Homework 4

## Problem1

### November 4, 2022

```
[21]: import numpy as np
     import matplotlib.pyplot as plt
     import pandas as pd
     from sklearn.datasets import load_breast_cancer
     from sklearn import datasets
     from sklearn import metrics
     from sklearn.naive_bayes import GaussianNB
     import seaborn as sns; sns.set()
     from sklearn.linear model import LogisticRegression
     from sklearn.model_selection import train_test_split
     from sklearn.datasets import make_blobs
     from sklearn.linear_model import LogisticRegression
     from sklearn.metrics import confusion matrix, classification report
     from sklearn.decomposition import PCA
     from sklearn.svm import SVC
     from sklearn.preprocessing import StandardScaler, MinMaxScaler
[22]: breast = load_breast_cancer()
[23]: breast_data = breast.data
     breast_data.shape
[23]: (569, 30)
[24]: breast input = pd.DataFrame(breast data)
     breast_input.head()
[24]:
                          2
                                 3
                                          4
                                                   5
                                                          6
                                                                   7
           0
                  1
     0 17.99 10.38 122.80 1001.0 0.11840 0.27760 0.3001 0.14710 0.2419
     1 20.57 17.77 132.90 1326.0 0.08474 0.07864 0.0869 0.07017 0.1812
     2 19.69 21.25 130.00 1203.0 0.10960 0.15990 0.1974 0.12790 0.2069
     3 11.42 20.38 77.58
                             386.1 0.14250 0.28390 0.2414 0.10520 0.2597
     4 20.29 14.34 135.10 1297.0 0.10030 0.13280 0.1980 0.10430 0.1809
             9
                      20
                                             23
                                                            25
                                                                            27 \
                             21
                                     22
                                                    24
                                                                    26
     0 0.07871 ... 25.38 17.33 184.60 2019.0 0.1622 0.6656 0.7119 0.2654
     1 0.05667 ... 24.99 23.41 158.80 1956.0 0.1238 0.1866
                                                                0.2416 0.1860
     2 0.05999 ... 23.57 25.53 152.50 1709.0 0.1444 0.4245 0.4504 0.2430
```

```
3 0.09744 ... 14.91 26.50
                                    98.87
                                            567.7 0.2098 0.8663 0.6869 0.2575
      4 0.05883 ... 22.54 16.67 152.20 1575.0 0.1374 0.2050 0.4000 0.1625
             28
      0 0.4601 0.11890
      1 0.2750 0.08902
      2 0.3613 0.08758
      3 0.6638 0.17300
      4 0.2364 0.07678
      [5 rows x 30 columns]
[25]: breast_labels = breast.target
      breast_labels.shape
[25]: (569,)
[26]: labels = np.reshape(breast_labels, (569,1))
      final_breast_data = np.concatenate([breast_data,labels],axis=1)
      final_breast_data.shape
[26]: (569, 31)
[27]: breast_dataset = pd.DataFrame(final_breast_data)
      features = breast.feature_names
      features
[27]: array(['mean radius', 'mean texture', 'mean perimeter', 'mean area',
             'mean smoothness', 'mean compactness', 'mean concavity',
             'mean concave points', 'mean symmetry', 'mean fractal dimension',
             'radius error', 'texture error', 'perimeter error', 'area error',
             'smoothness error', 'compactness error', 'concavity error',
             'concave points error', 'symmetry error',
             'fractal dimension error', 'worst radius', 'worst texture',
             'worst perimeter', 'worst area', 'worst smoothness',
             'worst compactness', 'worst concavity', 'worst concave points',
             'worst symmetry', 'worst fractal dimension'], dtype='<U23')
[28]: features_labels = np.append(features, 'Type')
      breast_dataset.columns = features_labels
      breast_dataset.head()
[28]:
        mean radius
                    mean texture mean perimeter mean area mean smoothness \
               17.99
                             10.38
      0
                                            122.80
                                                       1001.0
                                                                       0.11840
      1
               20.57
                             17.77
                                            132.90
                                                       1326.0
                                                                       0.08474
               19.69
                             21.25
                                            130.00
                                                       1203.0
                                                                       0.10960
      3
               11.42
                             20.38
                                            77.58
                                                        386.1
                                                                       0.14250
               20.29
                             14.34
                                            135.10
                                                       1297.0
                                                                       0.10030
```

```
0
                  0.27760
                                    0.3001
                                                         0.14710
                                                                          0.2419
                  0.07864
                                    0.0869
                                                         0.07017
                                                                          0.1812
      1
      2
                  0.15990
                                    0.1974
                                                         0.12790
                                                                          0.2069
                  0.28390
                                    0.2414
                                                                          0.2597
      3
                                                         0.10520
                  0.13280
                                    0.1980
                                                         0.10430
                                                                          0.1809
         mean fractal dimension ... worst texture worst perimeter worst area
      0
                        0.07871
                                             17.33
                                                              184.60
                                                                           2019.0
                                             23.41
      1
                        0.05667
                                                              158.80
                                                                           1956.0
      2
                        0.05999
                                             25.53
                                                              152.50
                                                                           1709.0
      3
                        0.09744 ...
                                             26.50
                                                               98.87
                                                                            567.7
                        0.05883 ...
                                             16.67
                                                              152.20
                                                                           1575.0
         worst smoothness worst compactness worst concavity worst concave points
                   0.1622
                                       0.6656
                                                         0.7119
                                                                                0.2654
      0
                                       0.1866
      1
                   0.1238
                                                         0.2416
                                                                                0.1860
      2
                   0.1444
                                       0.4245
                                                         0.4504
                                                                                0.2430
      3
                   0.2098
                                       0.8663
                                                         0.6869
                                                                                0.2575
                   0.1374
                                       0.2050
                                                         0.4000
                                                                                0.1625
         worst symmetry worst fractal dimension
                                                    Type
                 0.4601
                                                     0.0
      0
                                          0.11890
                 0.2750
      1
                                          0.08902
                                                     0.0
      2
                                                     0.0
                 0.3613
                                          0.08758
                 0.6638
                                          0.17300
                                                     0.0
                 0.2364
                                          0.07678
                                                     0.0
      [5 rows x 31 columns]
[29]: # Commented out due to scatter plot function needing number values
      #breast_dataset['Type'].replace(0, 'Benign',inplace=True)
      #breast_dataset['Type'].replace(1, 'Malignant', inplace=True)
[30]: breast_dataset.tail()
[30]:
           mean radius mean texture mean perimeter
                                                        mean area mean smoothness
      564
                 21.56
                                22.39
                                               142.00
                                                           1479.0
                                                                            0.11100
      565
                 20.13
                                28.25
                                               131.20
                                                           1261.0
                                                                            0.09780
                 16.60
                                28.08
      566
                                               108.30
                                                            858.1
                                                                            0.08455
      567
                 20.60
                                29.33
                                                140.10
                                                           1265.0
                                                                            0.11780
      568
                                24.54
                                                47.92
                                                                            0.05263
                  7.76
                                                            181.0
           mean compactness mean concavity mean concave points mean symmetry \
                    0.11590
                                     0.24390
                                                           0.13890
                                                                            0.1726
      564
                                     0.14400
                                                                            0.1752
      565
                    0.10340
                                                           0.09791
```

