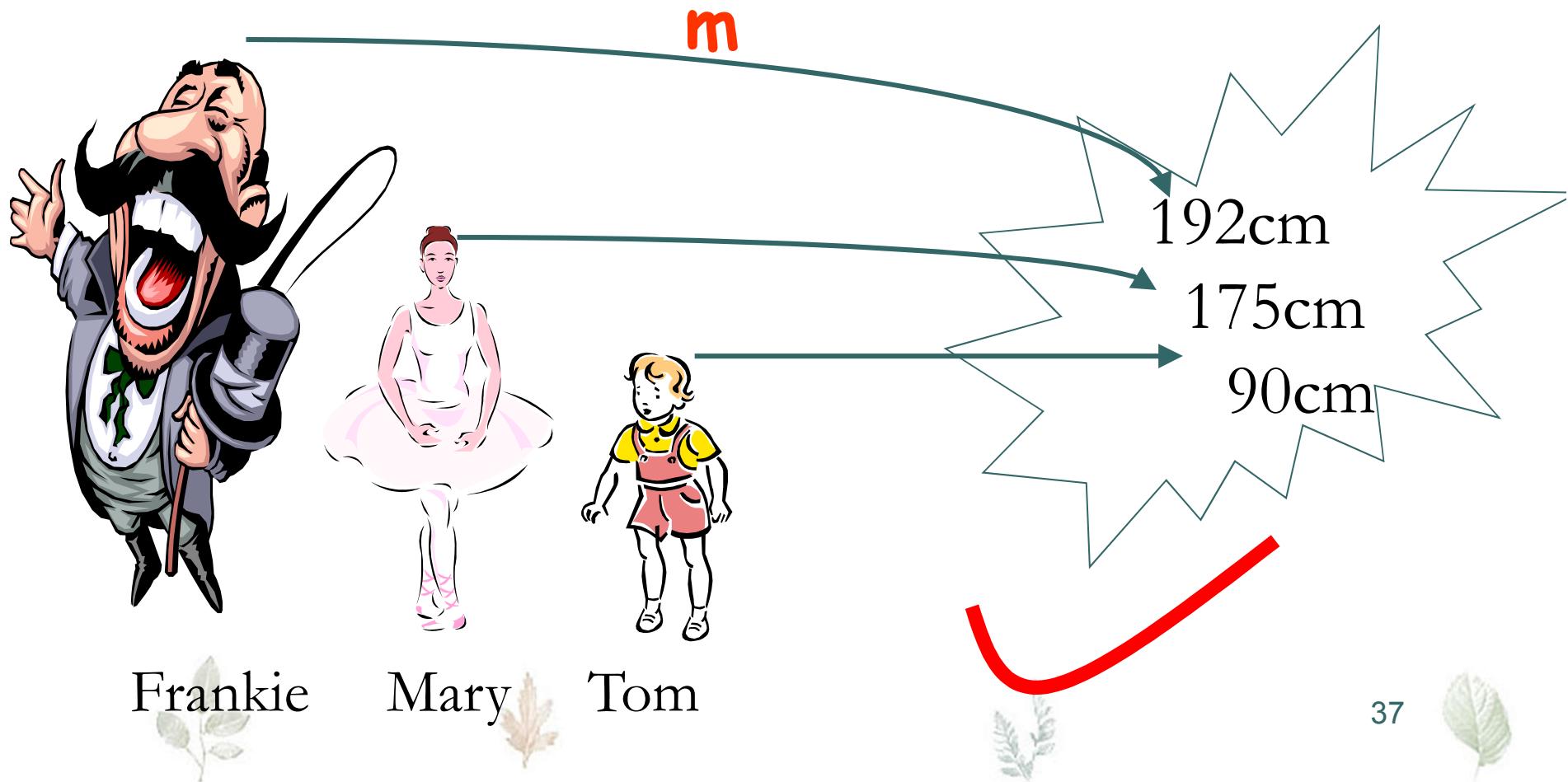


# Representation Condition (cont.)

Empirical relations	Numerical relations	Representation Condition
taller than	$x > y$	A is taller than B iff $M(A) > M(B)$
is tall	$x > 170$	A is tall iff $M(A) > 170$
much taller than	$x > y + 15$	A is much taller than B iff $M(A) > M(B) + 15$
x is higher than y if sitting on z's shoulder	$0.8z + 0.7x > y$	A is higher than B if sitting C's shoulders iff $0.8M(C) + 0.7M(A) > M(B)$

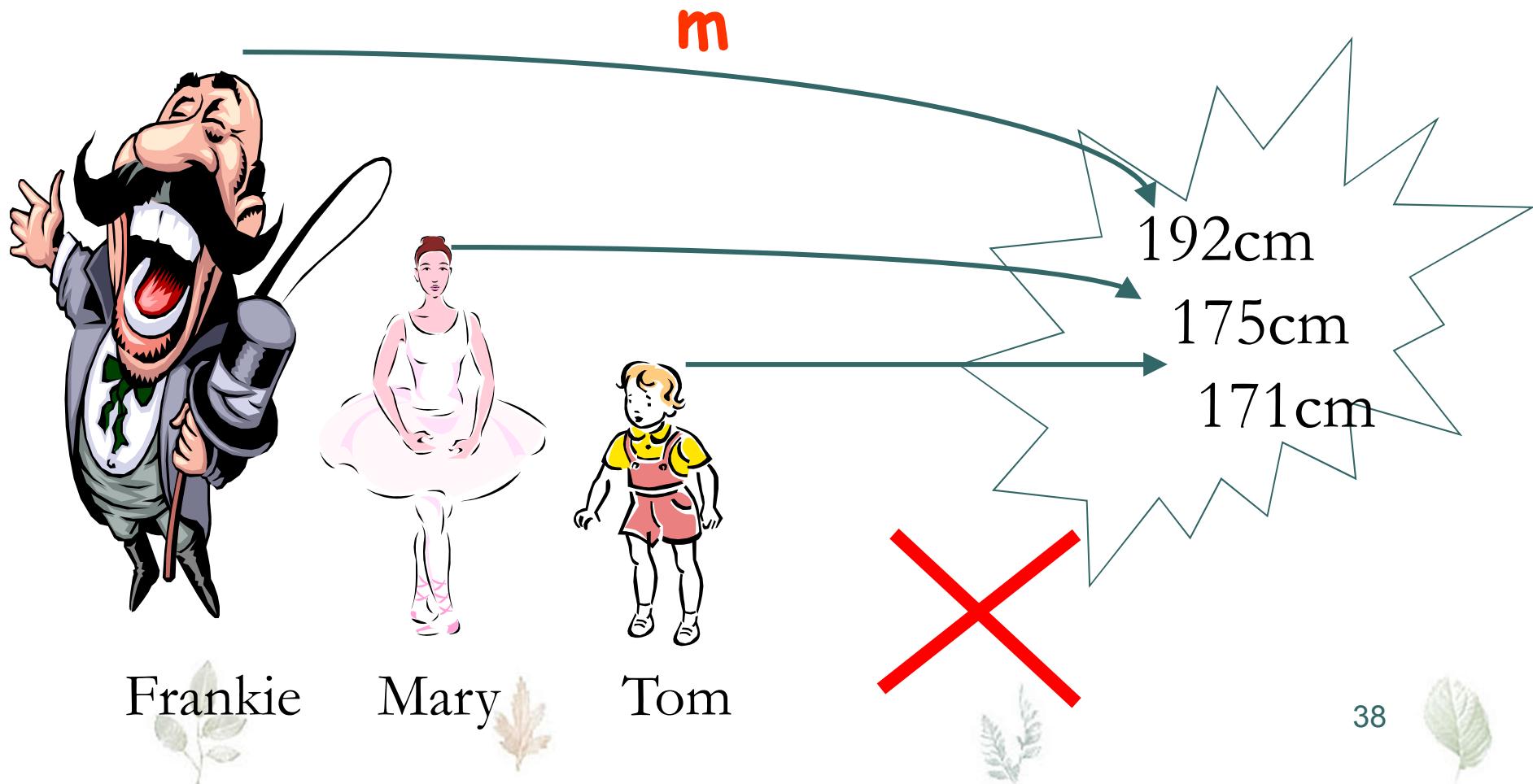
# Measuring

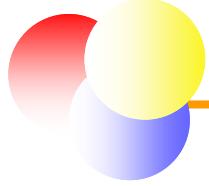
$$m(\text{Frankie}) = 192\text{cm}$$
$$m(\text{Mary}) = 175\text{cm}$$
$$m(\text{Tom}) = 90\text{cm}$$



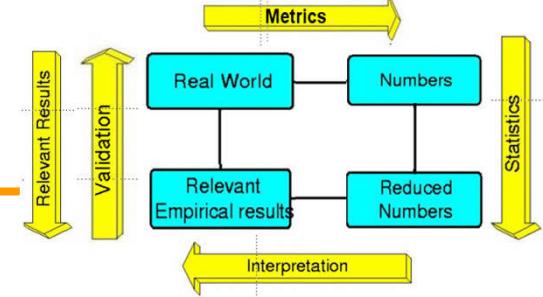
# Measuring

$m(\text{Frankie}) = 192\text{cm}$   
 $m(\text{Mary}) = 175\text{cm}$   
 $m(\text{Tom}) = 171\text{cm}$



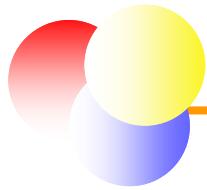


# Notice



- There may be **many different metrics** for a given attribute. Any metric that satisfies the representation condition is a **valid** metric
- The richer the empirical relation system, the **fewer** the valid metrics



