

## Stack And Queue of level ① }

- Stack Basics

- Normal Stack
- Dynamic Stack

- Queue Basics

- Normal Queue
- Dynamic Queue

- Two Stacks in Array

- Stack using Queue

- Push efficient
- Pop efficient

- Queue using Stack

- Push efficient
- Pop efficient

- Duplicate Brackets

- Balanced Brackets

## Lecture ③

- Next Greater to Right

HW

NGE to Left

NSE to Right

NSE to Left

- Stock Span

- Largest Histogram

- Sliding Window Maximum

## Lecture ④

</> Infix Evaluation

</> Infix Conversions

</> Prefix Evaluation And Conversions

</> Postfix Evaluation And Conversions

## Lecture ⑤

- Celebrity Problem

- Minimum Stack

→ with Extra Space

→ w/o Extra Space

- Smallest No following pattern

## Stack & Queue

{ level ② }

{ Thursday & Weekends }  
{ optional for FJP-2 }

### h2 - lecture ①

- K Stacks in Array
- K Queue in Array
- Circular Deque
- maximum Stack
- Middle Queue

### h2 - lecture ②

- Stack - Increment OP
- Max Frequency Stack
- Basic Calculator
  - I, II, III
- Expression Tree - Construct & Evaluate

## L2 - Lecture ③

- Reverse Stack
- Reverse Queue
- Sort Stack
- Sort Queue
- Interleave Queue

## L2 - Lecture ④

- Trapping Rain<sup>Θ</sup> Water - I & II
- Maximum Area Container
- Remove K Digits
- Remove Duplicate letters
- Lenienc smallest subset

## L2 - lecture 5

- Remove Outermost Parentheses
- Longest valid Parentheses
- Minimum Additions
- Minimum Removals - I & II
- Score of Parentheses
- Reverse Substrings

## L2 - lecture 6

- Validate Stack Sequence
- Asteroid Collision
- Exclusive Time of Fn
- No of Recent Calls
- Valid Word After Substitution

