

Digital Signal Processing

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Abstract—This manual provides a simple introduction to digital signal processing.

1 SOFTWARE INSTALLATION

Run the following commands

```
sudo apt-get update
sudo apt-get install libffi-dev libsndfile1 python3
  -scipy python3-numpy python3-matplotlib
sudo pip install cffi pysoundfile
```

2 DIGITAL FILTER

2.1 Download the sound file from

```
wget https://raw.githubusercontent.com/
gadepall/
EE1310/master/filter/codes/Sound_Noise.wav
```

2.2 You will find a spectrogram at <https://academo.org/demos/spectrum-analyzer>. Upload the sound file that you downloaded in Problem 2.1 in the spectrogram and play. Observe the spectrogram. What do you find?
Solution: There are a lot of yellow lines between 440 Hz to 5.1 KHz. These represent the synthesizer key tones. Also, the key strokes

are audible along with background noise.

2.3 Write the python code for removal of out of band noise and execute the code.

Solution:

```
import soundfile as sf
from scipy import signal

#read.wav file
input_signal,fs = sf.read('Sound_Noise.wav'
    )

#sampling frequency of input signal
sampl_freq = fs

#order of the frequency
order = 4

#cutoff frequency 4khz
cutoff_freq = 4000.0

#digital frequency
Wn = 2*cutoff_freq/sampl_freq

# b and a are numerators and denominator
  polynomials respectively
b,a = signal.butter(order,Wn,'low')

#filter the input signal with butterworth filter
output_signal = signal.filtfilt(b,a,input_signal
    )

#output_signal = signal.lfilter(b,a,
    input_signal)

#write the output signal into .wav file
sf.write('Sound_With_ReducedNoise.wav',
    output_signal,fs)
```

2.4 The output of the python script in Problem 2.3 is the audio file Sound_With_ReducedNoise.wav. Play the file in the spectrogram in Problem 2.2.

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What do you observe?

Solution: The key strokes as well as background noise is subdued in the audio. Also, the signal is blank for frequencies above 5.1 kHz.

3 DIFFERENCE EQUATION

3.1 Let

$$x(n) = \left\{ \underset{\uparrow}{1}, 2, 3, 4, 2, 1 \right\} \quad (3.1)$$

Sketch $x(n)$.

3.2 Let

$$y(n) + \frac{1}{2}y(n-1) = x(n) + x(n-2),$$

$$y(n) = 0, n < 0 \quad (3.2)$$

Sketch $y(n)$.

Solution: The following code yields Fig. 3.2.

```
wget https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/3-2.py
```

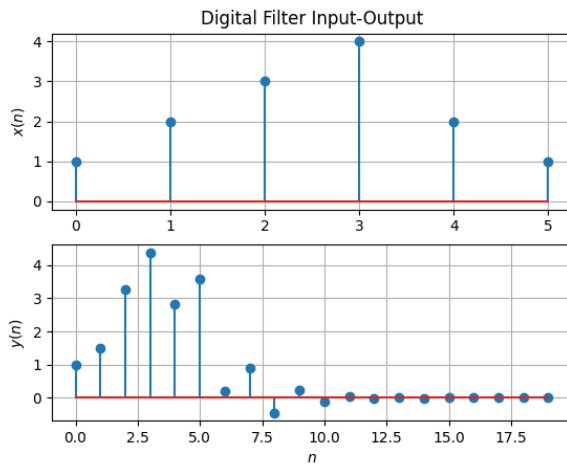


Fig. 3.2

3.3 Repeat the above exercise using a c code.

Solution: The following code yields x data and y data

```
wget https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/3-3.c
```

4 Z-TRANSFORM

4.1 The Z-transform of $x(n)$ is defined as

$$X(z) = \mathcal{Z}\{x(n)\} = \sum_{n=-\infty}^{\infty} x(n)z^{-n} \quad (4.1)$$

