

Simple Linear Regression

easy to understand.
Foundation Algorithm.

LR → Supervised Machine Learning Algorithm

Regression

Multiple LR Polynomial LR

Simple

1 input Column
1 output Column

Multiple input Column

Cgpa	gndu	12 th	stat	package
7.1				
4.7				
8.4				
8.1				

Cgpa/package

Cgpa	package
7.1	3.5
4.7	1.2
8.4	4.2
8.1	3.9

model → package

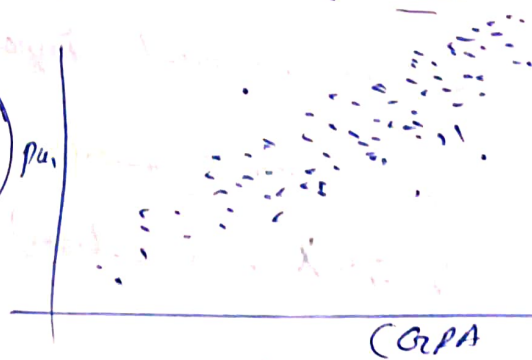
Cgpa

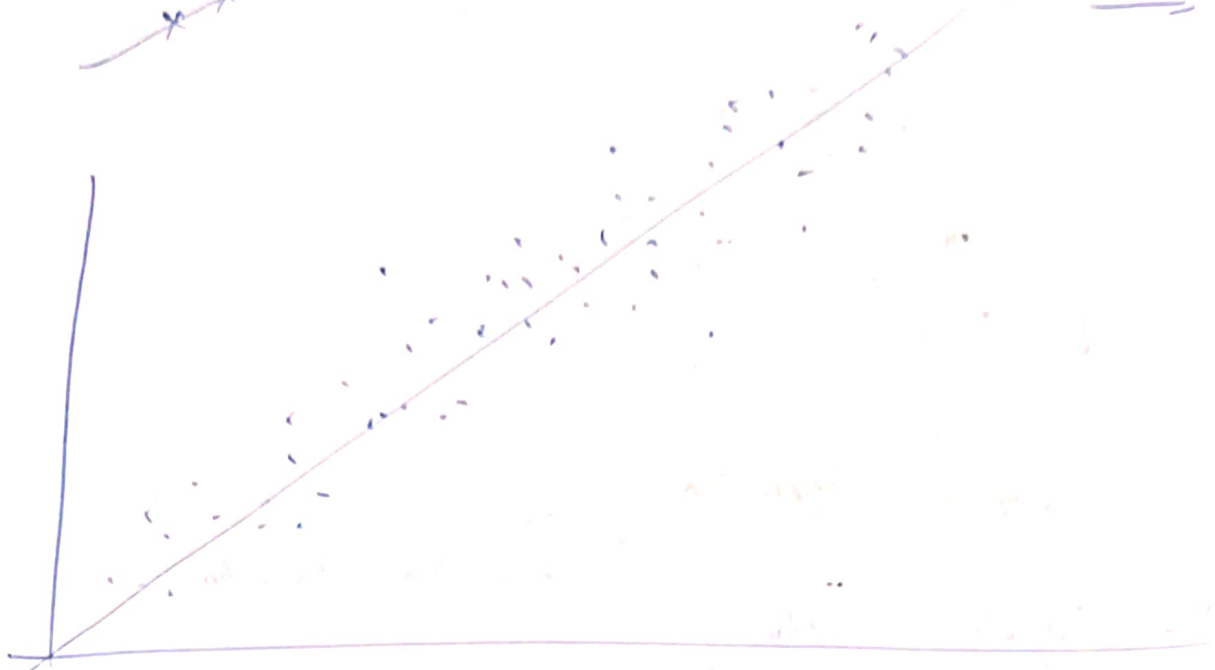
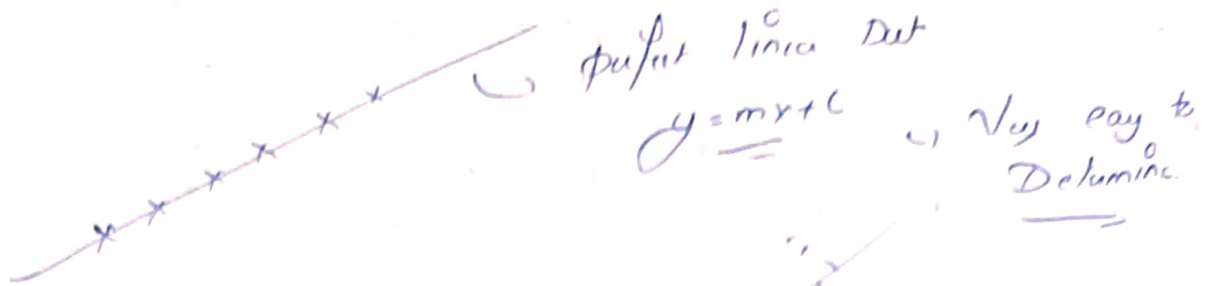
first, plot the Data

Real world Dataset

Sort of Linear Data

stochastic error → jo dekhne se hi ka hai





Same points se ekdam clearly.
pane hain.