# Lecture ①

- Stack Basics

- Normal Stack

- Dynamic Stack

- Queue Basics

- Normal Queue

- Dynamic Queue

- Two Stacks in Array

Monday 8:30 PM  
to 12 AM

- Dequeue using LL
- Stack using LL

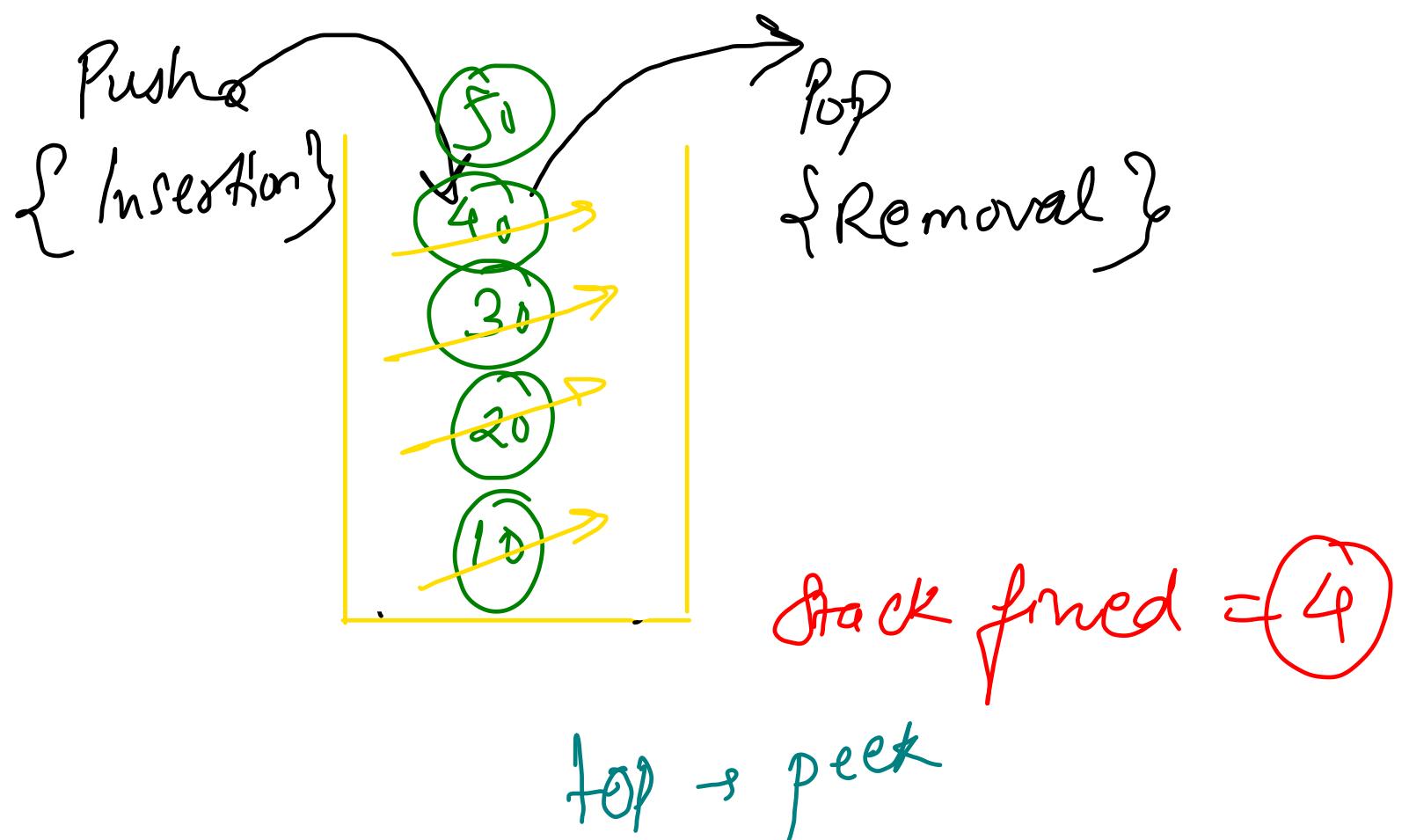
## Data Structures

- Array (1D, 2D, String)
- ArrayList
- Linked List

Stack

{ LIFO or FILO }

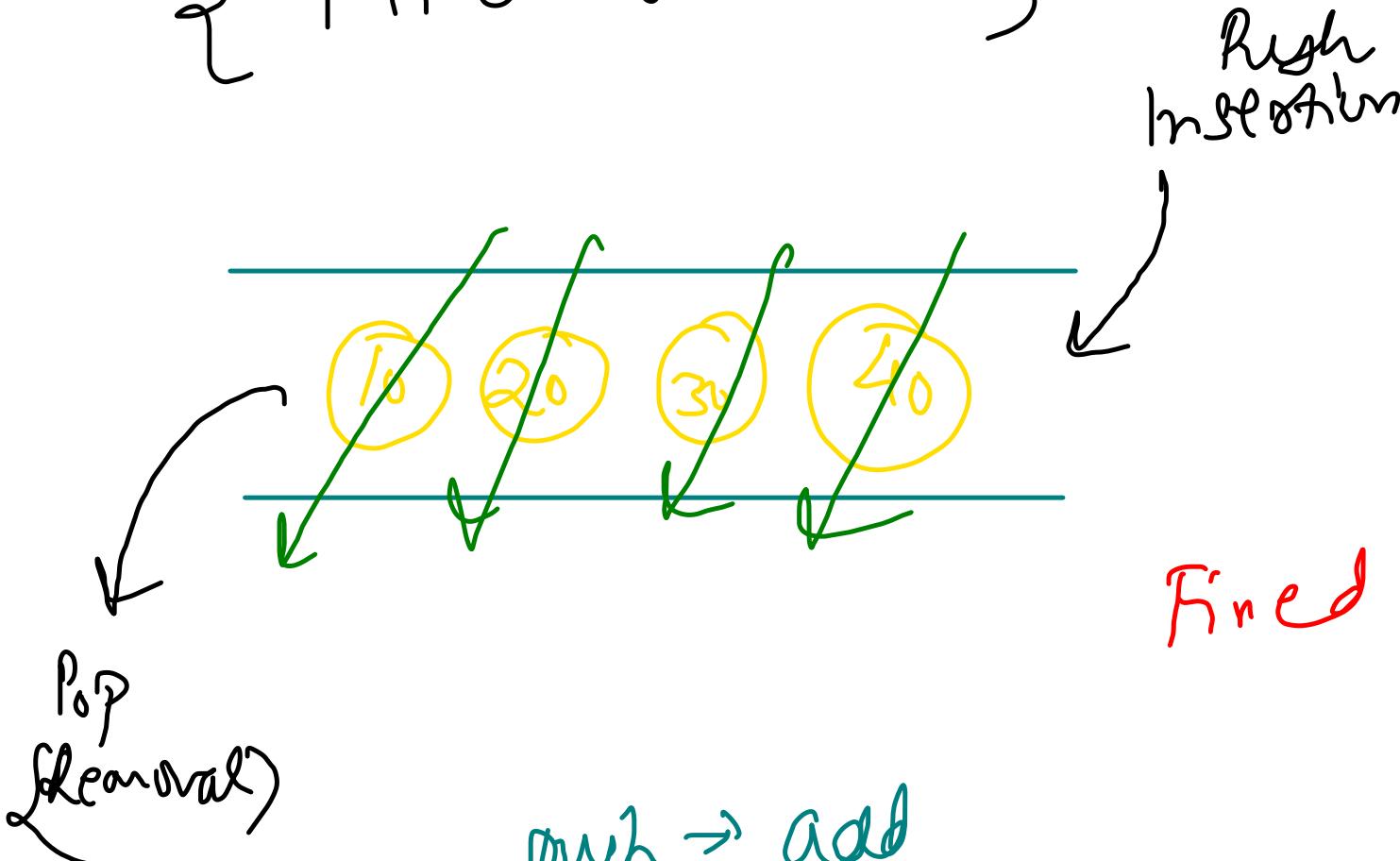
{ ~~eg~~   
earlier call  
stack /  
Function  
call stack }



- 0(1) → push (10) First In
- 0(1) → push (20)
- 0(1) → push (30)
- 0(1) → push (40) Last In
- 0(1) → ~~push (50)~~ → Stack overflow
- 0(1) → pop() → 40 First out
- 0(1) → pop() → 30
- 0(1) → pop() → 20
- 0(1) → pop() → 10 Last Out
- 0(1) →  $\begin{pmatrix} \text{top}() \\ \text{pop}() \end{pmatrix}$  → Stack Underflow

Queue

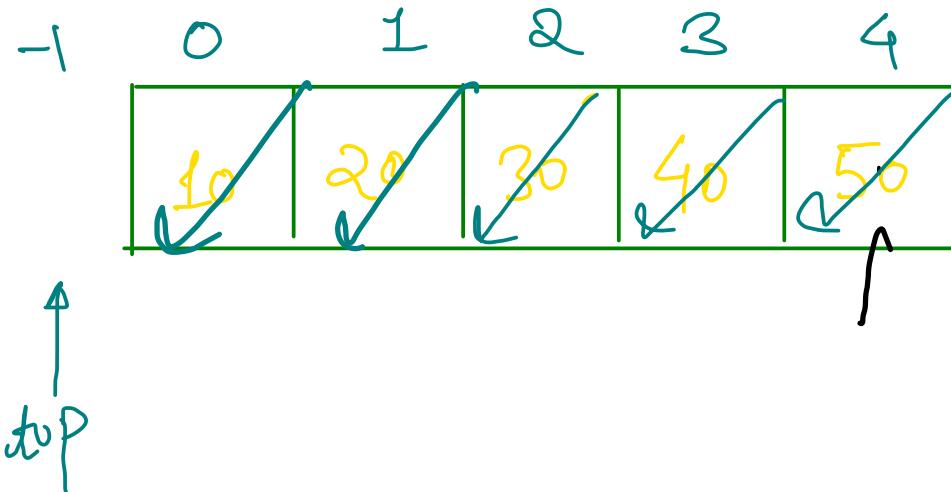
{ FIFO or LIFO }



push → add  
pop → remove  
front → peek

- 0(1) push (10) First in
- 0(2) push (20)
- 0(3) push (30)
- 0(4) push (40) Last in
- push(50) → Queue Overflow
- 0(1) pop () ; → 10 First out
- 0(1) pop () ; → 20
- 0(1) pop () ; → 30
- 0(1) pop () ; → 40 Last Out
- pop() ; → Queue underflow (-1)