Show that

$$\mathcal{Z}\{x(n-1)\} = z^{-1}X(z) \quad (4.2)$$

and find

$$\mathcal{Z}\{x(n-k)\} \quad (4.3)$$

Solution: From (4.1),

$$\mathcal{Z}\{x(n-k)\} = \sum_{n=-\infty}^{\infty} x(n-k)z^{-n} \quad (4.4)$$

$$= \sum_{n=-\infty}^{\infty} x(n)z^{-(n+k)} = z^{-k} \sum_{n=-\infty}^{\infty} x(n)z^{-n} \quad (4.5)$$

resulting in (4.2). Similarly, it can be shown that

$$\mathcal{Z}\{x(n-k)\} = z^{-k}X(z) \quad (4.6)$$

4.2 Obtain $X(z)$ for $x(n)$ defined in problem 3.1

Solution:

$$X(z) = \mathcal{Z}\{x(n)\} = \sum_{n=-\infty}^{\infty} x(n)z^{-n}$$

$$X(z) = \dots 0 + x(0)z^0 + x(1)z^{-1} + x(2)z^{-2} + x(3)z^{-3} + x(4)z^{-4} + \dots$$

$$= 1 + 2z^{-1} + 3z^{-2} + 4z^{-3} + 2z^{-4} + 1z^{-5}$$

4.3 Find

$$H(z) = \frac{Y(z)}{X(z)} \quad (4.7)$$

from (3.2) assuming that the Z-transform is a linear operation.

Solution: Applying (4.6) in (3.2),

$$Y(z) + \frac{1}{2}z^{-1}Y(z) = X(z) + z^{-2}X(z) \quad (4.8)$$

$$\Rightarrow \frac{Y(z)}{X(z)} = \frac{1 + z^{-2}}{1 + \frac{1}{2}z^{-1}} \quad (4.9)$$

4.4 Find the Z transform of

$$\delta(n) = \begin{cases} 1 & n = 0 \\ 0 & \text{otherwise} \end{cases} \quad (4.10)$$

and show that the Z-transform of

$$u(n) = \begin{cases} 1 & n \geq 0 \\ 0 & \text{otherwise} \end{cases} \quad (4.11)$$

is

$$U(z) = \frac{1}{1 - z^{-1}}, \quad |z| > 1 \quad (4.12)$$

Solution: It is easy to show that

$$\delta(n) \stackrel{z}{\rightleftharpoons} 1 \quad (4.13)$$

and from (4.11),

$$U(z) = \sum_{n=0}^{\infty} z^{-n} \quad (4.14)$$

$$= \frac{1}{1 - z^{-1}}, \quad |z| > 1 \quad (4.15)$$

using the formula for the sum of an infinite geometric progression.

4.5 Show that

$$a^n u(n) \stackrel{z}{\rightleftharpoons} \frac{1}{1 - az^{-1}} \quad |z| > |a| \quad (4.16)$$

Solution: $X(z) = \sum_{n=-\infty}^{\infty} x(n)z^{-n}$

$$\begin{aligned} X(z) &= \sum_{n=-\infty}^{-1} 0 + \sum_{n=0}^{\infty} a^n(1)z^{-n} \\ &= \sum_{n=0}^{\infty} (az^{-1})^n \\ &= \frac{1}{1 - az^{-1}} \end{aligned}$$

Also the series is convergent for $|z| > |a|$

4.6 Let

$$H(e^{j\omega}) = H(z = e^{j\omega}). \quad (4.17)$$

Plot $|H(e^{j\omega})|$. Comment. $H(e^{j\omega})$ is known as the *Discrete Time Fourier Transform* (DTFT) of $x(n)$.

Solution: The following code plots Fig. 4.6.

```
wget https://github.com/NarehBanderu13/EE3900-A1/blob/main/codes/4-6.py
```

run the command

```
python3 4-6.py
```

$$H(e^{j\omega}) = \frac{1 + e^{-2j\omega}}{1 + \frac{1}{2}e^{-j\omega}} \quad (4.18)$$

$$\Rightarrow |H(e^{j\omega})| = \frac{|1 + \cos 2\omega - j \sin 2\omega|}{|1 + \frac{1}{2} \cos \omega - \frac{1}{2} j \sin \omega|} \quad (4.19)$$

$$= \sqrt{\frac{(1 + \cos 2\omega)^2 + (\sin 2\omega)^2}{(1 + \frac{1}{2} \cos \omega)^2 + (\frac{1}{2} \sin \omega)^2}} \quad (4.20)$$