$m \rightarrow$ slope
 $b \rightarrow$ y-intercept } in points pe minimum Galti hain
 find that (m, b)

$$X = df.iloc[:, 0:1]$$

$$y = df.iloc[:, -1]$$

from sklearn.model_selection import train_test_split
 $X_{train}, X_{test}, y_{train}, y_{test} = \text{train_test_split}$

($X, y, \text{test_size} = 0.2,$
 $\text{random_state} = 2$)

from sklearn.linear_model import LinearRegression

$$lr = \text{LinearRegression}()$$

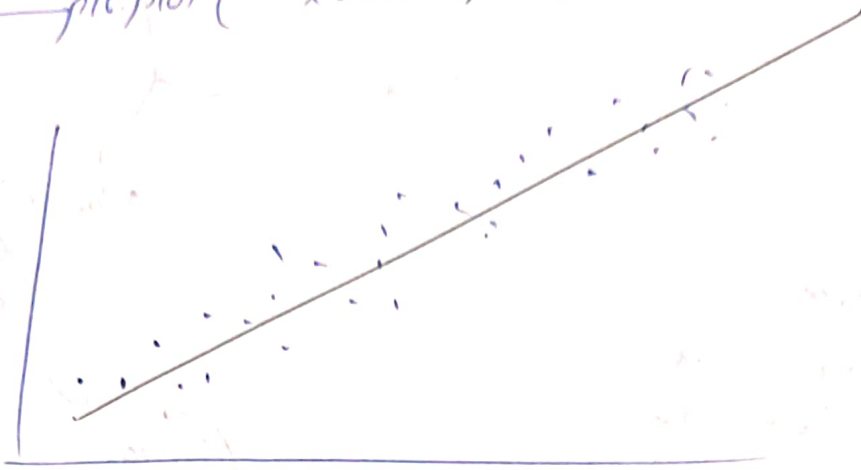
$$lr.\text{fit}(X_{train}, y_{train})$$

New ~~lr.predict(X_test.iloc[0])~~

lr.predict(X_test.iloc[0].values.reshape(1,1))

→ See the regression ^{line}

plot { plt.plot(X_test, lr.predict(X_test), color='red') }

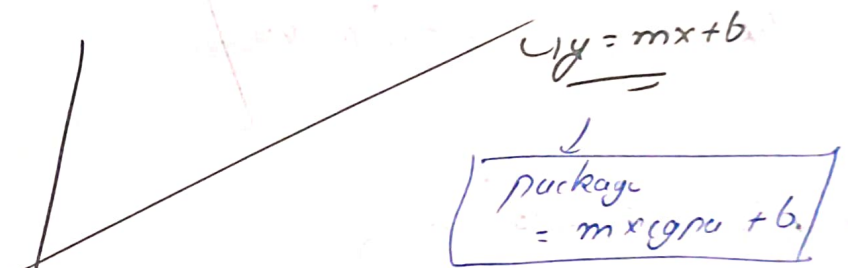


$m = \text{lr.coef}$ → Slope

$b = \text{lr.intercept}$

$y = mx + b$

Intuition



(m) → weightage (cgru pe kitna depend)

m ↓ (↑) → weightage of cgru on package

(b=0)

package = m * cgru

offset

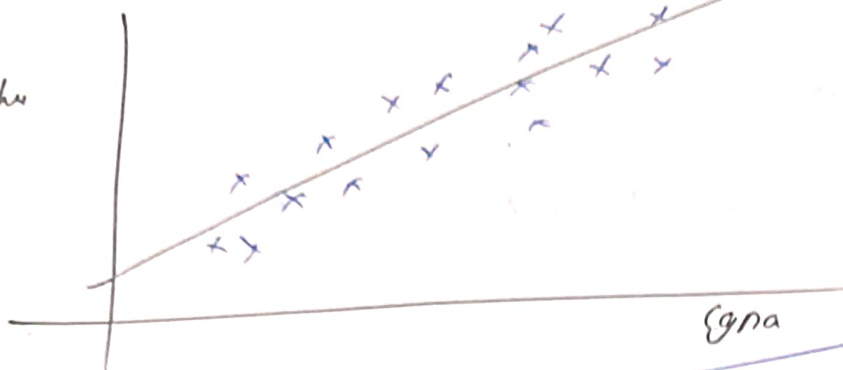
→ ki agar m=0 still kuch Logo

ex/ 0

SIMPLE LINEAR REGRESSION

MATHEMATICAL FORMULATION

Y-axis



best fit line
 $y = mx + b$

(m, b)