Stack



push(10)    top++    arr[top] = val

size() → 1 (top + 1)

pop() → 40

pop() → 30

pop() → 20

pop() → 10

pop() → Stack underflow (top = -1)

size() → 0

(1) Array  
capacity 5

(2) ArrayList

(3) linked list

push(20)

size() → 2

peek() → 20

return arr[top]

push(30)

peek() → 30

push(40)

push(50)

push(60) → Stack overflow

top = Cap - 1

10 ← pop() → inst val = arr[top]

top--;  
return val;

```
public static class CustomStack {  
    int[] arr;  
    int top;
```

```
public CustomStack(int cap) {  
    // Constructor -> O(1)  
    arr = new int[cap];  
    top = -1;  
}  
  
}
```

```
int size() {  
    // O(1)  
    return top + 1;  
}  
  
void display() {  
    // O(N)  
    for(int i=top; i>=0; i--){  
        System.out.print(arr[i] + " ");  
    }  
    System.out.println();  
}
```

size() == arr.length

```
void push(int val) {  
    // O(1)  
    if(top == arr.length - 1){  
        // Stack Overflow  
        System.out.println("Stack overflow");  
        return;  
    }  
  
    top++;  
    arr[top] = val;  
}
```

pop() == O

```
int pop() {  
    // O(1)  
    if(top == -1){  
        // Stack Underflow  
        System.out.println("Stack underflow");  
        return -1;  
    }  
  
    int val = arr[top];  
    top--;  
    return val;  
}  
  
int top() {  
    // O(1)  
    if(top == -1){  
        //  
    }  
  
    int val = arr[top];  
    return val;  
}
```

## Dynamic Stack



8 Slots

80

top ↑

Doubling



16 size

0(1) → push (0)

0(1) → push (20)

0(1) → push (30)

0(1) → push (40)

4K + 0(1) → push (50)

0(1) → push (60)

0(1) → push (70)

0(1) → push (80)

8K + 0(1) → push (90)

push (100) → 0(1)

push (110) → 0(1)

push (120) :

push (130) :

push (140) :

push (150) :

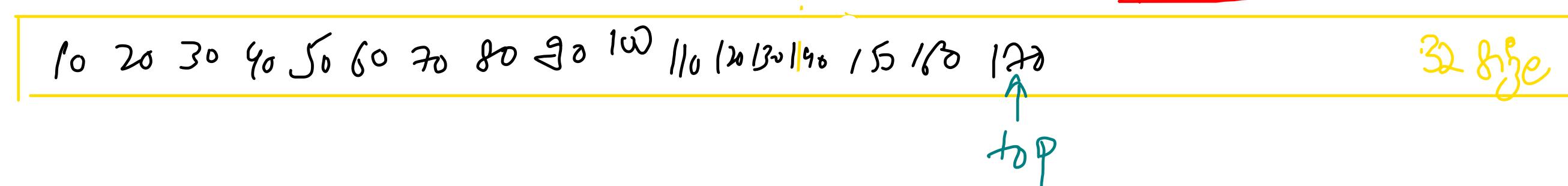
push (160) → 0(1)

push (170) → 16K + 0(1)

33<sup>rd</sup>, 65<sup>th</sup>, 129<sup>th</sup>

Doubling

top ↑



32 size

top ↑

(push in ArrayList)  
 (Avg) Amortized Time Complexity

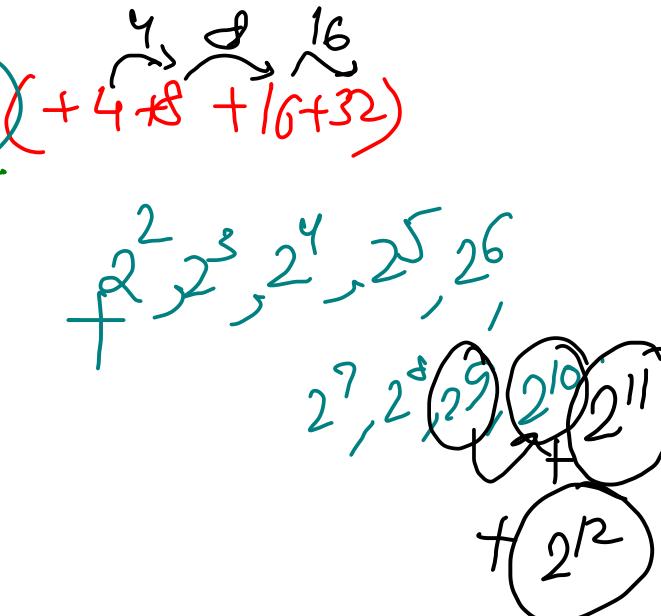
$$= \frac{\sum \text{Push Time}}{\text{No of times push is offered}}$$

