

UNIT-II

Symmetric Key Ciphers:-

Block cipher principles:-

DES -

AES -

Blowfish -

RC5 -

IDEA -

Block cipher operation -

Stream cipher, P

RC4 -

Asymmetric Key Ciphers:-

principles of public key

Crypto systems -

RSA algorithm -

Eigamal cryptography

Diffie-Hellman key exchange

Knapsack Algorithm.

* Block cipher principles:-

→ A block cipher is a symmetric-key encryption algorithm that processes data in fixed-size blocks using a secret key.

→ It transforms a plaintext

block into a cipher text.

→ Block ciphers are built in the Fiestel cipher structure.

→ Block cipher has a specific number of rounds and keys for generating ciphertext.

Some of these principles are:-

1) Number of Rounds:- The number of rounds is regularly considered in design criteria.

→ In DES we have 16 rounds ensuring it to be more secure while in AES we have 10 rounds which makes it more secure.

2) Design of Function F:-

→ The core part of the Fiestel Block cipher structure is the Round Function.

→ If the function is very much complicated to understand, more time hacker will take to decode the data.

→ you have to take non-linear functions, because linear functions are easy.

3) Confusion and Diffusion: The cipher should provide

3) Key Schedule Algorithm: It should be designed carefully to ensure that the keys used for encryption are independent & unpredictable.

→ The key schedule should also resist attacks that exploit weak or key-dependent properties of the cipher.

DES [Data Standard Data Encryption Standard]:

- It is a block cipher algorithm.
- It converts the plain text into cipher text.

* It has 16 rounds.

* The text size of plaintext & cipher text is 64 bits.

* The key size is 56 bits. The remaining 16 bits are removed.

* 8 bits are removed for parity and 8 bit for rearrangement.

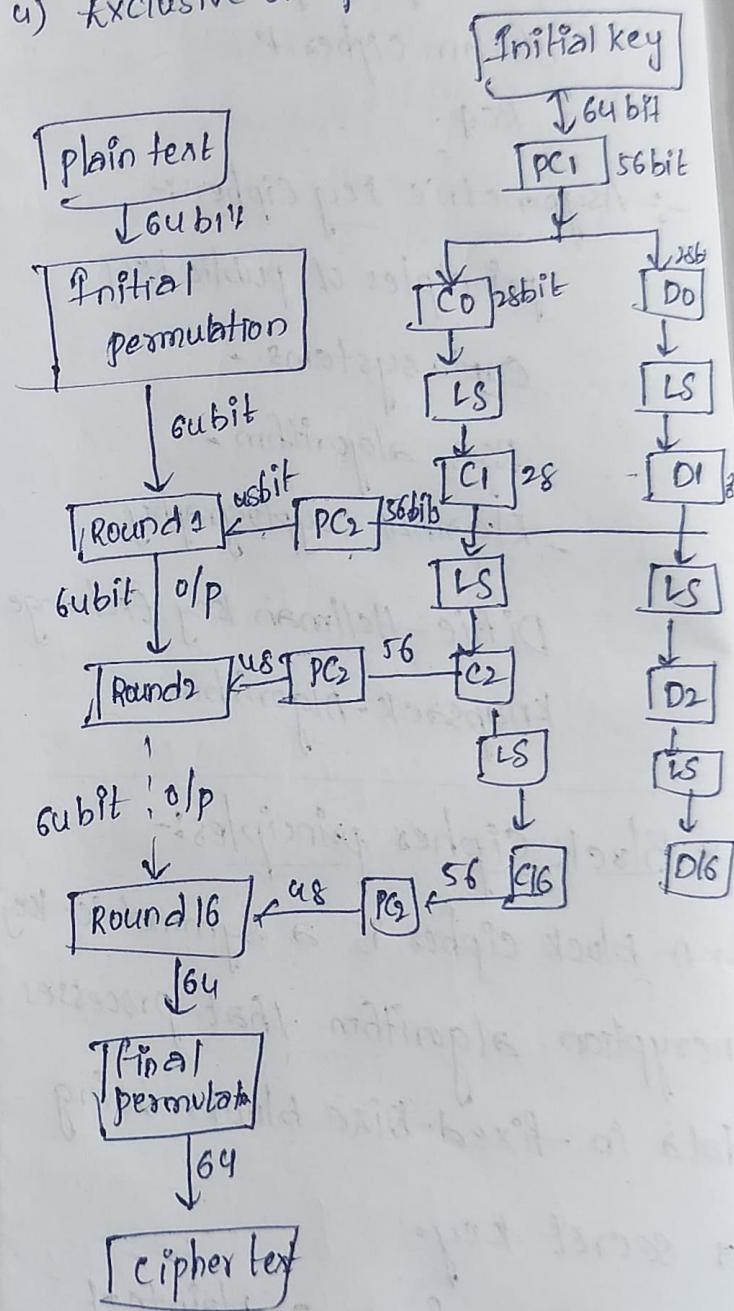
In each round 4 steps are performed

1) Dividing bits into two parts - 32 bits for each

2) Bit shuffling

3) Non linear substitutions

4) Exclusive OR operations



* In PC1, initially there are 64 bits
8 bits are removed from every
parity '8th' position

$$64 = (8 \times 8)$$

$$64 - 8 = 56$$

* Then apply left circular shift
after dividing 56 bits into 2 parts
C0 and D0, each having 28 bits

* D1 and C1 are obtained as result.

