

**Syllabus**

MICROWAVE TUBES: Limitations and Losses of conventional Tubes at Microwave Frequencies, Microwave Tubes - O Type and M Type Classifications, O-type Tubes: 2 Cavity Klystrons - Structure, Reentrant Cavities, Velocity Modulation Process and Applegate Diagram, Bunching Process and Small Signal Theory - Expressions for O/P Power and Efficiency. Reflex Klystrons - Structure, Velocity Modulation and Applegate Diagram, Mathematical Theory of Bunching, Power Output, Efficiency, Oscillating Modes and O/P Characteristics.

HELIX TWT: Types and Characteristics of Slow Wave Structures; Structure of TWT and Amplification Process (qualitative treatment), Suppression of Oscillations, Gain Considerations.

LEARNING OBJECTIVES

- ☛ Limitations and losses of conventional tubes at microwave frequencies.
- ☛ Microwave tubes and their classification as O-type and M-type.
- ☛ Structure, working of two cavity klystron O-type tube and derivation of its O/P power and efficiency expressions.
- ☛ Structure, working of reflex klystron O-type tube and derivation of its O/P power and efficiency expressions. Along with this oscillating modes and O/P characteristics of reflex klystron.
- ☛ Types and characteristics of slow wave structures used in travelling wave tubes.
- ☛ Structure, amplification process (qualitative treatment), suppression of oscillations and gain considerations of helix TWT

INTRODUCTION

Conventional vacuum tubes, such as triodes, tetrodes and pentodes are still used as signal sources of low output power at low microwave frequencies. However, these tubes are less preferred at microwave frequencies due to their limitations and losses.

In this unit, we study about limitations and losses of conventional vacuum tubes at microwave frequencies. In order to overcome these limitations and losses, O-type and M-type tubes were introduced. We then discuss about klystron amplifier, in fact we discuss the specialized tubes which were developed for microwave frequency application, and klystron is one such tube. Then, we will see reflex klystron as an oscillator, for oscillation we require feedback to be provided and we will see how reflex klystron provides the required feedback, we will see that these devices like klystron or reflex klystron they operate on the principle of velocity modulation. And finally, we will discuss traveling wave tubes or TWTs specially helix type.

Q13. What are the advantages of slowwave structures?**Ans:**

In TWT, the electron beam cannot accelerate faster than the waves travelling on wire. This is because of the waves travelling at the speed of light and increased in its amplitude along the length of TWT. Due to this drawback, bunching process does not occur.

Parameter	Value
1. Operating frequency	250 MHz- 100 GHz (60 GHz nominal)
2. Power	10 kW - 500 kW (CW) 30 MW (pulsed)
3. Power gain	15 dB - 70 dB (60 dB nominal)
4. Bandwidth	10 - 60 MHz
5. Noise figure	15 dB - 20 dB (sometimes > 25 dB)
6. Theoretical efficiency	58% (30 - 40% nominal)

Table

Q9. What is a reflex klystron?**Ans:**

The reflex klystron is a single cavity, variable frequency microwave generator oscillator. It has low power and low efficiency. It has electron gun similar to that of two-cavity klystron but of smaller size. As the size is small the beam does not require focusing.

Q10. Differentiate two cavity klystron and reflex klystron.**Ans:**

The differences between 2-cavity and reflex klystrons are mentioned in table,

Two-cavity Klystron	Reflex Klystron
1. It is a two-cavity (input and output cavities) device.	1. It is a single-cavity (only input cavity) device.
2. Catcher cavity is used as output cavity.	2. Repeller is used as output cavity.
3. Input and output cavities are used for modulation and demodulation respectively.	3. Single cavity is used for both modulation and demodulation.
4. Bunching of electrons is limited.	4. Maximum bunching of electrons can be obtained by adjusting repeller voltage.

Table

Q11. What are the applications of reflex klystrons?**Ans:**

Reflex klystron tube posses number of applications in communications where the variable frequency is required it finds applications in,

1. Microwave receivers as a local oscillator.
2. Compact microwave links.
3. Radar receivers.
4. Parametric amplifiers as a pump oscillator
5. Variable frequency microwave generators as a signal source.

Q12. What is a slow wave structure?**Ans:**

Slow-wave structures are the circuits, which provides interaction between electron beam and signal wave by reducing the velocity of wave in particular direction.

Nov/Dec.-18, (R13), Q10

Q14. What is the need of Helix in TWT?**Ans:**

The reasons for using helix in TWT,

1. Helix decreases the velocity of the wave in particular direction to establish the communication between signal and electron beam.
2. It provides the large gain over a wide bandwidth.
3. It offers low impedance.

Q15. Write the advantages of travelling wave tubes.**Ans:**

The advantages of TWT are,

1. TWTs have very high gain of about more than 40 dB.
2. Noise figure in TWTs is as low as 6 dB.
3. TWTs have highest BW among amplifiers i.e., 30 to 120%.
4. They have high power rating ranging from few watts to 20,000 W.

Q16. Mention the characteristics and applications of TWT.**Ans:****Characteristics of TWT**

Frequency of operation : 300 MHz to 50 GHz

Efficiency : 20 to 40%

Power gain : 40 dB to 60 dB

Bandwidth : about 800 MHz

Power output : upto 10 kWatts.

Applications of TWT

1. Travelling wave tubes are used as low noise RF amplifiers in,
2. These are used as repeater amplifier in wide band communication links and long distance telephony.
3. Travelling wave tubes are used as output power tubes in communication satellites because of its long tube life i.e., 50,000 hrs.
4. Due to larger power and bandwidth, continuous wave high power TWTs are used in troposcatter links.
5. Travelling wave tubes are also used in airborne and shipborne pulsed high power radars and ECM ground based radars.

The input admittance of the triode circuit is given by,

$$Y_a = \frac{i}{V}$$

From equations (3) and (5),

$$Y_a = \frac{V_{gt} [1 + j\omega L_g s_m - \omega^2 L_g C_g s]}{V_{gt} [1 + j\omega L_g s_m + R]}$$

$$= \frac{j\omega C_g s}{(1 - \omega^2 L_g C_g s) [1 + j\omega L_g s_m + R]}$$

$$= \frac{j\omega C_g s}{(1 - \omega^2 L_g C_g s) [1 + j\omega L_g s_m + R]}^{-1}$$

$$= \frac{j\omega C_g s}{(1 - \omega^2 L_g C_g s) \left[1 + \frac{j\omega L_g s_m}{1 - \omega^2 L_g C_g s} \right]}^{-1}$$

$$= \frac{j\omega C_g s}{(1 - \omega^2 L_g C_g s) \left[1 - \frac{j\omega L_g s_m}{1 - \omega^2 L_g C_g s} \right]}.$$

$$[\because (1+x)^{-1} = 1 - x + x^2 - x^3 + \dots \approx (1-x)]$$

Assuming $\omega^2 L_g C_g s \ll 1$,

$$\Rightarrow (1 - \omega^2 L_g C_g s) \approx 1$$

Then,

$$Y_a = j\omega C_g s [1 - j\omega L_g s_m]$$

$$= j\omega C_g s + \omega^2 s_m L_g C_g s$$

$$\therefore Y_a = \omega^2 s_m L_g C_g s + j\omega C_g s$$

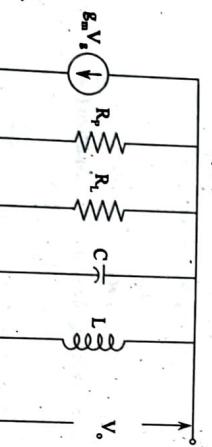
Hence proved.

Q19. Explain the gain bandwidth product limitation in conventional vacuum tubes.

Ans:

Figure shows the equivalent circuit of a vacuum tube amplifier. The transfer function for the circuit in figure is given by,

$$\text{Gain, } G = \frac{V_o(s)}{V_i(s)} = Z_o(s)$$



Figure

$$\text{Consider, } \frac{1}{Z_o(s)} = Y_o(s)$$

$$= CS + \frac{1}{LS} + \frac{1}{R_L} + \frac{1}{R_P}$$

$$(A \text{ after applying laplace transform})$$

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UNIT-1 (Microwave Tubes and Helix TWTs)

1.1.2 Microwave Tubes – O-type and M-type Classifications

Ans:

Microwave tubes are electron guns for generating electron beams. Microwave tubes not only generate but also amplify higher frequencies in the microwave range of frequency spectrum. Microwave sources (or) tubes are broadly classified into two types. They are,

1. Linear beam tubes (O-type)
2. Crossed field tubes (M-type).

The classification of microwave sources is shown in figure below:

R.H.S. Dividing the numerator and denominator by LCR on

$$Z_o(s) = \frac{S/C}{S^2 + S/CR + 1/LC}$$

The denominator gives the characteristic equation, the roots of which gives the extreme frequencies ω_1 and ω_2 ,

$$\omega_1 = -\frac{G}{2C} + \sqrt{\frac{G^2}{2C} - \frac{1}{LC}}$$

$$\omega_2 = -\frac{G}{2C} + \sqrt{\frac{G^2}{2C} - \frac{1}{LC}}$$

Where, $G = \frac{1}{R}$

Bandwidth, $BW = \omega_2 - \omega_1$

$$\Rightarrow BW = \left[-\frac{G}{2C} + \sqrt{\frac{G^2}{2C} - \frac{1}{LC}} \right] - \left[-\frac{G}{2C} - \sqrt{\frac{G^2}{2C} - \frac{1}{LC}} \right]$$

$$= 2 \sqrt{\left(\frac{G}{2C}\right)^2 - \left(\frac{1}{LC}\right)}$$

$$\text{Assuming } \left(\frac{G}{2C}\right)^2 \gg \frac{1}{LC}$$

$$\text{Then, } BW = 2 \sqrt{\left(\frac{G}{2C}\right)^2}$$

$$\Rightarrow BW = \frac{G}{C}$$

But, the maximum gain is achieved, when the circuit is at resonance.

Then, Gain at resonance is given by,

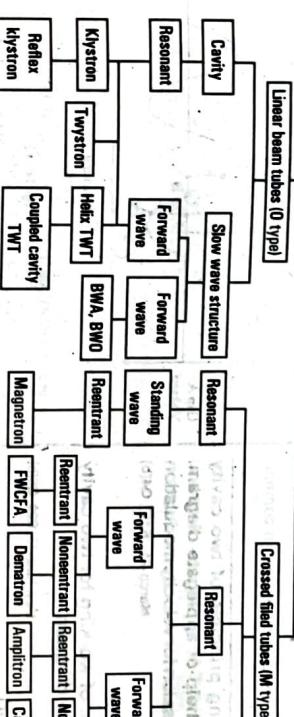
$$A_{\max} = \frac{g_m}{G}$$

$$\therefore \text{Gain bandwidth product} = A_{\max} \cdot BW$$

$$= \frac{g_m \cdot G}{G \cdot C} = \frac{g_m}{C}$$

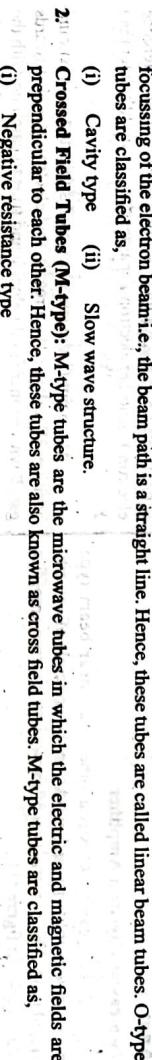
The gain bandwidth product is independent of frequency.

