

Digital Signal Processing

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CONTENTS

1	Software Installation	1
2	Digital Filter	1
3	Difference Equation	2
4	Z-transform	2
5	Impulse Response	4

Abstract—This manual provides a simple introduction to digital signal processing.

1 SOFTWARE INSTALLATION

Run the following commands

```
sudo apt-get update
sudo apt-get install libffi-dev libsndfile1 python3
  -scipy python3-numpy python3-matplotlib
sudo pip install cffi pysoundfile
```

2 DIGITAL FILTER

2.1 Download the sound file from

```
wget https://raw.githubusercontent.com/
gadepall/
EE1310/master/filter/codes/Sound_Noise.wav
```

2.2 You will find a spectrogram at <https://academo.org/demos/spectrum-analyzer>. Upload the sound file that you downloaded in Problem 2.1 in the spectrogram and play. Observe the spectrogram. What do you find?
Solution: There are a lot of yellow lines between 440 Hz to 5.1 KHz. These represent the synthesizer key tones. Also, the key strokes are audible along with background noise.

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2.3 Write the python code for removal of out of band noise and execute the code.

Solution:

```
import soundfile as sf
from scipy import signal

#read .wav file
input_signal,fs = sf.read('Sound_Noise.wav'
    )

#sampling frequency of input signal
sampl_freq = fs

#order of the frequency
order = 4

#cutoff frequency 4khz
cutoff_freq = 4000.0

#digital frequency
Wn = 2*cutoff_freq/sampl_freq

# b and a are numerators and denominator
  polynomials respectively
b,a = signal.butter(order,Wn,'low')

#filter the input signal with butterworth filter
output_signal = signal.filtfilt(b,a,input_signal
    )

#output_signal = signal.lfilter(b,a,
    input_signal)

#write the output signal into .wav file
sf.write('Sound_With_ReducedNoise.wav',
    output_signal,fs)
```

2.4 The output of the python script in Problem 2.3 is the audio file Sound_With_ReducedNoise.wav. Play the file in the spectrogram in Problem 2.2. What do you observe?

Solution: The key strokes as well as background noise is subdued in the audio. Also, the signal is blank for frequencies above 5.1 kHz.

3 DIFFERENCE EQUATION

3.1 Let

$$x(n) = \left\{ \underset{\uparrow}{1}, 2, 3, 4, 2, 1 \right\} \quad (3.1)$$

Sketch $x(n)$.

3.2 Let

$$y(n) + \frac{1}{2}y(n-1) = x(n) + x(n-2),$$

$$y(n) = 0, n < 0 \quad (3.2)$$

Sketch $y(n)$.

Solution: The following code yields Fig. 3.2.

```
wget https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/3-2.py
```

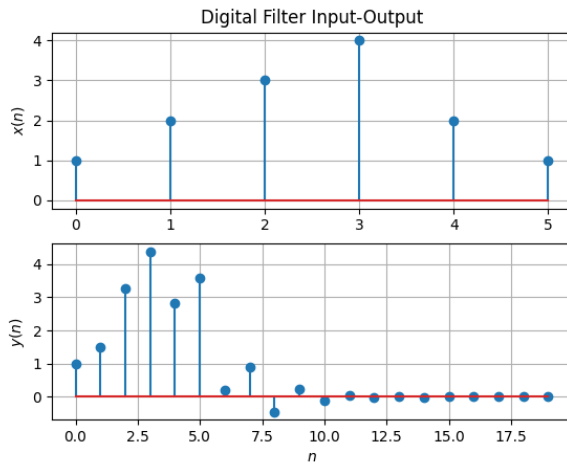


Fig. 3.2

3.3 Repeat the above exercise using a c code.

Solution: The following code yields x data and y data

```
wget https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/3-3.c
```

4 Z-TRANSFORM

4.1 The Z-transform of $x(n)$ is defined as

$$X(z) = \mathcal{Z}\{x(n)\} = \sum_{n=-\infty}^{\infty} x(n)z^{-n} \quad (4.1)$$