Left Circular Shift:-

* Move the bits based on Round
number

* for Rounds 1, 2, 9, 16 - 1 bit shift

other Rounds - 2 bit shift.

* Here in PC2, C1 and D1 are combined
to form 56 bits again, permuted
choice 2 is applied.

* 56 bits are rearranged,
permuted and in that 48 bits are
selected.

Round 1 - 48 bits are the key.

At last cipher text is 64 bit.

AES Algorithm:

- Advanced Encryption Standard
- It is a block cipher algorithm
- It has i/p array, state array
and a key array.

1) I/p Array

each cell = 1 byte / 8 bit

Total = 16 cells

$$16 \times 8 = 128 \text{ bits}$$

= 4 words (32 each)

In i/p array PT is represented.

2) State Array

- It is used to store intermediate
states within the rounds

S0,0	S0,1	S0,2	S0,3
S1,0	S1,1	S1,2	S1,3
S2,0	S2,1	S2,2	S2,3
S3,0	S3,1	S3,2	S3,3

Total 4 words.

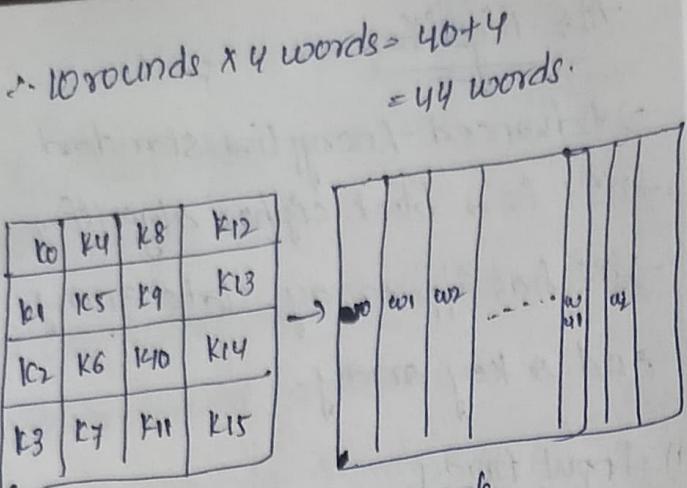
3) Key Array

Actually 4 words expanded into
16 words

Each round =

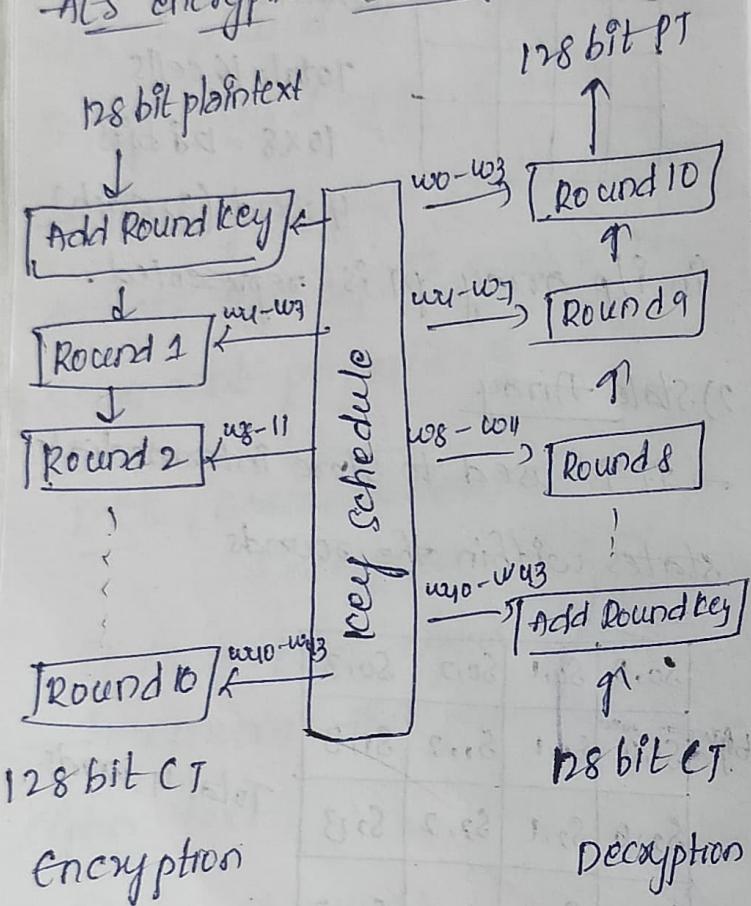
→ In AES there are 10 rounds

Each round = 4 words



4 words \rightarrow 44 words.

AES encryption & decryption



- * The Encryption & Decryption starts from Add Round Key.
- * Each process starts from Round 1 and ends with Round 10.

In each round we have 4 steps

- 1) Substitute Bytes
- 2) Shift Rows (LCS)
- 3) Mix Columns - Not in Round 10
- 4) Add Round Key.
 XOR operation between PT & key.

* 128 bit plain text is sending into the Add Round key along with the words $w_0, w_1, w_2, \& w_3$

* for each and every round we have four words.

* Total 44 words along with add round key.

* Then we will get 128 bit cipher text.

* This is the process of Encryption

* This process will continue until the 128 bit plain text is obtained.