$$= \sqrt{\frac{2 + 2 \cos 2\omega}{\frac{5}{4} + \cos \omega}} \quad (4.21)$$

$$= \sqrt{\frac{2(2 \cos^2 \omega)4}{5 + 4 \cos \omega}} \quad (4.22)$$

$$= \frac{4 |\cos \omega|}{\sqrt{5 + 4 \cos \omega}} \quad (4.23)$$

The period of the numerator is π and the de-

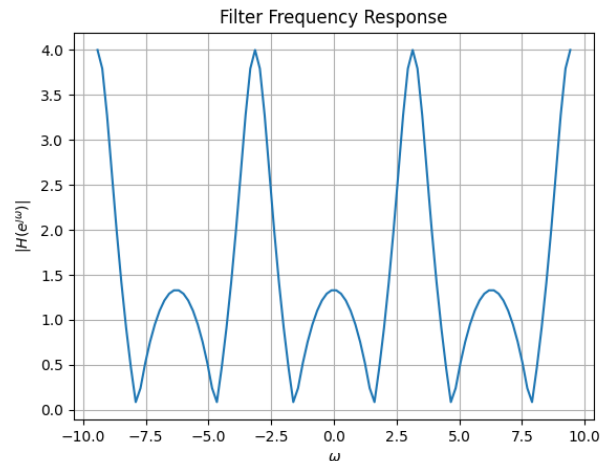


Fig. 4.6: $|H(e^{j\omega})|$

nominator is 2π taking the L.C.M of numerator and the denominator we get period as 2π

4.7 Express $h(n)$ in terms of $H(e^{2j\omega})$.

Solution:

$$\int_{-\pi}^{\pi} H(e^{j\omega}) e^{j\omega n} d\omega \quad (4.24)$$

$$= \int_{-\pi}^{\pi} \sum_{k=-\infty}^{\infty} h(k) e^{-j\omega k} e^{j\omega n} d\omega \quad (4.25)$$

$$= \sum_{k=-\infty}^{\infty} h(k) \int_{-\pi}^{\pi} e^{j\omega(n-k)} d\omega \quad (4.26)$$

Now,

$$\int_{-\pi}^{\pi} e^{j\omega(n-k)} d\omega = \begin{cases} \int_{-\pi}^{\pi} d\omega & n-k=0 \\ \frac{\exp(j\omega(n-k))}{j(n-k)} \Big|_{-\pi}^{\pi} & n-k \neq 0 \end{cases} \quad (4.27)$$

$$= \begin{cases} 2\pi & n-k=0 \\ 0 & n-k \neq 0 \end{cases} \quad (4.28)$$

$$= 2\pi\delta(n-k) \quad (4.29)$$

Thus,

$$\int_{-\pi}^{\pi} H(e^{j\omega}) e^{j\omega n} \omega = 2\pi \sum_{k=-\infty}^{\infty} h(k) \delta(n-k) \quad (4.30)$$

$$= 2\pi h(n) * \delta(n) \quad (4.31)$$

$$= 2\pi h(n) \quad (4.32)$$

Therefore, $h(n)$ is given by the inverse DTFT (IDTFT) of $H(e^{j\omega})$

$$h(n) = \frac{1}{2\pi} \int_{-\pi}^{\pi} H(e^{j\omega}) e^{j\omega n} \omega \quad (4.33)$$

5 IMPULSE RESPONSE

5.1 Using long division, find

$$h(n), \quad n < 5 \quad (5.1)$$

for $H(z)$ in (4.9).

Solution: From (4.9), we can write

$$H(z) = \frac{1 + z^{-2}}{1 + \frac{z^{-1}}{2}} \quad (5.2)$$

$$\begin{array}{r} 1 + z^{-1}/2 \overline{) \begin{array}{r} 2z^{-1} \quad -4 \\ 1 \quad +z^{-2} \\ \hline 2z^{-1} \quad +z^{-2} \\ \hline 1 \quad -2z^{-1} \\ -4 \quad -2z^{-1} \\ \hline 5 \end{array}} \end{array}$$

So we can replace (4.9) as,

$$\frac{1 + z^{-2}}{1 + \frac{z^{-1}}{2}} = 2z^{-1} - 4 + \frac{5}{1 + z^{-1}/2} \quad (5.3)$$