No of times push is offered

$$= \frac{(1+1+1+\dots + n)}{n} + (4+8+16+32)$$

$$= O(1)$$

$$\frac{n+k}{n} \approx 1 \quad \boxed{k/n \approx 1}$$



Memory Extra Allocation  $\rightarrow$  Least Possible

$$2^x = n$$

$$x = \log_2 n$$

$$a \sigma^{x-1} = n$$

$$a = 2$$

$$\sigma = 2$$

$$\frac{a(x-1)}{(x-1)} = 2 \left( \frac{2^{\log_2 n} - 1}{2 - 1} \right)$$

$$= \frac{2(n-1)}{1} = \boxed{n}$$

$$\frac{n+k}{n}$$

$$= \frac{n+n}{n}$$

$$= 2$$

$$O(1)$$

```
// change the code of this function according to the requirement
void push(int val) {
    if (tos == data.length - 1) {
        int[] temp = new int[2 * data.length];
        for(int i=0; i<data.length; i++){
            temp[i] = data[i];
        }
        data = temp;
    }

    tos++;
    data[tos] = val;
}
```

# Stack - using linked List {FIFO, LIFO}

SLH {head & tail}

addFirst → O(1)

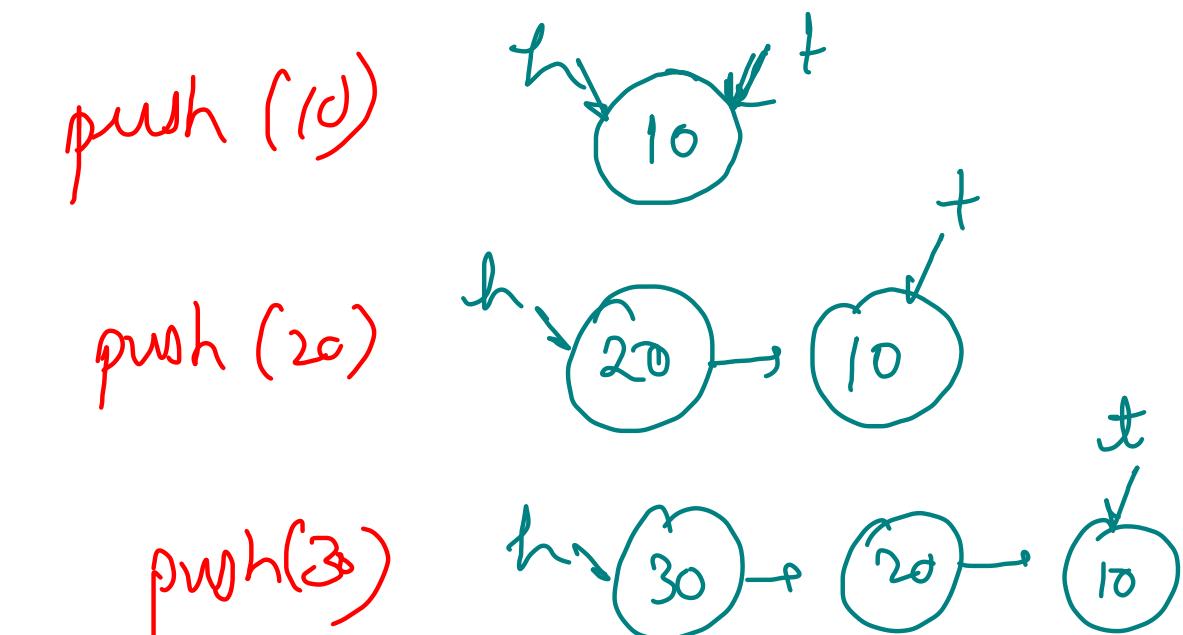
addLast → O(n)

removeFirst → O(1)

removeLast → O(n)

push → addFirst {O(1)}

pop → removeFirst {O(1)}



push(30)

③ pop()

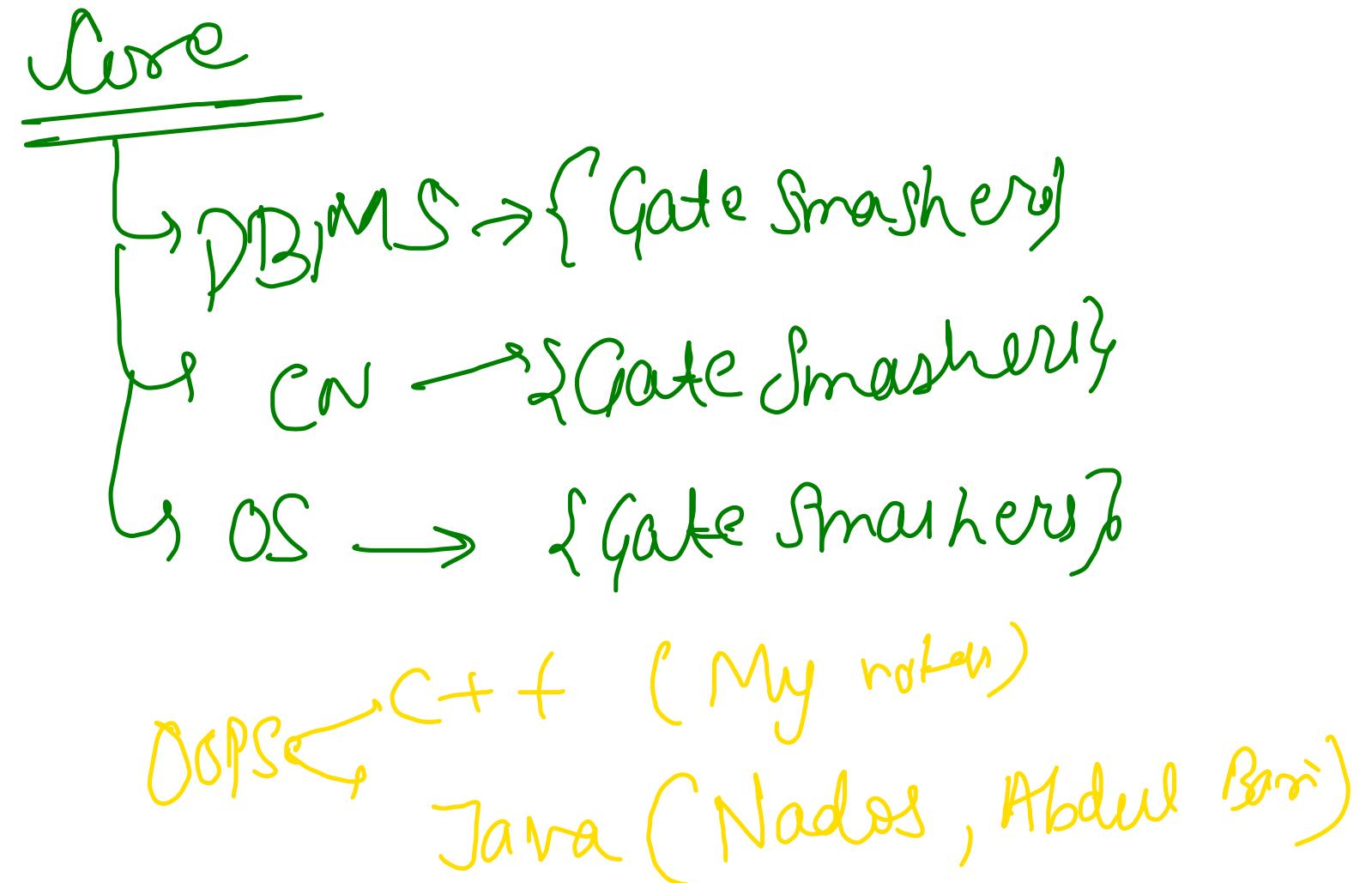
② pop()