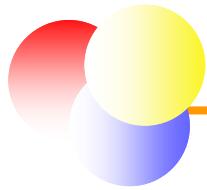


# Scales(刻度/尺度/标度)

- A scale is a triple **<ERS, NRS, m>**  
where
  - $ERS = \langle E, \mathcal{R}, O \rangle$  is an empirical relational sys
  - $NRS = \langle V, \mathfrak{I}, P \rangle$  is a numerical relational sys
  - $m : E \rightarrow V$  is a metric that **satisfies the Representation condition**

**Sometime, we refer to m alone as the scale**

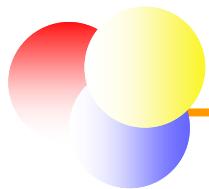




# Related Problems

- **How** do we determine one numerical relation system in preference to another?
- **How** do we know whether a particular empirical relation system has a representation in a given numerical relation system? (**existence**)
- **What** do we do when we have a number of different possible representations (and hence many scales) in the same numerical relation system?  
**(Uniqueness)**



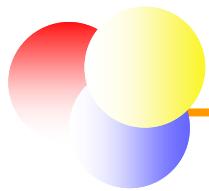


# Related Problems (cont.)

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- Answer to 1: Use the real number as possible
- Answer to 2: **Representation theorem**
  - D.H. Krantz. Foundations of Measurement. 1971
  - F.S. Roberts. Measure Theory with Applications to Decision Making Utility and the Social Sciences. 1979
- Answer to 3: **Transformation**
  - Height of persons can be measured with different scales, e.g., meters, centimeters
  - If  $m$  is a distance metric, then  $m' = \alpha m$  is also a distance metric. However,  $m' = m^2$  is not





# Related Problems (cont.)

## ■ Admissible Transformation

Given a scale  $\langle ERS, NRS, m \rangle$ , a transformation  $f$  is admissible if  $\langle ERS, NRS, m' \rangle$  is a scale, where  $m' = f \circ m$  is the composition of  $f$  and  $m$

## ■ Rescaling (換算)

$m'$  is called as a rescaling of  $m$

different types of scales permit different types of admissible transformation

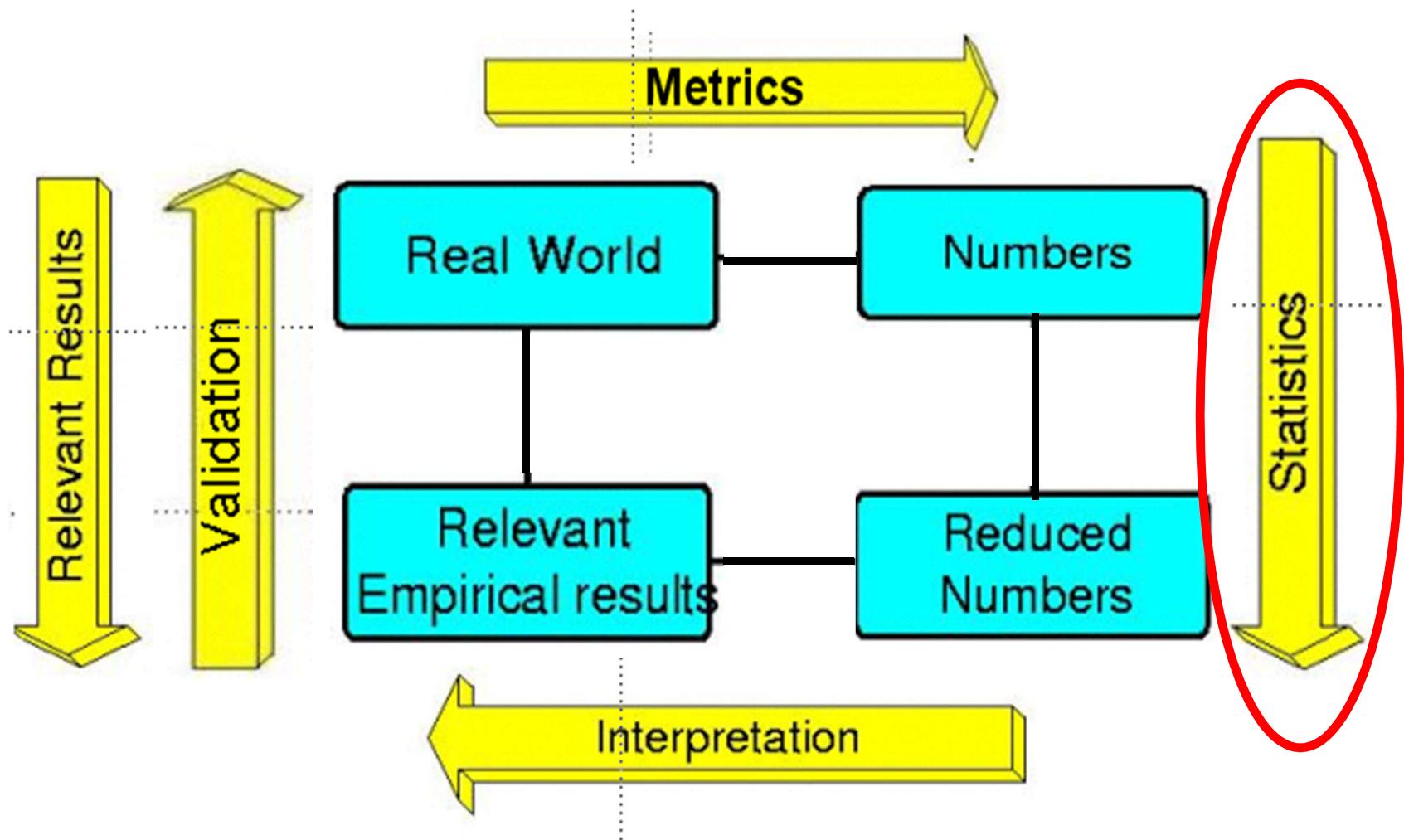


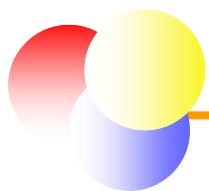
# **Section 3**

## **Scale Types**

- 
- Nominal Scale
  - Ordinal Scale
  - Interval Scale
  - Ratio Scale
  - Absolute Scale







# Nominal Scale

<ERS, NRS, m>

**Definition:** A scale is a **nominal** one if it divides the set of entities into categories, with no particular ordering among them

- The ERS consists only of different classes; there is no notion of ordering among the classes
- Any distinct numbering or symbolic representation of the classes is an acceptable metric, but there is no notion of magnitude associated with the numbers or symbols



- Admissible transformation  
**All one-to-one transformation**
- Notice  
It makes no sense to carry out any arithmetic operations on these numbers or order them
- Example: the location of faults

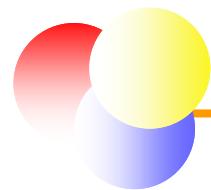
$$M_1(x) = \begin{cases} 1 & \text{if } x \text{ is specification fault} \\ 2 & \text{if } x \text{ is design fault} \\ 3 & \text{if } x \text{ is code fault} \end{cases}$$

$$M_2(x) = \begin{cases} 101 & \text{if } x \text{ is specification fault} \\ 2.73 & \text{if } x \text{ is design fault} \\ 69 & \text{if } x \text{ is code fault} \end{cases}$$



47





# Ordinal Scale

<ERS, NRS, m>

**Definition:** A scale is an ordinal one if it divides the set of entities into categories that are ordered

- The ERS consists of classes that are ordered with respect to the attribute
- Any mapping that preserves the ordering is acceptable
- The numbers represent ranking only, so addition, subtraction, and other arithmetic operations have no meaning



- Admissible transformation

All strictly monotonic functions

- Notice

Although we can compare values, we still cannot use them for arithmetic operations

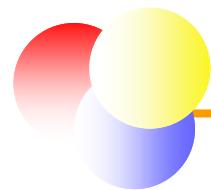
- Example: complexity of modules

$$M_1(x) = \begin{cases} 1 & \text{if } x \text{ is trivial} \\ 2 & \text{if } x \text{ is simple} \\ 3 & \text{if } x \text{ is moderate} \\ 4 & \text{if } x \text{ is complex} \\ 5 & \text{if } x \text{ is incomprehensible} \end{cases}$$



$$M_2(x) = \begin{cases} 1 & \text{if } x \text{ is trivial} \\ 3 & \text{if } x \text{ is simple} \\ 2 & \text{if } x \text{ is moderate} \\ 4 & \text{if } x \text{ is complex} \\ 10 & \text{if } x \text{ is incomprehensible} \end{cases}$$





# Interval Scale

<ERS, NRS, m>

**Definition:** In an interval scale, the distance between two values is the basis for meaningful statements

- An interval scale preserves order, as with an ordinal scale
- An interval scale preserves differences but not ratios
- Addition and subtraction are acceptable on the interval scale, but not multiplication and division

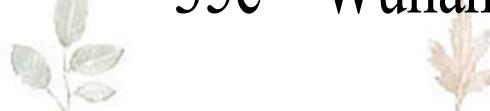


- Admissible transformation

$m' = am + b$  ( $a > 0$ ) (a subset of the monotonic functions that are admissible for ordinal scales.)