Figure



Figure

Original tubes (O-tubes) or linear beam tubes are classified into various categories as shown in figure.



Figure

Specifications of O-type Tubes	
1. Peak output power	$\approx 30 \text{ mW (maximum)}$
2. Beam voltage	$\approx 100 \text{ kV}$
3. Frequency	10 GHz
4. Average power output	700 kW (maximum)
5. Gain	30 - 70 dB
6. Efficiency	15 - 60%
7. Bandwidth	1 - 8% (Klystron) 10 - 15% (TWTs)

Application

O-type tubes are mainly used as amplifiers in communication systems.

Q22. Explain the working principle of two cavity klystron with the help of applegate diagram. Also write the expression for velocity modulation and voltage gain.

(or)

Explain the principle of working for two cavity klystron with velocity diagram.

May/June-13, R09, Q4(e)

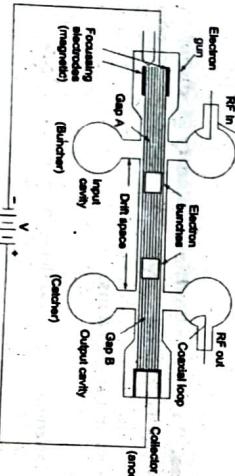
(or)
Explain the principle of a two cavity klystron with a neat diagram.

Nov.-13, (R09), Q4(e)

Ans:

Two-cavity Klystron Amplifier

A two-cavity klystron tube is a linear beam type microwave amplifier which works on the principle of velocity modulation. The construction of two-cavity klystron amplifier is as shown in figure (1).



At a point (say B) on the RF signal the alternating voltage is zero and going positive with the electric field across the gap A as zero. The electron which passes through the gap A is unaffected by the RF signal. Assuming this as the reference electron Y. Another electron Z, passes the gap slightly later than Y. At a point C, the late electron Z subjected to maximum positive RF voltage. As a result, this electron travels towards gap B with an increased velocity and tries to catch up with the reference electron. Similarly, an electron X called the early electron passes the gap A slightly before the reference electron X travels with a reduced velocity and falls back and the reference electron Y catches up with the early electron.

This shows that the changes in velocity of electron in accordance with the RF voltage results in velocity modulation of the electron beam.

The velocity of electrons accelerated by the high D.C. voltage V_0 is constant before entering the buncher grids and it can be expressed as,

Construction

In figure (1), klystron tube consists of a buncher or input cavity and catcher or output cavity. Since, the grids in each cavity are separated by a small gap they are named as re-entrant cavities.

The input cavity is excited with the help of an RF signal. The electron beam is injected into the tube reaches the gap between input cavity grids(drift space). Here, the electron velocity is varies in accordance with the input signal (velocity modulation).

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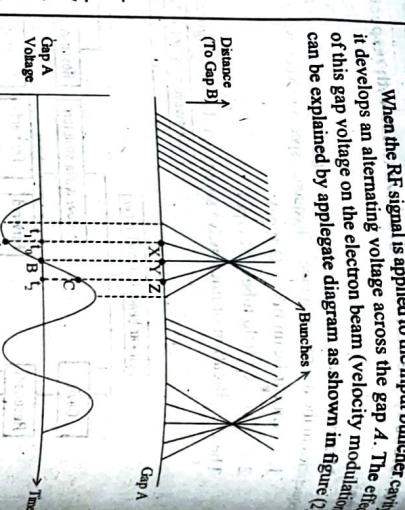


Figure (2)

Links

Y-axis

Time

Bunching

Links

Y-axis

</div

In reentrant cavities, the metallic boundaries are extended into the interior of cavity. Some of the shapes of reentrant cavities are as shown in figure (1).

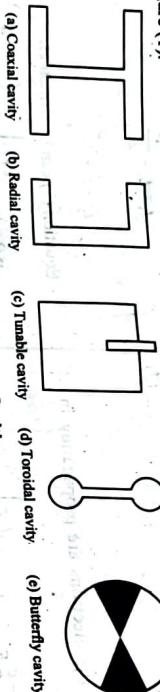


Figure 1: Reentrant Cavities

Consider a coaxial cavity with its equivalent circuit as shown in figure (2).

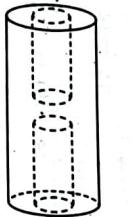


Figure 2

Coaxial cavity resembles a coaxial line shorted at two ends and joined by a capacitor at the center.

It's input impedance is given by,

$$Z_m = jZ_0 \tan(\beta d)$$

Where,

$$\beta = \frac{1}{2\pi} \sqrt{\frac{I}{\epsilon}} \ln\left(\frac{b}{a}\right)$$

The characteristic impedance of a coaxial line is given by,

$$Z_0 = \frac{1}{2\pi} \sqrt{\frac{I}{\epsilon}} \ln\left(\frac{b}{a}\right)$$

Substituting equation (2) in equation (1), we get,

$$Z_m = j \frac{1}{2\pi} \sqrt{\frac{I}{\epsilon}} \ln\left(\frac{b}{a}\right) \tan(\beta d)$$

But, inductance of cavity is given by,

$$L = \frac{2X_m}{\omega} = \frac{1}{\omega} \sqrt{\frac{I}{\epsilon}} \ln\left(\frac{b}{a}\right) \tan(\beta d)$$

and capacitance, $C_s = \frac{\epsilon \pi a^2}{d}$

At resonance, $\omega L = \frac{1}{\omega C_s}$

$$\Rightarrow \frac{\omega}{\omega} \sqrt{\frac{I}{\epsilon}} \ln\left(\frac{b}{a}\right) \tan(\beta d) = \frac{1}{\omega \pi a^2 \sqrt{\frac{I}{\epsilon}} \ln\left(\frac{b}{a}\right)}$$

$$\Rightarrow \tan \beta d = \frac{d}{\omega \pi a^2 \sqrt{\frac{I}{\epsilon}} \ln\left(\frac{b}{a}\right)}$$

$$\therefore \tan \beta d = \frac{d}{\omega \pi a^2 \sqrt{\frac{I}{\epsilon}} \ln\left(\frac{b}{a}\right)}$$

$$\therefore \tan \beta d = \frac{d}{\omega \pi a^2 \sqrt{\frac{I}{\epsilon}} \ln\left(\frac{b}{a}\right)}$$

Where,

$$V = \frac{1}{\omega \epsilon} \ln\left(\frac{b}{a}\right)$$

Consider a radial resonant cavity as shown in figure (3).

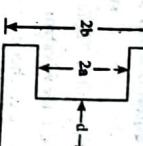


Figure 3

Here,

$$L = \frac{\mu}{2\pi} \ln\left(\frac{b}{a}\right)$$

$$C = \epsilon_0 \left[\frac{\pi a^2}{d} - 4a \ln \frac{0.765}{\sqrt{b^2 + (b-a)^2}} \right]$$

The resonant frequency of radial reentrant cavity is given by,

$$f_r = \frac{C}{2\pi \sqrt{\epsilon_r}} \left[\frac{a}{2d} - \frac{2}{\pi} \ln \frac{0.765}{\sqrt{b^2 + (b-a)^2}} \right] \ln \left(\frac{b}{a} \right)^{-1/2}$$

Q24. Compose and explain about two cavity klystron amplifier and derive its Bunching process.

Oct/Nov-20, (R16), Q5(a)

With the help of Applegate diagram, explain the bunching process and hence the velocity modulation in klystron amplifier.

April/May-18, (R13), Q5(a)

Explain in detail bunching process and obtain expression for bunching parameter in a two cavity klystron.

Nov/Dec-16, (R13), Q6

(or)

Discuss in detail bunching process for a two cavity klystron amplifier and obtain the expression for bunching parameter.

Nov/Dec-12, (R09), Q5(a)

Ans:

For answer refer Unit-1, Q22, Topic: Two-cavity klystron amplifier, Construction, working.

Bunching Process:

In a two cavity klystron amplifier, the electrons leave the buncher cavity, with a velocity given by,

$$v(t) = v_0 \left[1 + \frac{\beta V}{2V_0} \sin \left(\omega t - \frac{\theta_s}{2} \right) \right]$$

This effect of velocity modulation produces an electron beam, which passes through the buncher cavity at three possibilities. They are,

1. When the voltage is zero
2. When the voltage is positive
3. When the voltage is negative.

In a klystron amplifier, electron bunching is formed due to the propagation of electrons with different velocities. The electron beam coming from the cathode is affected by input RF voltage applied at the buncher cavity. At zero RF voltage, the electron moves with its actual velocity v_0 and becomes the bunching center. For a maximum positive voltage, the electron accelerates with a velocity greater than v_0 in the same manner. The electron that passes the cavity at maximum negative voltage decelerates with the velocity less than v_0 .

The beam electrons drift into dense clusters with a separation gap of ΔL along the input wave as shown in figure below.

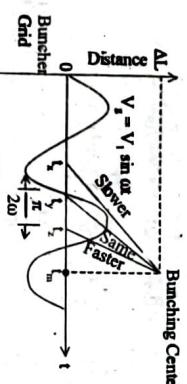


Figure 4: Bunching Process

The distance of an electron at 't' from the buncher grid to the location of dense electron bunching is given by,

$$\Delta L = v_0(t_m - t) \quad \dots (1)$$

Similarly, the distances for the electrons at 't_1' and 't_2' are,

$$\Delta L = v_{min} (t_m - t_1) = v_{min} \left(t_m - t_2 + \frac{\pi}{2\omega} \right) \quad \dots (2)$$

$$\Delta L = v_{max} (t_m - t_1) = v_{max} \left(t_m - t_2 - \frac{\pi}{2\omega} \right) \quad \dots (3)$$

From the expression $v(t)$, the minimum and maximum velocities are obtained as,

$$v_{min} = v_0 \left[1 - \frac{\beta V}{2V_0} \right] \quad [\because t_1 = -\frac{\pi}{2\omega}, \theta_s = 0] \quad \dots (4)$$

$$v_{max} = v_0 \left[1 + \frac{\beta V}{2V_0} \right] \quad [\because t_1 = \frac{\pi}{2\omega}, \theta_s = 0] \quad \dots (5)$$

Substituting equation (4) in equation (2),

$$\Delta L = v_0 \left[1 - \frac{\beta V}{2V_0} \right] \left[(t_m - t_1) + \frac{\pi}{2\omega} \right] \quad \dots (6)$$

Substituting equation (5) in equation (3),

$$\Delta L = v_0 \left[1 + \frac{\beta V}{2V_0} \right] \left[(t_m - t_2) - \frac{\pi}{2\omega} \right] \quad \dots (7)$$

Then, the necessary condition for those electrons at t'_1 and t'_2 to meet at the same distance, ΔL is,

$$\frac{v_0}{2\omega} \frac{\pi}{2} - v_0 \frac{\beta V_1}{2V_0} (t'_2 - t'_1) - v_0 \frac{\beta V_1}{2V_0} \frac{\pi}{2\omega} = 0 \quad \dots (8)$$

Ans:

For answer refer Unit-1, Q24, Topic: Bunching Process.

Output Power of a Two Cavity Klystron

The RF voltage at the catcher cavity is given by,

$$\text{RF voltage} = V_2 \sin \omega t'_2$$

Where,

t'_2 – Time taken by electron to reach catcher.