Closed form
 Solution

(ek formula bana sakte ho
 using Differential or
 Integration ke)

the it is a Closed form
 Solution

$$\text{like } x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Direct formula

(OLS)
 Ordinary Least
 Square

$$b = \bar{y} - m\bar{x} \quad \left| \quad m = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sum_{i=1}^n (x_i - \bar{x})^2}$$

$\bar{x} \rightarrow$ mean
 $\bar{y} \rightarrow$ mean

Non-closed
 form
 Solution

(Gradient Descent
 technique)

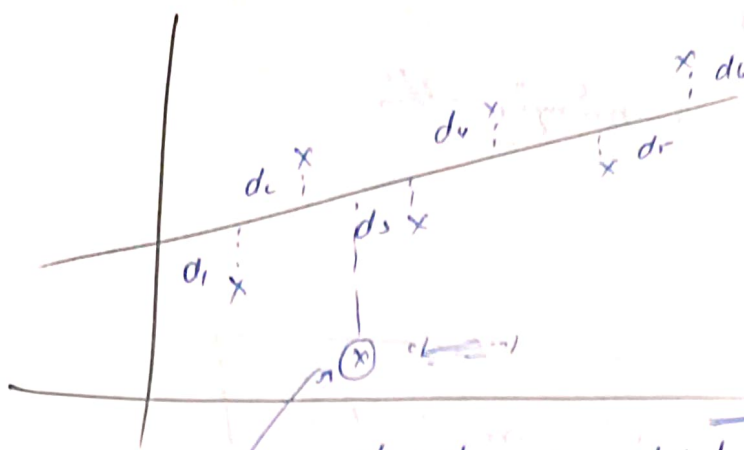
High Dimension main
 jyada chalta
 Hai.

Internally Sklearn

(LR) \rightarrow OLS impl

SGD Regu \rightarrow Gradient
 Descent
 implemented

(m, b) ki value nikalna



$$E = d_1 + d_2 + d_3 + \dots + d_n$$

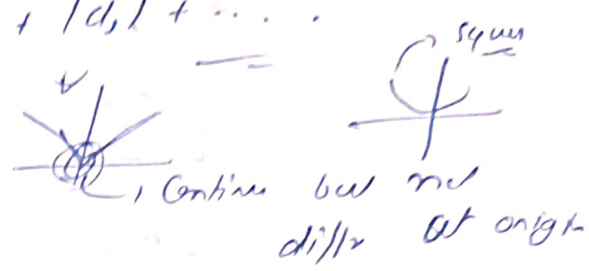
} Squares hunda

$$E = d_1^2 + d_2^2 + \dots + d_n^2$$

Why we use squared error

$$E = |d_1| + |d_2| + |d_3| + \dots$$

Reason - 1
Reason - 2



Outlier ko penalise karna chahota hai

Refer to including the influence / weight of outliers when training a model so they don't spoil the results.
jo data ko error hai usko exaggerate karna.

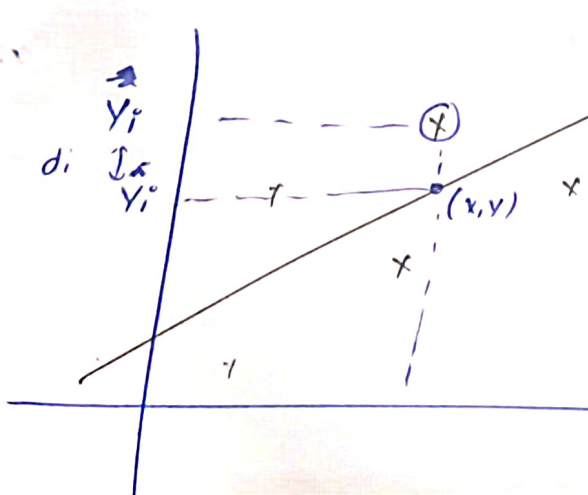
Here Squared error used \rightarrow penalizes outliers more strongly
 \rightarrow is differentiable
 \rightarrow gives a clean Mathematical solution