① pop()

pop() → stack underflow

$h = t = \text{null}$

```
public static class LLToStackAdapter {  
    LinkedList<Integer> list;  
  
    public LLToStackAdapter() {  
        list = new LinkedList<>();  
    }  
  
    int size() {  
        return list.size();  
    }  
  
    void push(int val) {  
        list.addFirst(val);  
    }  
  
    int pop() {  
        if(size() == 0){  
            System.out.println("Stack underflow");  
            return -1;  
        }  
        return list.removeFirst();  
    }  
  
    int top() {  
        if(size() == 0){  
            System.out.println("Stack underflow");  
            return -1;  
        }  
        return list.getFirst();  
    }  
}
```



# Queue using Lh

Lh {head & tail}

$\text{addFirst} \rightarrow O(1)$

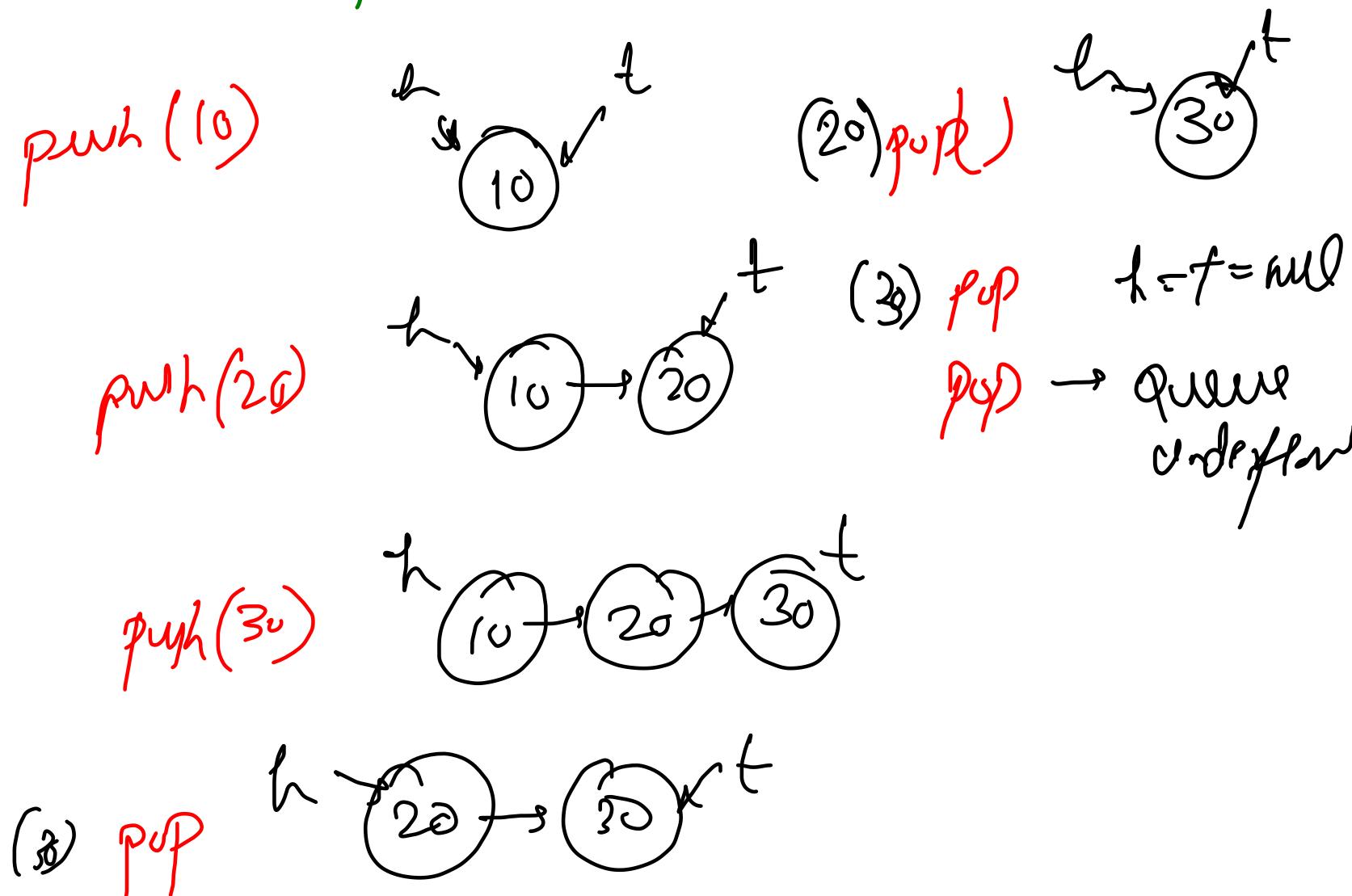
$\text{addLast} \rightarrow O(1)$

$\text{removeFirst} \rightarrow O(1)$

$\text{removeLast} \rightarrow O(n)$

push  $\rightarrow$  addLast

pop  $\rightarrow$  removeFirst



```
public static class LLToQueueAdapter {
    LinkedList<Integer> list;

    public LLToQueueAdapter() {
