8/11/2017 LinearRegression

## LinearRegression

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require(MASS)

## Loading required package: MASS

```
# Loading the data
SwimDataLoading<-read.table("swim.dat")</pre>
SwimData<-as.matrix(SwimDataLoading)</pre>
seqData = seq(from=1,to=11,by=2)
# creating a BiWeekly sequence
ByWeekly<-matrix(seqData,6,1)</pre>
ByWeekly<-cbind(rep(1,6),ByWeekly)</pre>
# Initializing the prior values
# creating the fucntion to calcualte the Gibbs Sammpling
functionlinearRegOfSwim<-function(Data, ByWeekly){</pre>
  NumberOfFeatures<-2
  Beta0<-matrix(c(23,0),2,1)
  CoVarienceSigma0<-matrix(c(1,0,0,1),2,2)
  sigma0<-1
  nu0<-2
  Data<-as.vector(Data)</pre>
#initial values
  SamplingSize<-10000
  FinalBeta<-GibbsSigmaUpdate<-NULL
  RegressionModelResult<-lm(Data~ByWeekly[,-1])
  SummaryRegression<-summary(RegressionModelResult)$coef</pre>
  SSR<-sum((Data-(ByWeekly%*%SummaryRegression))^2)
  sampleVariance<-SSR/(length(Data)-NumberOfFeatures)</pre>
# Gibbbs iterative sampling starts here
# im sampling 10,000 samples here
for(i in 1:SamplingSize){
  temp =((t(ByWeekly))%*%ByWeekly)/sampleVariance)
  VarianceOfBeta<-solve(solve(CoVarienceSigma0)+temp)</pre>
  temp2= (t(ByWeekly)%*%Data)
  mu<-VarianceOfBeta%*%((solve(CoVarienceSigma0))%*%Beta0)+temp2/sampleVariance)</pre>
  SummaryRegression<-mvrnorm(1,mu,VarianceOfBeta)</pre>
  SSR<-sum((Data-(ByWeekly%*%SummaryRegression))^2)
  phi2<-rgamma(1,(nu0+length(Data))/2,((nu0*sigma0)+SSR)/2)</pre>
  sampleVariance<-(1/phi2)</pre>
  FinalBeta<-rbind(FinalBeta, SummaryRegression)
  GibbsSigmaUpdate<-rbind(GibbsSigmaUpdate,sampleVariance)</pre>
}
```

```
# The resultant Gibbs
GibbsResultantDataframe<-data.frame(FinalBeta,GibbsSigmaUpdate)</pre>
colnames(GibbsResultantDataframe)<-c("BetaBeta0","BetaBeta1","GibbsSigmaUpdate")</pre>
return(GibbsResultantDataframe)
}
# Call the gibbs sampling to calcualte the Swimmers info
Swimmer1BetaCoefs<-functionlinearRegOfSwim(SwimData[1,],ByWeekly)</pre>
Swimmer2BetaCoefs<-functionlinearRegOfSwim(SwimData[2,],ByWeekly)</pre>
Swimmer3BetaCoefs<-functionlinearRegOfSwim(SwimData[3,],ByWeekly)</pre>
Swimmer4BetaCoefs<-functionlinearRegOfSwim(SwimData[4,],ByWeekly)</pre>
Swimmer1Means<-colMeans(Swimmer1BetaCoefs)</pre>
Swimmer2Means<-colMeans(Swimmer2BetaCoefs)</pre>
Swimmer3Means<-colMeans(Swimmer3BetaCoefs)</pre>
Swimmer4Means<-colMeans(Swimmer4BetaCoefs)</pre>
# printing the mean of the each swimmers calculated value
print(Swimmer1Means)
##
           BetaBeta0
                             BetaBeta1 GibbsSigmaUpdate
##
         23.1642964
                            -0.0403233
                                               0.4689561
print(Swimmer2Means)
##
           BetaBeta0
                             BetaBeta1 GibbsSigmaUpdate
##
        23.10578943
                            0.03843639
                                              0.47793640
print(Swimmer3Means)
##
           BetaBeta0