* Blow fish:

- * It is a block cipher algorithm
 - * It is a symmetric key cryptography
 - * The input size is 64 bits
 - * The key size is variable length key i.e from 32 to 448 bits
 - * It is more secure
- Properties
- * It is very fast.
 - * It takes less memory
 - * It is simple to understand.

Blow fish Algorithm has 2 parts

- 1) Key generation
- 2) Data encryption

* Key generation:

- 1) Keys are stored in an array

$$k_1, k_2, k_3, \dots, k_n \quad [1 \leq n \leq 14]$$

- * Length of each block is 32 bits
 $(32 \times 14 = 448 \text{ bits})$

- 2) Initialize an array (P)

$$p_1, p_2, p_3, \dots, p_{18}$$

length of each word is 32 bits

- 3) Initialize s-boxes (4)
↳ substitution

$$S_1 \Rightarrow S_0, S_1, \dots, S_{255}$$

$$S_2 \Rightarrow S_0, S_1, \dots, S_{255}$$

$$S_3 \Rightarrow \dots$$

$$S_4 \Rightarrow \dots$$

- 4) Initialize each element of P-array and S-boxes with hexadecimal values

- 5) XOR operations are performed

$$p_1 = p_1 \text{ XOR } k_1$$

$$p_2 = p_2 \text{ XOR } k_2$$

:

$$p_{14} = p_{14} \text{ XOR } k_{14} \quad (\text{because only 14 keys})$$

$$p_{15} = p_{15} \text{ XOR } k_1$$

:

$$p_{18} = p_{18} \text{ XOR } k_4$$

- 6) Take 64 bit PT (Initially all bits are '0')
subkey is generated

② Data Encryption:

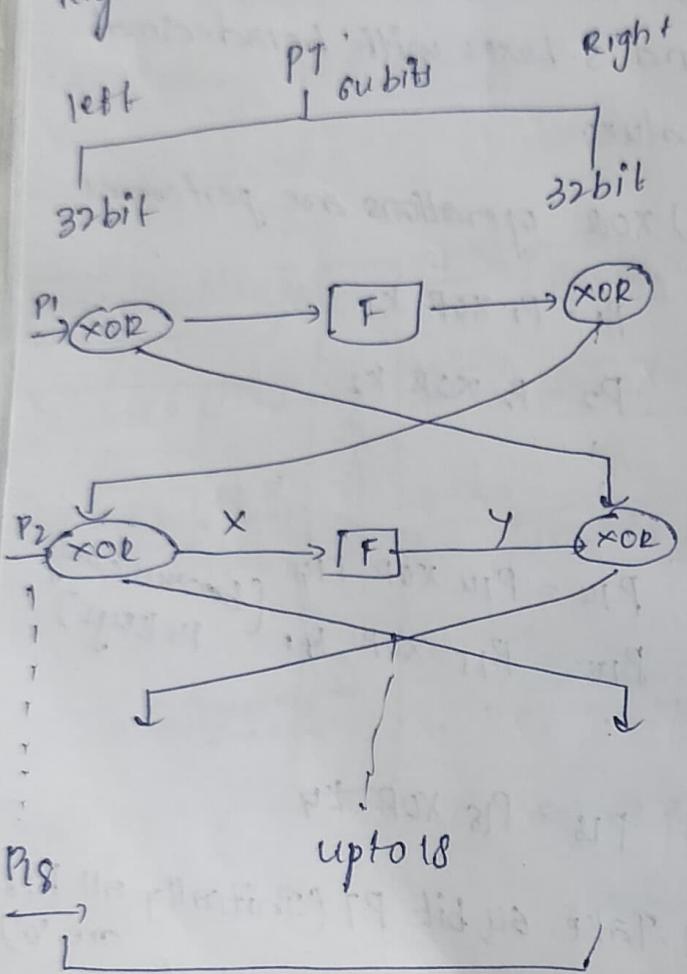
- * Divide the plain text into two parts

- * Then perform XOR operation with p_1 with left 32 bit

we will get output 'x'