        list = new LinkedList<>();
    }

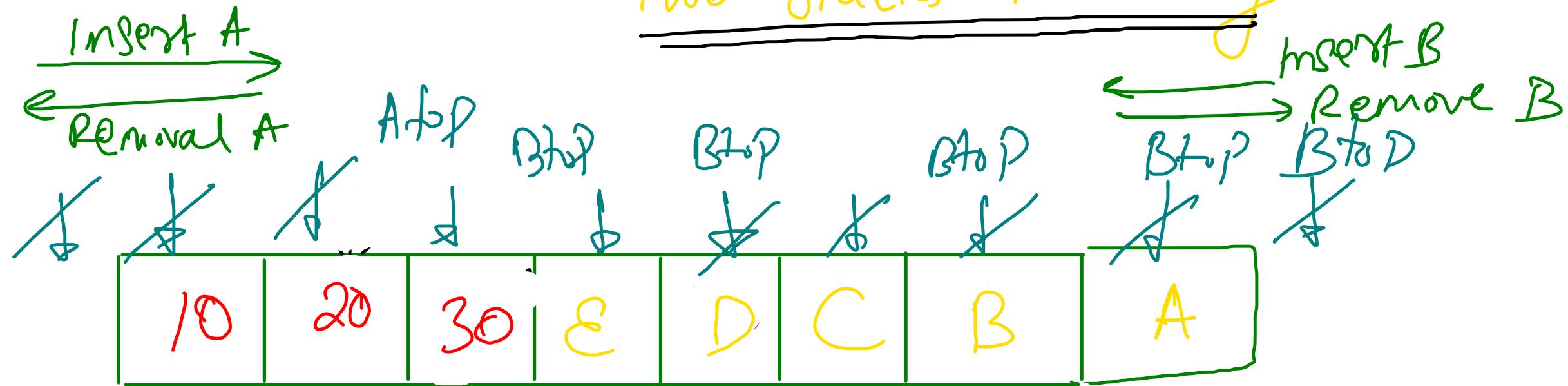
    int size() {
        return list.size();
    }

    void add(int val) {
        list.addLast(val);
    }

    int remove() {
        if(size() == 0) {
            System.out.println("Queue underflow");
            return -1;
        }
        return list.removeFirst();
    }

    int peek() {
        if(size() == 0) {
            System.out.println("Queue underflow");
            return -1;
        }
        return list.getFirst();
    }
}
```

## Two stacks in Array



### 1st stack

push(10)  
push(20)  
push(30)  
push(C)  
push(E)  
pop()

### 2nd stack

push(A)  
push(B)  
push(C)  
push(D)  
push(E)  
pop()

## Stack & Queue → Basic's

### • Stack Basic's

→ Normal Stack

→ Dynamic Stack

→ using hh

### • Queue Basic's

→ Normal Queue

→ Dynamic Queue

→ using hh

• Two stacks in Array

• Stack using Queue

→ Push efficient

→ Pop efficient

• Queue using Stack

→ Push efficient

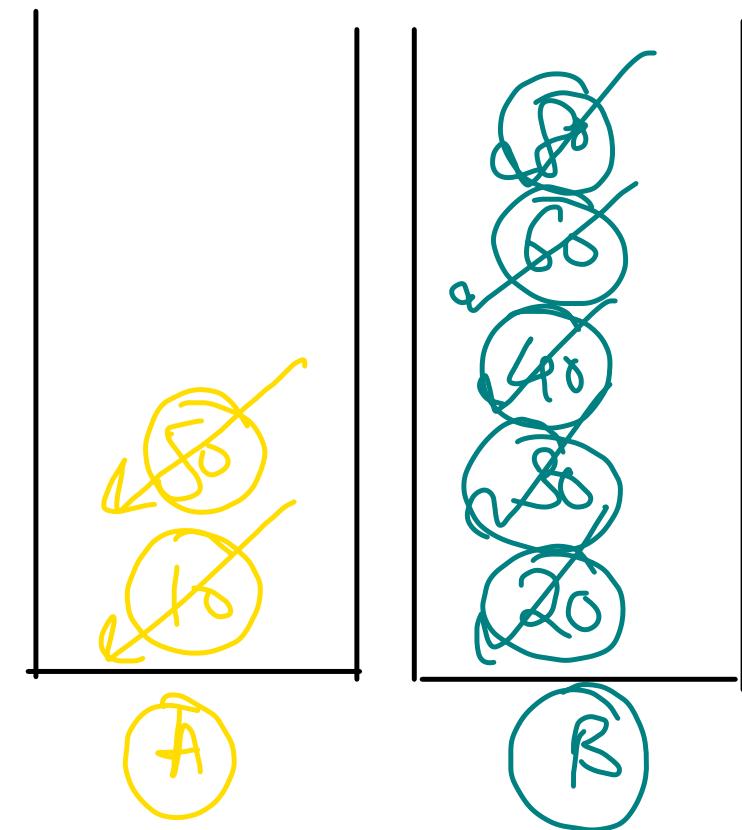
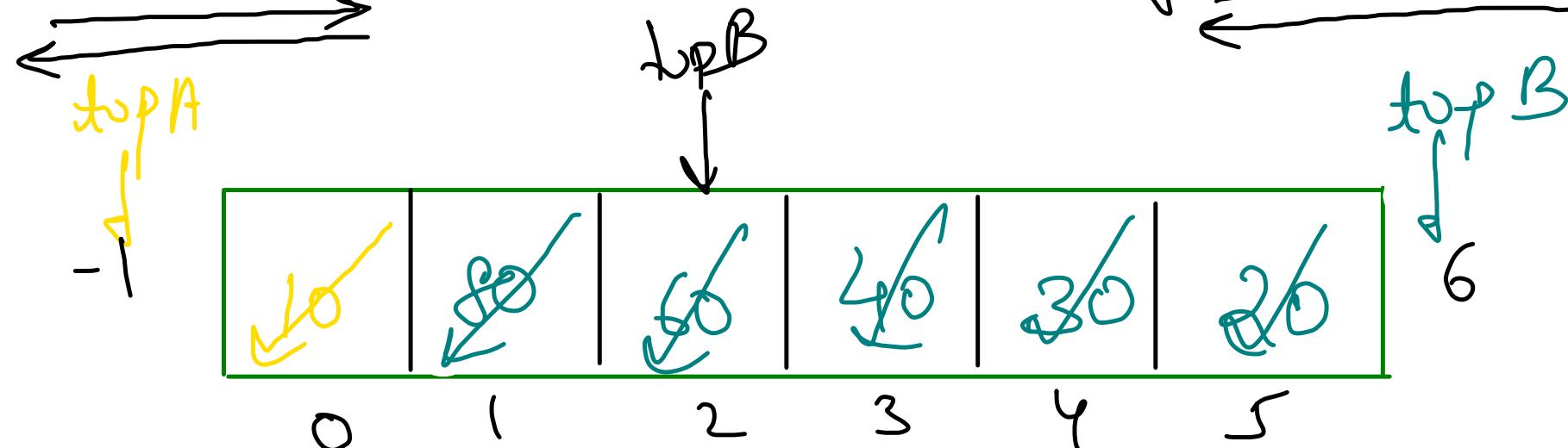
→ Pop efficient