Show that

$$\mathcal{Z}\{x(n-1)\} = z^{-1}X(z) \quad (4.2)$$

and find

$$\mathcal{Z}\{x(n-k)\} \quad (4.3)$$

Solution: From (4.1),

$$\mathcal{Z}\{x(n-k)\} = \sum_{n=-\infty}^{\infty} x(n-k)z^{-n} \quad (4.4)$$

$$= \sum_{n=-\infty}^{\infty} x(n)z^{-(n+k)} = z^{-k} \sum_{n=-\infty}^{\infty} x(n)z^{-n} \quad (4.5)$$

resulting in (4.2). Similarly, it can be shown that

$$\mathcal{Z}\{x(n-k)\} = z^{-k}X(z) \quad (4.6)$$

4.2 Obtain $X(z)$ for $x(n)$ defined in problem 3.1

Solution:

$$X(z) = \mathcal{Z}\{x(n)\} = \sum_{n=-\infty}^{\infty} x(n)z^{-n}$$

$$X(z) = \dots 0 + x(0)z^0 + x(1)z^{-1} + x(2)z^{-2} + x(3)z^{-3} + x(4)z^{-4} + \dots$$

$$= 1 + 2z^{-1} + 3z^{-2} + 4z^{-3} + 2z^{-4} + 1z^{-5}$$

4.3 Find

$$H(z) = \frac{Y(z)}{X(z)} \quad (4.7)$$

from (3.2) assuming that the Z-transform is a linear operation.

Solution: Applying (4.6) in (3.2),

$$Y(z) + \frac{1}{2}z^{-1}Y(z) = X(z) + z^{-2}X(z) \quad (4.8)$$

$$\Rightarrow \frac{Y(z)}{X(z)} = \frac{1 + z^{-2}}{1 + \frac{1}{2}z^{-1}} \quad (4.9)$$

4.4 Find the Z transform of

$$\delta(n) = \begin{cases} 1 & n = 0 \\ 0 & \text{otherwise} \end{cases} \quad (4.10)$$

and show that the Z-transform of

$$u(n) = \begin{cases} 1 & n \geq 0 \\ 0 & \text{otherwise} \end{cases} \quad (4.11)$$

is

$$U(z) = \frac{1}{1 - z^{-1}}, \quad |z| > 1 \quad (4.12)$$

Solution: It is easy to show that

$$\delta(n) \stackrel{Z}{=} 1 \quad (4.13)$$

and from (4.11),

$$U(z) = \sum_{n=0}^{\infty} z^{-n} \quad (4.14)$$

$$= \frac{1}{1 - z^{-1}}, \quad |z| > 1 \quad (4.15)$$

using the formula for the sum of an infinite geometric progression.

4.5 Show that

$$a^n u(n) \stackrel{Z}{=} \frac{1}{1 - az^{-1}} \quad |z| > |a| \quad (4.16)$$

Solution: $X(z) = \sum_{n=-\infty}^{\infty} x(n)z^{-n}$

$$\begin{aligned} X(z) &= \sum_{n=-\infty}^{-1} 0 + \sum_{n=0}^{\infty} a^n(1)z^{-n} \\ &= \sum_{n=0}^{\infty} (az^{-1})^n \\ &= \frac{1}{1 - az^{-1}} \end{aligned}$$

Also the series is convergent for $|z| > |a|$

4.6 Let

$$H(e^{j\omega}) = H(z = e^{j\omega}). \quad (4.17)$$

Plot $|H(e^{j\omega})|$. Comment. $H(e^{j\omega})$ is known as the *Discrete Time Fourier Transform* (DTFT) of $x(n)$.

Solution: The following code plots Fig. 4.6.

```
wget https://github.com/NarehBanderu13/EE3900-A1/blob/main/codes/4-6.py
```

run the command

```
python3 4-6.py
```

$$H(e^{j\omega}) = \frac{1 + e^{-2j\omega}}{1 + \frac{1}{2}e^{-j\omega}} \quad (4.18)$$

$$\Rightarrow |H(e^{j\omega})| = \frac{|1 + \cos 2\omega - j \sin 2\omega|}{|1 + \frac{1}{2} \cos \omega - \frac{1}{2} j \sin \omega|} \quad (4.19)$$

$$= \sqrt{\frac{(1 + \cos 2\omega)^2 + (\sin 2\omega)^2}{(1 + \frac{1}{2} \cos \omega)^2 + (\frac{1}{2} \sin \omega)^2}} \quad (4.20)$$