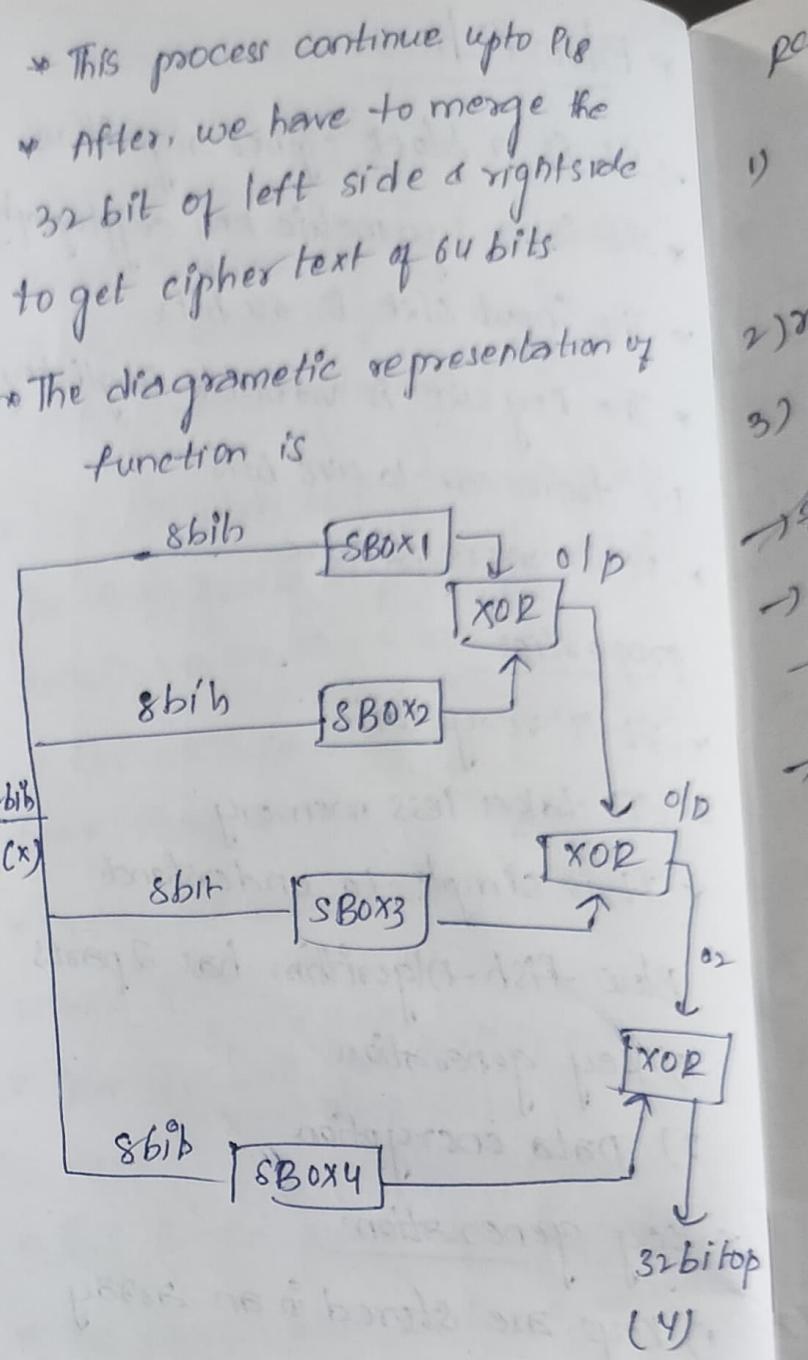
- This output will sent into a function and do the function we will get output 'y'.

- The output 'y' and 32 bit of Right side will do the XOR operation



CT is generated

- The output of XOR operation of left side will send to right side vice-versa



RC5 Algorithm:

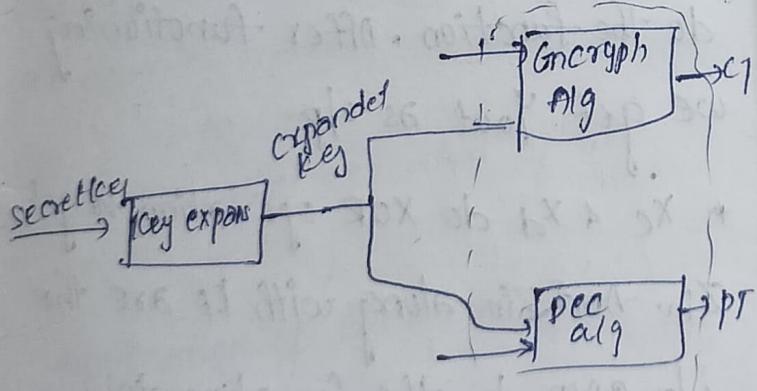
- RC stands for Rivest cipher
- It is designed by Ronald Rivest
- RC5 is a block cipher technique
- It is a symmetric block cipher that means same secret key is used for both enc & dec

RCA having three parameters

- 1) w - word size [16, 32, 64]
encrypts two word blocks [$2w$]
 - 2) r - No. of rounds [0, 1, ..., 255]
 - 3) b - No. of bytes [0, 1, ..., 255]
- It's similar to DES
→ Based on choosing ' w ' remaining things will be based
→ More rounds provides an increased level of security.

RCA algorithm having three algorithms components

- 1) Key expansion algorithm
- 2) Encryption algorithm
- 3) Decryption "



Advantages:

- 1) High level of security
- 2) fast encryption & decryption
- 3) flexible key length.

Dis:

- 1) vulnerable to side-channel attacks
- 2) Limited adoption
- 3) patent issues.

IDEA [International data Encryption Algorithm].

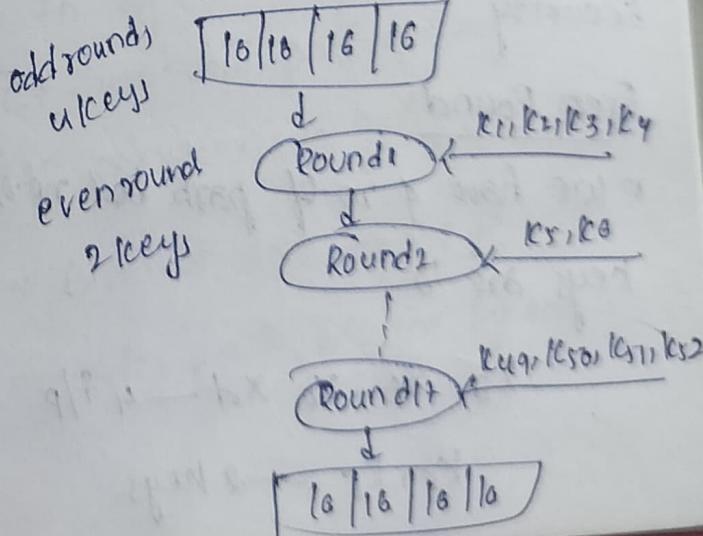
- It is a Block cipher algorithm
- Symmetric key cryptography
- Feistel cipher.