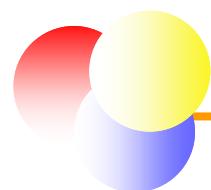
- Example

$$M_1(x) = \begin{cases} 15c & \text{Shanghai} \\ 20c & \text{Beijing} \\ 25c & \text{Zhengzhou} \\ 30c & \text{Nanjing} \\ 35c & \text{Wuhan} \end{cases}$$



$$M_2(x) = \begin{cases} 59F & \text{Shanghai} \\ 68F & \text{Beijing} \\ 77F & \text{Zhengzhou} \\ 86F & \text{Nanjing} \\ 95F & \text{Wuhan} \end{cases}$$





# Ratio Scale

<ERS, NRS, m>

**Definition:** A ratio scale allows the definition of meaningful statements of the kind “twice as much” on the single values of the metric.

- Preserves ordering, the size of intervals between entities, and ratios between entities
- There is a zero element, representing total lack of the attribute
- The measurement mapping must start at zero and increase at equal intervals, known as units
- All arithmetic can be meaningfully applied to it



- Admissible transformation:

$$m' = am \quad (a>0)$$

- Notice:

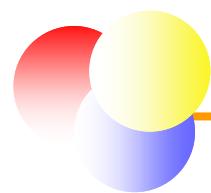
It makes sense to add and subtract ratio metrics, and to multiply and divide them by constants

- Example:

The length of physical objects

The length of software code





# Absolute Scale

<ERS, NRS, m>

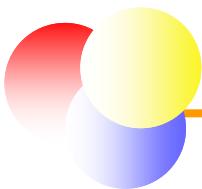
**Definition:** A scale that only allows for the identify transformation.

- The measurement for an absolute scale is made simply by counting the number of elements in the entity set
- There is only one possible measurement mapping, namely actual number
- All arithmetic analysis of the resulting count is meaningful



- Admissible transformation:  
the identity transformation:  $m' = m$
- Example:
  - LOC is a ratio scale of program length
  - LOC is a absolute scale of the attribute “number of lines of code” of a program
  - “number of years” is a ratio-scale metric of a person’s age





# Summary: scales of measurement

Scale Types	Admissible Transformation	Examples
Nominal	Bijections	Labeling, classifying entities
Ordinal	Monotonically increasing	Preference, hardness, air quality, intelligence tests
Interval	Positive linear	Relative time, temperature
Ratio	Proportionality	Time interval, length
Absolute	Identity	Counting entities



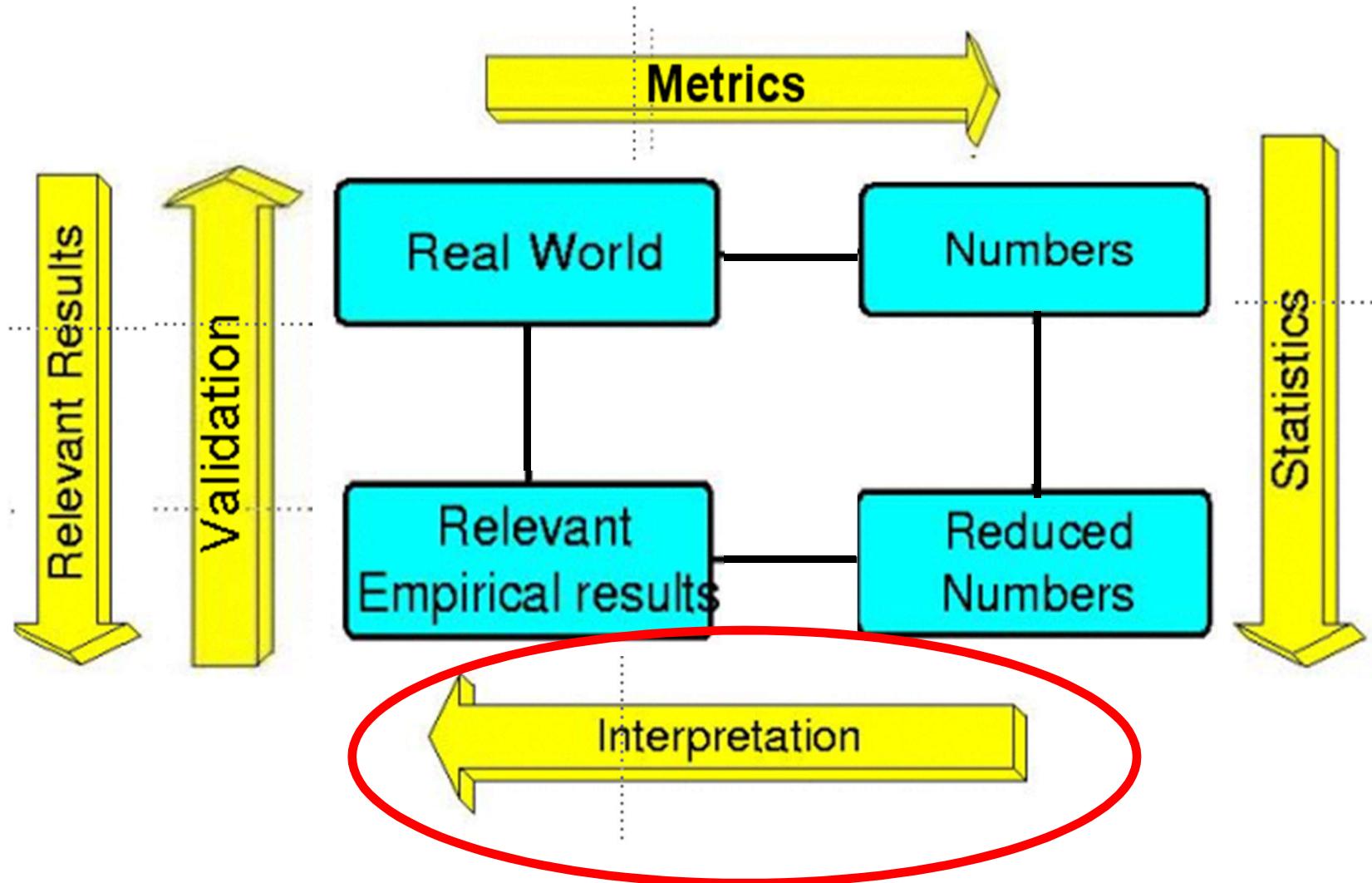
## Section 4

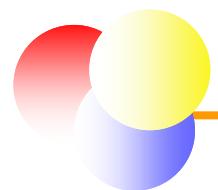
# Meaningfulness in Measurement

---

- The notion of meaningfulness
- Operations on metrics







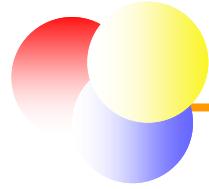
# Discussion

The President of the United States is 125  
years old

**true or false?**

**meaningful?**





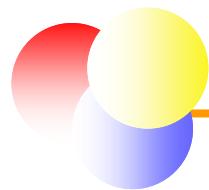
# The notion of meaningfulness

- Definition

A statement involving measurement is meaningful iff its **truth value** is **invariant of transformations of allowable scales**

statements and inferences based on data from measurement scales are meaningful if and only if their truth (or falsity) remains unchanged under all admissible transformations of all the scales involved





# Examples

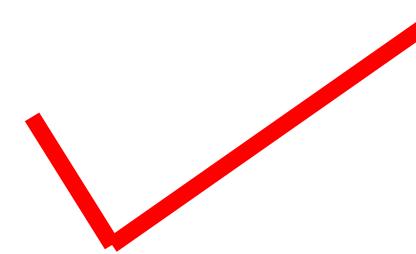
1) Fred is twice as tall as Jane

tallness is **a ratio scale**:  $M' = aM$

If  $M$  and  $M'$  are different metrics of height, then

$$M(\text{Fred}) = 2M(\text{Jane}) \quad \text{and} \quad M'(\text{Fred}) = 2M'(\text{Jane})$$

are **either both true or both false**



$$\left. \begin{array}{l} \text{Fred is 180cm tall} \\ \text{Jane is 90cm tall} \end{array} \right\} M(\text{Fred}) = 2 * M(\text{Jane})$$

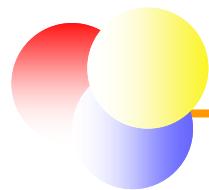
same as:

$$\left. \begin{array}{l} \text{Fred is 1.80m tall} \\ \text{Jane is 0.9m tall} \end{array} \right\} M'(\text{Fred}) = 2 * M'(\text{Jane})$$



$$1\text{m} = 100\text{cm}$$





## Examples (cont.)

- 2) The temperature in Tokyo is twice that in London

$$\left. \begin{array}{l} C(\text{Tokyo}) = 40 \\ C(\text{London}) = 20 \end{array} \right\} ^{\circ}$$

$$C(\text{Tokyo}) = 2 * C(\text{London})$$



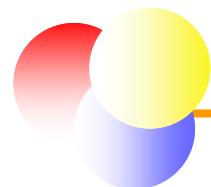
**Temperature is an interval scale**

$$F = \frac{9}{5} C + 32$$

$$\left. \begin{array}{l} F(\text{Tokyo}) = 104 \\ F(\text{London}) = 68 \end{array} \right\} ^{\circ}$$

$$C(\text{Tokyo}) \neq 2 * C(\text{London})$$





## Examples (Cont.)

- 3) The difference in temperature between Tokyo and London today is twice what it was yesterday

Yesterday

$$\left. \begin{array}{l} C(\text{Tokyo}) = 35^\circ \\ C(\text{London}) = 25^\circ \end{array} \right\} 10$$