mean compactness mean concavity mean concave points mean symmetry

```
567
                    0.27700
                                     0.35140
                                                          0.15200
                                                                           0.2397
      568
                    0.04362
                                     0.00000
                                                          0.00000
                                                                           0.1587
           mean fractal dimension ... worst texture worst perimeter worst area \
                          0.05623 ...
                                               26.40
                                                                            2027.0
      564
                                                                166.10
      565
                          0.05533 ...
                                               38.25
                                                                155.00
                                                                            1731.0
      566
                          0.05648 ...
                                               34.12
                                                                126.70
                                                                            1124.0
      567
                          0.07016 ...
                                               39.42
                                                                184.60
                                                                            1821.0
      568
                          0.05884 ...
                                               30.37
                                                                 59.16
                                                                             268.6
           worst smoothness worst compactness worst concavity \
      564
                    0.14100
                                        0.21130
                                                          0.4107
                                        0.19220
                                                          0.3215
      565
                    0.11660
      566
                    0.11390
                                        0.30940
                                                          0.3403
      567
                    0.16500
                                        0.86810
                                                          0.9387
      568
                    0.08996
                                        0.06444
                                                          0.0000
           worst concave points worst symmetry worst fractal dimension Type
      564
                         0.2216
                                          0.2060
                                                                   0.07115
                                                                             0.0
      565
                         0.1628
                                          0.2572
                                                                   0.06637
                                                                             0.0
      566
                         0.1418
                                          0.2218
                                                                   0.07820
                                                                             0.0
      567
                         0.2650
                                          0.4087
                                                                   0.12400
                                                                             0.0
      568
                         0.0000
                                          0.2871
                                                                   0.07039
                                                                             1.0
      [5 rows x 31 columns]
[31]: # 80% Training split
      y = breast_dataset.loc[:,['Type']].values
      x = breast_dataset.loc[:, features].values
      x = StandardScaler().fit_transform(x)
      X_train, X_test, Y_train, Y_test = train_test_split(x, y, train_size=0.8,_
      →test size=0.2)
      y[:10]
[31]: array([[0.],
             [0.],
             [0.],
             [0.],
             [0.],
             [0.],
             [0.],
             [0.],
             [0.],
             [0.]])
```

0.09251

0.05302

0.1590

566

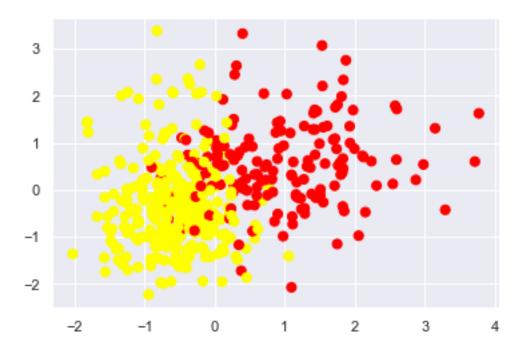
0.10230

## 1 Problem 1

Use the cancer dataset to build an SVM classifier to classify the type of cancer (Malignant vs. benign). Use the PCA feature extraction for your training. Perform N number of independent training (N=1, ..., K).