I/p size = 64 bits - 16, 16, 16, 16

key size = 128 bits - into 52 subkeys

No. of rounds = 17

Plaintext = 64



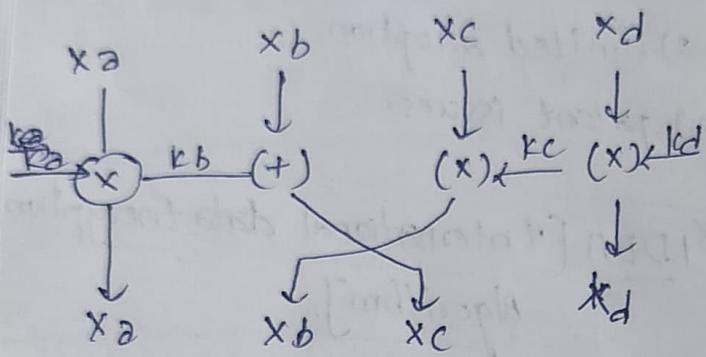
Odd Rounds:

Input is divided in four parts

keys are '4'

$$x_a \quad x_b \quad x_c \quad x_d \rightarrow i/p$$

$$k_a \quad k_b \quad k_c \quad k_d \rightarrow \text{keys}$$



* x_a & k_a are the o/p and new x_a is generated as o/p.

* x_d and k_d are the i/p & new x_d is generated as o/p

* But in case of x_b & x_c the o/p's of x_b, k_b and x_c, k_c are swapped each other in order to ensure security.

Even Round:

* we have 4 no. of parts but no. of keys are '2'

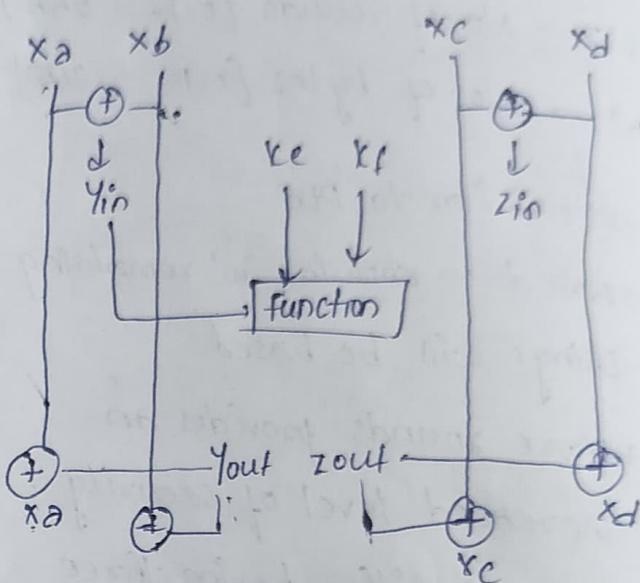
$$x_a, x_b, x_c, x_d \rightarrow 4 \text{ i/p}$$

$$k_e, k_f \rightarrow 2 \text{ keys}$$

$$y_{in} = x_a \oplus x_b$$

$$z_{in} = x_c \oplus x_d$$

$$\text{Now } i/p = 2 \text{ & key} = 2$$



$$x_a = x_a \oplus y_{out}$$

$$x_b = x_b \oplus y_{out}$$

$$x_c = x_c \oplus z_{out}$$

$$x_d = x_d \oplus z_{out}$$

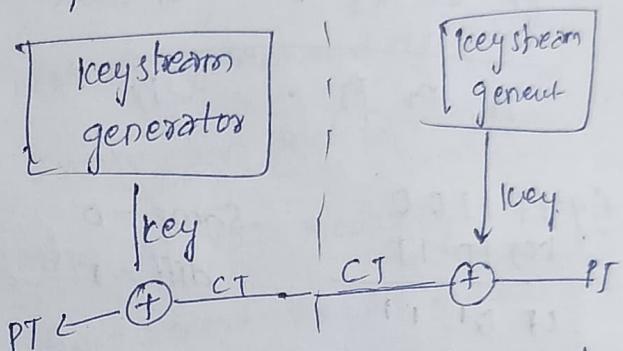
* x_a & x_b do XOR operation to get y_{in} and along k_e are the i/p's to do the function. After functioning we get y_{out} as o/p.

* x_c & x_d do XOR operation to get z_{in} . And z_{in} along with k_f are the i/p given to the function to generate the z_{out} as o/p

- * x_B and y_{out} will do XOR operation to get x_B as O/P
- * x_C & z_{out} will do XOR operation to get x_C as O/P
- * x_D and z_{out} will do XOR operation to get x_D as O/P

* Stream Cipher

- A stream cipher is a type of symmetric encryption that encrypts data one bit or byte at a time by combining it with keystream generated from a shared secret key
- * plain text is divided into number of streams



- * keys are generated from keystream generator

- * Bitwise XOR operation is performed b/w the key & PT. As a result we get CT.