$$= \sqrt{\frac{2 + 2 \cos 2\omega}{\frac{5}{4} + \cos \omega}} \quad (4.21)$$

$$= \sqrt{\frac{2(2 \cos^2 \omega)4}{5 + 4 \cos \omega}} \quad (4.22)$$

$$= \frac{4 |\cos \omega|}{\sqrt{5 + 4 \cos \omega}} \quad (4.23)$$

The period of the numerator is π and the de-

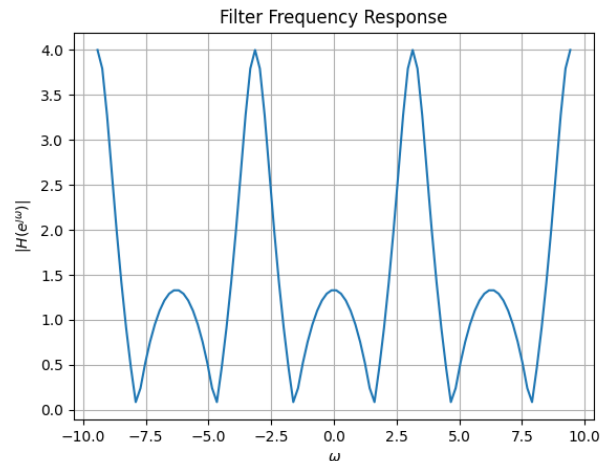


Fig. 4.6: $|H(e^{j\omega})|$

nominator is 2π taking the L.C.M of numerator and the denominator we get period as 2π

4.7 Express $h(n)$ in terms of $H(e^{2j\omega})$.

Solution:

$$\int_{-\pi}^{\pi} H(e^{j\omega}) e^{j\omega n} d\omega \quad (4.24)$$

$$= \int_{-\pi}^{\pi} \sum_{k=-\infty}^{\infty} h(k) e^{-j\omega k} e^{j\omega n} d\omega \quad (4.25)$$

$$= \sum_{k=-\infty}^{\infty} h(k) \int_{-\pi}^{\pi} e^{j\omega(n-k)} d\omega \quad (4.26)$$

Now,

$$\int_{-\pi}^{\pi} e^{j\omega(n-k)} d\omega = \begin{cases} \int_{-\pi}^{\pi} d\omega & n-k=0 \\ \frac{\exp(j\omega(n-k))}{j(n-k)} \Big|_{-\pi}^{\pi} & n-k \neq 0 \end{cases} \quad (4.27)$$

$$= \begin{cases} 2\pi & n-k=0 \\ 0 & n-k \neq 0 \end{cases} \quad (4.28)$$

$$= 2\pi\delta(n-k) \quad (4.29)$$

Thus,

$$\int_{-\pi}^{\pi} H(e^{j\omega}) e^{j\omega n} \omega = 2\pi \sum_{k=-\infty}^{\infty} h(k) \delta(n-k) \quad (4.30)$$

$$= 2\pi h(n) * \delta(n) \quad (4.31)$$

$$= 2\pi h(n) \quad (4.32)$$

Therefore, $h(n)$ is given by the inverse DTFT (IDTFT) of $H(e^{j\omega})$

$$h(n) = \frac{1}{2\pi} \int_{-\pi}^{\pi} H(e^{j\omega}) e^{j\omega n} \omega \quad (4.33)$$

5 IMPULSE RESPONSE

5.1 Using long division, find

$$h(n), \quad n < 5 \quad (5.1)$$

for $H(z)$ in (4.9).

Solution: From (4.9), we can write

$$H(z) = \frac{1 + z^{-2}}{1 + \frac{z^{-1}}{2}} \quad (5.2)$$

$$\begin{array}{r} 1 + z^{-1}/2 \overline{) \begin{array}{r} 2z^{-1} \quad -4 \\ 1 \quad +z^{-2} \\ \hline 2z^{-1} \quad +z^{-2} \\ \hline 1 \quad -2z^{-1} \\ -4 \quad -2z^{-1} \\ \hline 5 \end{array}} \end{array}$$

So we can replace (4.9) as,

$$\frac{1 + z^{-2}}{1 + \frac{z^{-1}}{2}} = 2z^{-1} - 4 + \frac{5}{1 + z^{-1}/2} \quad (5.3)$$

Now we can expand the second term of above expression as an infinite geometric series,

$$\frac{5}{1 + z^{-1}/2} = 5 \left(1 + \left(\frac{-1}{2z} \right) + \left(\frac{-1}{2z} \right)^2 + \dots \right) \quad (5.4)$$

where we assume $\left| \frac{1}{2z} \right| < 1$. So (5.3) will become,

$$= 2z^{-1} - 4 + 5 + \frac{-5}{2}z^{-1} + \frac{5}{4}z^{-2} + \frac{-5}{8}z^{-3} + \frac{5}{16}z^{-4} + \dots \quad (5.5)$$

$$= 1z^0 + \frac{-1}{2}z^{-1} + \frac{5}{4}z^{-2} + \frac{-5}{8}z^{-3} + \frac{5}{16}z^{-4} + \dots \quad (5.6)$$