- 1. Identify the optimum number of K, principal components that achieve the highest classification accuracy.
- 2. Plot your classification accuracy, precision, and recall over a different number of Ks.
- 3. Explore different kernel tricks to capture non-linearities within your data. Plot the results and compare the accuracies for different kernels.
- 4. Compare your results against the logistic regression that you have done in homework 3. Make sure to explain and elaborate your results.

```
[32]: # Determine how linear datset currently is
plt.scatter(X_train[:, 0], X_train[:, 1], c=Y_train, s=50, cmap='autumn');
```



```
[33]: model = SVC(kernel='linear', C=1E10)
    model.fit(X_train, Y_train.ravel())

[33]: SVC(C=100000000000.0, kernel='linear')

[34]: # Perform training with K number of prinicipal components
    Accuracy = []
    Precision_B = []
    Recall_B = []
```

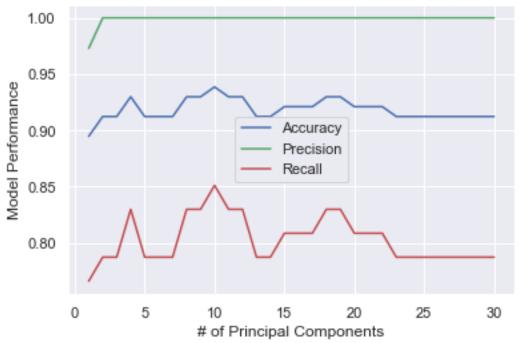
```
Precision_M = []
Recall_M = []
max_accuracy = 0;
\max_{k} = 0;
k = range(1,len(features)+1)
for i in k:
   pca final = PCA(n components=i)
    # df_train_pca = pca_final.fit_transform(X_train)
    # df_test_pca = pca_final.transform(X_test)
   principalComponents = pca_final.fit_transform(x)
   principalDF = pd.DataFrame(data = principalComponents)
   X_train, X_test, Y_train, Y_test = train_test_split(principalDF, y,_
 stest_size=0.2, random_state = 0)
   sc X = StandardScaler()
   X_train = sc_X.fit_transform(X_train)
   X_test = sc_X.fit_transform(X_test)
   svc = SVC(kernel='linear', C=0.01)
   model_SVC = svc.fit(X_train, Y_train.ravel())
   Y_pred = model_SVC.predict(X_test)
    #Accuracy.append(metrics.accuracy_score(Y_test, Y_pred))
    #Precision.append(metrics.precision_score(Y_test, Y_pred))
    #Recall.append(metrics.recall_score(Y_test, Y_pred))
    classReport = classification_report(Y_test, Y_pred, output_dict=True)
    classData = pd.DataFrame(classReport)
   Accuracy.append(classData.values[0,2])
   Precision_B.append(classData.values[0,0])
   Precision_M.append(classData.values[0,1])
   Recall B.append(classData.values[1,0])
   Recall_M.append(classData.values[1,1])
   if Accuracy[i-1] > max_accuracy:
       \max k = i
       max_accuracy = Accuracy[i-1]
print(metrics.classification report(Y test, Y pred))
print(metrics.confusion_matrix(Y_test, Y_pred))
print("The optimal number of principal components:",
      max_k, "with an accuracy of: ", max_accuracy)
```

	precision	recall	f1-score	support
0.0	1.00	0.79	0.88	47
1.0	0.87	1.00	0.93	67
accuracy			0.91	114
macro avg	0.94	0.89	0.91	114

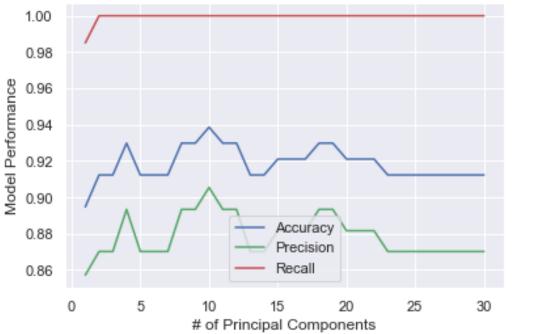
```
0.92 0.91
     weighted avg
                                           0.91
                                                      114
     [[37 10]
      [ 0 67]]
     The optimal number of principal components: 10 with an accuracy of:
     0.9385964912280702
[35]: # Linear Kernel: Benign Performance
     plt.plot(k, Accuracy, 'b', label="Accuracy")
     plt.plot(k, Precision_B, 'g', label="Precision")
     plt.plot(k, Recall_B, 'r', label="Recall")
     plt.xlabel("# of Principal Components")
     plt.ylabel("Model Performance")
     plt.title("Principal Components vs. Model Performance with Benign (Linear ∪
       plt.legend()
     plt.show()
     # Linear Kernel: Malignant Performance
     plt.plot(k, Accuracy, 'b', label="Accuracy")
     plt.plot(k, Precision_M, 'g', label="Precision")
     plt.plot(k, Recall_M, 'r', label="Recall")
     plt.xlabel("# of Principal Components")
     plt.ylabel("Model Performance")
     plt.title("Principal Components vs. Model Performance with Malignant (Linear ∪

→Kernal)")
     plt.legend()
     plt.show()
```