Then, the energy given by the electron to the bunch is,

$$E = (-e)V_2 \sin \omega t'_2$$

Where,

e – Charge associated with the electron.

The average energy (i.e., power) applied to the RF field is given as,

$$(I_m - I_p) = \frac{\pi V_0}{\alpha \beta V_1} \quad \dots (9)$$

By substituting equation (9) in equation (1), the expression for minimum distance at which bunching occurs is obtained as,

$$\Delta L = \frac{V_0}{\alpha \beta V_1} \frac{\pi V_0}{2\omega} \quad [\because V_0 \gg V_1]$$

From the above condition,

$$(t'_2 - t'_1) = \frac{\pi V_0}{\alpha \beta V_1} \quad \dots (9)$$

By substituting equation (9) in equation (1), the expression for minimum distance at which bunching occurs is obtained as,

$$\Delta L = \frac{V_0}{\alpha \beta V_1} \frac{\pi V_0}{2\omega} \quad [\because V_0 \gg V_1]$$

The transit time for an electron to travel a distance 'L' is,

$$T = t'_2 - t'_1 = \frac{L}{v(t'_1)} \quad \dots (1)$$

$$\therefore T = T_0 \left[1 - \frac{\beta V_1}{2V_0} \sin \left(\omega t'_1 - \frac{\pi}{2} \right) \right] \quad [\because T_0 = \frac{L}{v_0}]$$

This can be expressed in terms of radians as,

$$\omega T = \omega t'_2 - \omega t'_1$$

$$\omega T = \theta_0 - X \sin \left(\omega t'_1 - \frac{\theta_0}{2} \right)$$

Here, $\frac{\omega L}{v_0}$ is replaced by θ_0 and $\frac{\beta V_1}{2V_0}$ θ_0 is replaced by 'X'.

Where,

X – Bunching parameter of a klystron

$$X = \frac{\beta V_1}{2V_0} \theta_0$$

$$\omega t'_2 = \omega t'_1 + \frac{\alpha L}{v_0} \left[1 - \frac{V_1}{2V_0} \sin \omega t'_1 \right]$$

$$P_{\text{out}} = 0.58 I_0 V_2^2 \quad \text{Hence, } \eta = \frac{P_{\text{out}}}{P_{\text{in}}} = \frac{0.58 I_0 V_2^2}{I_0 V_0} = \frac{0.58 V_2^2}{V_0}$$

$$\text{Substituting the value of } \omega t'_2 \text{ in equation (1),}$$

$$P_{\text{avg}} = \frac{1}{2\pi} \int_{-\pi/2}^{\pi/2} -eV_2 \sin \left[\omega t'_1 + \theta_0 + \frac{\alpha L}{v_0} \left[1 - \frac{V_1}{2V_0} \sin \omega t'_1 \right] \right] d(\omega t'_1) \quad \dots (3)$$

$$\Rightarrow \% \eta = \frac{0.58 V_2^2}{V_0} \times 100$$

Where,

$$T_0 – \text{Transit time without RF voltage } V_1 = \frac{L}{v_0}$$

$$\theta_0 – \text{Transit angle without RF voltage } V_1 = \frac{\alpha L}{v_0}$$

Equation (3) represents a Bessel function and its solution is given as,

$$P_{\text{avg}} = -eV_2 J_1(\lambda) \sin \theta_0$$

Where,

$$J_1(\lambda) \text{ – Bessel function of first order for the argument } \lambda.$$

Assuming 'N' number of electrons moving from buncher to catcher cavity, then the average energy associated is given as,

$$P_{\text{avg}} = NP_{\text{avg}} = -NeV_2 J_1(\lambda) \sin \theta_0$$

Where,

$$I_o – \text{Output current (Me)}$$

The maximum value of output power is given by,

$$P_{\text{max}} = [J_1(\lambda)]_{\text{max}} I_o V_2$$

$$\left[\because \sin \theta_0 = -1, \text{ where } \theta_0 = 2\pi - \frac{\pi}{2} \right]$$

$[J_1(\lambda)]_{\text{max}}$ value is 0.58 for $X = 1.84$ from the Bessel function table.

$$\text{Hence, } P_{\text{out}} = P_{\text{max}} = (0.58) I_o V_2$$

$$\therefore P_{\text{out}} = 0.581 I_o V_2$$

Efficiency of a Two Cavity Klystron: The efficiency of a two cavity klystron is defined as,

$$\eta = \frac{P_{\text{out}}}{P_{\text{in}}} = \frac{P_{\text{out}}}{I_o V_0}$$

The expression for D.C. input power, P_{in} is given by,

$$P_{\text{in}} = I_o V_0 \left[1 - \frac{V_1}{2V_0} \sin \omega t'_1 \right]$$

Where,

$$V_0 – \text{Anode voltage}$$

$$I_o – \text{Output current}$$

The output power, P_{out} of amplifier is given as,

$$P_{\text{out}} = 0.58 I_0 V_2^2$$

Depending on the cavity tuning and the various D.C. voltages, the feedback path between two cavity resonators is properly matched. The conditions for sustained oscillations are,

$$\theta + \alpha + \frac{\pi}{2} = 2\pi n \text{ radians}$$

And gain-bandwidth product($\alpha\beta$) = 1

Where,

$$\theta – \text{Total phase shift in the resonators and the feedback cable.}$$

$\alpha + \frac{\pi}{2}$ – Phase angle between buncher and catcher voltages

n – integer.

If the two resonators oscillate in phase i.e., $\theta = 0$, then the maximum output power is obtained at the output of oscillator.

Substituting $\theta = 0$ in equation (1),

$$\alpha = 2\pi n - \frac{\pi}{2} \quad \dots (2)$$

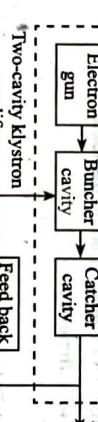


Figure: Block Diagram Representation of a Two-Cavity Klystron Oscillator

This oscillator must satisfy Barkhausen criterion. Depending on the cavity tuning and the various D.C. voltages, the feedback path between two cavity resonators is properly matched. The conditions for sustained oscillations are,

$$\theta + \alpha + \frac{\pi}{2} = 2\pi n \text{ radians}$$

And gain-bandwidth product($\alpha\beta$) = 1

Where,

$$\theta – \text{Total phase shift in the resonators and the feedback cable.}$$

$\alpha + \frac{\pi}{2}$ – Phase angle between buncher and catcher voltages

If the two resonators oscillate in phase i.e., $\theta = 0$, then the maximum output power is obtained at the output of oscillator.

Substituting $\theta = 0$ in equation (1),

$$\alpha = 2\pi n - \frac{\pi}{2} \quad \dots (2)$$

The above condition is also necessary for obtaining the sustained oscillations.

If the resonators are over coupled, the oscillations can be obtained over wide range. Whereas a linear variation in frequency with accelerating voltage is possible for a critically coupled klystron oscillator. The high frequency stability of oscillator is obtained by,

- Controlling the temperature of the resonators.
- Use of regulated power supplies.

Advantages of Two-cavity Klystron Oscillator

- It is the lowest-noise microwave source.
- Two-cavity klystron oscillator generates more power than reflex klystron oscillator.

- It requires only one high-voltage supply.

Application: This oscillator is used in the illuminator systems or missile targeting radars.

Q27. A two cavity klystron amplifier has the following

- V₀** = 1200 V, **I₀** = 25 mA, **R₀** = 30 kΩ,
f = 10 GHz, **d** = 1 mm, **L** = 4 cm, **R_{in}** = 30 kΩ.

Calculate,

- The input voltage for maximum output voltage.
- The voltage gain in decibels.
- Efficiency.

Ans:

Given that,

For a two cavity klystron amplifier,

V₀ = 1200 V

I₀ = 25 mA

R₀ = 30 kΩ

f = 10 GHz

d = 1 mm

L = 4 cm

R_{in} = 30 kΩ

I₀ = 25 mA

R₀ = 30 kΩ

V₀ = 1200 V

X = Bunching parameter

V₀ – D.C. voltage between anode and cathode

θ_0 – Transit angle without RF voltage

β_1 – Beam coupling coefficient

- The input voltage applied at two cavity klystron is given by,

$$V_1 = \frac{2XV_0}{\beta_1 R_0} \quad \dots (1)$$

Where,

X – Bunching parameter

V₀ – D.C. voltage between anode and cathode

θ_0 – Transit angle without RF voltage

β_1 – Beam coupling coefficient

$$\text{And, } \theta_0 = \frac{\alpha d}{V_0} = \frac{2\pi \times L}{0.593 \times 10^6 \sqrt{V_0}} \quad [: V_0 = 0.593 \times 10^6 \sqrt{V_0}]$$

$$= \frac{2\pi \times 10 \times 10^9 \times 4 \times 10^{-2}}{0.593 \times 10^6 \sqrt{1200}}$$

$$= 12.347 \text{ rad} \approx 122.35 \text{ rad}$$

i.e., D.C. transit angle, $\theta_0 = 122.35 \text{ rad}$

Beam coupling coefficient is given by,

$$\beta_1 = \frac{\sin \frac{\theta_0}{2}}{\theta_0} = \frac{\sin 61.175}{122.35} = 0.052$$

Given that, θ_0 = Average gap transit angle = $\frac{\alpha d}{V_0}$

$$\theta_0 = \frac{2\pi \times 10 \times 10^9 \times 10^{-3}}{0.593 \times 10^6 \sqrt{1200}} = 3.059 \text{ rad}$$

Then,

$$\beta_1 = \frac{\sin \frac{\theta_0}{2}}{\theta_0} = \frac{\sin (3.059/2)}{3.059/2} = 0.653$$

On substituting corresponding values in equation (1),

$$V_{1(\text{max})} = \frac{3.68 \times 1200}{0.653 \times 122.35} = 55.273 \text{ V}$$

$\therefore V_{1(\text{max})} = 55.273 \text{ V}$

(ii) Voltage gain, A_v is given by,

$$A_v = \frac{V_2}{V_{1(\text{max})}} \quad \dots (2)$$

Where,

$$V_2 = \beta_0 I_2 R_{in}$$

$$= \beta_0 I_2 R_0$$

$$\Rightarrow I_2 = 2J_0(X)$$

$$\text{For, } X = 1.84$$

$$\therefore I_2 = 2 \times 0.582 \quad (\text{From Bessel function table})$$

$$\therefore I_2 = 2 \times 2.5 \times 10^{-3} \times 0.582$$

$$= 29.1 \text{ mA}$$

Then, $V_2 = \beta_0 I_2 R_{in}$

$$= \beta_0 I_2 R_0 \quad [: \beta_0 = \beta_1]$$

$$\Rightarrow V_2 = 15.81 \times 10^3 \text{ V}$$

And the expression for output voltage of a two cavity klystron is given by,

$$\text{Output voltage, } V_2 = (A_v) V_1$$

$$20 \log_{10} \frac{V_2}{V_1} = 20$$

$$\Rightarrow \log_{10} \frac{V_2}{V_1} = 1$$

$$\frac{V_2}{V_1} = 10^1$$

$$\Rightarrow V_2 = 10 V_1$$

$$\therefore V_2 = 15.81 \times 10^3 \text{ V}$$

(or)

$$\therefore V_2 = 0.653 \times 29.1 \times 10^{-3} \times 30 \times 10^3$$

$$= 570.069 \text{ V}$$

On substituting corresponding values in equation (2),

$$A_v = \frac{570.069}{55.273} = 10.314$$

$$A_v (\text{dB}) = 20 \log (10.314) = 20.269 \text{ dB}$$

$$\therefore A_v = 20.269 \text{ dB}$$

For maximum output power, $X = 1.84$

$$\text{And, } \theta_0 = \frac{\alpha d}{V_0} = \frac{2\pi \times L}{0.593 \times 10^6 \sqrt{V_0}} \quad [: V_0 = 0.593 \times 10^6 \sqrt{V_0}]$$

$$= \frac{2\pi \times 10 \times 10^9 \times 4 \times 10^{-2}}{0.593 \times 10^6 \sqrt{1200}}$$