• Duplicate Brackets

• Balanced Brackets

# Two Stacks in Array

*size = 6*



(A)

push(10)

pop()

push(50)

pop()  
Stack overflow

push(70) → Stack overflow

pop()

(B)

push(20)

pop()

push(30)

pop()

push(40)

pop()

push(60)

pop()

push(80)

pop() → Stack underflow

```
int[] data;
int top1;
int top2;

public TwoStack(int cap) {
    data = new int[cap];
    top1 = -1;
    top2 = cap;
}
```

```
int pop1() { → O(1)
    if(top1 == -1){
        // Stack 1 Underflow
        System.out.println("Stack underflow");
        return -1;
    }

    int val = data[top1];
    top1--;
    return val;
} → O(1)

int pop2() { → O(1)
    if(top2 == data.length){
        // stack 2 underflow
        System.out.println("Stack underflow");
        return -1;
    }

    int val = data[top2];
    top2++;
    return val;
}
```

```
void push1(int val) { → O(1)
    if(size1() + size2() == data.length){
        //Stack overflow
        System.out.println("Stack overflow");
        return;
    }

    top1++;
    data[top1] = val;
} → O(1)

void push2(int val) { → O(1)
    if(size1() + size2() == data.length){
        //Stack overflow
        System.out.println("Stack overflow");
        return;
    }

    top2--;
    data[top2] = val;
}
```

```
int size1() { → O(1)
    return (top1 + 1);
}

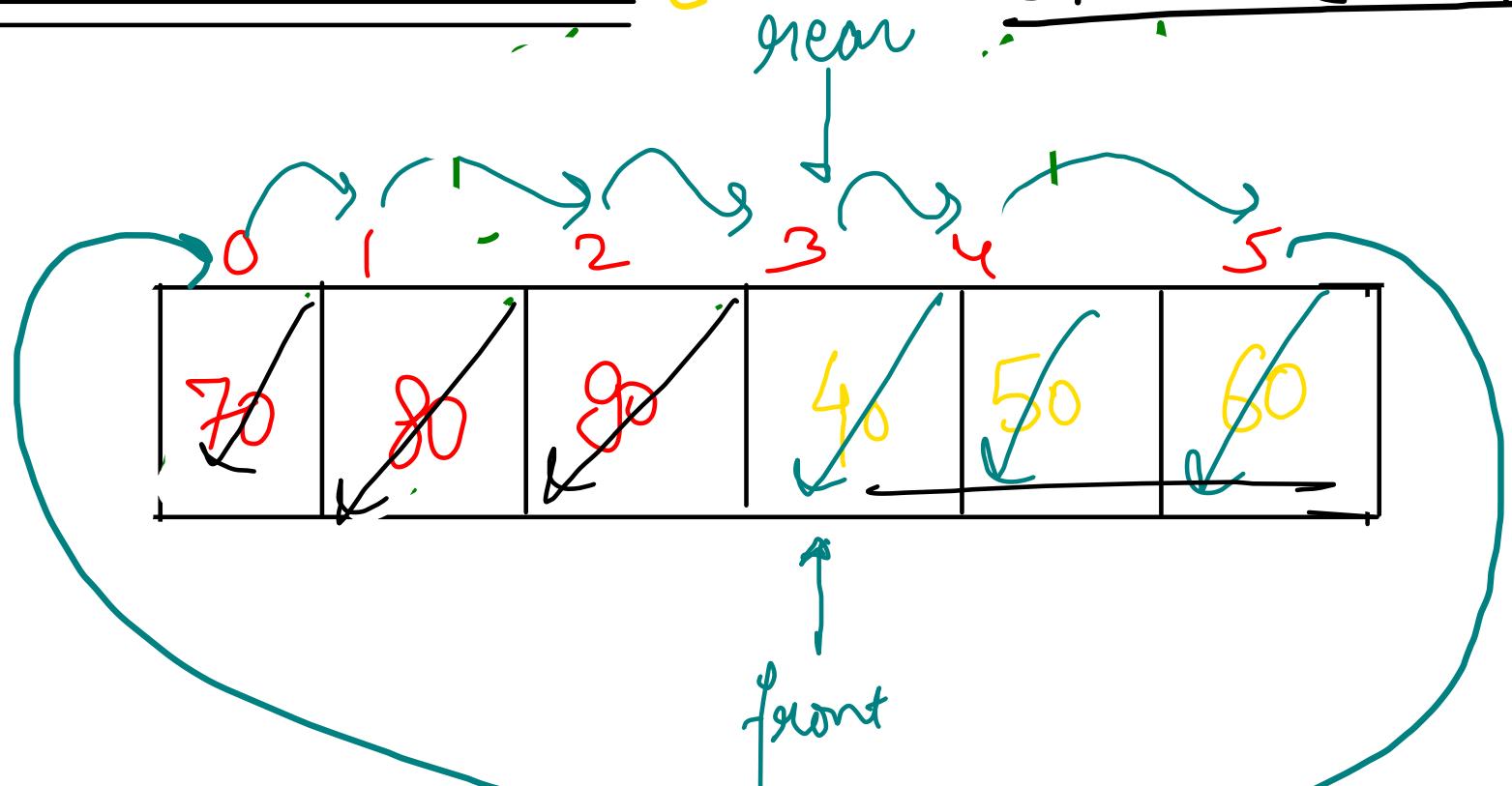
int size2() { → O(1)
    return (data.length - top2);
}
```

```
int top1() { → O(1)
    if(top1 == -1) {
        System.out.println("Stack underflow");
        return -1;
    }
    return data[top1];
} → O(1)

int top2() { → O(1)
    if(top2 == data.length) {
        System.out.println("Stack underflow");
        return -1;
    }
    return data[top2];
}
```