# Principal Components vs. Model Performance with Malignant (Linear Kernal)



```
[36]: # Perform training with K number of prinicipal components (Poly Kernel)
      Accuracy = []
      Precision_B = []
      Recall_B = []
      Precision_M = []
      Recall_M = []
      max_accuracy = 0
      \max_k = 0
      k = range(1,len(features)+1)
      for i in k:
          pca_final = PCA(n_components=i)
          # df_train_pca = pca_final.fit_transform(X_train)
          # df_test_pca = pca_final.transform(X_test)
          principalComponents = pca_final.fit_transform(x)
          principalDF = pd.DataFrame(data = principalComponents)
          X_train, X_test, Y_train, Y_test = train_test_split(principalDF, y,__
       ⇔test_size=0.2, random_state = 0)
          sc_X = StandardScaler()
          X_train = sc_X.fit_transform(X_train)
          X_test = sc_X.fit_transform(X_test)
          svc = SVC(kernel='poly', C=0.1, degree = 15)
          model_SVC = svc.fit(X_train, Y_train.ravel())
          Y_pred = model_SVC.predict(X_test)
          #Accuracy.append(metrics.accuracy_score(Y_test, Y_pred))
          #Precision.append(metrics.precision_score(Y_test, Y_pred))
          #Recall.append(metrics.recall_score(Y_test, Y_pred))
          classReport = classification_report(Y_test, Y_pred, output_dict=True)
          classData = pd.DataFrame(classReport)
          Accuracy.append(classData.values[0,2])
          Precision_B.append(classData.values[0,0])
          Precision_M.append(classData.values[0,1])
          Recall_B.append(classData.values[1,0])
          Recall_M.append(classData.values[1,1])
          if Accuracy[i-1] > max_accuracy:
              \max k = i
              max_accuracy = Accuracy[i-1]
      print(metrics.classification_report(Y_test, Y_pred))
      print(metrics.confusion_matrix(Y_test, Y_pred))
      print("The optimal number of principal components:",
            max_k, "with an accuracy of: ", max_accuracy)
```

```
precision recall f1-score support

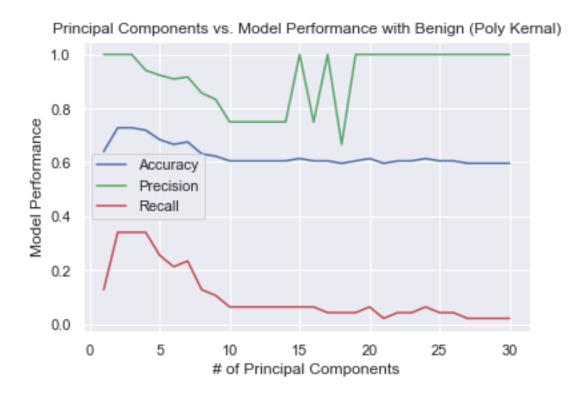
1.00 0.02 0.04 47
```