New

$$E = \sum_{i=1}^n d_i^2$$

\rightarrow even function defined by J also

\rightarrow minimum karaino (m, b) chahiye.



$$d_i^2 = (y_i - \hat{y}_i)^2$$

$$\hat{y} = mx + b$$

$$E = \sum_{i=1}^n (y_i^c - \hat{y}_i^c)^2 \rightarrow \text{minimize this}$$

$$\hat{y}_i^c = m x_i^c + b$$

$$* E_{(m,b)} = \sum_{i=1}^n (y_i^c - m x_i^c - b)^2$$

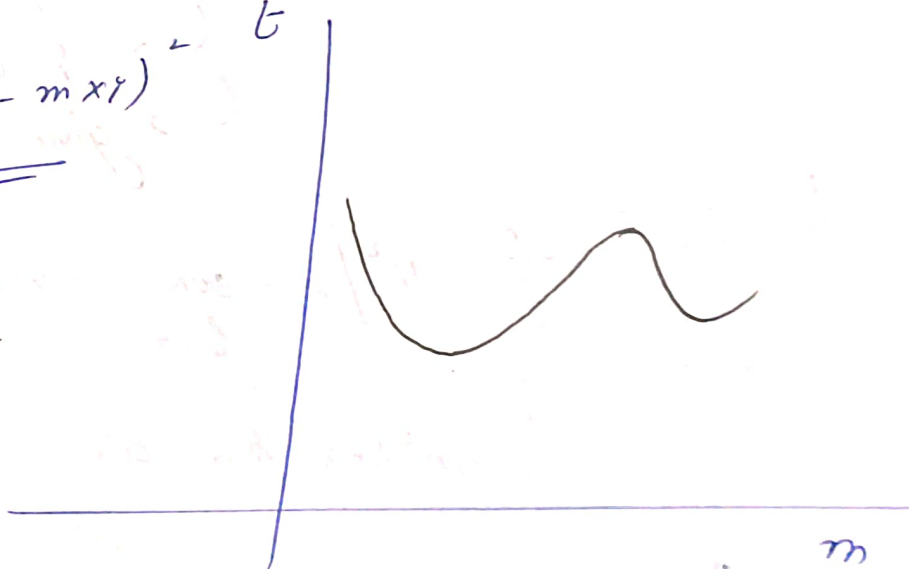
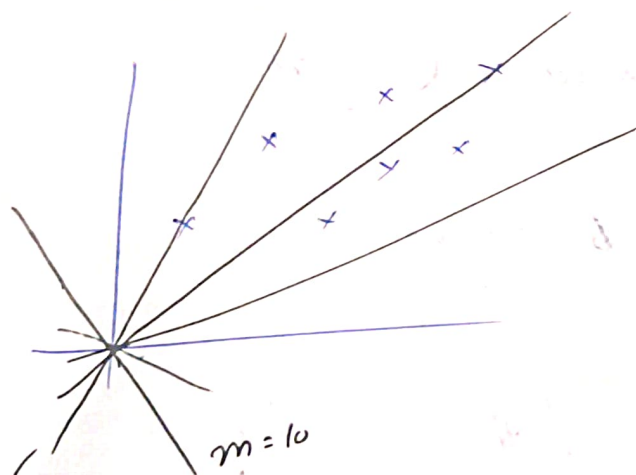
$$E(m,b) = \sum_{i=1}^n (y_i^c - m x_i^c - b)^2 \rightarrow \text{minimize}$$

$y = f(x)$ x in setting known for y .

$(m,b) \rightarrow$ an setting known.