Now to get $h(n)$ for $n < 5$ we will compare (5.6) with the below equation,

$$H(z) = \sum_{n=-\infty}^{\infty} h(n)z^{-n} \quad (5.7)$$

$h(n)$ will be the coefficient of z^{-n} .

Using this, from (5.6) we can write,

$$h(0) = 1 \quad (5.8)$$

$$h(1) = \frac{-1}{2} \quad (5.9)$$

$$h(2) = \frac{5}{4} \quad (5.10)$$

$$h(3) = \frac{-5}{8} \quad (5.11)$$

$$h(4) = \frac{5}{16} \quad (5.12)$$

And for $n < 0$ $h(n) = 0$.

For $n > 5$, we can get $h(n)$ from the geometric series,

$$h(n) = 5 \left(\frac{-1}{2} \right)^n \quad (5.13)$$

5.2 Find an expression for $h(n)$ using $H(z)$, given that

$$h(n) \stackrel{Z}{\rightleftharpoons} H(z) \quad (5.14)$$

and there is a one to one relationship between $h(n)$ and $H(z)$. $h(n)$ is known as the *impulse response* of the system defined by (3.2).

Solution: The $H(z)$ can be written as,

$$H(z) = \frac{1}{1 + \frac{z^{-1}}{2}} + \frac{z^{-2}}{1 + \frac{z^{-1}}{2}} \quad (5.15)$$

From (4.16) we can write it as,

$$h(n) = \left(\frac{-1}{2} \right)^n u(n) + \left(\frac{-1}{2} \right)^{n-2} u(n-2) \quad (5.16)$$

5.3 Sketch $h(n)$. Is it bounded? Justify Theoretically.

Solution: Download the code for the plot 5.3 from the below link,

```
wget https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/5-3.py
```

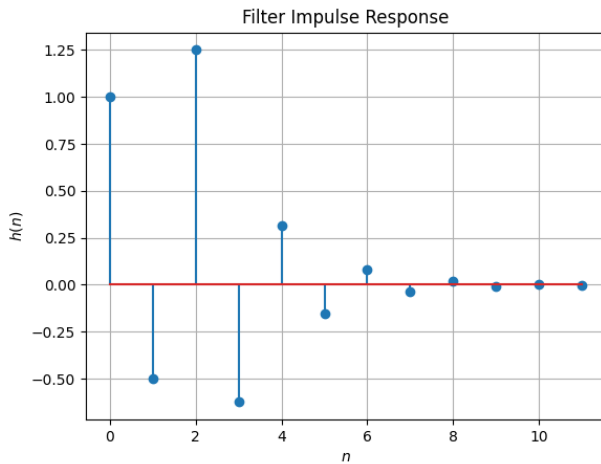


Fig. 5.3: $h(n)$ as inverse of $H(n)$

From the plot it seems like $h(n)$ is bounded and becomes smaller in magnitude as n increases. Using (5.16), we can get theoretical expression as,

$$h(n) = \begin{cases} 0 & , n < 0 \\ \left(\frac{-1}{2}\right)^n & , 0 \leq n < 2 \\ 5\left(\frac{-1}{2}\right)^n & , n \geq 2 \end{cases} \quad (5.17)$$

A sequence $\{x_n\}$ is said to be bounded if and only if there exist a positive real number M such that,

$$|x_n| \leq M, \forall n \in \mathcal{N} \quad (5.18)$$

So to say $h(n)$ is bounded we should able to find the M which satisfies (5.18).