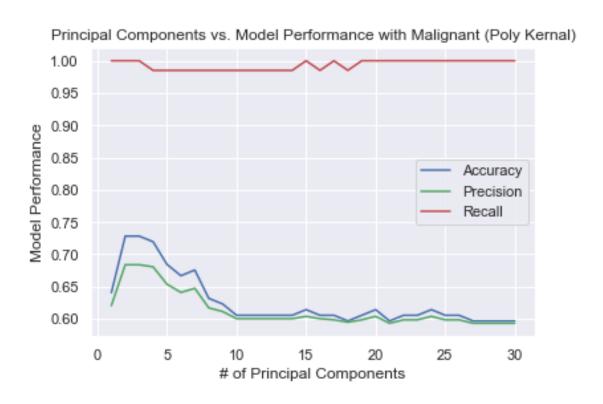
0.0

```
0.59
                                  1.00
                                             0.74
              1.0
                                                         67
                                             0.60
                                                        114
         accuracy
        macro avg
                        0.80
                                   0.51
                                             0.39
                                                        114
     weighted avg
                        0.76
                                   0.60
                                             0.45
                                                        114
     [[ 1 46]
      [ 0 67]]
     The optimal number of principal components: 2 with an accuracy of:
     0.7280701754385965
[37]: # Poly Kernel: Benign Performance
      plt.plot(k, Accuracy, 'b', label="Accuracy")
      plt.plot(k, Precision_B, 'g', label="Precision")
      plt.plot(k, Recall_B, 'r', label="Recall")
      plt.xlabel("# of Principal Components")
      plt.ylabel("Model Performance")
      plt.title("Principal Components vs. Model Performance with Benign (Poly⊔

→Kernal)")
      plt.legend()
      plt.show()
      # Poly Kernel: Malignant Performance
      plt.plot(k, Accuracy, 'b', label="Accuracy")
      plt.plot(k, Precision_M, 'g', label="Precision")
      plt.plot(k, Recall_M, 'r', label="Recall")
      plt.xlabel("# of Principal Components")
      plt.ylabel("Model Performance")
      plt.title("Principal Components vs. Model Performance with Malignant (Poly⊔

→Kernal)")
      plt.legend()
      plt.show()
```





```
[38]: | # Perform training with K number of prinicipal components (rbf kernel)
      Accuracy = []
      Precision_B = []
      Recall_B = []
      Precision M = []
      Recall_M = []
      max_accuracy = 0
      \max_{k}
      k = range(1,len(features)+1)
      for i in k:
          pca final = PCA(n components=i)
          # df_train_pca = pca_final.fit_transform(X_train)
          # df_test_pca = pca_final.transform(X_test)
          principalComponents = pca_final.fit_transform(x)
          principalDF = pd.DataFrame(data = principalComponents)
          X_train, X_test, Y_train, Y_test = train_test_split(principalDF, y,__
       ⇔test_size=0.2, random_state = 0)
          sc_X = StandardScaler()
          X_train = sc_X.fit_transform(X_train)
          X_test = sc_X.fit_transform(X_test)
          svc = SVC(kernel='rbf', C=10, gamma=0.01)
          model_SVC = svc.fit(X_train, Y_train.ravel())
          Y_pred = model_SVC.predict(X_test)
          #Accuracy.append(metrics.accuracy_score(Y_test, Y_pred))
          #Precision.append(metrics.precision_score(Y_test, Y_pred))
          #Recall.append(metrics.recall_score(Y_test, Y_pred))
          classReport = classification_report(Y_test, Y_pred, output_dict=True)
          classData = pd.DataFrame(classReport)
          Accuracy.append(classData.values[0,2])
          Precision_B.append(classData.values[0,0])
          Precision_M.append(classData.values[0,1])
          Recall_B.append(classData.values[1,0])
          Recall_M.append(classData.values[1,1])
          if Accuracy[i-1] > max_accuracy:
              \max k = i
              max_accuracy = Accuracy[i-1]
      print(metrics.classification_report(Y_test, Y_pred))
      print(metrics.confusion_matrix(Y_test, Y_pred))
      print("The optimal number of principal components:",
            max_k, "with an accuracy of: ", max_accuracy)
```

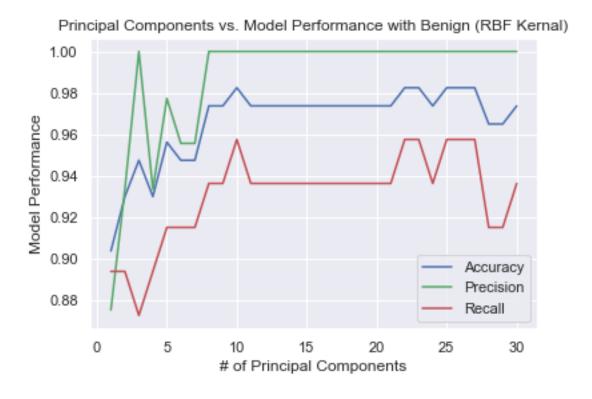
```
precision recall f1-score support

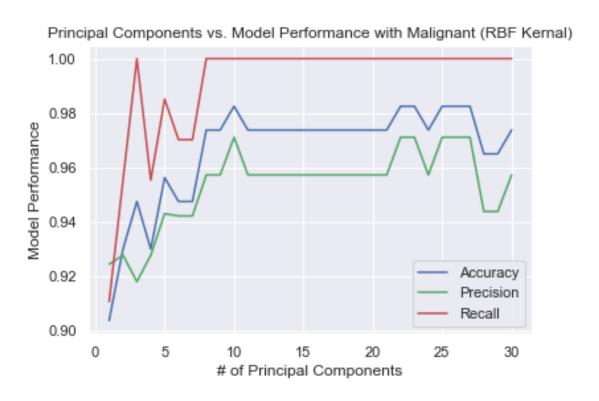
1.00 0.94 0.97 47
```