- * In dec, with the help of key & CT, we will perform a bitwise XOR operation to get PT

- * Bitwise XOR means it will consider each bit one by one.

Application of Block cipher

- 1) Data Enc
- 2) File & Disk Encryption
- 3) Virtual private Networks

Explanation

$$\begin{array}{ccccccc} m_1 & m_2 & m_3 & \dots & m_i & \rightarrow PT \\ k_1 & k_2 & k_3 & \dots & k_i & \rightarrow keys \\ \hline c_1 & c_2 & c_3 & \dots & c_i & \rightarrow CT \end{array}$$

(ciphertext \oplus key \Rightarrow PT) decryption

$$\begin{array}{ccccccc} c_1 & c_2 & c_3 & \dots & c_i \\ k_1 & k_2 & k_3 & \dots & k_i \\ \hline p_1 & p_2 & p_3 & \dots & p_i \end{array}$$

$$\begin{array}{l} \text{eg. PT } 1100 \\ \text{key } 1011 \\ \hline \text{CT } 0111 \end{array}$$

Same = 0
diff = 1

RC4

→ stream cipher algorithm.

Procedure

- 1) uses an array (s) - state vector of length 256 bits (0-255)
- 2) It has a key encoded with ASCII
- 3) It has a key array of length 256 (0-255)

RC4 algorithm has three steps

- 1) key scheduling
- 2) key stream generation
- 3) encryption & decryption

① Key scheduling

* No. of iterations is equal to size of s-array.

Initialize $j=0$

for $i=0$ to 255 do

state vector
key array

$$j = [j + s(i) + T(i)] \bmod 256$$

swap $(s[i], s[j])$

eg. s-array [0 1 2 3 4 5 6 7]

key-array [1 2 3 6]

PT = [1 2 2 2]

Initialize T-array with key
S & T should be same.

T = [1 2 3 6 1 2 3 6]
(0) (1) (2) (3)

i) $j=0$

for $i=0$ to 7

$j = [0+0+1] \bmod 8$

$1 \bmod 8 = 1$

swap $s[0] \& s[1]$

s = [1 0 2 3 4 5 6 7]

$$\text{ii) } \begin{aligned} j &= 1 \text{ for } i = 0 \text{ to } 7 \\ j &= [1+0+2] \bmod 8 \\ &= 3 \bmod 8 = j \\ &= 3 \end{aligned}$$

swap $s(1)$ & $s(3)$ $\rightarrow s(1)$

$$s = [1 \ 3 \ 2 \ 0 \ 4 \ 5 \ 6 \ 7]$$

iii) for $i=2$,

for $i=2$,

$$j = [3+2+3]$$

$$j = 8$$

$$= 8 \bmod 8 = 1$$

$j=0$: swap $s(2)$ & $s(0)$

$$s = [2 \ 3 \ 1 \ 0 \ 4 \ 5 \ 6 \ 7]$$

iv) for $i=3$

$$\begin{aligned} j &= [4+3+6] \\ &= 13 \bmod 8 = 5 \end{aligned}$$

swap $s(3)$ & $s(5)$

stream generation:-

No. of iterations is equal to
size of key (4)

$$i, j = 0$$

while (true)

$$i = (i+1) \bmod 256$$

$$j = (j+s(i)) \bmod 256$$

swap $(s[i], s[j])$;

$$t = (s[i]+s[j]) \bmod 256$$

$$k = s[t];$$

for 1st iteration we get $k(0)$

for 2nd

1
}
2

$k(1)$

\Rightarrow New key is obtained & used
for encryption and decryption.

* Encryption and Decryption:-

Enc PT XOR New key.

first convert the PT + new key
into binary

$$\text{PT} = 1222$$

$$\text{PT} = 0001 \ 0010 \ 0010 \ 0010$$

$$\text{key} = () \quad () \quad () \quad ()$$

$$C1 =$$

Decryption - CT XOR New key.

* Principles of public key:

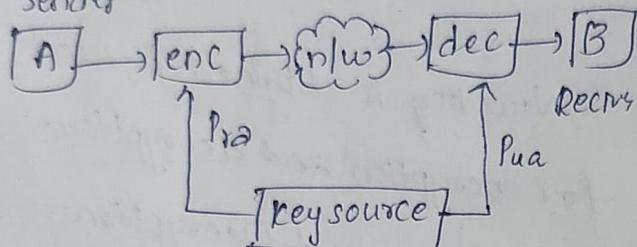
for asymmetric key cryptography
we have different key for enc & dec

These are two principals:

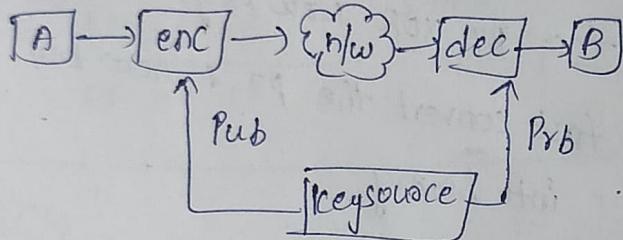
1) Authentication

2) Confidentiality.

① Sender



②



* Here the sender sends the PT & it will encrypted with the help of key which is named as private, taken from key source.