m $b=0$

$$E(m) = \sum_{i=1}^n (y_i^c - m x_i^c)^2 \quad \bar{E}$$



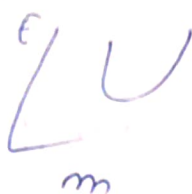
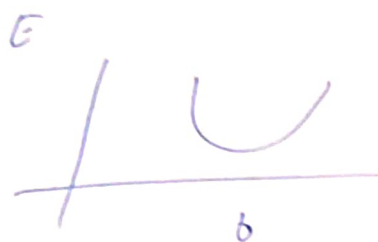
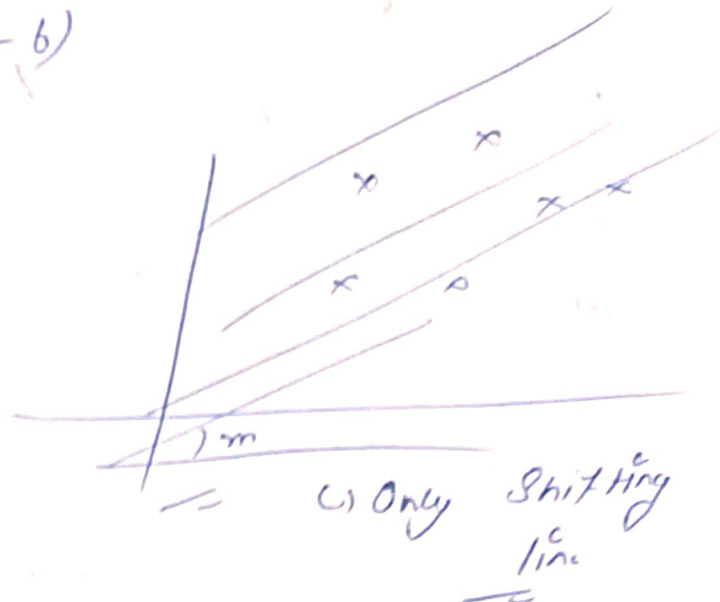
Only m change

\therefore rotate

m ko ghumane se

$m=1$ b

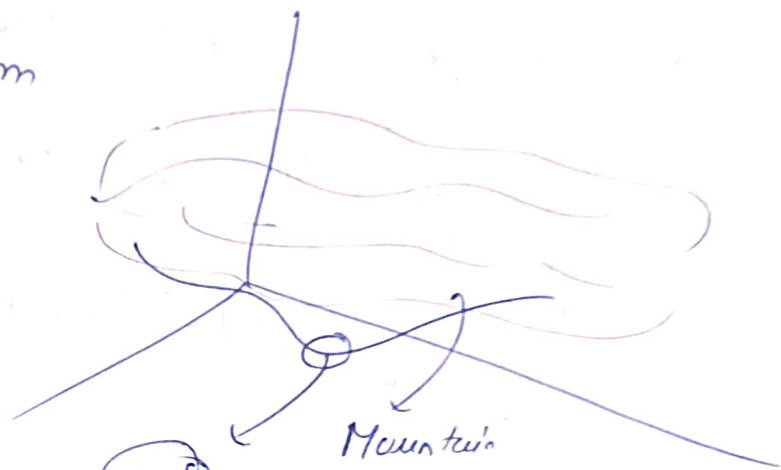
$$E(b) = \sum_{i=1}^n (y_i^c - x_i^c - b)^2$$



$E(x)$

$\hookrightarrow f(x, y)$

\therefore partial Derivative
kano padega.



Slope = 0
Derivative to
Zero
maxima / minima

$$\frac{\partial E}{\partial b} = \frac{\partial}{\partial b} \left(\sum (y_i^c - m x_i^c - b)^2 \right) = 0$$

$$= \sum \frac{\partial}{\partial b} (y_i^c - m x_i^c - b)^2$$

$$= \sum 2 (y_i^c - m x_i^c - b) (-1) = 0$$

$$\text{So } \sum (y_i^c - m x_i^c - b) = 0$$

$$\sum y_i^c - \sum m x_i^c - \sum b = 0$$

$$\frac{b+b+b \dots n \text{ times}}{n}$$

$$\frac{n b}{n} = b$$

$$\boxed{\bar{y} - m \bar{x} = b}$$

b ko fit karoge. Seed wala m ko nibal Denge.

$$E = \sum (y_i - mx_i - \bar{y} + m\bar{x})^2$$

$$\frac{\partial E}{\partial m} = \sum \frac{\partial}{\partial m} (y_i - mx_i - \bar{y} + m\bar{x})^2 = 0$$

$$= \sum 2(y_i - mx_i - \bar{y} + m\bar{x})((-x_i) + \bar{x}) = 0$$

$$\Rightarrow \sum -2(y_i - mx_i - \bar{y} + m\bar{x})(x_i - \bar{x}) = 0$$

$$\Rightarrow \sum ((y_i - \bar{y}) - m(x_i - \bar{x}))(x_i - \bar{x})$$

$$= \sum ((y_i - \bar{y})(x_i - \bar{x}) - m(x_i - \bar{x})^2) = 0$$

$$\Rightarrow \frac{\sum (y_i - \bar{y})(x_i - \bar{x})}{\sum (x_i - \bar{x})^2} = m$$