0.0

```
0.96
              1.0
                                   1.00
                                             0.98
                                                         67
                                             0.97
                                                        114
         accuracy
        macro avg
                         0.98
                                   0.97
                                             0.97
                                                        114
     weighted avg
                         0.97
                                   0.97
                                             0.97
                                                        114
     [[44 3]
      [ 0 67]]
     The optimal number of principal components: 10 with an accuracy of:
     0.9824561403508771
[39]: # RBF Kernel: Benign Performance
      plt.plot(k, Accuracy, 'b', label="Accuracy")
      plt.plot(k, Precision_B, 'g', label="Precision")
      plt.plot(k, Recall_B, 'r', label="Recall")
      plt.xlabel("# of Principal Components")
      plt.ylabel("Model Performance")
      plt.title("Principal Components vs. Model Performance with Benign (RBF Kernal)")
      plt.legend()
      plt.show()
      # RBF Kernel: Malignant Performance
      plt.plot(k, Accuracy, 'b', label="Accuracy")
      plt.plot(k, Precision_M, 'g', label="Precision")
      plt.plot(k, Recall_M, 'r', label="Recall")
      plt.xlabel("# of Principal Components")
      plt.ylabel("Model Performance")
      plt.title("Principal Components vs. Model Performance with Malignant (RBF_{\sqcup}

→Kernal)")
      plt.legend()
      plt.show()
```





[]:	
[]:	

# Problem2

### November 4, 2022

```
[140]: import numpy as np
       import matplotlib.pyplot as plt
       import pandas as pd
       from sklearn.datasets import load_breast_cancer
       from sklearn import datasets
       from sklearn import metrics
       from sklearn.naive_bayes import GaussianNB
       import seaborn as sns; sns.set()
       from sklearn.linear_model import LogisticRegression
       from sklearn.model_selection import train_test_split
       from sklearn.datasets import make_blobs
       from sklearn.linear_model import LogisticRegression
       from sklearn.metrics import confusion matrix, classification report
       from sklearn.decomposition import PCA
       from sklearn.svm import SVC
       from sklearn.svm import SVR
       from sklearn.preprocessing import StandardScaler, MinMaxScaler
       from sklearn.metrics import mean_squared_error
       from sklearn.metrics import r2_score
[141]: housing = pd.DataFrame(pd.read_csv("./Housing.csv"))
       housing.head()
[141]:
                         bedrooms
                                    bathrooms
                                                stories mainroad guestroom basement
             price area
        13300000 7420
                                 4
                                            2
                                                      3
                                                             yes
                                                                        no
                                                                                 no
       1 12250000 8960
                                 4
                                             4
                                                      4
                                                             yes
                                                                        no
                                                                                 no
       2 12250000 9960
                                 3
                                             2
                                                      2
                                                             yes
                                                                        no
                                                                                 yes
       3 12215000 7500
                                 4
                                             2
                                                      2
                                                             yes
                                                                        no
                                                                                 yes
       4 11410000 7420
                                 4
                                             1
                                                      2
                                                             yes
                                                                       yes
                                                                                 yes
         hotwaterheating airconditioning parking prefarea furnishingstatus
       0
                                                 2
                                                                   furnished
                      no
                                     yes
                                                        yes
       1
                                                 3
                                                                   furnished
                                     yes
                                                        no
                      no
       2
                                                 2
                                                              semi-furnished
                                                        yes
                      no
                                      no
       3
                                                 3
                                                                   furnished
                      no
                                     yes
                                                        yes
       4
                                     yes
                                                                   furnished
                      no
                                                         no
```

	price	area	bedrooms	bathrooms	stories	${\tt mainroad}$	guestroom	\
0	13300000	7420	4	2	3	1	0	
1	12250000	8960	4	4	4	1	0	
2	12250000	9960	3	2	2	1	0	
3	12215000	7500	4	2	2	1	0	
4	11410000	7420	4	1	2	1	1	
	1 2 3	13300000 1 12250000 2 12250000 3 12215000	price area 13300000 7420 1 12250000 8960 2 12250000 9960 3 12215000 7500 4 11410000 7420	0       13300000       7420       4         1       12250000       8960       4         2       12250000       9960       3         3       12215000       7500       4	0       13300000       7420       4       2         1       12250000       8960       4       4         2       12250000       9960       3       2         3       12215000       7500       4       2	0       13300000       7420       4       2       3         1       12250000       8960       4       4       4         2       12250000       9960       3       2       2         3       12215000       7500       4       2       2	0       13300000       7420       4       2       3       1         1       12250000       8960       4       4       4       1         2       12250000       9960       3       2       2       1         3       12215000       7500       4       2       2       1	1     12250000     8960     4     4     4     1     0       2     12250000     9960     3     2     2     1     0       3     12215000     7500     4     2     2     1     0

	basement	hotwaterheating	airconditioning	parking	prefarea	\
0	0	0	1	2	1	
1	0	0	1	3	0	
2	1	0	0	2	1	
3	1	0	1	3	1	
4	1	0	1	2	0	

furnishingstatus

0	furnished
1	furnished
2	semi-furnished
3	furnished
4	furnished

## 1 Problem 2

Develop a SVR regression model that predicts housing price based on the following input variables:

Area, bedrooms, bathrooms, stories, mainroad, guestroom, basement, hotwaterheating, airconditioning, parking, prefarea

- 1. Plot your regression model for SVR similar to the sample code provided on Canvas.
- 2. Compare your results against linear regression with regularization loss that you already did in homework1.
- 3. Use the PCA feature extraction for your training. Perform N number of independent training (N=1, ..., K). Identify the optimum number of K, principal components that achieve the highest regression accuracy.
- 4. Explore different kernel tricks to capture non-linearities within your data. Plot the results and compare the accuracies for different kernels.

```
[143]: | # Obtain SVR model and compare performance with linear regression
       input_vars = ['area', 'bedrooms', 'bathrooms', 'stories',
                   'mainroad', 'guestroom', 'basement', 'hotwaterheating',
                   'airconditioning', 'parking', 'prefarea']
       x = housing[input_vars]
       y = housing['price']
       y.head()
[143]: 0
            13300000
            12250000
       2
           12250000
       3
            12215000
            11410000
       Name: price, dtype: int64
[144]: # Training split and feature scaling
       standScale = StandardScaler()
       # x = standScale.fit_transform(x)
       # X train, X test, Y train, Y test = train test_split(x, y, train_size=0.8, ___
       \hookrightarrow test\_size=0.2)
       # Y train.head()
       X_train, X_test, Y_train, Y_test = train_test_split(x, y, test_size=0.2,_
        →random state = 0)
       print(X_train.shape, X_test.shape, Y_train.shape, Y_test.shape)
       sc_X = StandardScaler()
       X_train = sc_X.fit_transform(X_train)
       X_test = sc_X.fit_transform(X_test)
      (436, 11) (109, 11) (436,) (109,)
[152]: svr_lin = SVR(kernel='linear', C=1e6)
       y lin = svr lin.fit(X train, Y train).predict(X test)
       svr_poly = SVR(kernel='poly', C=1e6, degree=2)
       y_poly = svr_poly.fit(X_train, Y_train).predict(X_test)
       svr_rbf = SVR(kernel='rbf', C=1e6, gamma=0.1)
       y_rbf = svr_rbf.fit(X_train, Y_train).predict(X_test)
[151]: plt.scatter(Y_test, y_lin, label = 'Linear Kernel')
       plt.scatter(Y_test, y_poly, label = 'Polynomial Kernel')
       plt.scatter(Y_test, y_rbf, label = 'Radial Basis Function Kernel')
       plt.xlabel("Actual Price")
       plt.ylabel("Predicted Price")
       plt.title("Actual vs. Predicted Price of Housing")
       plt.legend()
       plt.show()
```



```
[147]: # Linear Kernel
       Accuracy_lin = []
       max_accuracy_lin = 0
       \max_k_{\min} = 0
       k = range(1,len(input_vars)+1)
       for i in k:
           pca_final = PCA(n_components=i)
           # df_train_pca = pca_final.fit_transform(X_train)
           \# df\_test\_pca = pca\_final.transform(X\_test)
           principalComponents = pca_final.fit_transform(x)
           principalDF = pd.DataFrame(data = principalComponents)
           X_train, X_test, Y_train, Y_test = train_test_split(principalDF, y,_
        →test_size=0.2, random_state = 0)
           print(X_train.shape, X_test.shape, Y_train.shape, Y_test.shape)
           sc_X = StandardScaler()
           X_train = sc_X.fit_transform(X_train)
           X_test = sc_X.transform(X_test)
           svr = SVR(kernel='linear', C=1e6)
```

```
model_SVR = svr.fit(X_train, Y_train)
           Y_pred = model_SVR.predict(X_test)
           #Accuracy_lin.append(mean_squared_error(Y_test, Y_pred))
           Accuracy_lin.append(r2_score(Y_test, Y_pred))
           #Accuracy_lin.append(model_SVR.score(Y_test, Y_pred))
           if Accuracy_lin[i-1] > max_accuracy_lin:
               \max k \lim = i
               max_accuracy_lin = Accuracy_lin[i-1]
       print("The optimal number of principal components:",
             max_k_lin, "with an accuracy of: ", max_accuracy_lin)
      (436, 1) (109, 1) (436,) (109,)
      (436, 2) (109, 2) (436,) (109,)
      (436, 3) (109, 3) (436,) (109,)
      (436, 4) (109, 4) (436,) (109,)
      (436, 5) (109, 5) (436,) (109,)
      (436, 6) (109, 6) (436,) (109,)
      (436, 7) (109, 7) (436,) (109,)
      (436, 8) (109, 8) (436,) (109,)
      (436, 9) (109, 9) (436,) (109,)
      (436, 10) (109, 10) (436,) (109,)