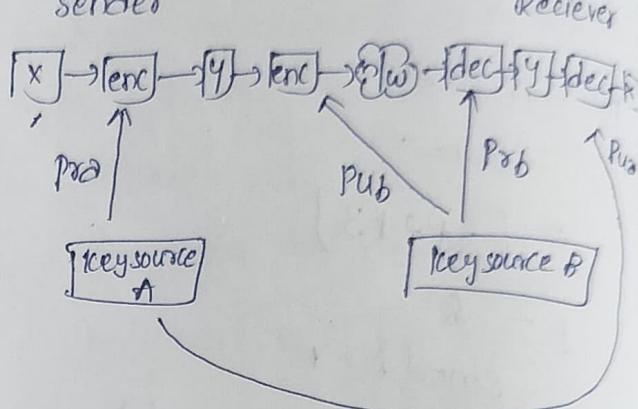
* Then the encrypted message will enter into a n/w and come out of this n/w then to decrypt the msg we are using public n key from the key source

At last the cipher text is converted into plain text which is received by receiver

* This is Authentication.

2) Confidentiality.

sender



For confidentiality we have diff key sources (A & B)

* The keysource A will generate the public A & private A keys which is provided to x (sender)

* The keysource B will generate the private B & public B which is provided to receiver

* The private B key of keysource B provided to receiver & public B key of keysource B is provided to sender.

* Crypto Systems:

An asymmetric key cryptosystem uses two different keys for security operations

- public key → shared openly for enc
- private key → kept secret for dec

Asymmetric crypto systems are used for

- confidentiality
- authentication
- digital signature
- key exchange

Components:

1) Key generation algorithm

- Generate pair of keys
- keys are mathematically related

2) Encryption algorithm

- Uses the receiver's public key to convert PT → CT

3) Decryption alg

- Uses the private key to recover PT from CT

Ensures confidentiality

4) Digital Signature Algorithm:

- sender signs a message using their private key.
- anyone can verify using public key

Examples of Asymmetric Cryptosystems:

1) RSA:

- used for encryption & digital signatures

2) Diffie-Hellman

- key exchange protocol
- allows two parties to generate a shared secret

3) ElGamal:

- used for enc & digital signatures

Characteristics:

- Two key mechanism
- High security
- Slower than symmetric

Useful for:

- Secure key exchange
- secure email

* RSA algorithm:

→ It is one of the public key ENC algorithm used for both enc & dec of data.

→ In this the P.T.CT, key values are represented in numbers, integers for some 'n' value and ranges from 0, n-1

→ By Ron Rivest Shamir Adleman

→ It is a block cipher method

$$\text{ENC: } C = M^e \pmod{n}$$

$$\text{Dec: } M = C^d \pmod{n}$$

$M \rightarrow PT$

$C \rightarrow CT$

$n \rightarrow \text{integer}$

public key { e, n }

public key { d, n }

Steps:

1) Select p, q values where p, q are prime numbers

2) calculate 'n' $n = p \times q$

3) calculate $\phi(n)$ Euler's totient function

$$\phi(n) = (p-1)(q-1)$$

4) select 'e' value where 'e' is relatively prime to $\phi(n)$

$$\gcd(\phi(n), e) = 1$$

5) calculate $d = d \times \text{mod } \phi(n) = 1$

$$6) \text{ ENC } [C = m^e \pmod{n}]$$

$$7) \text{ DEC } [m = C^d \pmod{n}]$$

$$\text{eg: } 1) p=3 \quad q=5$$

$$2) n = p \times q$$

$$n = 3 \times 5$$

$$n = 15$$

$$3) \phi(n) = (p-1)(q-1)$$

$$= (3-1)(5-1)$$

$$= 2 \times 4 = 8$$

$$4) \gcd(\phi(n), e) = 1$$

$$5) \phi(n) = 8 \in \{1, 2, 4, 7\}$$

$$6) d \times e \pmod{\phi(n)} = 1$$

$$d \times 3 \pmod{8} = 1$$

$$\therefore 1 \times 3 \pmod{8} = 3 \pmod{8} = 3$$

$$2 \times 3 \pmod{8} = 6 \pmod{8} = 6$$

$$3 \times 3 \pmod{8} = 9 \pmod{8} = 1$$

$$\text{ENC: } C = 5^3 \pmod{15}$$

$$C = 125 \pmod{15}$$

$$[C = 5]$$

$$\text{DEC: } m = C^d \pmod{n}$$

$$= 5^3 \pmod{15}$$

$$= 125 \pmod{15} \quad [m=5]$$

* Elgamal Cryptography

→ Asymmetric key cryptography.

① select large prime number (p) = 11

② select a dec. key also called as private key

$$\boxed{d=3}$$

③ select second part of encryption key (e_1) = 2

$$\boxed{e_1=2}$$

④ select third part of enc key calculate

$$e_2 = e_1^d \bmod p$$

$$= (2)^3 \bmod 11$$

$$= 8 \bmod 11$$

$$\boxed{e_2=8}$$

⑤ public key = (e_1, e_2, p) & private key = d

$$\text{pub} = (2, 8, 11)$$

ENC

1) select random integer (r)