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Given that,

(Model Paper, Q27(b) | Nov/Dec.-17, (R13), Q5(b))

Given that, θ_0 = Average gap transit angle = $\frac{\alpha d}{V_0}$

For a two cavity klystron,

Input power, $P_{in} = 10 \text{ mW}$

Voltage gain, $A_v = 20 \text{ dB}$

R_{in} of input cavity, $R_{in(\text{input})} = 25 \text{ k}\Omega$

R_{in} of output cavity, $R_{in(\text{output})} = 40 \text{ k}\Omega$

Load resistance, $R_L = 40 \text{ k}\Omega$

Input voltage, $V_1 = ?$

Output voltage, $V_2 = ?$

Power delivered to the load, $P_{out} = ?$

Input voltage, $V_1 = \sqrt{(P_{in}) R_{in(\text{input})}}$

Then, the expression for input voltage of a two cavity klystron is given by,

$$V_1 = \sqrt{(10 \times 10^{-3}) \times (25 \times 10^3)}$$

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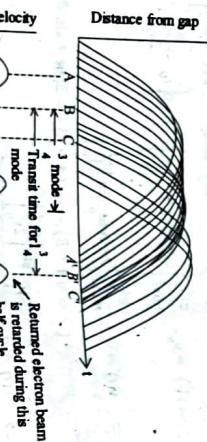


Figure: Applegate Diagram with Gap Voltage for a Reflex Klystron

The velocity with which electrons leave the cavity is given as,

$$v(t_1) = V_0 \left[1 + \frac{\alpha \beta}{2} \sin \omega t_1 \right] \quad \dots (1)$$

Where,

t_1 – Time at which electrons pass through the centre of the cavity.

Then, the force exerted in the electric field 'E' is given

$$F = ma = -eE \quad \dots (2)$$

$\Rightarrow m a = -eE$

Assuming, the electrons are propagating in z -direction, then

$$\frac{d^2 z}{dt^2} = -\frac{e}{m} E, \quad \left[\because a = \frac{d^2 z}{dt^2} \right] \quad \dots (3)$$

The instantaneous gap voltage, V' is given by,

$$\text{Field intensity, } E_t = \frac{V_0 + V_0 - V_R}{L} \quad \dots (4)$$

$$= \frac{(V_0 - V_R) + V \sin \omega t}{L} \quad \dots (5)$$

Since, $(V_0 - V_R) \gg V \sin \omega t$,

$$\Rightarrow E_t = \frac{(V_0 - V_R)}{L} \quad \dots (4)$$

Where,

$$L \text{ – Width of the cavity gap}$$

Substituting E_t value in equation (3),

$$\frac{d^2 z}{dt^2} = \frac{-e}{m} \frac{(V_0 - V_R)}{L} \quad \dots (6)$$

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$$\begin{aligned} \frac{dz}{dt} &= \int \frac{-e}{m} \frac{(V_0 - V_R)}{L} dt = \frac{-e (V_0 - V_R)}{m L} \int \frac{dt}{t_1} + C \\ &\Rightarrow \frac{dz}{dt} = \frac{-e (V_0 - V_R)}{m L} (t_1 - t_1) + C \\ \text{At } t = t_1, \quad &\frac{dz}{dt} = v(t_1) \\ &\Rightarrow \frac{dz}{dt} \Big|_{t=t_1} = v(t_1) \\ &\Rightarrow C = v(t_1) \end{aligned}$$

$$\begin{aligned} \theta_0 &= \omega(t_2 - t_1) = \omega T_0 \\ &= \left(n + \frac{3}{4} \right) 2\pi \\ \text{Hence,} \quad &\frac{dz}{dt} = \frac{-e (V_0 - V_R)}{m L} (t_1 - t_1) + v(t_1) \end{aligned}$$

Here, t_1 is the time at which electron pass through mid point or the gap for the first time. Assuming that t_1 is the time at which the electron returns to the gap from the repeller space. Hence, at $t = t_2$ equation (5) becomes,

$$\frac{dz}{dt} = \frac{-e (V_0 - V_R)}{m L} (t_2 - t_1) + v(t_1) \quad \dots (5)$$

$$v(t_2) = \frac{-e (V_0 - V_R)}{m L} (t_2 - t_1) + v(t_1)$$

$$\text{Here, } v(t_2) = -v(t_1)$$

$$\Rightarrow -v(t_1) = \frac{-e (V_0 - V_R)}{m L} (t_2 - t_1) + v(t_1) \quad [\because v(t_2) = -v(t_1)]$$

$$\Rightarrow 2v(t_1) = \frac{e (V_0 - V_R)}{m L} (t_2 - t_1) \quad \dots (6)$$

$$\Rightarrow t_2 - t_1 = \frac{2m v(t_1)}{e (V_0 - V_R)}$$

$$\text{From equation(2),} \quad t_2 - t_1 = \frac{2m L}{e (V_0 - V_R)} \int_0^1 \left[1 + \frac{\alpha \beta}{2} \sin \omega t_1 \right] dt \quad \dots (6)$$

$$\text{Multiplying by } \omega \text{ on both sides,} \quad t_2 - t_1 = \frac{2m L}{e (V_0 - V_R)} \int_0^1 \left[\frac{\beta V}{2} \sin \omega t_1 \right] dt \quad \dots (7)$$

$$= \frac{2m L}{e (V_0 - V_R)} \int_0^1 \left[\frac{\beta V}{2} \sin \omega t_1 \right] dt \quad \dots (7)$$

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$$= \frac{2m L}{e (V_0 - V_R)} \int_0^1 \left[\frac{\beta V}{2} \sin \omega t_1 \right] dt \quad \dots (7)$$

In order to obtain the maximum power output of reflex klystron, a maximum amount of kinetic energy needs to be transferred from the returning electrons to the cavity walls. For a maximum energy transfer, the round-trip transmit angle is obtained as,

$$\begin{aligned} \theta_0 &= \omega(t_2 - t_1) = \omega T_0 \\ &= \left(n + \frac{3}{4} \right) 2\pi \\ &= 2\pi n + \frac{3\pi}{2} \end{aligned}$$

Efficiency of Reflex Klystron

The efficiency of the reflex klystron is given by the ratio of P_{ac} to P_{dc} .

$$\eta = \frac{P_{ac}}{P_{dc}} = \frac{P_{out}}{P_{in}} \quad \dots (8)$$

The input and output powers of the reflex klystron are given by,

$$\begin{aligned} P_{in} &= V_0 I_0 \\ \text{and } P_{out} &= \frac{2V_0 I_0 X J_1(X)}{2\pi n + \frac{3\pi}{2}} \end{aligned}$$

$$\eta = \frac{P_{out}}{P_{in}} = \frac{1.252}{\pi(1+3/4)} = 0.2278$$

$$\eta = \frac{1.252}{2\pi(n+3/4)}$$

$$\eta = \frac{1.252}{22.78\%}$$

The maximum efficiency is obtained for $n = 1$ and maximum of $X J_1(X)$ is 1.252 for $X = 2.408$.

$$\eta_{max} = \frac{1.252}{\pi(1+3/4)} = 0.2278$$

$$\eta = \frac{1.252}{22.78\%}$$

Q33. Derive the expressions for repeller voltage and electronic efficiency of reflex klystron.

$$P_{ac} = P_{out} = \frac{V_1 I_2}{2}$$

$$P_{out} = V_1 I_0 \beta J_1(X)$$

From the expression of bunching parameter is,

$$X' = \frac{V_0 \theta_0}{2V_0} \quad \left[\because \alpha = \frac{V_0}{V_1} \right] \quad \dots (6)$$

$$X' = \frac{\beta \alpha \theta_0}{2} \quad \dots (6)$$

Here,

$$\theta_0 = \omega T_0 \quad \dots (7)$$

$$X' = \frac{V_0 \theta_0}{2V_0} \quad \dots (7)$$

The electrons injected into the tube travel with an initial velocity, v_0 and V_0 is the dc voltage applied across the tube. Then, the energy of the electron is equal to the kinetic energy gained by the electrons i.e.,

$$\frac{1}{2}mv_0^2 = eV_0$$

$$\Rightarrow V_0 = \frac{m v_0^2}{2e} \quad \dots (1)$$

$$\Rightarrow V_0 = \frac{m v_0^2}{2e} \quad \dots (1)$$

The transit angle, θ_0 is defined as,

$$\theta_0 = \frac{-2mL\omega_0}{e(V_R - V_0)}$$

Where,

$\frac{e}{m}$ – Electron charge mass ratio

L – Distance between cavity gap and repeller electrode

ω – Frequency of operation in radians per second

V_0 – Velocity of electron

V_R – Repeller voltage.

$$\Rightarrow V_0 = \frac{-\theta_0 e(V_R - V_0)}{2mL\omega_0}$$

Substituting 'V₀' value in equation (1),

$$V_0 = \frac{m}{2e} \left| \frac{\theta_0 e(V_R - V_0)}{2mL\omega_0} \right|^2$$

$$V_0 = \frac{e}{m} \times \frac{1}{8} (\theta_0)^2 \frac{(V_R - V_0)^2}{L^2 \omega_0^2}$$

$$\frac{8mV_0^2 L^2 \omega_0^2}{e(\theta_0)^2} = (V_R - V_0)^2$$

$$V_R - V_0 = \sqrt{\frac{8mV_0^2 L^2 \omega_0^2}{e(\theta_0)^2}}$$

$$\Rightarrow V_R = V_0 + 2 \sqrt{2V_0 \left(\frac{m}{e} \right) \theta_0}$$

$$\Rightarrow V_R = V_0 + \frac{2m\theta_0}{\theta_0} \sqrt{2V_0 \left(\frac{m}{e} \right)}$$

Substituting, $\frac{e}{m} = 1.759 \times 10^{11} \text{ C/kg}$ in above equation,

$$\therefore V_R = V_0 + \frac{(6.74 \times 10^{-9}) \omega_0 L}{\theta_0} \sqrt{V_0}$$

When the net admittance is less than zero, oscillations are produced in the reflex klystron.

As, $Y_t = G_t + jB_t$

Then, the condition for oscillation is,

$$|1 - G_t| \geq G$$

Ans: Figure (1) shows the equivalent circuit of a reflex klystron oscillator.