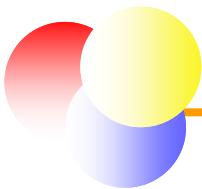
Today

$$\left. \begin{array}{l} C(\text{Tokyo}) = 40^\circ \\ C(\text{London}) = 20^\circ \end{array} \right\} 20$$

$$|C(\text{TokyoT}) - C(\text{LondonT})| = 2 * (C(\text{TokyoY}) - C(\text{LondonY}))$$
$$\left. \begin{array}{l} F(\text{Tokyo}) = 95^\circ \\ F(\text{London}) = 77^\circ \end{array} \right\} 18$$
$$\left. \begin{array}{l} F(\text{Tokyo}) = 104^\circ \\ F(\text{London}) = 68^\circ \end{array} \right\} 36$$

$$|F(\text{TokyoT}) - F(\text{LondonT})| = 2 * (F(\text{TokyoY}) - F(\text{LondonY}))$$





## Examples (Cont.)

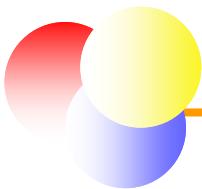
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- 4) The President of the United States is 125 years old
- 5) A semantic error takes twice as long to fix as a syntactic error
- 6) A semantic error is twice as complex as a syntactic error

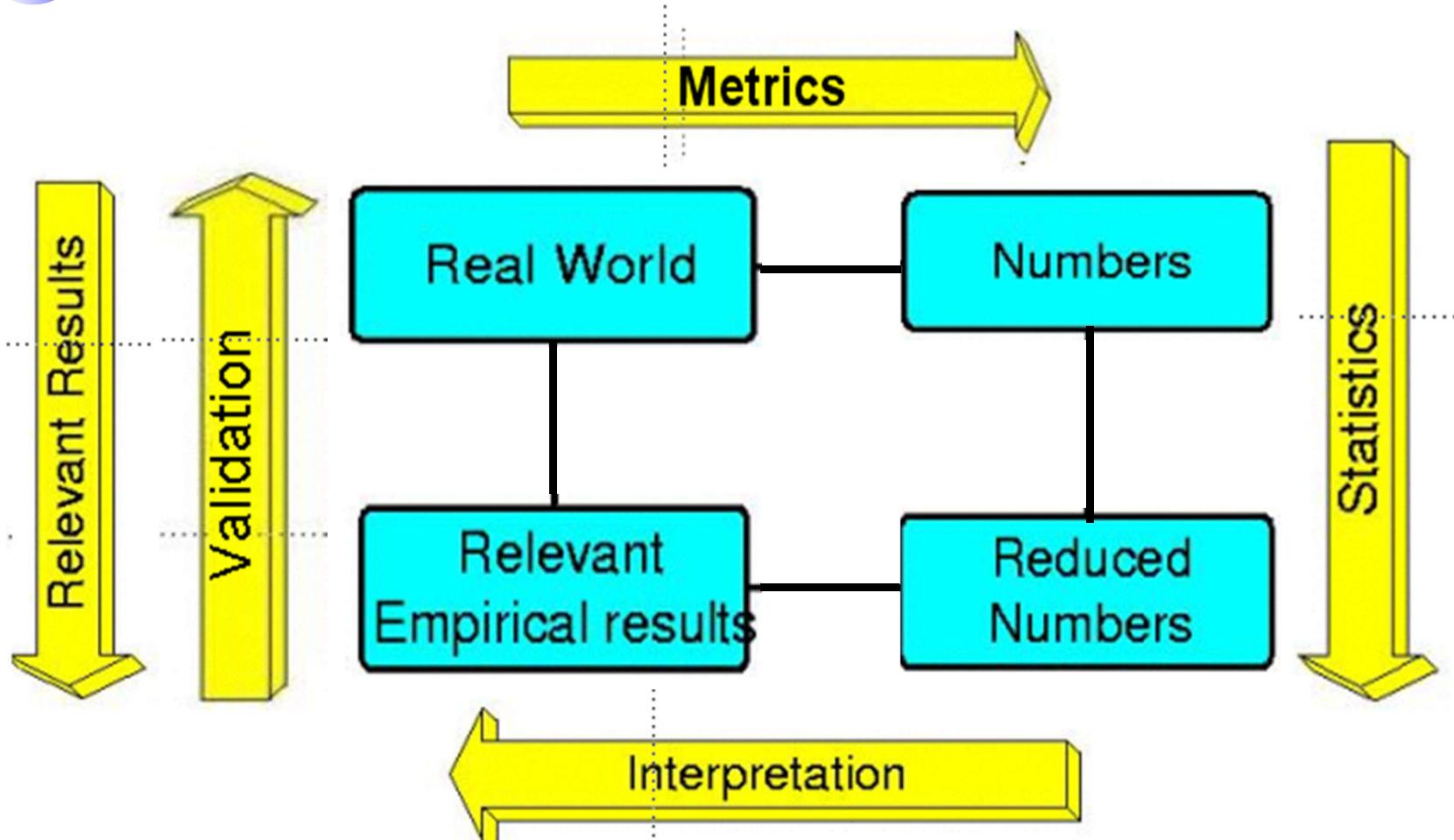


# Scale types and Statistics(P59)

Scale Type	Defining Relations	Examples of statistic	Appropriate statistical tests
Nominal	Equivalence	Mode Frequency	Non-parametric
Ordinal	Equivalence Greater than	Median Percentile Spearman r Kendall W	Non-parametric
Interval	Equivalence Greater than Known ratio of any intervals	Mean Standard deviation Person product-moment correlation Multiple product-moment correlation	Non-parametric
Ratio	Equivalence Greater than Known ratio of any intervals Known ratio of any two scale values	Geometric mean Coefficient of variation	Non-parametric and parametric



# Summary



## 实例分析

- L. Briand, et al. Property-based software engineering measurement. IEEE TSE 1996
- J. Al-Dallal, L. Briand. A precise method-method interaction-based cohesion metric for object-oriented classes. ACM TOSEM 2012

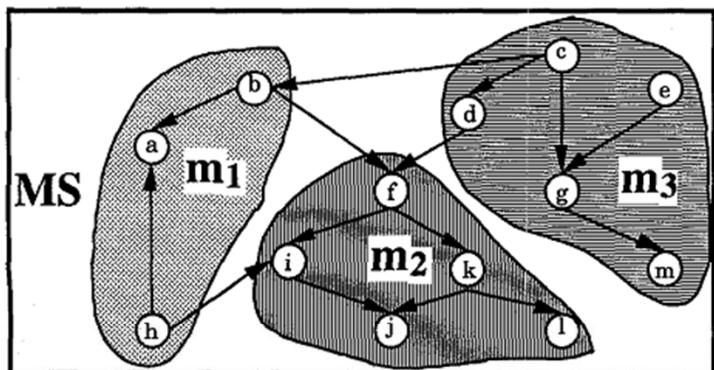


# L. Briand, et al. Property-based software engineering measurement. IEEE TSE 1996

**DEFINITION 3: Size.** *The size of a system S is a function  $\text{Size}(S)$  that is characterized by the following properties Size.1-Size.3.*

**PROPERTY SIZE.1: Nonnegativity.** The size of a system  $S = \langle E, R \rangle$  is nonnegative

$$\text{Size}(S) \geq 0 \quad (\text{Size.I}) \quad \square$$



**PROPERTY SIZE.2: Null Value.** The size of a system  $S = \langle E, R \rangle$  is null if  $E$  is empty

$$E = \emptyset \Rightarrow \text{Size}(S) = 0 \quad (\text{Size.II}) \quad \square$$

**PROPERTY SIZE.3: Module Additivity.** The size of a system  $S = \langle E, R \rangle$  is equal to the sum of the sizes of two of its modules  $m_1 = \langle E_{m1}, R_{m1} \rangle$  and  $m_2 = \langle E_{m2}, R_{m2} \rangle$  such that any element of  $S$  is an element of either  $m_1$  or  $m_2$

$$(m_1 \subseteq S \text{ and } m_2 \subseteq S \text{ and } E = E_{m1} \cup E_{m2} \text{ and } E_{m1} \cap E_{m2} = \emptyset) \\ \Rightarrow \text{Size}(S) = \text{Size}(m_1) + \text{Size}(m_2) \quad (\text{Size.III}) \quad \square$$



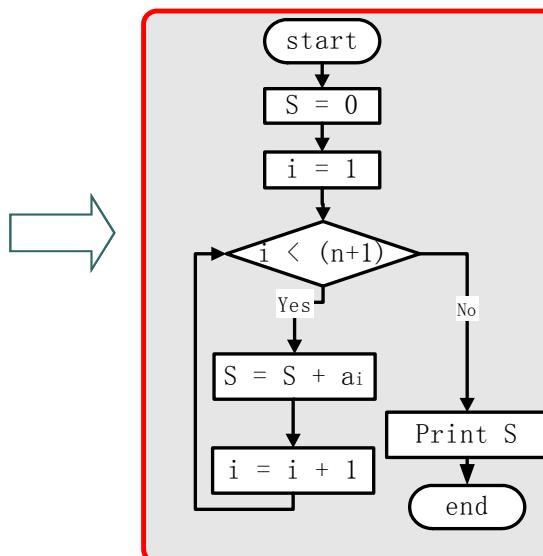
# L. Briand, et al. Property-based software engineering measurement. IEEE TSE 1996

思考1：LOC是size度量吗？

思考2：WMC是size度量吗？

$$\begin{aligned}\text{圈复杂性 } v(G) &= e - n + 2p \\ &= 8 - 8 + 2 \times 1 \\ &= 2\end{aligned}$$

```
void sum()
{
    S=0;
    i=1;
    while(i<n+1)
    {
        S=S+a[i];
        i=i+1;
    }
    printf("S is %d", s);
}
```