$$r=4$$

2) calculate $C_1 = g^r \bmod p$

$$= 2^4 \bmod 11 = 16 \bmod 11 \\ = 5$$

$$\boxed{C_1=5}$$

$$\text{calculate } C_2 = (P \times e_2^r) \bmod p$$

$$= (7 \times 8^4) \bmod 11$$

$$= 28672 \bmod 11 = 6$$

$$\boxed{C_2=6}$$

$$CT = (C_1, C_2) = (5, 6)$$

DEC

$$1) PT = [C_2 \times (C_1)^d]^{-1} \bmod p$$

$$= (6 \times (5)^3)^{-1} \bmod 11$$

$$= 6(125)^{-1} \bmod 11$$

$$= 6(125)^1 \bmod 11$$

$$= 125 \times 2 \bmod 11 = 1$$

$$\text{If } x=3 \quad 125 \times 3 \bmod 11 = 375 \bmod 11 \\ = 1$$

$$\boxed{x=3}$$

$$6 \times 3 \bmod 11 = 18 \bmod 11 = 7$$

$$PT = 7$$

∴ Correct =

Diffie-Hellman key exchange

- It is a asymmetric key
- It is used to exchange keys b/w sender and Receiver

* It just exchange the key, doesn't perform any enc/dec algorithm.

1) consider prime number 'q'
calculate 'x'. 'x' is relatively prime to 'q'

2) user 'A' generate key
select a private key ' x_A '

→ calculate public key

$$[Y_A = \alpha^{x_A} \bmod q]$$

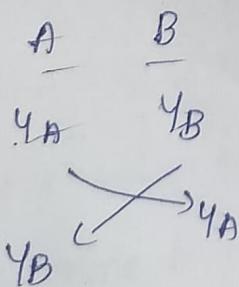
3) user 'B' generate key

Select a private key ' x_B '

calculate public key

$$[Y_B = \alpha^{x_B} \bmod q]$$

4) Exchange key values

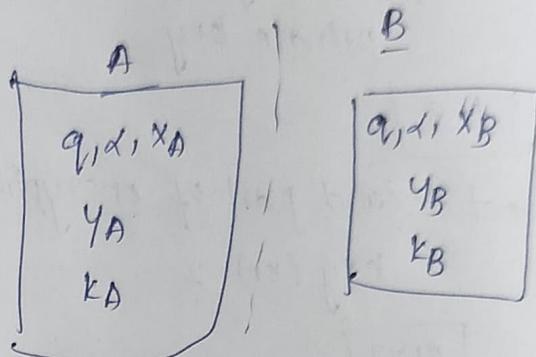


5) User A generate Secret Key

$$[K_A = Y_B^{x_A} \bmod q]$$

6) User B generate Secret Key

$$[K_B = Y_A^{x_B} \bmod q]$$



Ex: $q=11, d=7, x_A=5, x_B=7$ find Y_A, Y_B, K_A, K_B

$$\cdot d=1 \Rightarrow (a^i \bmod q) = i = 1 \text{ to } 10, a=2$$

$$1 \bmod 11 = 1$$

$$2 \bmod 11 = 2$$

$$3 \bmod 11 = 3$$

$d \neq$ as it generate same values

$$i.e. 1$$

$$d=2$$

$$2^1 \bmod 11 = 2$$

$$2^2 \bmod 11 = 4$$

$$2^3 \bmod 11 = 8$$

$$2^4 \bmod 11 = 5$$

$$2^5 \bmod 11 = 10$$

$$\therefore d=2$$

Step 2 User A

private key $x_A = 5$

$$y_A = \alpha^{x_A} \mod q$$

$$y_A = 2^5 \mod 11$$

$$\boxed{y_A = 10}$$

Step 3 User B

private key $x_B = 7$

$$y_B = \alpha^{x_B} \mod q$$

$$y_B = 2^7 \mod 11$$

$$\boxed{y_B = 7}$$

Step 4 A B

$$x_A = 5 \quad x_B = 7$$

$$y_A = 10 \quad y_B = 7$$

$$\alpha = 2 \quad \alpha = 2$$

$$q = 11 \quad q = 11$$

$$y_B = 7 \quad y_A = 10$$

Step 5 User A generate secret key

$$k_A = y_B^{x_A} \mod q$$

$$k_A = 7^5 \mod 11$$

Step 6

$$k_B = y_A^{x_B} \mod q$$

$$= 10^7 \mod 11$$

$$k_B =$$

* knapsack Algorithm:-

* It was proposed by Hellman

* It is a Asymmetric key cryptography

Ex (weights) = (1, 6, 8, 15 & 24)

⇒ In general knapsack, we select weights to achieve a sum

$$\text{sum} = \frac{30}{\text{II}}$$

1, 6, 8, and 15

$$\begin{array}{r}
 PT = \begin{array}{rrr} 1 & 0 & 0 \\ 1 & 6 & 8 \\ \hline 1 & 0 & 0 \end{array} \begin{array}{rrr} 1 & 1 & 0 \\ 1 & 6 & 8 \\ \hline 1 & 6 & 8 \end{array} \\
 \begin{array}{r} 11 \\ 18 \\ 24 \\ \hline 40 \end{array} \quad \begin{array}{r} 10 \\ 15 \\ 24 \\ \hline 40 \end{array} \quad \begin{array}{r} 10 \\ 15 \\ 24 \\ \hline 40 \end{array} \\
 \end{array}$$

$\rightarrow 1+6+15=22$

CT = plain text × corresponding weight

$$CT = 40 \quad 22.$$

key Generation

1) public key (Hard knapsack)

2) private key (Easy knapsack)