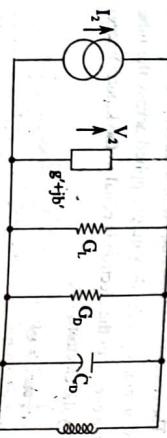


Figure (1)

will be a spiral. The transadmittance, Y_t is a function of transit angle θ_0 .

$$\text{For } n = 0, \theta_0 = 2m\pi - \frac{\pi}{2}, \theta_0 = \frac{\pi}{2}$$

$$n = 1, \theta_0 = \frac{3\pi}{2}, \theta_0 = \frac{\pi}{2}$$

$$n = 2, \theta_0 = \frac{7\pi}{4}$$

$$n = 3, \theta_0 = \frac{11\pi}{4}$$

$$n = 4, \theta_0 = \frac{15\pi}{4}$$

From equations (1) and (2),

$$Y_t = \frac{2I_0 J(X) e^{-\theta_0}}{V_t e^{-\theta_0/2}}$$

Where,

$$I_0 = \text{D.C current}$$

$J(X)$ – First order bessel function

V_t – Amplitude of the input RF signal.

But, the amplitude of the input RF signal of the reflex klystron is given by,

$$V_t = \frac{2V_0 X}{\beta \theta_0}$$

Substituting 'V_t' value in equation (3),

$$Y_t = \frac{2I_0 J(X) e^{-\theta_0}}{2V_0 X e^{-\theta_0/2}}$$

$$Y_t = \frac{I_0 \theta_0 J(X)}{V_0 X}$$

$$Y_t = \frac{I_0 \theta_0 J(X)}{V_0 X}$$

Q34. Derive the expression for transadmittance condition of reflex klystron oscillator and explain the condition of oscillation from admittance spiral.

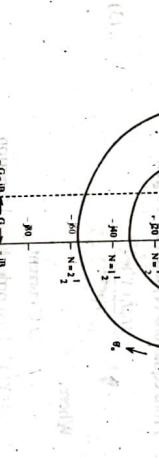
Ans:

The performance of a reflex klystron depends on two types of characteristics. They are,

1. Voltage Characteristics

The required specific combinations of anode and repeller voltages are used to produce the oscillations and that will give a favourable transit time i.e., $T = \left(\frac{n+3}{4} \right)$.

The possible oscillation combinations and optimum combinations are shown by shaded areas and heavy lines respectively in figure (1). For different values of 'n', i.e., $n = 1, 2, 3, \dots$ the reflex klystron oscillator is operated in different modes. The mode with larger output power is not advantageous but it should have higher voltages as shown in figure (1). This leads to the possibility of lower efficiencies and insulation problems. Hence, modes corresponding to $n = 2$ or $n = 3$ are most widely used.



Q35. Explain the performance characteristics of a reflex klystron tube with neat sketch.

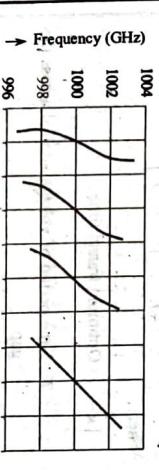
Ans:

The performance of a reflex klystron depends on two types of characteristics. They are,

1. Voltage Characteristics

The required specific combinations of anode and repeller voltages are used to produce the oscillations and that will give a favourable transit time i.e., $T = \left(\frac{n+3}{4} \right)$.

Figure (2): Power Output and Frequency Characteristics of Reflex Klystron



Q36. Draw the mode curves of reflex klystron and derive the relation between mode number and repeller in reflex klystron.

Ans: (Model Paper, Q3(a) | Nov/Dec.-17, (R13), Q5(e))

Mode Curves of Reflex Klystron

The curves which describe the variations in power output and frequency with changes in the repeller voltage are called mode curves, which are shown in figure.

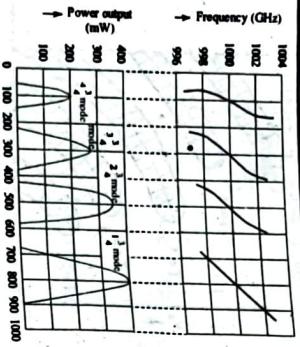


Figure 1: Power Output and Frequency Characteristics of Reflex Klystron

Relation between Mode Number and Repeller

In a reflex klystron, the electron bunch formed at the repeller must reach the cavity resonator at the transit time, so that the electrons bunch is severely decelerated. In the process of deceleration, the electrons give up their energy, which is used to reinforce the oscillations in the cavity.

This transit time is expressed as,

$$T_0' = \frac{n + \frac{3}{4}}{\frac{1}{f}} \quad \left[\because T = \frac{1}{f} \right] \quad \dots (1)$$

Where,
 $\left(n + \frac{3}{4} \right)$ - Optimum transit time

T - Time period of voltage applied across the gap.

And the transit angle is expressed as,
 $\theta_0' = \omega T_0' = 2\pi \left(n + \frac{3}{4} \right) \frac{1}{f} \quad \left[\because \omega = 2\pi f \right] \quad \dots (2)$

Where, $n = 0, 1, 2, 3, \dots$

The transit time and transit angle shown in equations (1) and (2) respectively represent that, the reflex klystron operates at different drift times which are called modes. These modes are defined for different 'n' values given as,

Mode number, $N_0' = \left(n + \frac{3}{4} \right)$

Where,

$$n = 0 \text{ is called } \frac{3}{4} \text{ mode}$$

When the anode voltage (V_A) and resonant frequencies are fixed, the mode number and repeller are related as,

$$\frac{(|V_R| + V_0)}{(|V_R| + V_0)} = \frac{N_0'}{N_1'} \quad \dots (1)$$

Where, $|V_R|$ and $|V_0|$ are the repeller voltages that are used to operate the klystron in mode numbers N_0' and N_1' respectively.

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Q37. Derive the expression for transadmittance condition of oscillation from admittance spiral.

Ans: Transadmittance of Reflex Klystron Oscillator: Figure (1) shows the equivalent circuit of a reflex klystron oscillator.

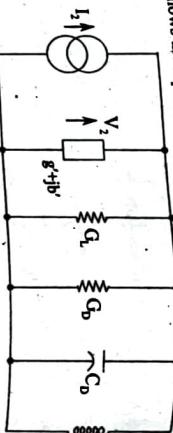


Figure 1)

The output current, I_0 of the reflex klystron in the phasor form is given by,

$$I_0 = 2I_0 J_1(X') e^{-j\theta_0} \quad \dots (1)$$

and the output voltage, V_2 of the reflex klystron in the phasor form is given by,

$$V_2 = V_0 e^{-j\theta_0} \quad \dots (2)$$

Then, the transadmittance or electronic admittance is given by,

$$Y_R = \frac{I_0}{V_2} = \frac{I_0}{V_0 e^{-j\theta_0}} \quad \dots (3)$$

From equations (1) and (2), we get,

$$Y_R = \frac{2I_0 J_1(X') e^{-j\theta_0}}{V_0 e^{-j\theta_0}} \quad \dots (3)$$

Where,
 I_0 = D.C current

$J_1(X')$ = First order bessel function

V_1 = Amplitude of the input RF signal.

But, the amplitude of the input RF signal of the reflex klystron is given by,

$$V_1 = \frac{2V_0 X'}{B_0 \theta_0} \quad \dots (4)$$

Substituting ' V_1 ' value in equation (3), we get,

$$Y_R = \frac{2I_0 J_1(X') e^{-j\theta_0}}{2B_0 X' V_0 e^{-j\theta_0}} \quad \dots (4)$$

Where,

$$n = 0 \text{ is called } \frac{3}{4} \text{ mode etc.}$$

Figure 2: Electronic Admittance Spiral of a Reflex Klystron

Q38. Explain about electronic and mechanical tuning in reflex klystron.

Ans:

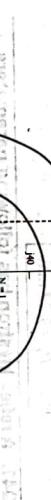
Electronic Tuning
Electronic tuning is possible by adjusting of the repeller voltage (V_R). The tuning range is about ± 8 MHz at X-band and ± 80 MHz for submillimeter klystron.

Then, the condition for oscillation is,

$$|1 - G_0| \geq G \quad \dots (1)$$

Where, $|V_R|$ and $|V_0|$ are the repeller voltages that are used to operate the klystron in mode numbers N_0' and N_1' respectively.

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Upto $n = 7$, the oscillations are possible in reflex klystron practically. The corresponding electronic admittance spiral of a reflex klystron is shown in figure (2).

From equation (2) and (3), we get,

$$Y_R + V_0 = \sqrt{\frac{8ms^2V_0}{e} \left(\frac{1}{2\pi n - \frac{\pi}{2}} \right)} \quad \dots (3)$$

Substituting the value of $V_R + V_0$ from equation (1),

$$\frac{dV_R}{d\omega} = \frac{8ms^2\omega V_0}{e} \times \sqrt{\frac{1}{8ms^2V_0}} \quad \dots (2)$$

If repeller voltage is varied by even 2%, frequency changes considerably.

As the variation in frequency is quite sensitive to repeller voltage adjustments, it draws large current and get overheated. The precaution to be taken that the repeller voltage need to be applied prior to application of anode voltage and connection of a protective diode across the klystron, so that repeller can never become positive.

Mechanical Tuning

Mechanical tuning of reflex klystron may range from ± 20 MHz at X-band to ± 4 GHz at 200 GHz frequency.

The frequency of resonance is mechanically adjusted using tunable screws or posts. When a screw or sliding piston is used to tune cavity piston, the Q decreases due to the presence of current flowing through tuning elements. The resonant frequency gets affected by the dielectric materials. In the other method, consists of a wall is used to adjusted and fro by means of a screw, which tightens or loosens small linear posts. This method can be used with permanent cavities, which are built into reflex klystrons (as a form of limited frequency shifting). Hence, there is a possibility of changing the resonant frequency through mechanical tuning.

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- Q39. Design the input voltage and electronic efficiency when the beam voltage $V_0 = 250$ V, beam current $I_0 = 10$ mA, and the signal voltage $V_s = 25$ V are the parameters of a reflex klystron which operates at the mode $n = 2$.**

Ans: Given that,

For a reflex klystron,

Beam voltage, $V_0 = 250$ V

Beam current, $I_0 = 10$ mA

Signal voltage, $V_s = 25$ V

Operating mode, $n = 2$

Input voltage, $V_1 = ?$

Electronic efficiency, $\eta = ?$

Then, the input voltage V_1 of a reflex klystron can be obtained as,

$$V_1 = \frac{2V_0X'}{\beta_0\theta}$$

With 20% power dissipated in the cavity power delivered to load $P_L = ?$

The expression for input power is given by,

$$P_{in} = V_1 I_0 = 40 \text{ mW}$$

The output power of reflex klystron is given by,

$$P_{out} = \frac{2V_0^2 \times J_1(X')}{2\pi n - \frac{\pi}{2}} = \frac{2P_{in} J_1(X')}{2\pi n - \frac{\pi}{2}}$$

As 20% of the power delivered by beam is dissipated in cavity walls 80% power is delivered to load,

$$\Rightarrow P_L = 9.09 \times 10^{-3} \times \frac{80}{100} = 7.27 \text{ mW}$$

Q41. A reflex klystron has following parameters. Calculate,

- (i) The repeller voltage for which the tube can oscillate in $1 \frac{3}{4}$ mode.

(ii) The direct current necessary to give a microwave gap voltage of 200 V.

(iii) Electron efficiency.