For $n < 0$,

$$|h(n)| \leq 0 \quad (5.19)$$

For $0 \leq n < 2$,

$$|h(n)| = \left|\frac{-1}{2}\right|^n \quad (5.20)$$

$$= \left(\frac{1}{2}\right)^n \leq 1 \quad (5.21)$$

And for $n \geq 2$,

$$|h(n)| = \left|5\left(\frac{-1}{2}\right)^n\right| \quad (5.22)$$

$$= \left(\frac{5}{2}\right)^n \leq \frac{5}{4} \quad (5.23)$$

From above three cases, we can get M as,

$$M = \max\left\{0, 1, \frac{5}{4}\right\} \quad (5.24)$$

$$= \frac{5}{4} \quad (5.25)$$

Therefore, $h(n)$ is bounded using (5.18) with $M = \frac{5}{4}$ i.e.,

$$|h(n)| \leq \frac{5}{4} \forall n \in \mathcal{N} \quad (5.26)$$

5.4 Convergent? Justify using the ratio test.

Solution: We can say a given real sequence $\{x_n\}$ is convergent if

$$\lim_{n \rightarrow \infty} \left| \frac{x_{n+1}}{x_n} \right| < 1 \quad (5.27)$$

This is known as Ratio test.

In this case the limit will become,

$$\lim_{n \rightarrow \infty} \left| \frac{h(n+1)}{h(n)} \right| = \lim_{n \rightarrow \infty} \left| \frac{5\left(\frac{-1}{2}\right)^{n+1}}{5\left(\frac{-1}{2}\right)^n} \right| \quad (5.28)$$

$$= \lim_{n \rightarrow \infty} \left| \frac{-1}{2} \right| \quad (5.29)$$

$$= \frac{1}{2} \quad (5.30)$$

As $\frac{1}{2} < 1$, from root test we can say that $h(n)$ is convergent.

5.5 The system with $h(n)$ is defined to be stable if

$$\sum_{n=-\infty}^{\infty} h(n) < \infty \quad (5.31)$$

Is the system defined by (3.2) stable for the impulse response in (5.14)?

Solution: From (5.16),

$$\sum_{n=-\infty}^{\infty} h(n) = \sum_{n=-\infty}^{\infty} \left(\left(\frac{-1}{2} \right)^n u(n) + \left(\frac{-1}{2} \right)^{n-2} u(n-2) \right) \quad (5.32)$$

$$= 2 \left(\frac{1}{1 + \frac{1}{2}} \right) \quad (5.33)$$

$$= \frac{4}{3} \quad (5.34)$$

\therefore the system is stable.

5.6 Verify the above result using a python code.

Solution: Download the python code from the below link

wget <https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/5-6.py>

Then run the following command,

python3 5-6.py

5.7 Compute and sketch $h(n)$ using

$$h(n) + \frac{1}{2}h(n-1) = \delta(n) + \delta(n-2), \quad (5.35)$$

This is the definition of $h(n)$.

Solution: Download the code for the plot 5.7 from the below link,

wget <https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/5-7.py>

Note that this is same as 5.3.

For $n < 0$, $h(n) = 0$ and,

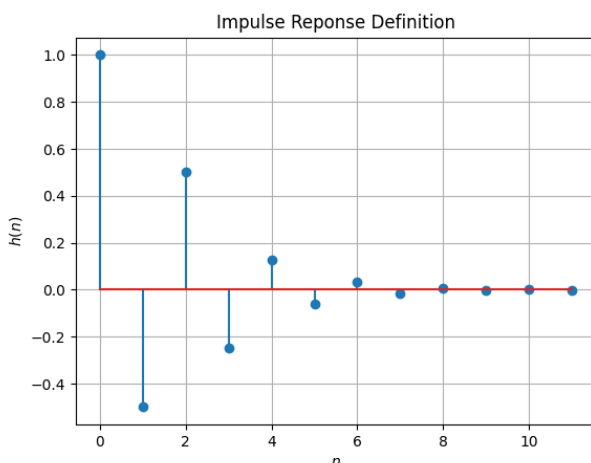


Fig. 5.7: From the definition of $h(n)$

$$h(0) = \delta(0) \quad (5.36)$$

$$= 1 \quad (5.37)$$

For $n = 1$,

$$h(1) + \frac{1}{2}h(0) = \delta(1) + \delta(-1) \quad (5.38)$$

$$\Rightarrow h(1) = -\frac{1}{2}h(0) \quad (5.39)$$

$$= -\frac{1}{2} \quad (5.40)$$

$n = 2$,

$$h(2) + \frac{1}{2}h(1) = 0 + \delta(0) \quad (5.41)$$

$$h(2) = 1 + \frac{1}{4} \quad (5.42)$$

$$= \frac{5}{4} \quad (5.43)$$

And for $n > 2$ RHS will be 0 so,

$$h(n) = -\frac{1}{2}h(n-1) \quad (5.44)$$

Overall

$$h(n) = \begin{cases} 0 & , n < 0 \\ 1 & , n = 0 \\ -\frac{1}{2} & , n = 1 \\ \frac{5}{4} & , n = 2 \\ -\frac{1}{2}h(n-1) & , n > 2 \end{cases} \quad (5.45)$$

5.8 Compute

$$y(n) = x(n) * h(n) = \sum_{k=-\infty}^{\infty} x(k)h(n-k) \quad (5.46)$$

Comment. The operation in (5.46) is known as *convolution*.