Now we can expand the second term of above expression as an infinite geometric series,

$$\frac{5}{1 + z^{-1}/2} = 5 \left(1 + \left(\frac{-1}{2z} \right) + \left(\frac{-1}{2z} \right)^2 + \dots \right) \quad (5.4)$$

where we assume $\left| \frac{1}{2z} \right| < 1$. So (5.3) will become,

$$= 2z^{-1} - 4 + 5 + \frac{-5}{2}z^{-1} + \frac{5}{4}z^{-2} + \frac{-5}{8}z^{-3} + \frac{5}{16}z^{-4} + \dots \quad (5.5)$$

$$= 1z^0 + \frac{-1}{2}z^{-1} + \frac{5}{4}z^{-2} + \frac{-5}{8}z^{-3} + \frac{5}{16}z^{-4} + \dots \quad (5.6)$$

Now to get $h(n)$ for $n < 5$ we will compare (5.6) with the below equation,

$$H(z) = \sum_{n=-\infty}^{n=\infty} h(n)z^{-n} \quad (5.7)$$

$h(n)$ will be the coefficient of z^{-n} .

Using this, from (5.6) we can write,

$$h(0) = 1 \quad (5.8)$$

$$h(1) = \frac{-1}{2} \quad (5.9)$$

$$h(2) = \frac{5}{4} \quad (5.10)$$

$$h(3) = \frac{-5}{8} \quad (5.11)$$

$$h(4) = \frac{5}{16} \quad (5.12)$$

And for $n < 0$ $h(n) = 0$.

For $n > 5$, we can get $h(n)$ from the geometric series,

$$h(n) = 5 \left(\frac{-1}{2} \right)^n \quad (5.13)$$

5.2 Find an expression for $h(n)$ using $H(z)$, given that

$$h(n) \stackrel{Z}{\rightleftharpoons} H(z) \quad (5.14)$$

and there is a one to one relationship between $h(n)$ and $H(z)$. $h(n)$ is known as the *impulse response* of the system defined by (3.2).

Solution: The $H(z)$ can be written as,

$$H(z) = \frac{1}{1 + \frac{z^{-1}}{2}} + \frac{z^{-2}}{1 + \frac{z^{-1}}{2}} \quad (5.15)$$

From (4.16) we can write it as,

$$h(n) = \left(\frac{-1}{2} \right)^n u(n) + \left(\frac{-1}{2} \right)^{n-2} u(n-2) \quad (5.16)$$

5.3 Sketch $h(n)$. Is it bounded? Justify Theoretically.

Solution: Download the code for the plot 5.3 from the below link,

```
wget https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/5-3.py
```

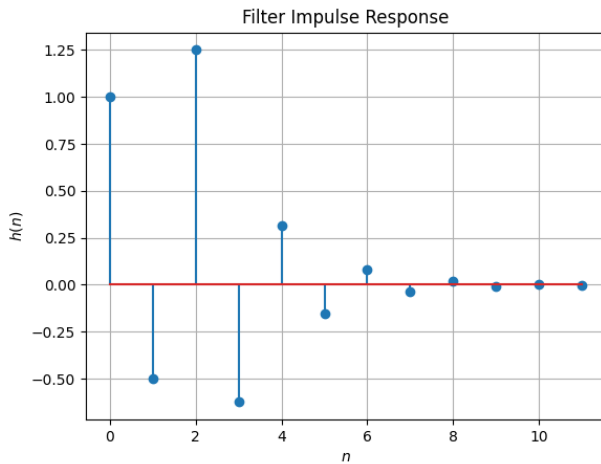


Fig. 5.3: $h(n)$ as inverse of $H(n)$

From the plot it seems like $h(n)$ is bounded and becomes smaller in magnitude as n increases. Using (5.16), we can get theoretical expression as,

$$h(n) = \begin{cases} 0 & , n < 0 \\ \left(\frac{-1}{2}\right)^n & , 0 \leq n < 2 \\ 5\left(\frac{-1}{2}\right)^n & , n \geq 2 \end{cases} \quad (5.17)$$

A sequence $\{x_n\}$ is said to be bounded if and only if there exist a positive real number M such that,

$$|x_n| \leq M, \forall n \in \mathcal{N} \quad (5.18)$$

So to say $h(n)$ is bounded we should be able to find the M which satisfies (5.18).