Ans: Given that,

For a reflex klystron,

$V_0 = 800$ V, $L = 1.5$ mm, $R_{sh} = 15$ k Ω , $f = 9$ GHz.

maximum. This means $J_1(X') = 0.582$ for $X' = 1.841$. Then,

$$V_1 = \frac{2V_0X'}{\left(n + \frac{3}{4}\right)2\pi} \quad [\because \beta_0 = 1]$$

$$= \frac{2 \times 250 \times 1.841}{2 \times 2 \times 2.2} = 53.25 \text{ V}$$

and the electronic efficiency of a reflex klystron is obtained as,

$$\eta = \frac{2X'J_1(X')}{2\pi n - \frac{\pi}{2}}$$

$$= \frac{2X'J_1(X')}{2\pi \left(n + \frac{3}{4}\right)}$$

$$= \frac{2 \times 1.841 \times 0.582}{2 \times 1.124} = 12.4\%$$

Q40. A reflex klystron operates at the peak of the $n = 2$ mode. The dc power input is 40 mW and the ratio of V_1 over V_0 is 0.278. If 20% of power delivered by the beam is dissipated in the cavity walls, find the power delivered to the load. (V_1 = Signal voltage and V_0 = Beam voltage).

- (i) For the tube to oscillate in $n = 1 \frac{3}{4}$ mode, the required direct current, $I_0 = ?$

- (ii) For producing a microwave gap voltage $V_1 = 200$ V, required direct current, $I_0 = ?$

- (iii) Electrons efficiency, $\eta = ?$

- (i) For the tube to oscillate in $n = 1 \frac{3}{4}$ mode, the repeller voltage is obtained as,

Since, $\frac{V_0}{(V_R + V_0)^2} = \frac{1}{8} \frac{1}{\omega^2 L^2} \frac{e}{m} \left[2\pi n - \frac{\pi}{2}\right]^2$

$\Rightarrow \frac{V_0}{(V_R + V_0)^2} = \frac{0.00037}{8 \times 7.19 \times 10^{15}} = 0.00037$

$\therefore V_R + V_0 = 800$

$\therefore V_R + V_0 = 21621.62$

$\therefore V_R = 1470 - 800 = 670 \text{ V}$

Beam current, $I_0 = 60$ mA

Maximum power, $P_{max} = ?$

Repeller voltage, $V_R = ?$

Operating frequency, $f = 5$ GHz

DC beam voltage, $V_0 = 250$ V

Repeller space, $L = 0.1$ cm

Mode, $N = 1 \frac{3}{4}$

Given that,

For a reflex klystron,

Operating frequency, $f = 5$ GHz

DC beam voltage, $V_0 = 250$ V

Repeller space, $L = 0.1$ cm

Mode, $N = 1 \frac{3}{4}$

Given that,

For a reflex klystron,

Operating frequency, $f = 5$ GHz

DC beam voltage, $V_0 = 250$ V

Repeller space, $L = 0.1$ cm

Mode, $N = 1 \frac{3}{4}$

Given that,

For a reflex klystron,

Operating frequency, $f = 5$ GHz

DC beam voltage, $V_0 = 250$ V

Repeller space, $L = 0.1$ cm

Mode, $N = 1 \frac{3}{4}$

Given that,

For a reflex klystron,

Operating frequency, $f = 5$ GHz

DC beam voltage, $V_0 = 250$ V

Repeller space, $L = 0.1$ cm

Mode, $N = 1 \frac{3}{4}$

Given that,

For a reflex klystron,

Operating frequency, $f = 5$ GHz

DC beam voltage, $V_0 = 250$ V

Repeller space, $L = 0.1$ cm

Mode, $N = 1 \frac{3}{4}$

Given that,

For a reflex klystron,

Operating frequency, $f = 5$ GHz

DC beam voltage, $V_0 = 250$ V

Repeller space, $L = 0.1$ cm

Mode, $N = 1 \frac{3}{4}$

Given that,

For a reflex klystron,

Operating frequency, $f = 5$ GHz

DC beam voltage, $V_0 = 250$ V

Repeller space, $L = 0.1$ cm

Mode, $N = 1 \frac{3}{4}$

Given that,

For a reflex klystron,

Operating frequency, $f = 5$ GHz

DC beam voltage, $V_0 = 250$ V

Repeller space, $L = 0.1$ cm

Mode, $N = 1 \frac{3}{4}$

Given that,

For a reflex klystron,

Operating frequency, $f = 5$ GHz

DC beam voltage, $V_0 = 250$ V

Repeller space, $L = 0.1$ cm

Mode, $N = 1 \frac{3}{4}$

Given that,

For a reflex klystron,

Operating frequency, $f = 5$ GHz

DC beam voltage, $V_0 = 250$ V

Repeller space, $L = 0.1$ cm

Mode, $N = 1 \frac{3}{4}$

1.2 HELIX TWTs

1.2.1 Types and Characteristics of Slow-wave Structures

Q43. Discuss the significance and types of Helix TWTs.

(or)

Ans: Explain in detail about slow-wave structures.

Slow-wave Structures

The circuits that are used to decrease the wave velocity in a particular direction to meet the electron beam with input RF signal wave are known as slow-wave structures.

In microwave tubes, the frequency of resonance is maintained by reducing the inductance and capacitance while increasing the operating frequency of resonator. Furthermore, the resonator circuit is not suitable for producing the large output power and it has limited gain-bandwidth product. Thus, in order to generate large gain over a wide bandwidth, non resonant periodic or slow-wave structures are used in microwave tubes.

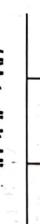
The most commonly used slow wave structures in microwave tubes are as shown in figure.



(a) Helical line



(c) Zig Zag line



(b) Folded-back line



(d) Interdigital line

(e) Corrugated waveguide.

Figure: Slowwave Structure

Slow-wave Structures are introduced into the microwave devices to change the phase velocity of a microwave signal in accordance with electron beam for effective communication. The helical line structures with a concentric conducting cylinders are frequently used in microwave tubes.

Significance

In travelling wave tube(TWT), the electrons in the tube travel with a constant velocity i.e., velocity of light. Hence, no electron accelerates faster than the travelling wave on wire. Thus, the formation of bulk cluster(bunching) in TWTs is eliminated. This drawback can be overcome by using slow wave structures. These allows the bunching process by reducing the speed of travelling waves below the electron beam speed. This setup also produces large gain over a wide band width.

Q44. What is a slow wave structure? List the different slow wave structures. Mention their relative merits and demerits.

Ans: Slow-wave Structure

For answer refer Unit-1, Q43.

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UNIT-1 (Microwave Tubes and Helix TWTs)

1. Merits and Demerits of Different Slow-wave Structures

1.1. Helical-Line

Merits

- Helix structure provides sufficient bandwidth required for broadband travelling wave tubes.
- It features good chromatic dispersion.
- The fluctuations of its output parameters in broadband range are very small.
- Helical-wave system provides wideband characteristics.

Demerits

- Suitable for low temperature experiments.
- Efficiency is less.
- Gain is reduced by the internal attenuator.
- It suffers from manufacturing problems at high frequencies.
- Sufficient amount of heat dissipation is not provided.

1.2 Folded-Back Line

Merits

- Folded-back transmission line is suitable in designing Backward Wave Oscillators (BWO)
- It supports the characteristics of helix structure.

Demerits

- Bandwidth is limited.
- Weight is more.
- Cost is more.
- Heat dissipation is good.
- The structure suffers from fabrication problems.

1.3 Zig-zag Line

Merits

- This structure forms inductive part of slow wave structure which provides synchronization with electron beam.
- It performs shaping of dispersion characteristics.
- Insertion loss is reduced.

Demerits

- Weight is more at very high frequencies.
- Cost is more.

1.4 Interdigital Line

Merits

- The dispersion is negative, due to which design of amplifier and BWO (Backward Wave Oscillator) is made easy.
- Heat dissipation is good.

Demerits

- Requires high temperature for operation.
- The structure suffers from fabrication problems.

UNIT-2 (Travelling Wave Tubes)

5. Corrugated Waveguide

Merits

- Coupling efficiency is high.
- It is suitable for high frequency applications.
- Propagation loss is very less.
- Narrow bandwidth is provided.
- Weight is more.
- Various difficulties are encountered at the time of manufacture.

Demerits

- With a neat sketch explain the structure and principle of operation of TWT amplifier.
- Refer Only Working

1.2.2 Structure of TWT and Amplification Process (Qualitative Treatment), Suppression of Oscillations, Gain Considerations

Q45. What is the significance of slow wave structure?

Ans: Explain the amplification process in TWT.

(or) Nov/Dec-21, (R13), Q7(e)

Explain how a helical TWT achieve amplification.

(or) Nov/Dec-18, (R13), Q7(e)

Explain how amplification takes place in Helix TWT?

(or) Nov/Dec-17, (R13), Q7(e)

Explain the principle of working of travelling wave tube.

(or) Nov/Dec-16, (R13), Q7(e)

Significance of Slow-wave Structure

For answer refer Unit-1, Q43. Topic: Significance.

Travelling Wave Tube

Travelling wave tube is a wide bandwidth or broadband microwave amplifier or voltage amplifier which is designed to provide high gain and low noise when used in a microwave equipment.

Construction
The construction of a helix travelling wave tube is as shown in figure (1).

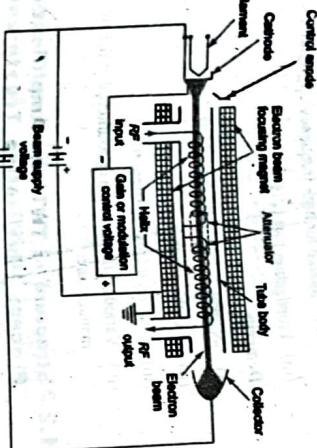


Figure 1: Travelling Wave Tube

In figure (1), the TWT consists of an electron gun, which when gets heated to generate electron beam that accelerates along the tube axis. Two magnets surrounding the tube provides magnetic field to focus the electrons into a narrow beam.

TWT is a non-resonant type microwave tube. Since, a slow wave structure(helical coil) is arranged along the axis of the tube. The input signal travels along the helical path and generates electric field at the center. TWT is designed in such a way that the speed/velocity of the travelling wave is maintained closer to speed of electron beam multiplied by the ratio of pitch of helix to helix circumference. The electron beam injected into the tube interacts with input signal wave. The bunching occurs in the tube due to the velocity modulation which further traverse the electron energy to travelling wave.

Working: When a RF signal wave is injected into the helix slow wave guide, it travels in the form of axial E-field. As the signal travels through helix, the electron bunches release energy which result in amplification.

The denser bunch of electrons amplifies the signal until the RF wave and electron beam travel down the tube length. This energy of the bunch compensates the loss in system and mismatch are attenuated by the attenuator, placed at the centre of interaction region.

The reflected waves produced due to impedance mismatch are attenuated by the attenuator, placed at the centre of interaction region.

The interaction between accelerating field, electron beam and retarding field is as shown in figure (2).

UNIT-1 (Microwave Tubes and Helix TWTs)

Q47. Establish the mathematical relation for power gain in a TWT amplifier, and explain the parameters involved.

Ans: Consider a perfectly matched structure with an attenuator is placed at the centre of the tube.