L. Briand, et al. Property-based software engineering measurement. IEEE TSE 1996

思考3：Size的3个性质描述的是 $\mathcal{R}$ 还是 $\mathfrak{I}$ ？

- A scale is a triple  $\langle ERS, NRS, m \rangle$ , where
  - $ERS = \langle E, \mathcal{R}, O \rangle$  is an empirical relational sys
  - $NRS = \langle V, \mathfrak{I}, P \rangle$  is a numerical relational sys
  - $m : E \rightarrow V$  is a metric that **satisfies the Representation condition**

$$(m_1 \subseteq S \text{ and } m_2 \subseteq S \text{ and } E = E_{m1} \cup E_{m2} \text{ and } E_{m1} \cap E_{m2} = \emptyset) \\ \Rightarrow \text{Size}(S) = \text{Size}(m_1) + \text{Size}(m_2)$$

$$(m_1 \subseteq S \text{ and } m_2 \subseteq S \text{ and } E = E_{m1} \cup E_{m2} \text{ and } E_{m1} \cap E_{m2} = \emptyset) \\ \Rightarrow S \approx m_1 \oplus m_2$$



L. Briand, et al. Property-based software engineering measurement. IEEE TSE 1996

思考4：如果一个度量满足**Size**的3个性质，它是  
一个“好”的度量吗？

**Size:** 3个性质

**Length:** 5个性质

**Complexity:** 5个性质

**Cohesion:** 4个性质

**Coupling:** 5个性质



J. Al-Dallal, L. Briand. A precise method-method interaction-based cohesion metric for object-oriented classes. ACM TOSEM 2012

提出了一个新的内聚性度量LSCC  
证明它满足Cohesion的4个性质

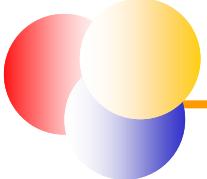
## 5. THEORETICAL VALIDATION

We validate LSCC using the properties for a class cohesion metric proposed by Briand et al. [1998] and discussed in Section 2.1.

PROPERTY LSCC.1. *The LSCC metric complies with the non-negativity and normalization property.*

PROOF. The minimum value for the LSCC metric for a class is 0 when the class has either (1) several methods and no attributes or (2) several methods such that none of their pairs share a common attribute. The maximum value for the LSCC metric for a class is 1 when the class has (1) one or more attributes and no methods (2) one method





# Summary

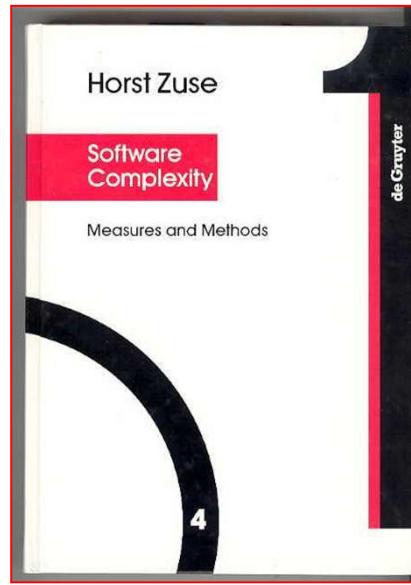
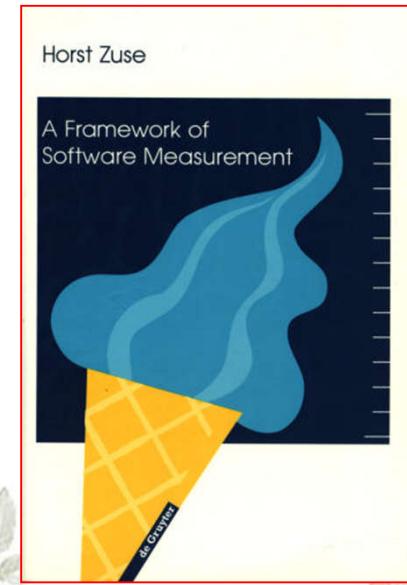
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- Scale?
- Scale type?
- Meaningful?
- Operations on metrics?

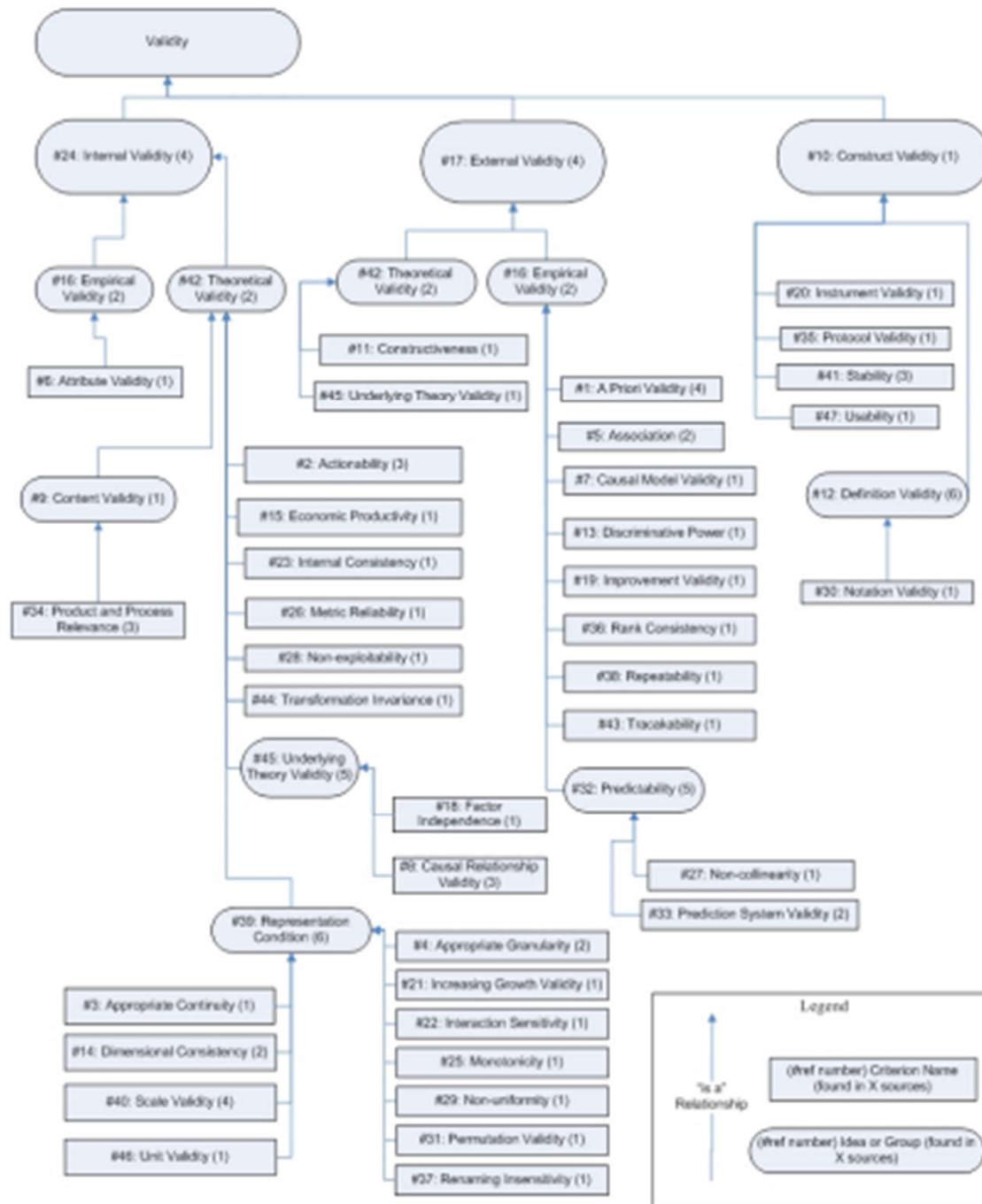


# Further reading

- S. Morasca. Foundations of a weak measurement-theoretic approach to software measurement. 2003
- A. Meneely, et al. [Validating software metrics: a spectrum of philosophies](#). ACM TOSEM 2012



# 47个标准



**Thanks for your time and  
attention!**



# 练习：用Understand收集数据

---

(1) Understand介绍

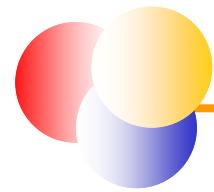
(2) 下载gcc 2.8

<http://ftp.gnu.org/gnu/gcc/gcc-2.8.0.tar.gz>

(3) 编写一个Perl脚本，为gcc 2.8上的函数收集，  
以.csv文件格式输出：

函数名, 相对路径, CountLineCode, CountPath,  
Cyclomatic, MaxNesting, Knots, CountInput,  
CountOutput

在10月29日前提交：Perl脚本以及数据集



# Understand

<http://www.scitools.com/>

The screenshot shows the homepage of [scitools.com](http://www.scitools.com/). At the top, there's a navigation bar with links for "Understand", "GitAhead", "Contact", "Buy", and social media icons for Facebook and a shopping cart. The "support@scitools.com" email address is also visible. Below the navigation, there are two main product sections: "Understand™" and "GitAhead™". The "Understand" section includes links for "Free Trial", "Update", and "Buy", along with options for "Legacy Code Maintenance", "Visual Static Analysis", and "C++ Editor". The "GitAhead" section includes links for "Free Trial" and "Buy", along with a "Revision Control" link. A large central banner features the text "VISUALIZE YOUR CODE" in white, bold, sans-serif font against a dark blue background with glowing cyan lines. Below the banner, several logos of well-known companies are displayed: Adobe, Boeing, Apple, IBM, NASA, Siemens, BMW, General Dynamics, and Toyota.