      (436, 11) (109, 11) (436,) (109,)
      The optimal number of principal components: 8 with an accuracy of:
      0.6869222993273993
[148]: # Poly Kernel
      Accuracy_poly = []
      max_accuracy_poly = 0
       \max_{k} poly = 0
       k = range(1,len(input_vars)+1)
       for i in k:
           pca_final = PCA(n_components=i)
           # df_train_pca = pca_final.fit_transform(X_train)
           \# df\_test\_pca = pca\_final.transform(X\_test)
           principalComponents = pca_final.fit_transform(x)
           principalDF = pd.DataFrame(data = principalComponents)
           X_train, X_test, Y_train, Y_test = train_test_split(principalDF, y,_
        stest_size=0.2, random_state = 0)
           print(X_train.shape, X_test.shape, Y_train.shape, Y_test.shape)
           sc X = StandardScaler()
           X_train = sc_X.fit_transform(X_train)
           X_test = sc_X.transform(X_test)
```

```
svr = SVR(kernel='poly', C=1e6)
           model_SVR = svr.fit(X_train, Y_train)
           Y_pred = model_SVR.predict(X_test)
           #Accuracy_poly.append(mean_squared_error(Y_test, Y_pred))
           Accuracy_poly.append(r2_score(Y_test, Y_pred))
           #Accuracy_poly.append(model_SVR.score(Y_train, Y_test))
           if Accuracy_poly[i-1] > max_accuracy_poly:
               \max_k_{poly} = i
               max_accuracy_poly = Accuracy_poly[i-1]
       print("The optimal number of principal components:",
             max_k_poly, "with an accuracy of: ", max_accuracy_poly)
      (436, 1) (109, 1) (436,) (109,)
      (436, 2) (109, 2) (436,) (109,)
      (436, 3) (109, 3) (436,) (109,)
      (436, 4) (109, 4) (436,) (109,)
      (436, 5) (109, 5) (436,) (109,)
      (436, 6) (109, 6) (436,) (109,)
      (436, 7) (109, 7) (436,) (109,)
      (436, 8) (109, 8) (436,) (109,)
      (436, 9) (109, 9) (436,) (109,)
      (436, 10) (109, 10) (436,) (109,)
      (436, 11) (109, 11) (436,) (109,)
      The optimal number of principal components: 5 with an accuracy of:
      0.5109504213287848
[149]: # RBF Kernel
      Accuracy_rbf = []
       max_accuracy_rbf = 0
      \max_{k} p = 0
       k = range(1,len(input_vars)+1)
       for i in k:
           pca_final = PCA(n_components=i)
           # df_train_pca = pca_final.fit_transform(X_train)
           # df_test_pca = pca_final.transform(X_test)
           principalComponents = pca_final.fit_transform(x)
           principalDF = pd.DataFrame(data = principalComponents)
           X_train, X_test, Y_train, Y_test = train_test_split(principalDF, y,_
        stest_size=0.2, random_state = 0)
           print(X_train.shape, X_test.shape, Y_train.shape, Y_test.shape)
           sc_X = StandardScaler()
           X_train = sc_X.fit_transform(X_train)
           X_test = sc_X.transform(X_test)
```

```
svr = SVR(kernel='rbf', C=1e6)
           model_SVR = svr.fit(X_train, Y_train)
           Y_pred = model_SVR.predict(X_test)
           #Accuracy_rbf.append(mean_squared_error(Y_test, Y_pred))
           Accuracy_rbf.append(r2_score(Y_test, Y_pred))
           #Accuracy_rbf.append(model_SVR.score(Y_train, Y_test))
           if Accuracy_rbf[i-1] > max_accuracy_rbf:
               \max k rbf = i
               max_accuracy_rbf = Accuracy_rbf[i-1]
       print("The optimal number of principal components:",
             max_k_rbf, "with an accuracy of: ", max_accuracy_rbf)
      (436, 1) (109, 1) (436,) (109,)
      (436, 2) (109, 2) (436,) (109,)
      (436, 3) (109, 3) (436,) (109,)
      (436, 4) (109, 4) (436,) (109,)
      (436, 5) (109, 5) (436,) (109,)
      (436, 6) (109, 6) (436,) (109,)
      (436, 7) (109, 7) (436,) (109,)
      (436, 8) (109, 8) (436,) (109,)
      (436, 9) (109, 9) (436,) (109,)
      (436, 10) (109, 10) (436,) (109,)
      (436, 11) (109, 11) (436,) (109,)
      The optimal number of principal components: 5 with an accuracy of:
      0.5794939259825025
[150]: plt.plot(k, Accuracy_lin, 'b', label="Linear")
      plt.plot(k, Accuracy_poly, 'r', label="Poly")
       plt.plot(k, Accuracy_rbf, 'g', label="RBF")
       plt.xlabel("# of Principal Components")
       plt.ylabel("Model Performance")
       plt.title("Principal Components vs. Accuracy")
       plt.legend()
       plt.show()
```