Solution: Download the code for plot 5.8 from the below link

wget <https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/5-8.py>

5.9 Express the above convolution using a Toeplitz matrix.

Solution: Download the python code from the below link for the plot 5.9,

wget <https://github.com/NareshBandaru13/EE3900-A1/blob/main/codes/5-9.py>

Then run the following command,

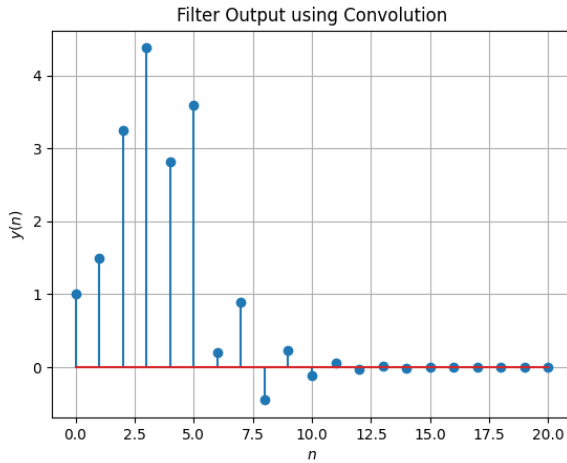


Fig. 5.8: $y(n)$ using the convolution definition

```
python3 5-9.py
```

From (5.46), we express $y(n)$ as

$$y(n) = \sum_{k=-\infty}^{\infty} x(k) h(n-k) \quad (5.47)$$

To understand how we can use a Toeplitz matrix, we will see what we are doing in (5.46)

$$y(0) = x(0) h(0) \quad (5.48)$$

$$y(1) = x(0) h(1) + x(1) h(0) \quad (5.49)$$

$$y(2) = x(0) h(2) + x(1) h(1) + x(2) h(0) \quad (5.50)$$

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The same thing can be written as,

$$y(0) = \begin{pmatrix} h(0) & 0 & 0 & \dots & \dots & 0 \end{pmatrix} \begin{pmatrix} x(0) \\ x(1) \\ x(2) \\ \vdots \\ \vdots \\ x(5) \end{pmatrix} \quad (5.51)$$

$$y(1) = \begin{pmatrix} h(1) & h(0) & 0 & 0 & \dots & \dots & 0 \end{pmatrix} \begin{pmatrix} x(0) \\ x(1) \\ x(2) \\ \vdots \\ \vdots \\ x(5) \end{pmatrix} \quad (5.52)$$

$$y(2) = \begin{pmatrix} h(2) & h(1) & h(0) & 0 & \dots & \dots & 0 \end{pmatrix} \begin{pmatrix} x(0) \\ x(1) \\ x(2) \\ \vdots \\ \vdots \\ x(5) \end{pmatrix} \quad (5.53)$$

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Using Toeplitz matrix of $h(n)$ we can simplify it as,

$$y(n) = \begin{pmatrix} h(0) & 0 & 0 & \dots & \dots & 0 \\ h(1) & h(0) & 0 & \dots & \dots & 0 \\ h(2) & h(1) & h(0) & \dots & \dots & 0 \\ \vdots & \vdots & \vdots & \ddots & \ddots & \vdots \\ 0 & 0 & 0 & \dots & \dots & h(m-1) \end{pmatrix} \begin{pmatrix} x(0) \\ x(1) \\ x(2) \\ \vdots \\ \vdots \\ x(5) \end{pmatrix} \quad (5.54)$$

Now from (??) we will take n

$$x(n) = \begin{pmatrix} 1 \\ 2 \\ 3 \\ 4 \\ 2 \\ 1 \end{pmatrix} \quad (5.55)$$

And from (5.17)

$$h(n) = \begin{pmatrix} 1 \\ -0.5 \\ 1.25 \\ \vdots \\ \vdots \end{pmatrix} \quad (5.56)$$