All Industries  
Aerospace  
Automotive  
Defense  
Electronics  
**Energy**  
Entertainment  
Financial  
Gaming  
Healthcare  
Manufacturing  
Retail  
Software  
Technology  
Telecommunications  
Transportation



CORNING



**Rockwell**  
Automation

Microsoft

A red rectangular box surrounds the Microsoft logo and text.

NORTHROP GRUMMAN



**Australian Government**  
Department of Defence

AEROFLEX



Mercedes-Benz

**GENERAL DYNAMICS**







intuit®

ConocoPhillips



THE AEROSPACE  
CORPORATION



NOKIA



Mentor  
Graphics®

RAIN BIRD





CardinalHealth



communications



Go Further

SONY



Canon



CISCO

ExxonMobil

3M

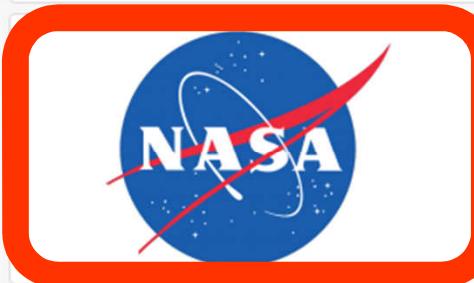
**Rockwell  
Collins**



Donaldson.  
Filtration Solutions

Novell.





**memorex**™

**SIEMENS**



**TOYOTA**



**SAMSUNG**



**Alcatel-Lucent**

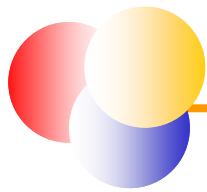




ORACLE®



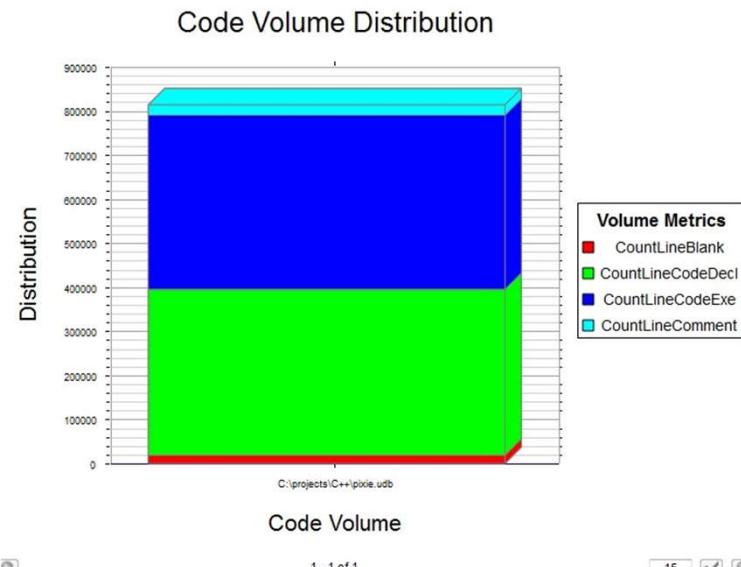
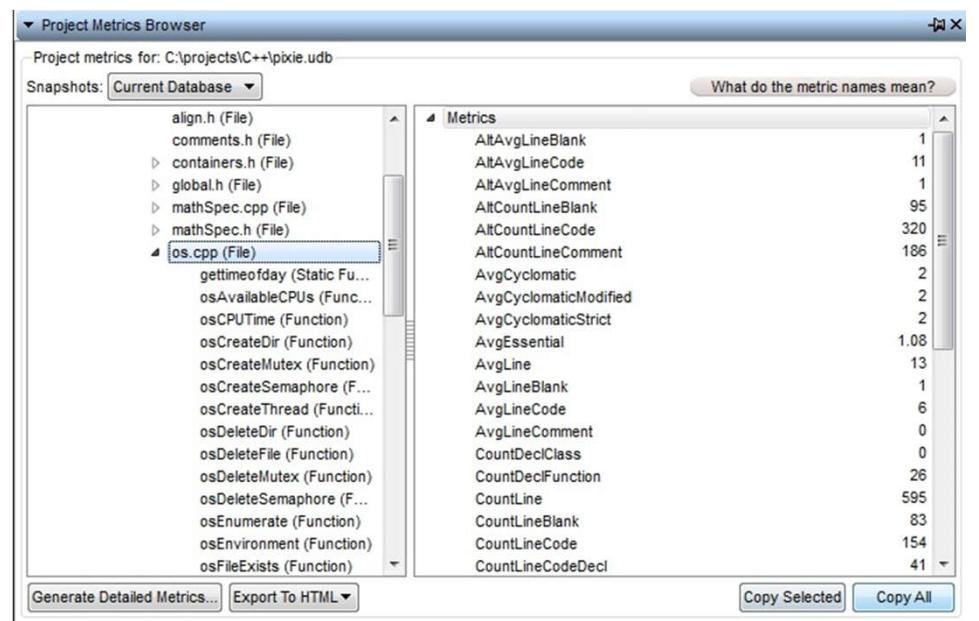




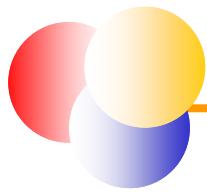
# Understand: Metrics

## 1. Standard metrics

- ① Complexity metrics (20+)
- ② Volume metrics (40+)
- ③ Object-oriented metrics (~30)

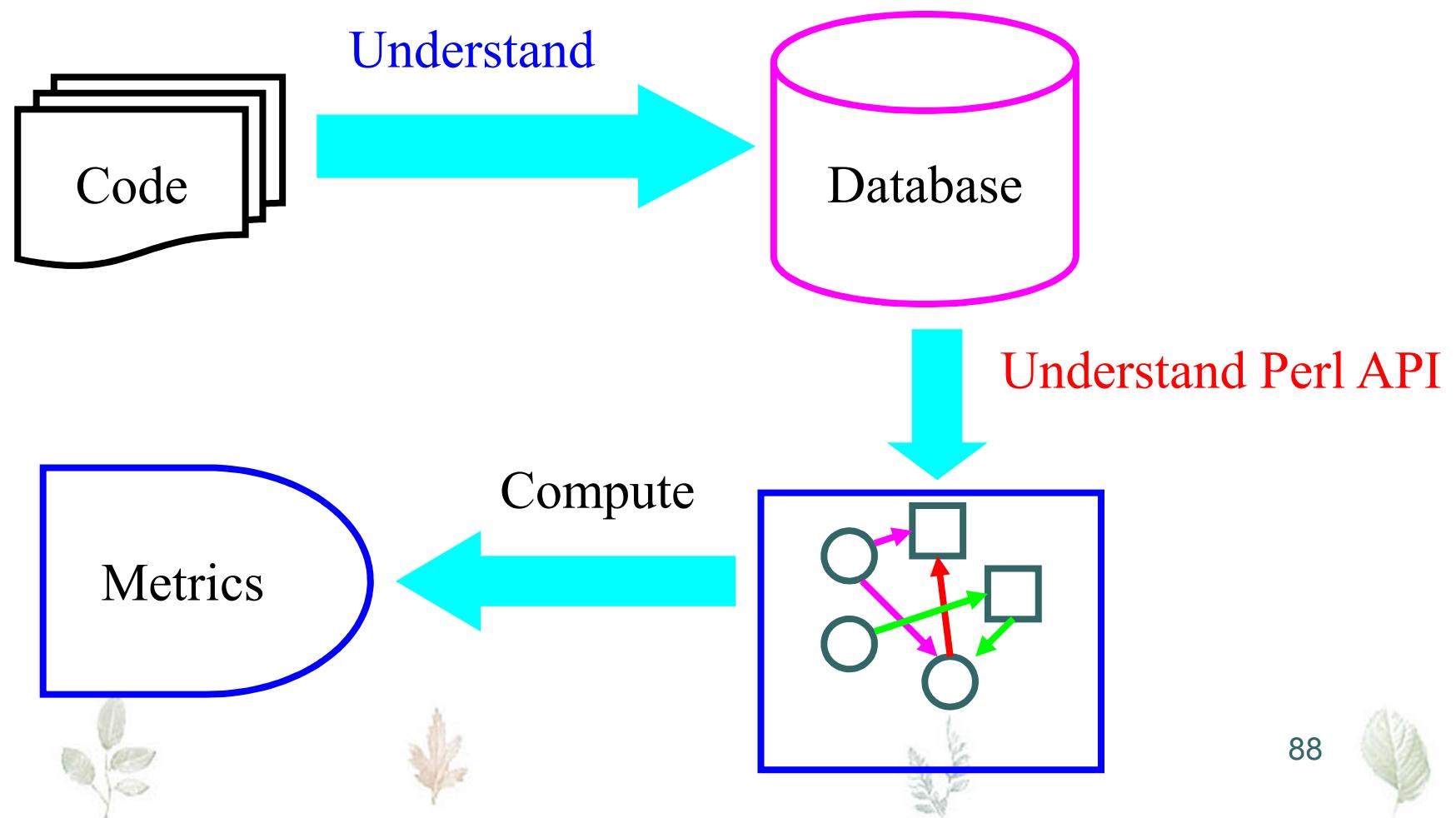


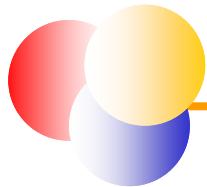
87



# Understand: Metrics

## 2. Custom Metrics





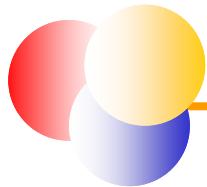
# Understand: Metrics

## Perl Script example 1

### List of Files

```
use Understand;  
$db = Understand::open("test.udb");  
foreach $file ($db->ents("File")) {  
  
    # print the long name (ie, show directory names)  
    print $file->longname(), "\n";  
}
```