The overall voltage is the sum of individual voltages of forward travelling waves.

$$V(z) = V_1 e^{-\gamma_1 z} + V_2 e^{-\gamma_2 z} + V_3 e^{-\gamma_3 z}$$

Figure 2: Interaction between Electron Beam and Electric Field

The time taken by the signal to travel along the wire is given by,

$$T = \frac{P}{V_p} = \sqrt{\frac{p^2 + (\pi d)^2}{C}}$$

Where,

$$p = \text{Helix pitch}$$

$$d = \text{Helix diameter}$$

Since, the electrons experience more retarding field than accelerating field, the bunch formation increases with increase in field amplitude. This results in large amplification of signal voltage at helix output.

$$\Rightarrow V_p = \frac{Cp}{p^2 + (\pi d)^2} \approx \frac{Cp}{\pi d}, p \ll \pi d$$

The electrons gets accelerated when the electron field is applied against the electron flow and when applied along the electron flow, decelerates the electron. This density modulation results in electron bunch formation.

Since, the electrons experience more retarding field than accelerating field, the bunch formation increases with increase in field amplitude. This results in large amplification of signal voltage at helix output.

Q46. Explain with neat sketch, the principle of operation of a TWT amplifier and write the equations for the maximum voltage gain and efficiency.

Ans:

TWT Amplifier

For answer refer Unit-1, Q45.

Gain and Efficiency Equations

The expression for power gain (in dB) of a TWT is given by,

$$A_p = -9.54 + 47.3 NC \text{ dB}$$

Where,

$$N = \text{Length of slow wave structure (in m)}$$

$$C - \text{Gain parameter} = \left(\frac{I_0}{4V_0} \right)^{1/3}$$

$$V_0 - \text{dc beam voltage}$$

$$I_0 - \text{dc beam current}$$

$$Z_0 - \text{Characteristics impedance of the helix.}$$

The efficiency of TWT is in the range of 20% to 40%.

By simultaneously solving above equations (4), (5) and (6) for $I(0) = 0$ and $V_1(0) = 0$, the solution obtained is,

$$V_1 = V_2 = V_3 = \frac{V(0)}{3} \quad \dots (7)$$

As the wave increases exponentially (with distance) becomes equal to the voltage of the growing wave for sufficiently large value of 'z'.

For $z = I, V_1 = -\beta, C = \frac{\sqrt{3}}{2} + j\beta, \left(1 + \frac{C}{2}\right)l$

Then, the total input current is given by,

$$i(z) = -\frac{I_0}{2V_0C^2} \cdot \frac{V_1 e^{-\gamma_1 z}}{\delta_1^2} - \frac{I_0}{2V_0C^2} \cdot \frac{V_2 e^{-\gamma_2 z}}{\delta_2^2} - \frac{I_0}{2V_0C^2} \cdot \frac{V_3 e^{-\gamma_3 z}}{\delta_3^2} \quad \dots (1)$$

$$\Rightarrow i(z) = -\sum_{n=1}^3 \frac{I_0}{2V_0C^2} \frac{V_n e^{-\gamma_n z}}{\delta_n^2} \quad \dots (2)$$

Where,

$$V_{\phi}, I_{\phi} - \text{Beam voltage and current}$$

γ_1 - Forward wave whose amplitude grows exponentially with distance.

γ_2 - Forward wave whose amplitude decays exponentially with distance.

γ_3 - Forward wave whose amplitude remains constant.

$$C - \text{Gain parameter.}$$

$$C = \left[\frac{L Z_0}{4V_0} \right]^{1/3}$$

$$\delta = (-j)^{1/3}$$

since, $C \delta < 1, E_1 = \gamma V, \gamma = \beta_c (1 - C \delta)$, the total wave velocity is given by,

$$\gamma_1(z) = \frac{I_0}{2V_0C} \cdot \frac{V_1 e^{-\gamma_1 z}}{\delta_1} + \frac{I_0}{2V_0C} \cdot \frac{V_2 e^{-\gamma_2 z}}{\delta_2} + \frac{I_0}{2V_0C} \cdot \frac{V_3 e^{-\gamma_3 z}}{\delta_3}$$

$$= \sum_{n=1}^3 \frac{I_0}{2V_0C} \frac{V_n e^{-\gamma_n z}}{\delta_n} \quad \dots (3)$$

where,

$$V_0 = \sqrt{\left(\frac{2\pi}{m}\right)} V_0$$

$$\beta_c = \frac{\omega}{V_0}$$

At the input reference point i.e., $z = 0$

$$V(0) = V_1 + V_2 + V_3 \quad \dots (4)$$

$$i(0) = -\frac{I_0}{2V_0C^2} \left[\frac{V_1}{\delta_1^2} + \frac{V_2}{\delta_2^2} + \frac{V_3}{\delta_3^2} \right] \quad \dots (5)$$

Q48. Explain the significance of slow wave structure in the amplification process. List out the major differences between TWT and klystron amplifier.

(or)
Compare the performance of TWT with klystron amplifier.

Ans: Significance of Slow Wave Structure
For answer refer Unit-1, Q43. Topic: Significance.

Ans: Comparison between TWT and Klystron Amplifier

Comparison between TWT and Mentioned Klystron Amplifier

The differences between TWT and Klystron amplifiers are as mentioned in table.

Traveling Wave Tube (TWT)	Klystron Amplifier
1. In TWT, the electrons interact with a travelling wave.	1. In Klystron amplifier, the electrons interact with a standing wave.
2. The interaction is distributed along the helical axis.	2. The interaction between electrons and standing wave is localized.
3. It can amplify over a broadband of frequencies, as there are no high 'Q' resonant circuits in TWT.	3. In Klystron amplifiers, the amplification over broadband of frequencies is limited by high 'Q' resonant circuits.
4. In TWT, the RF signal that interrupts the electron velocities is from the helix.	4. In Klystron amplifiers, the RF signal that interrupts the electron velocities is from a resonant cavity.
5. These are also called as broad band devices.	5. These are also called as narrow band devices.
6. These tubes can operate in a frequency range of 0.5 GHz to 95 GHz.	6. These amplifiers can operate in a frequency range of 250 MHz to 100 GHz.
7. The efficiency of these tubes is 5 to 20%.	7. The efficiency of these amplifiers is 30 to 40%.
8. These are used as low noise RF amplifier in broadband microwave receivers.	8. These are used as power output tubes in UHF-TV transmitters and radar transmitter.

Table

Q49. How oscillations are prevented in a Travelling Wave Tube?

Ans:

As the slow wave structure of travelling wave tube is bidirectional, the signal can propagate in both the directions. When output of the coupler reflects the signal, it reflects backward along slow wave structure and serves as a feedback signal. This results oscillations in the travelling wave tube.

In travelling wave tube, oscillations are produced due to bunching. The bunching is the process in which electrons in the beam travel with higher speed than the wave travelling on the wire and interact with travelling wave fields due to velocity modulation. In order to prevent oscillations in TWT, it is necessary to slow down the speed of bunches. This can be accomplished by transferring the electron energy to the travelling wave fields with correct polarity. This increases the amplitude of travelling wave along the TWT axis. As a result, the speed of electrons decreases and they cannot travel faster than the wave travelling on wire. Thus, no bunching takes place and no oscillations are produced.

The above drawback can be overcome by using a slow wave structure, which reduces the speed of travelling wave below speed of electrons in the beam.

Q50. What are the different modes of operation of TWT and explain them.

(or) Dec.-19, (R16), Q7

What are the different oscillating modes in TWT and explain them.

(or) May/June-19, (R15), Q1(a)

Explain why there are four propagation constants in TWT and derive equations to these propagation constants.

The electronic equation of the traveling wave tube is given by,

$$i = j \frac{\beta_r I_0}{2V_0(\beta_r - \gamma^2)} E_1$$

Where,

E_1 – Convention current in the electron beam
 β_r – Phase constant of the electron beam

I_0 – D.C beam current
 γ – Propagation constant = $\alpha_r + j\beta$
 V_0 – D.C beam voltage.

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UNIT-1 (Microwave Tubes and Helix TWTs)

And the circuit equation of traveling wave tube is given by,

$$E_1 = - \frac{V_0^2 z_0}{\gamma^2 - \gamma_0^2} i \quad (2)$$

Where,

γ_0 – Propagation constant for $i = 0$

z_0 – Characteristic impedance.

The mode of travelling wave tube can be obtained by solving equations (1) and (2) simultaneously for the propagation constants. The solutions for propagation constants represents different modes of travelling wave in the tube. Basically, four different modes of travelling wave are possible in O-type travelling tube as there are four distinct solutions for propagation constants.

From equations (1) and (2),

$$(\gamma^2 - \gamma_0^2)(\beta_r - \gamma^2) = -j \frac{V_0^2 z_0 \beta_r I_0}{2V_0} \quad (3)$$

The above equation has four roots as it is a fourth order equation in γ . By using the approximation,

$$\gamma_0 = j\beta_r \quad (4)$$

Equation (3) reduces to,

$$(\gamma^2 - (\beta_r)^2)(\beta_r - \gamma^2) = -j \frac{V_0^2 z_0 \beta_r I_0}{2V_0} \quad (5)$$

$$(\gamma + j\beta_r)(\gamma - j\beta_r)^3 = 2C^3 \beta_r^2 \gamma^2$$

Where, C – Gain parameter of traveling wave tube

$$C = \left[\frac{I_0 z_0}{4V_0} \right]^{1/3} \quad (6)$$

The equation (5) represents that, there is one backward traveling wave corresponding to $e^{j\beta_r z}$ and three forward traveling waves corresponding to $e^{-j\beta_r z}$. Assume that the propagation constant of forward traveling waves as,

$$\theta = \sqrt{\gamma^2 - (\beta_r)^2} \quad (7)$$

Substituting the value of γ in equation (5), we have,

$$(\beta_r - \beta_r C\theta, -j\beta_r)^3 (\beta_r - \beta_r C\theta + j\beta_r)^2 = 2C^3 \beta_r^2 (\beta_r - \beta_r C\theta)^2$$

$$(-\beta_r C\theta)^3 (2j\beta_r - \beta_r C\theta) = 2C^3 \beta_r^2 [-\beta_r^2 - (\beta_r C\theta)^2 - 2j\beta_r^2 C\theta]$$

Since $C\theta \ll 1$, neglecting all $C\theta$ and higher order $C\theta$ terms we have,

$$(-\beta_r C\theta)^3 (2j\beta_r) = 2C^3 \beta_r^2 (-\beta_r^2) \Rightarrow \delta = (-j)^{1/3}$$

The above equation can also be written as,

$$\delta = (-j)^{1/3} = e^{-j[\frac{\pi}{2} + 2m\pi/3]} \quad (\because n = 0, 1, 2) \quad (9)$$

At $n = 0$, the first root δ_1 is,

$$\delta_1 = e^{-j\frac{\pi}{6}} = \frac{\sqrt{3} - j}{2} \quad (10)$$

UNIT-7 (Microwave Tubes and Helix TWTs)

At $n = 1$, the second root δ_2 is,

$$\delta_2 = e^{-\frac{J\pi}{6}} = -\frac{\sqrt{3}-J}{2}$$

At $n = 2$, the third root δ_3 is,

$$\delta_3 = e^{-\frac{J\pi}{6}} = J$$

Similarly, assuming the propagation constant for backward travelling wave as,

$$\gamma = -J\beta, -\beta, C\delta_4$$

Then the fourth root, δ_4 is obtained by substituting equation (13) in equation (5),

$$\Rightarrow \delta_4 = -J\beta^2$$

Thus, the four propagation constant values are given by,

$$\gamma_1 = -\beta, C\frac{\sqrt{3}}{2} + J\beta, \left(1 + \frac{C}{2}\right)$$

$$\gamma_2 = \beta, C\frac{\sqrt{3}}{2} + J\beta, \left(1 + \frac{C}{2}\right)$$

$$\gamma_3 = J\beta, (1 - C)$$

$$\gamma_4 = -J\beta, \left(1 - \frac{C}{2}\right)$$

The above four equations of propagation constant represents the four different modes of travelling wave. The wave corresponding to γ_1 is a forward wave and its amplitude grows exponentially with distance. This wave propagates with phase velocity lower than electron beam velocity and the energy flows from electron beam to the wave.