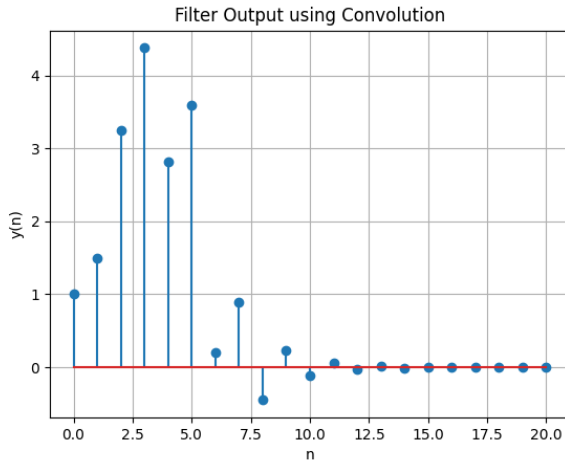


Fig. 5.9: Convolution of $x(n)$ and $h(n)$ using toeplitz matrix

Now using (5.54),

$$y(n) = x(n) * h(n) \quad (5.57)$$

$$= \begin{pmatrix} 1 & 0 & 0 & . & . & .0 \\ -0.5 & 1 & 0 & . & . & .0 \\ 1.25 & -0.5 & 1 & . & . & .0 \\ & & .. & & & \\ 0 & 0 & 0 & . & . & . \end{pmatrix} \begin{pmatrix} x(0) \\ x(1) \\ x(2) \\ . \\ . \\ x(5) \end{pmatrix} \quad (5.58)$$

$$= \begin{pmatrix} 1 \\ 1.5 \\ 3.25 \\ . \\ . \\ . \end{pmatrix} \quad (5.59)$$

5.10 Show that

$$y(n) = \sum_{k=-\infty}^{\infty} x(n-k)h(k) \quad (5.60)$$

Solution: Substitute $k := n - k$ in (5.46), we

will get

$$y(n) = \sum_{k=-\infty}^{\infty} x(k)h(n-k) \quad (5.61)$$

$$= \sum_{n-k=-\infty}^{\infty} x(n-k)h(k) \quad (5.62)$$

$$= \sum_{k=-\infty}^{\infty} x(n-k)h(k) \quad (5.63)$$

$$(5.64)$$

6 DFT

6.1 Compute

$$X(k) \triangleq \sum_{n=0}^{N-1} x(n)e^{-j2\pi kn/N}, \quad k = 0, 1, \dots, N-1 \quad (6.1)$$

and $H(k)$ using $h(n)$.

Solution: Download the below python code for the plot ??,

```
wget https://github.com/Charanyash/EE3900-Digital_Signal_Processing/blob/master/Sound%201/Codes/dft.py
```

And run the following command in the terminal,

```
python3 dft.py
```

6.2 Compute

$$Y(k) = X(k)H(k) \quad (6.2)$$

Solution: Download the below python code for the plot ??,

```
wget https://github.com/Charanyash/EE3900-Digital_Signal_Processing/blob/master/Sound%201/Codes/Y_K.py
```

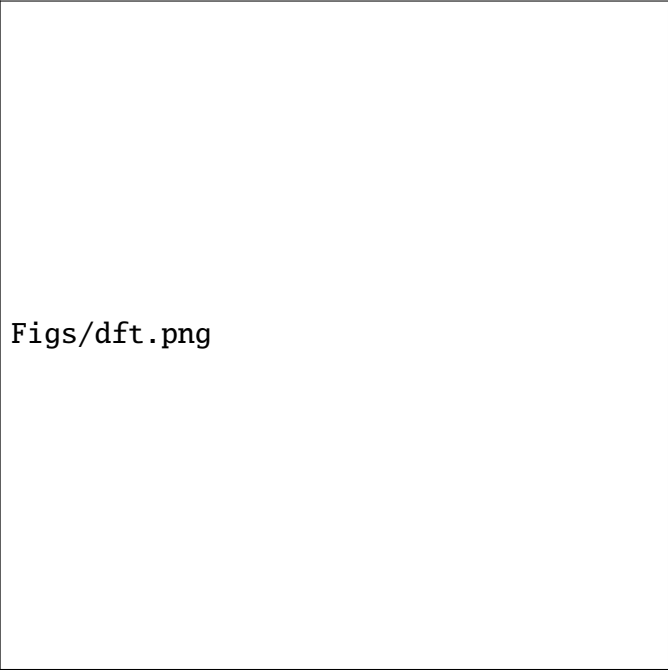
Then run the following command in the terminal,

```
python3 Y_K.py
```