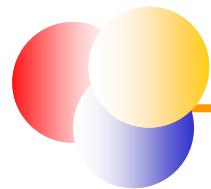
# Understand: Metrics

## Perl Script example 2

### Cyclomatic Complexity of Functions

```
use Understand;  
$db = Understand::open("test.udb");  
  
# lookup a specific metric  
foreach $func ($db->ents("Function")) {  
    $val = $func->metric("Cyclomatic");  
  
    # only if metric is defined for entity  
    print $func->name(), " = ", $val, "\n" if  
    defined($val);  
}
```





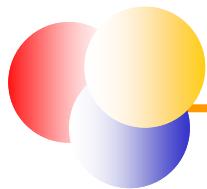
# Understand: Metrics

## Perl Script example 3

### Called By Graphs of Functions

```
use Understand;  
$db = Understand::open("test.udb");  
  
# loop through all functions  
foreach $func ($db->ents("Function")) {  
    $file = "callby_" . $func->name() . ".png";  
    print $func->longname(), " -> ", $file, "\n";  
    $func->draw("Called By", $file);  
}
```





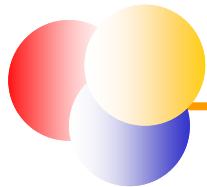
# Understand: Metrics

## Perl Script example 4

### Lexical stream

```
use Understand;  
$db = Understand::open("test.udb");  
  
$file = $db->lookup("test.cpp");  
$lexer = $file->lexer();  
  
foreach $lexeme ($lexer->lexemes()) {  
    print $lexeme->text();  
    if ($lexeme->ent()) {  
        print "@";  
    }  
}
```





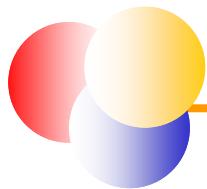
# Understand: Metrics

## Perl Script example 5

### Global Variable Usage

```
use Understand;  
  
$db = Understand::open("test.udb");  
  
foreach $var ($db->ents("Global Object ~Static")) {  
    print $var->name(), ":\n";  
    foreach $ref ($var->refs()) {  
        printf "  %-8s %-16s %s (%d, %d)\n",  
            $ref->kindname(), $ref->ent()->name(),  
            $ref->file()->name(), $ref->line(),  
            $ref->column();  
    }  
    print "\n";  
}
```





# Understand: Metrics

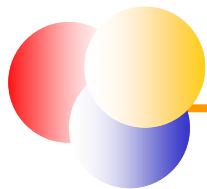
<https://scitools.com/support/perl-api/>

The screenshot shows the SciTools Understand website with the following details:

- Header:** support@scitools.com, Search input field, Home, Features, Buy, Support, Customers, Contact, Blog, Download Free Trial, Current Users Download Here.
- Breadcrumbs:** Support > API/Plugins > Perl API
- Title:** Perl API
- Text:** Understand includes a PERL API which allows you to directly query the Understand database. If you want to create your own report, or gather information in a manner that we didn't foresee in Understand, you can access the information yourself via the API. The API can be accessed in several different ways: most of the scripts are designed to be run from Understand's GUI on the currently opened database. They can also be run from the command line, and some plugins are designed to interact directly with Understand.
- Section:** Run Scripts in Understand
- Description:** To run a script from inside of Understand, use Tools->Run a Command, configure any necessary parameters, and hit run. The resulting output can then be double-clicked to visit the referenced source.
- Image:** A screenshot of the "Run a command" dialog and the "Command Window". The dialog shows "Command: C:\stl\scripts\\_bigfiles.pl", "Parameters: -size 1000", and "Working Directory". The "Capture Output" checkbox is checked. The "Command Window" shows the output of the command, listing files and their sizes:

```
Pixie-2.2.6\src\sdrc\pp2.c,1590
Pixie-2.2.6\src\ri\brickmap.cpp,1563
Pixie-2.2.6\src\ri\bl1.cpp,1483
Pixie-2.2.6\src\ri\radiance.cpp,1418
Pixie-2.2.6\src\ri\executeMisc.cpp,1410
Pixie-2.2.6\src\ri\stochastic.cpp,1292
```



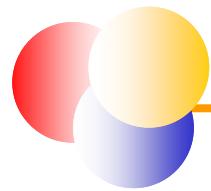


# Understand: Metrics

More detailed example scripts are shipped with Understand in the SciTools/scripts/perl folder.

- ① Report entities that are defined more than once
- ② Report variables that are not initialized
- ③ Report unused functions
- ④ Lists all global variables and where they are defined
- ⑤ Report duplicate code
- ⑥ Report dead code
- ⑦ ...





# Understand: Metrics

## ActiveState Komodo IDE

<http://komodoide.com/>

The screenshot shows the homepage of the ActiveState Komodo IDE website. At the top, there's a navigation bar with links for Store, My Account, a phone number (1.866.631.4581), Contact Sales, Solutions, Editions, Industry, Support, Resources, Blog, and a search icon. Below the navigation is a breadcrumb trail: Home » Solutions » Komodo IDE: The Best IDE for Web and Mobile App Development. The main headline reads "KOMODO IDE: THE BEST IDE FOR WEB AND MOBILE APP DEVELOPMENT". A red-bordered box contains the text "NEW RELEASE!" and "KOMODO 10.2 IS NOW AVAILABLE.", with a "Download" button. To the right is a yellow hexagonal logo featuring a white Komodo dragon. Below the main headline, there's a section titled "ALL OF THE INTEGRATIONS AND FRAMEWORKS YOU NEED" with a descriptive paragraph about the IDE's features.

ActiveState  
THE OPEN SOURCE LANGUAGES COMPANY

SOLUTIONS EDITIONS INDUSTRY SUPPORT RESOURCES BLOG

Contact Sales

Home » Solutions » Komodo IDE: The Best IDE for Web and Mobile App Development

## KOMODO IDE: THE BEST IDE FOR WEB AND MOBILE APP DEVELOPMENT

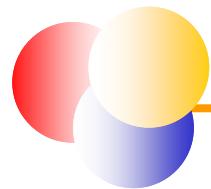
NEW RELEASE!

KOMODO 10.2 IS NOW AVAILABLE.

Download

ALL OF THE INTEGRATIONS AND FRAMEWORKS YOU NEED

Komodo IDE includes all of the integrations you need to stay in-the-zone and get more done. Get your favorite frameworks, languages, and tools in one cross-platform, polyglot IDE.

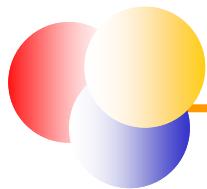


# Understand: Metrics

## ActiveState Komodo IDE

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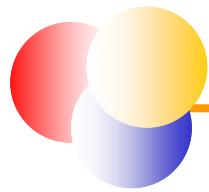