The wave corresponding to γ_2 is a forward wave and its amplitude decays exponentially with distance. This wave propagates with a phase velocity lower than electron beam velocity and the energy flows from wave to the electron beam.

The wave corresponding to γ_3 is a forward wave and its amplitude remains constant. This wave propagates with a phase velocity higher than the electron beam velocity and there is no net exchange of energy.

The wave corresponding to γ_4 is a backward wave and there is no change in amplitude. This wave propagates with a phase velocity higher than the electron beam velocity and there is no net exchange of energy.

Q51. A TWT operates with following parameters, $V_b = 2.5$ kV, $I_b = 25$ mA, $Z_0 = 10$ Ω , circuit length $L = 50$, $f = 9$ GHz. Find the gain parameter and power gain.

Ans:

Given that,

For a TWT,

$$V_b = 2.5 \text{ kV}$$

$$I_b = 25 \text{ mA}$$

$$Z_0 = 10 \Omega$$

$$L = 50$$

$$f = 9 \text{ GHz}$$

Gain parameter, $C = ?$

Power gain, $A_p = ?$

$$\Rightarrow V_0 = \frac{m}{2e} \left(\frac{P_e}{nd} \right)^2$$

$$C = \left[\frac{I_b Z_0}{4 V_b} \right]^{1/3}$$

$$\Rightarrow C = \left[\frac{25 \times 10^{-3} \times 10^{-13}}{4 \times 2.5 \times 10^3} \right]^{1/3}$$

$$= 2.92 \times 10^{-2}$$

$$C = \left[\frac{25 \times 10^{-3} \times 10^{-13}}{4 \times 2.92 \times 10^{-2}} \right]^{1/3}$$

$$= 2.92 \times 10^{-2}$$

$$\text{The expression for power gain of TWT is given by,}$$

$$A_p = -9.54 + 47.3 \times 10^{-2}$$

$$= -9.54 + 47.3 \times 50 \times 2.92 \times 10^{-2}$$

$$= 59.52$$

$$\therefore A_p = 59.52 \text{ dB}$$

Q52. A helical TWT has diameter of 3 mm with 40 turns per cm. Calculate axial phase velocity and the anode voltage at which the TWT can be operated for useful gain.

Ans:

Given that,

For a helical TWT,

$$\text{Diameter, } d = 3 \text{ mm}$$

$$\text{Number of turns, } N = 40 \text{ turns/cm}$$

$$\text{Axial phase velocity, } (V_p) = ?$$

$$\text{(i) Axial phase velocity, } (V_p) = ?$$

$$\text{(ii) Anode voltage, } (V_a) = ?$$

$$\text{(iii) All Four propagation constants.}$$

(Model Paper, Q3(b) | Nov/Dec-18, R13, Q6(b))
(or)

A TWT operates under following parameters
beam voltage $V_b = 3$ kV, beam current $I_b = 20$ mA, characteristic impedance of helix $Z_0 = 10$, circuit length $N = 50$ and frequency $f = 10$ GHz. Determine,

(i) Gain parameter
(ii) Output power gain in dB. Nov-15, (R09, Q6a)
(Refer Only (i) Gain parameter and (ii) Output power gain)

Given that,
For a TWT,
 $V_b = 3 \text{ kV}$
Beam voltage, $V_b = 3$ kV
Beam current, $I_b = 20$ mA
Characteristic impedance, $Z_0 = 10$ Ω
Circuit length, $N = 50$
Frequency, $f = 10$ GHz

- (i) Gain parameter, $C = ?$
(ii) Output power gain, A_p (dB) = ?
(iii) Propagation constant $\gamma_1 = ?$, $\gamma_2 = ?$, $\gamma_3 = ?$, $\gamma_4 = ?$

The expression for gain parameter of a helix TWT is given by,

$$C = \left[\frac{4Z_0}{4\pi} \right]^{1/2} = \left[\frac{20 \times 10^{-3} \times 10}{4 \times 3 \times 10^3} \right]^{1/2}$$

$$= 0.0255$$

$$\therefore C = 2.55 \times 10^{-2}$$

- (ii) The output power gain of helix TWT is given by,

$$A_p = -9.54 + 47.3 NC$$

$$= -9.54 + 47.3 \times 50 \times 2.55 \times 10^{-2}$$

$$\therefore A_p = 50.77 \text{ dB}$$

- (iii) The four propagation constants γ_1 , γ_2 , γ_3 and γ_4 are given by,

$$\gamma_1 = -\beta C \sqrt{\frac{1}{2}} + j\beta (1 + C/2)$$

$$\gamma_2 = -\beta C \sqrt{\frac{1}{2}} - j\beta (1 + C/2)$$

$$\gamma_3 = -\beta C \sqrt{\frac{1}{2}} + j\beta (1 + C/2)$$

$$\gamma_4 = -\beta C \sqrt{\frac{1}{2}} - j\beta (1 + C/2)$$

- Given that, $\beta = 1.93 \times 10^3 \text{ rad/m}$

- Where, $\beta = \frac{\alpha}{V_0}$ and $\alpha = 2 \text{ Np/m}$

$$\beta = \frac{\alpha}{V_0}$$

$$= \frac{2 \times 10^6}{0.592 \times 10^6 / (3 \times 10^3)}$$

$$\beta = 1.93 \times 10^3 \text{ rad/m}$$

$$\therefore \gamma_1 = -1.93 \times 10^3 \times 2.55 \times 10^{-2} \times 0.87 + j1.93 \times 10^3 \left[1 + \frac{2.55 \times 10^{-2}}{2} \right]$$

$$\therefore \gamma_1 = -42.82 + j1934.61$$

$$\therefore \gamma_1 = -42.82 + j1934.61$$

$$\gamma_2 = \beta, C \sqrt{\frac{1}{2}} + j\beta (1 + C/2)$$

$$\gamma_3 = \beta, C \sqrt{\frac{1}{2}} - j\beta (1 + C/2)$$

$$\gamma_4 = \beta, C \sqrt{\frac{1}{2}} + j\beta (1 + C/2)$$

$$= 1.93 \times 10^3 \times 2.55 \times 10^{-2} \times 0.87 + j1.93 \times 10^3 \left(1 + \frac{2.55 \times 10^{-2}}{2} \right)$$

$$= 1.93 \times 10^3 (1 - 2.55 \times 10^{-2})$$

$$\therefore \gamma_3 = j1880.78$$

$$\gamma_4 = -j\beta, (1 - C^2/4)$$

$$= -j1.93 \times 10^3 \left[1 + \frac{2.55 \times 10^{-2}}{4} \right]$$

$$\therefore \gamma_4 = -j1930$$

Ans: Given that,

For a O-type travelling wave tube,

Operating frequency, $f = 2 \text{ GHz}$

Pitch angle of the slow wave structure, $\psi = 4.4^\circ$

Attenuation constant, $\alpha = 2 \text{ Np/m}$

Propagation constant, $\gamma = ?$

The phase velocity along pitch of the TWT is given by,

$$\nu_p = C \sin \psi$$

$$= 3 \times 10^8 \times \sin(4.4^\circ)$$

$$= 23.016 \times 10^6 \text{ m/sec}$$

The phase constant, β is given by,

$$\beta = \frac{\alpha}{\nu_p}$$

$$= \frac{2\pi f}{23.016 \times 10^6}$$

$$= 545.984 \text{ rad/m}$$

Then, the propagation constant of the travelling wave tube is given by,

$$\gamma = \alpha + j\beta$$

$$= 2 + j545.984$$

$$= 545.988 \angle 89.79^\circ \text{ m}^{-1}$$

$$\therefore \gamma = 545.988 \angle 89.79^\circ \text{ m}^{-1}$$

Frequently Asked & Important Questions

Q1. What are the limitations of conventional tubes at microwave frequencies?

Ans: Refer Q1. (Dec.-19, (R16), Q1(e) | Nov./Dec.-16, (R13), Q1(e)) **REPEATED 2 TIMES**

Q2. How microwave tubes are classified?

Ans: Refer Q3. (May/June-19, (R15), Q1(f) | Nov./Dec.-17, (R13), Q1(e)) **REPEATED 2 TIMES**

Q3. In detail explain the limitations of conventional tubes at microwave frequencies.

Ans: Refer Q17. (March-21, (R16), Q4(e) | April/May-18, (R13), Q6(b) | May/June-13, (R09, Q6(b)) | Nov./Dec.-12, (R09), Q6(e)) **REPEATED 4 TIMES**

Q4. Explain the working principle of two cavity Klystron with the help of applegate diagram. Also write the expression for velocity modulation and voltage gain.

Ans: Refer Q22. (March-21, (R16), Q4(b) | May/June-13, (R09, Q6(b)) | Nov.-13, (R09), Q5(e)) **REPEATED 3 TIMES**

Q5. Compose and explain about two cavity Klystron amplifier and derive its Bunching process.

Ans: Refer Q24. (Oct/Nov.-20, (R16), Q5(e) | April/May-18, (R13), Q6(a) | Nov./Dec.-16, (R13), Q6 | Nov./Dec.-12, (R09), Q5(b)) **REPEATED 4 TIMES**

Q6. Explain briefly about the construction and operation of reflex klystron oscillator.

Ans: Refer Q32. (Nov.-15, (R16), Q5(b) | May/June-13, (R09, Q5(e)) | Nov.-15, (R16), Q5(b)) **REPEATED 2 TIMES**

Q7. How the oscillations are generated in reflex klystron and explain bunching process with apple gate diagram and also derive the equation for efficiency.

Ans: Refer Q31. (Dec.-19, (R16), Q5(f) | March-21, (R16), Q5(a)) **REPEATED 2 TIMES**

Q8. What is the significance of slow wave structure? Explain the amplification process in TWT.

Ans: Refer Q45. (March-21, (R16), Q5(b) | Nov./Dec.-18, (R13), Q7(a) | Nov./Dec.-17, (R13), Q7(b)) **REPEATED 5 TIMES**

Q9. Explain the significance of slow wave structure in the amplification process. List out the major differences between TWT and klystron.

Ans: Refer Q48. (Nov./Dec.-17, (R13), Q7(e) | May/June-19, (R15), Q7(b)) **REPEATED 2 TIMES**

Q10. What are the different modes of operation of TWT and explain them.

Ans: Refer Q50. (Dec.-19, (R16), Q7 | May/June-19, (R15), Q7(b) | Nov.-13, (R09), Q6(a)) **REPEATED 3 TIMES**

Q11. A TWT operates under following parameters,

Beam voltage $V_0 = 3$ kV, beam current $I_0 = 20$ mA, characteristic impedance of helix $Z_0 = 10 \Omega$, circuit length, $N = 50$ and frequency $f = 10$ GHz. Determine,

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