6.3 Compute

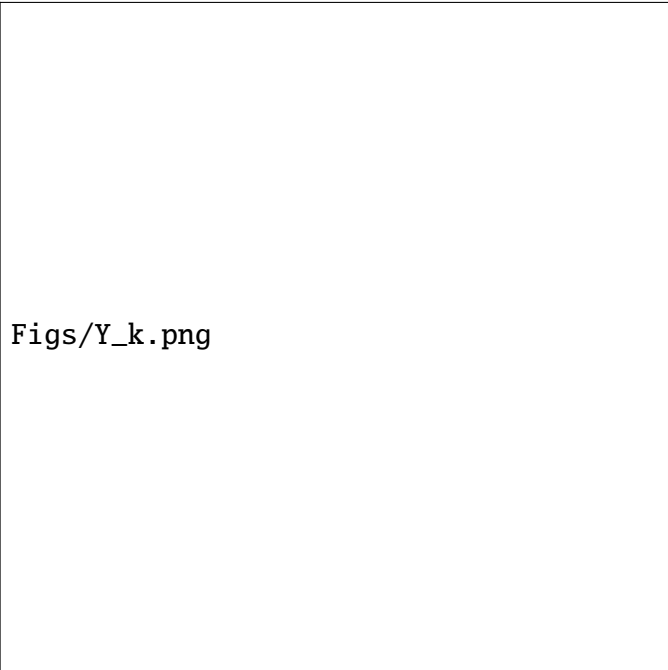
$$y(n) = \frac{1}{N} \sum_{k=0}^{N-1} Y(k) \cdot e^{j2\pi kn/N}, \quad n = 0, 1, \dots, N-1 \quad (6.3)$$

Solution: Download the below python code for the plot ??,



Figs/dft.png

Fig. 6.1: Plot of real part of Discrete Fourier Transforms of $x(n)$ and $h(n)$




Figs/Y_k.png

Fig. 6.2: $Y(k)$ as the product of $X(k)$ and $H(k)$

```
wget https://github.com/Charanyash/EE3900-Digital_Signal_Processing/blob/master/Sound%201/Codes/yndft_dif.py
```

Then run the following command,

```
python3 yndft_dif.py
```



Figs/yndft_dif.png

Fig. 6.3: $y(n)$ using IDFT and difference equation

6.4 Repeat the previous exercise by computing $X(k)$, $H(k)$ and $y(n)$ through FFT and IFFT.

Solution: Download the below python code for the plot ??,

```
wget https://github.com/Charanyash/EE3900-Digital_Signal_Processing/blob/master/Sound%201/Codes/yn_ifft.py
```

Then run the following command,

```
python3 yn_ifft.py
```

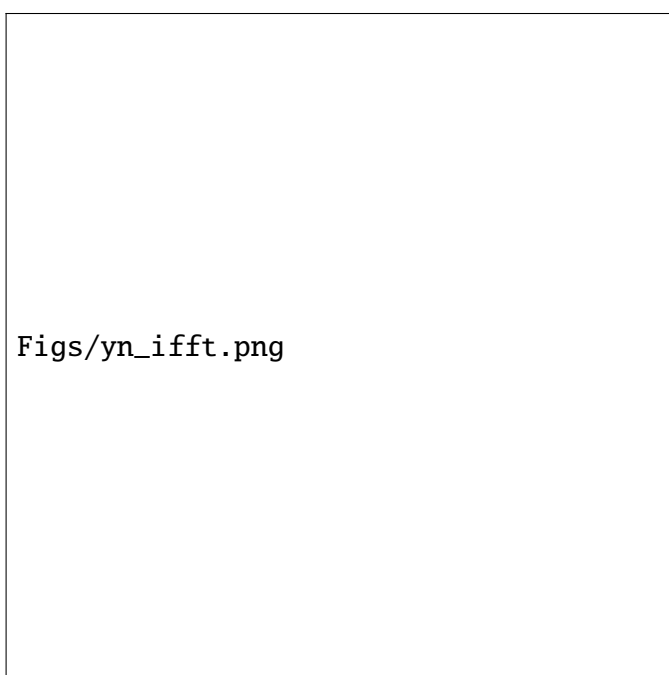


Fig. 6.4: The plot of $y(n)$ using IFFT