For $n < 0$,

$$|h(n)| \leq 0 \quad (5.19)$$

For $0 \leq n < 2$,

$$|h(n)| = \left|\frac{-1}{2}\right|^n \quad (5.20)$$

$$= \left(\frac{1}{2}\right)^n \leq 1 \quad (5.21)$$

And for $n \geq 2$,

$$|h(n)| = \left|5\left(\frac{-1}{2}\right)^n\right| \quad (5.22)$$

$$= \left(\frac{5}{2}\right)^n \leq \frac{5}{4} \quad (5.23)$$

From above three cases, we can get M as,

$$M = \max\left\{0, 1, \frac{5}{4}\right\} \quad (5.24)$$

$$= \frac{5}{4} \quad (5.25)$$

Therefore, $h(n)$ is bounded using (5.18) with $M = \frac{5}{4}$ i.e.,

$$|h(n)| \leq \frac{5}{4} \forall n \in \mathcal{N} \quad (5.26)$$

5.4 Convergent? Justify using the ratio test.

Solution: We can say a given real sequence $\{x_n\}$ is convergent if

$$\lim_{n \rightarrow \infty} \left| \frac{x_{n+1}}{x_n} \right| < 1 \quad (5.27)$$

This is known as Ratio test.

In this case the limit will become,

$$\lim_{n \rightarrow \infty} \left| \frac{h(n+1)}{h(n)} \right| = \lim_{n \rightarrow \infty} \left| \frac{5\left(\frac{-1}{2}\right)^{n+1}}{5\left(\frac{-1}{2}\right)^n} \right| \quad (5.28)$$

$$= \lim_{n \rightarrow \infty} \left| \frac{-1}{2} \right| \quad (5.29)$$

$$= \frac{1}{2} \quad (5.30)$$

As $\frac{1}{2} < 1$, from root test we can say that $h(n)$ is convergent.

5.5 The system with $h(n)$ is defined to be stable if

$$\sum_{n=-\infty}^{\infty} h(n) < \infty \quad (5.31)$$

Is the system defined by (3.2) stable for the impulse response in (5.14)?

Solution: From (5.16),

$$\sum_{n=-\infty}^{\infty} h(n) = \sum_{n=-\infty}^{\infty} \left(\left(\frac{-1}{2} \right)^n u(n) + \left(\frac{-1}{2} \right)^{n-2} u(n-2) \right) \quad (5.32)$$

$$= 2 \left(\frac{1}{1 + \frac{1}{2}} \right) \quad (5.33)$$

$$= \frac{4}{3} \quad (5.34)$$

\therefore the system is stable.

5.6 Verify the above result using a python code.

Solution: Download the python code from the below link

wget <https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/5-6.py>

Then run the following command,

python3 5-6.py

5.7 Compute and sketch $h(n)$ using

$$h(n) + \frac{1}{2}h(n-1) = \delta(n) + \delta(n-2), \quad (5.35)$$

This is the definition of $h(n)$.

Solution: Download the code for the plot 5.7 from the below link,

wget <https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/5-7.py>

Note that this is same as 5.3.