# Understand: Metrics

## Supported Languages

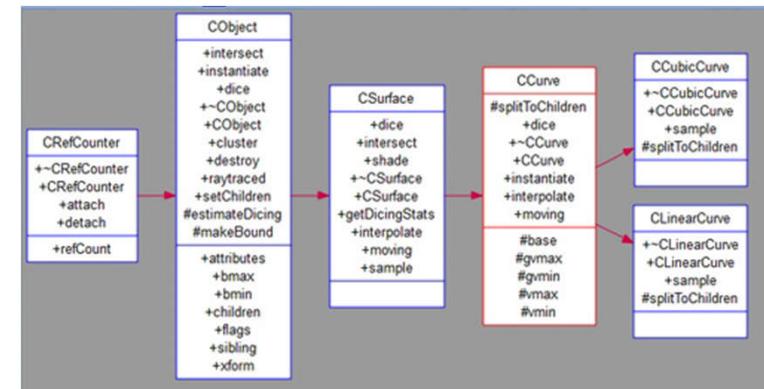
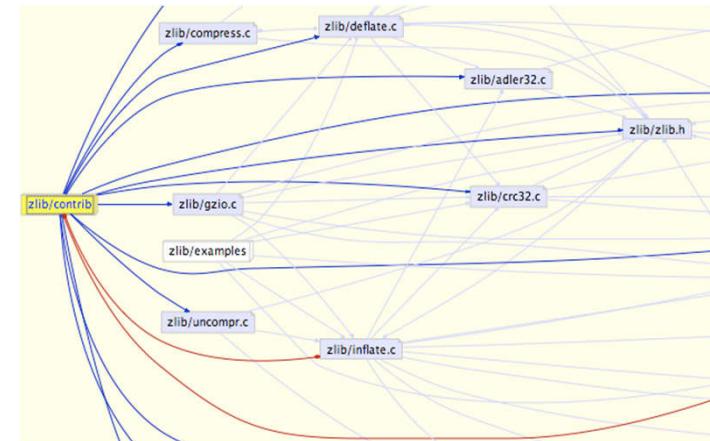
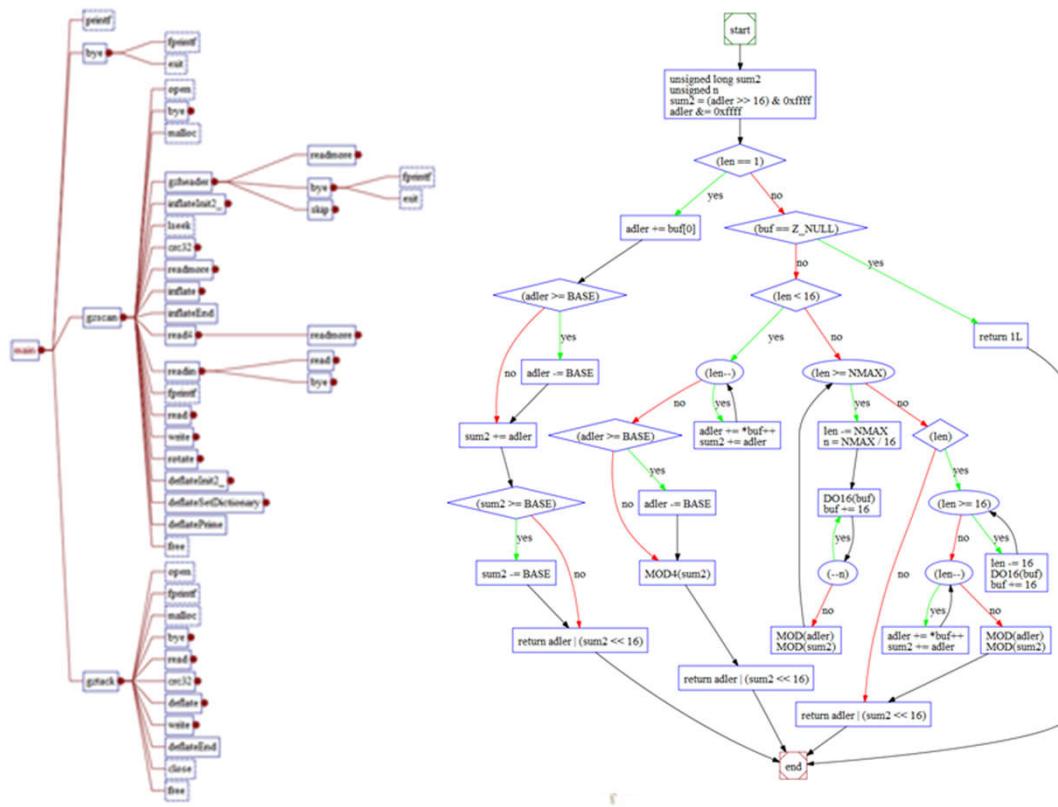
- Ada
- COBOL
- Coldfire 68k Assembly
- C/C++
- C#
- Fortran
- Java
- Jovial
- Pascal
- PL/M
- Python
- VHDL
- Web languages: PHP, HTML, CSS, JavaScript

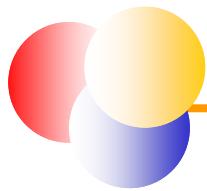




# Understand: 其他功能

- 编码规范检查
  - 依赖图抽取





# Understand

- A. Koru, et al. Comparing high-change modules and modules with the highest measurement values in two large scale open-source products. IEEE TSE, 2005
- Y. Zhou, et al. Examining the potentially confounding effect of class size on the associations between object-oriented metrics and change-proneness. IEEE TSE 2009
- ...



100



## CountLineCode

Formula: Code && ! Inactive

Result (for function printHello()): 11

```
void SayHello::printHello(){
    switch(i){
        case 0:
            cout << "Hello World" << endl;
        case 1:
            cout << "HELLO WORLD!" << endl;
        default: //A comment here
            for(int m=0; m < j; m++);
            cout << "hello world" << endl;
    }
#define A VERY_NICE_VARIABLE
    cout << "Inactive Line" << endl; // Inactive
#endif
}
```

Code	Comment	Preprocessor	Declarative	Executable	Inactive
1	0	0	1	0	0
1	0	0	0	1	0
1	0	0	0	1	0
1	0	0	0	1	0
1	0	0	0	1	0
1	0	0	0	1	0
1	1	0	0	1	0
1	0	0	1	1	0
1	0	0	0	1	0
1	0	0	0	0	0
0	0	1	0	0	0
0	0	0	0	0	1
1	1	0	0	0	1
0	0	1	0	0	0
0	0	0	0	0	0
1	0	0	0	0	0



## CountPath

**Formula:** The number of paths through the code. This can grow really fast since each if doubles the number of paths through the code.

**Result (for function pathDemo): 4**

void pathDemo(){	Paths:
if(a) dothis();	red-purple red-blue
if(b) dothat();	green-purple green-blue
}	



## MaxNesting

Formula: MAX(nesting)

Result (for function cyclomaticDemo()): 4

	Cur Nest
void cyclomaticDemo(){	0
bool a=true,b=true,c=true;	0
	0
if(a    (b && c)){	1
while(a? b : c){	2
for(int i=0; i < 10; i ++){	3
switch(i){	4
case 1:	4
case 2:	4
cout<<i<<endl;	4
break;	4
case 5:	4
break;	4
default:	4
cout<<i<<endl;	4
}	4
}	3
}	2
}	1
}	1
try{	1
do{	2
cout<<a<<b<<c<<endl;	2
}while(a);	2
}	1
catch(...){	1
}	1
}	1
}	0



## CountInput

Entity Kind: "c global object, c local object, c member object, c parameter, c function"

Reference Kind: "c use ~ptr ~inactive, c callby ~inactive"

Notes: recursive function calls and local variables that are not class static variables are not included.

Result (for class function inOutFunc): 6

Referenced Entity	Entity Kind	Reference Kind
metrictestknots.h	C Code File	C Definein
in1	C Parameter	C Define
in2	C Parameter	C Define
inout1	C Parameter	C Define
inout2	C Parameter	C Define
out1	C Parameter	C Define
out2	C Parameter	C Define
in	C Object Global	C Use
in1	C Parameter	C Use
in2	C Parameter	C Use
inout1	C Parameter	C Deref Use
inout2	C Parameter	C Use
out	C Object Global	C Set
in1	C Parameter	C Use
inout1	C Parameter	C Deref Set
in2	C Parameter	C Use
inout2	C Parameter	C Set
in1	C Parameter	C Use
out1	C Parameter	C Deref Set
in2	C Parameter	C Use
out2	C Parameter	C Set
somefunc	C Unknown Function	C Call
in1	C Parameter	C Set
in2	C Parameter	C Set

```
int in = 1;
int out = 1;

int inOutFunc(int in1, int in2, int *inout1, int &inout2, int *out1, int &out2){
    *inout1 = in1;
    inout2 = in2;

    *out1 = in1;
    out2 = in2;

    in1 = somefunc();
    in2 = 2;

    int randomint = 3;
    in1 = randomint;

    return 4;
}

void callingfunc(){
    int a,b,c,d;
    int myval = inOutFunc(1,2,a,b,c,d);
    int temp = out;
    int l = a + b + c + d;
}
```

These are all repeats of entities already counted above.



## CountOutput

Entity Kind: "c global object, c local object, c member object, c parameter, c function"

Reference Kind: "c set, c modify, c call ~inactive"

Notes: recursive function calls, local variables that are not class static variables, and parameters that are pass by value are not included. Also counts non-void return type as 1.

Result (for class function inOutFunc): 7

Referenced Entity	Entity Kind	Reference Kind
metrictestknots.h	C Code File	C Definein
in1	C Parameter	C Define
in2	C Parameter	C Define
inout1	C Parameter	C Define
inout2	C Parameter	C Define
out1	C Parameter	C Define
out2	C Parameter	C Define
in	C Object Global	C Use
in1	C Parameter	C Use
in2	C Parameter	C Use
inout1	C Parameter	C Deref Use
inout2	C Parameter	C Use
out	C Object Global	C Set
in1	C Parameter	C Use
inout1	C Parameter	C Deref Set
in2	C Parameter	C Use
inout2	C Parameter	C Set
in1	C Parameter	C Use
out1	C Parameter	C Deref Set

```
int in =1;
int out = 1;

int inOutFunc(int in1, int in2, int *inout1, int &inout2, int *out1, int &out2) {
    out = in + in1 + in2 + *inout1 + inout2;

    *inout1 = in1;
    inout2 = in2;

    *out1 = in1;
    out2 = in2;

    in1 = somefunc();
    in2 = 2;

    int randomint = 3;
    in1 = randomint;

    return 4;
}

void callingfunc(){
    int a,b,c,d;
    int myval = inOutFunc(1,2,a,b,c,d);
    int temp = out;
    int l = a + b + c + d;
}
```

## Knots

Description: Measure of overlapping jumps. If a piece of code has arrowed lines indicating where every jump in the flow of control occurs, a knot is defined as where two such lines cross each other. The number of knots is proportional to the complexity of the control flow.

<https://www.scitools.com/documents/imagesMetrics/KnotsC.png>



## Cyclomatic Complexity

Description: McCabe Cyclomatic complexity as per the original NIST paper on the subject.

Edges - Nodes + Connected Components

McCabe also proved that the cyclomatic complexity of any structured program with only one entrance point and one exit point is equal to the number of decision points contained in that program plus one (refer to section V for the proof). Understand counts the keywords for decision points (FOR, WHILE, etc) and then adds 1. For a switch statement, each 'case' is counted as 1 and the 'switch' itself adds one to the final Cyclomatic Complexity count.

<https://www.scitools.com/documents/imagesMetrics/CyclomaticC.png>