                             BetaBeta1 GibbsSigmaUpdate
##
        22.72575656
                            0.01046978
                                              0.47284365
print(Swimmer4Means)
##
           BetaBeta0
                             BetaBeta1 GibbsSigmaUpdate
       23.572798997
##
                          -0.008088089
                                             0.474590738
```

```
#b
# Sampling one sample from all the different 10,000 gibbs iterations Beta values
Ssigma <- sqrt(mean(Swimmer2BetaCoefs$GibbsSigmaUpdate))</pre>
BetasObtainedThroughGibbs<-data.matrix(Swimmer1BetaCoefs[,1:2])</pre>
DataX<-matrix(c(1,15),2,1)
PredictedMean<-BetasObtainedThroughGibbs%*%DataX
PredictedY1<-vector()</pre>
# will return the 10,000 new samples with those particular parameters
PredictedY1<-apply(PredictedMean, 1, function(xx) rnorm(1,xx,Ssigma) )</pre>
BetasObtainedThroughGibbs<-data.matrix(Swimmer2BetaCoefs[,1:2])</pre>
DataX<-matrix(c(1,15),2,1)
PredictedMean<-BetasObtainedThroughGibbs%*%DataX
PredictedY2<-vector()
PredictedY2<-apply(PredictedMean, 1, function(xx) rnorm(1,xx,Ssigma) )</pre>
BetasObtainedThroughGibbs<-data.matrix(Swimmer3BetaCoefs[,1:2])</pre>
DataX<-matrix(c(1,15),2,1)</pre>
PredictedMean<-BetasObtainedThroughGibbs%*%DataX
PredictedY3<-vector()</pre>
PredictedY3<-apply(PredictedMean, 1, function(xx) rnorm(1,xx,Ssigma) )</pre>
BetasObtainedThroughGibbs<-data.matrix(Swimmer4BetaCoefs[,1:2])</pre>
DataX<-matrix(c(1,15),2,1)</pre>
PredictedMean<-BetasObtainedThroughGibbs%*%DataX
PredictedY4<-vector()</pre>
PredictedY4<-apply(PredictedMean, 1, function(xx) rnorm(1,xx,Ssigma) )</pre>
# 3. Prediction / classification
# for each row we see who is the swimmer with max value? that particualr individual repesents that particualr row in the cla
ssification
Y predict<-data.frame(PredictedY1, PredictedY2, PredictedY3, PredictedY4)
# In all 10,000 checking how many times the Swimmer 1 is greater or Swimmer one got classified
swimmer1<-
mean(Y predict$PredictedY1>Y predict$PredictedY2&Y predict$PredictedY1>Y predict$PredictedY3&Y predict$PredictedY1>Y predict$P
```

```
redictedY4)
 swimmer2<-
mean(Y predict$PredictedY2>Y predict$PredictedY1&Y predict$PredictedY2>Y predict$PredictedY3&Y predict$PredictedY2>Y predict$PredictedY2>Y predict$PredictedY3&Y predict$PredictedY2>Y predict$PredictedY3&Y predict$PredictedY3&Y predict$PredictedY2>Y predict$PredictedY3&Y predict*PredictedY3&Y predict*Predict
redictedY4)
swimmer3<-
mean(Y_predict$PredictedY3>Y_predict$PredictedY1&Y_predict$PredictedY3>Y_predict$PredictedY2&Y_predict$PredictedY3>Y_predict$P
redictedY4)
 swimmer4<-
mean(Y predict$PredictedY4>Y predict$PredictedY1&Y predict$PredictedY4>Y predict$PredictedY2&Y predict$PredictedY4>Y
redictedY3)
print(swimmer1)
## [1] 0.0931
print(swimmer2)
## [1] 0.4302
print(swimmer3)
## [1] 0.1497
print(swimmer4)
## [1] 0.327
# See if sum of all these approx to 1
print(swimmer1+swimmer2+swimmer3+swimmer4)
## [1] 1
```