For $n < 0$, $h(n) = 0$ and,

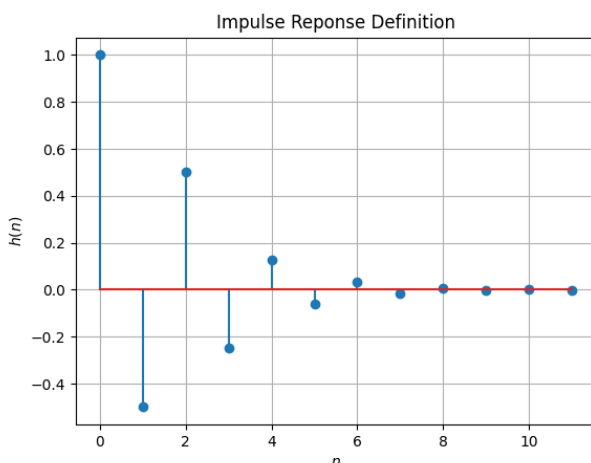


Fig. 5.7: From the definition of $h(n)$

$$h(0) = \delta(0) \quad (5.36)$$

$$= 1 \quad (5.37)$$

For $n = 1$,

$$h(1) + \frac{1}{2}h(0) = \delta(1) + \delta(-1) \quad (5.38)$$

$$\Rightarrow h(1) = -\frac{1}{2}h(0) \quad (5.39)$$

$$= -\frac{1}{2} \quad (5.40)$$

$n = 2$,

$$h(2) + \frac{1}{2}h(1) = 0 + \delta(0) \quad (5.41)$$

$$h(2) = 1 + \frac{1}{4} \quad (5.42)$$

$$= \frac{5}{4} \quad (5.43)$$

And for $n > 2$ RHS will be 0 so,

$$h(n) = -\frac{1}{2}h(n-1) \quad (5.44)$$

Overall

$$h(n) = \begin{cases} 0 & , n < 0 \\ 1 & , n = 0 \\ -\frac{1}{2} & , n = 1 \\ \frac{5}{4} & , n = 2 \\ -\frac{1}{2}h(n-1) & , n > 2 \end{cases} \quad (5.45)$$

5.8 Compute

$$y(n) = x(n) * h(n) = \sum_{k=-\infty}^{\infty} x(k)h(n-k) \quad (5.46)$$

Comment. The operation in (5.46) is known as *convolution*.

Solution: Download the code for plot 5.8 from the below link

wget <https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/5-8.py>

5.9 Express the above convolution using a Toeplitz matrix.

Solution: Download the python code from the below link for the plot 5.9,

wget <https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/5-9.py>

Then run the following command,

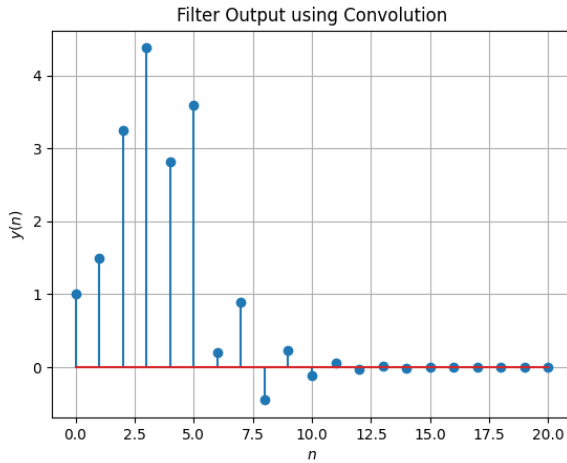


Fig. 5.8: $y(n)$ using the convolution definition

```
python3 5-9.py
```

From (5.46), we express $y(n)$ as

$$y(n) = \sum_{k=-\infty}^{\infty} x(k) h(n-k) \quad (5.47)$$

To understand how we can use a Toeplitz matrix, we will see what we are doing in (5.46)

$$y(0) = x(0) h(0) \quad (5.48)$$

$$y(1) = x(0) h(1) + x(1) h(0) \quad (5.49)$$

$$y(2) = x(0) h(2) + x(1) h(1) + x(2) h(0) \quad (5.50)$$

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The same thing can be written as,

$$y(0) = \begin{pmatrix} h(0) & 0 & 0 & \dots & \dots & 0 \end{pmatrix} \begin{pmatrix} x(0) \\ x(1) \\ x(2) \\ \vdots \\ \vdots \\ x(5) \end{pmatrix} \quad (5.51)$$

$$y(1) = \begin{pmatrix} h(1) & h(0) & 0 & 0 & \dots & \dots & 0 \end{pmatrix} \begin{pmatrix} x(0) \\ x(1) \\ x(2) \\ \vdots \\ \vdots \\ x(5) \end{pmatrix} \quad (5.52)$$

$$y(2) = \begin{pmatrix} h(2) & h(1) & h(0) & 0 & \dots & \dots & 0 \end{pmatrix} \begin{pmatrix} x(0) \\ x(1) \\ x(2) \\ \vdots \\ \vdots \\ x(5) \end{pmatrix} \quad (5.53)$$

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Using Toeplitz matrix of $h(n)$ we can simplify it as,

$$y(n) = \begin{pmatrix} h(0) & 0 & 0 & \dots & \dots & 0 \\ h(1) & h(0) & 0 & \dots & \dots & 0 \\ h(2) & h(1) & h(0) & \dots & \dots & 0 \\ \vdots & \vdots & \vdots & \ddots & \ddots & \vdots \\ 0 & 0 & 0 & \dots & \dots & h(m-1) \end{pmatrix} \begin{pmatrix} x(0) \\ x(1) \\ x(2) \\ \vdots \\ \vdots \\ x(5) \end{pmatrix} \quad (5.54)$$

Now from (??) we will take n

$$x(n) = \begin{pmatrix} 1 \\ 2 \\ 3 \\ 4 \\ 2 \\ 1 \end{pmatrix} \quad (5.55)$$

And from (5.17)

$$h(n) = \begin{pmatrix} 1 \\ -0.5 \\ 1.25 \\ \vdots \\ \vdots \end{pmatrix} \quad (5.56)$$

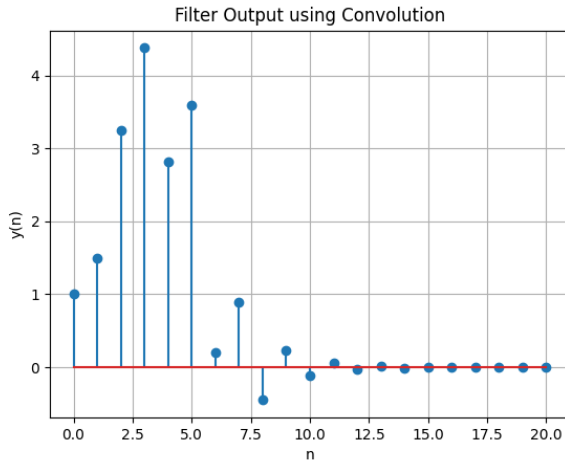


Fig. 5.9: Convolution of $x(n)$ and $h(n)$ using toeplitz matrix

will get

$$y(n) = \sum_{k=-\infty}^{\infty} x(k)h(n-k) \quad (5.61)$$

$$= \sum_{n-k=-\infty}^{\infty} x(n-k)h(k) \quad (5.62)$$

$$= \sum_{k=-\infty}^{\infty} x(n-k)h(k) \quad (5.63)$$

$$(5.64)$$

6 DFT

6.1 Compute

$$X(k) \triangleq \sum_{n=0}^{N-1} x(n)e^{-j2\pi kn/N}, \quad k = 0, 1, \dots, N-1 \quad (6.1)$$

and $H(k)$ using $h(n)$.

Solution: Download the below python code for the plot 6.1,

```
wget https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/6-1.py
```

And run the following command in the terminal,

```
python3 6-1.py
```

Now using (5.54),

$$y(n) = x(n) * h(n) \quad (5.57)$$

$$= \begin{pmatrix} 1 & 0 & 0 & \cdot & \cdot & \cdot & 0 \\ -0.5 & 1 & 0 & \cdot & \cdot & \cdot & 0 \\ 1.25 & -0.5 & 1 & \cdot & \cdot & \cdot & 0 \\ & & \cdot & \cdot & \cdot & \cdot & \cdot \\ & & \cdot & \cdot & \cdot & \cdot & \cdot \\ 0 & 0 & 0 & \cdot & \cdot & \cdot & \cdot \end{pmatrix} \begin{pmatrix} x(0) \\ x(1) \\ x(2) \\ \cdot \\ \cdot \\ x(5) \end{pmatrix} \quad (5.58)$$

$$= \begin{pmatrix} 1 \\ 1.5 \\ 3.25 \\ \cdot \\ \cdot \\ \cdot \end{pmatrix} \quad (5.59)$$

5.10 Show that

$$y(n) = \sum_{k=-\infty}^{\infty} x(n-k)h(k) \quad (5.60)$$

Solution: Substitute $k := n - k$ in (5.46), we

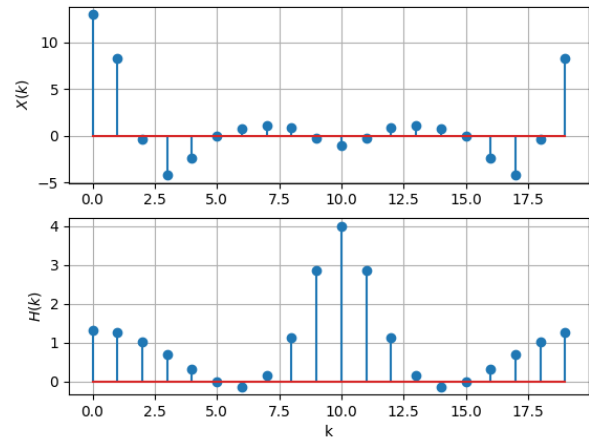


Fig. 6.1: Plot of real part of Discrete Fourier Transforms of $x(n)$ and $h(n)$

6.2 Compute

$$Y(k) = X(k)H(k) \quad (6.2)$$

Solution: Download the below python code for the plot 6.2,


```
wget https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/6-2.py
```

Then run the following command in the terminal,

```
python3 6-2.py
```

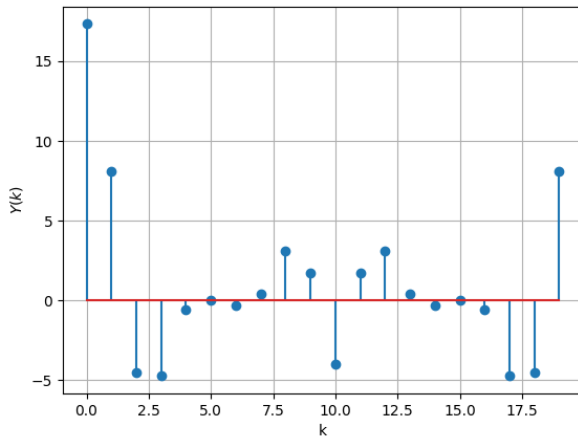


Fig. 6.2: $Y(k)$ as the product of $X(k)$ and $H(k)$

6.3 Compute

$$y(n) = \frac{1}{N} \sum_{k=0}^{N-1} Y(k) \cdot e^{j2\pi kn/N}, \quad n = 0, 1, \dots, N-1 \quad (6.3)$$

Solution: Download the below python code for the plot 6.3,

```
wget https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/6-3.py
```

Then run the following command,

```
python3 6-3.py
```

6.4 Repeat the previous exercise by computing $X(k)$, $H(k)$ and $y(n)$ through FFT and IFFT.

Solution: Download the below python code for the plot 6.4,

```
wget https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/6-4.py
```

Then run the following command,

```
python3 6-4.py
```

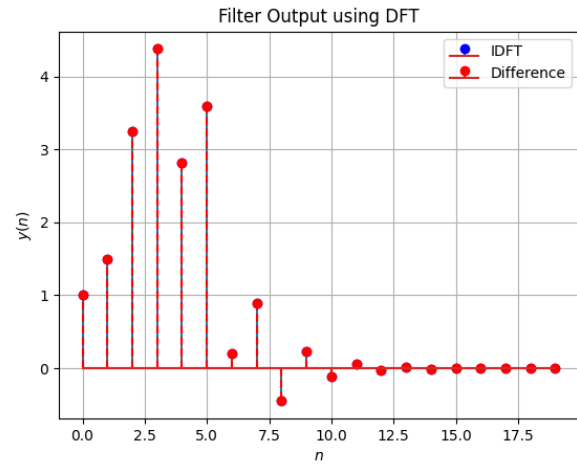


Fig. 6.3: $y(n)$ using IDFT and difference equation

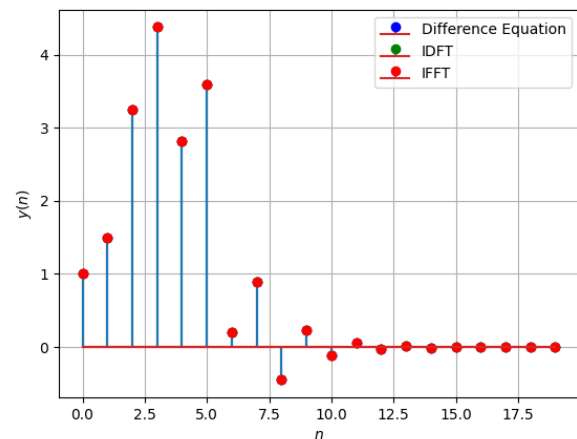


Fig. 6.4: The plot of $y(n)$ using IFFT