Normal Queue {Circular}

$$f/\gamma = (f(\gamma+1))/n$$



push(10)  
push(20)  
push(30)  
push(40)  
push(50)  
push(60)  
push(70)  
push(70) → Queue Overflow

pop() → 10  
pop() → 20  
pop() → 30  
push(70)  
push(80)  
push(90)  
push(100)

pop() → 40  
pop() → 50  
pop() → 60  
pop() → 70  
pop() → 80  
pop() → 90

```
int[] data;
int front;
int rear;
int size;

public CustomQueue(int cap) {
    data = new int[cap];
    front = 0;
    rear = 0;
    size = 0;
}

int size() {
    return size;
}
```

```
void display() {  $\mathcal{O}(N)$ 
    int counter = size();
    int idx = front;
    while(counter-- > 0){
        System.out.print(data[idx] + " ");
        idx = (idx + 1) % data.length;
    }
    System.out.println();
```

```
void add(int val) {  $\mathcal{O}(1)$ 
    if(size() == data.length){
        System.out.println("Queue overflow");
        return;
    }
    data[rear] = val;
    size++;
    rear = (rear + 1) % data.length;
}
```

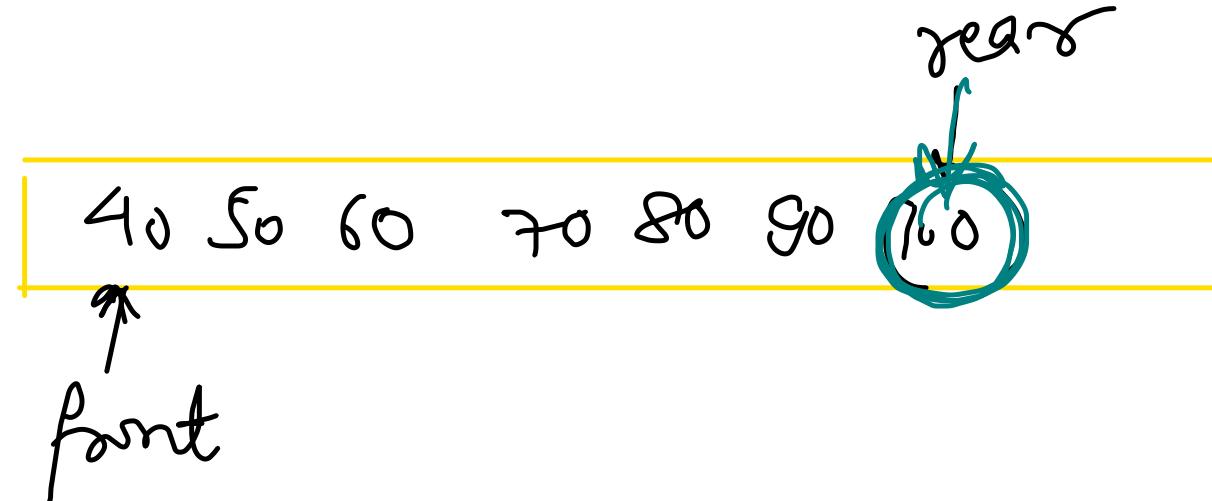
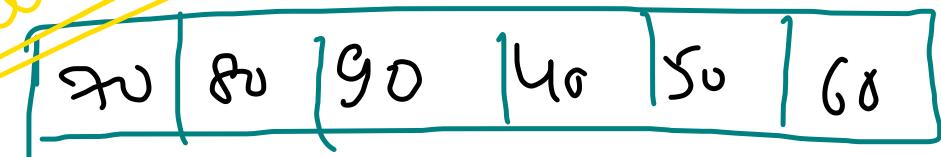
```
int remove() {  $\mathcal{O}(1)$ 
    if(size() == 0){
        System.out.println("Queue underflow");
        return -1;
    }

    int val = data[front];
    size--;
    front = (front + 1) % data.length;
    return val;
}

int peek() {  $\mathcal{O}(1)$ 
    if(size() == 0){
        System.out.println("Queue underflow");
        return -1;
    }

    int val = data[front];
    return val;
}
```

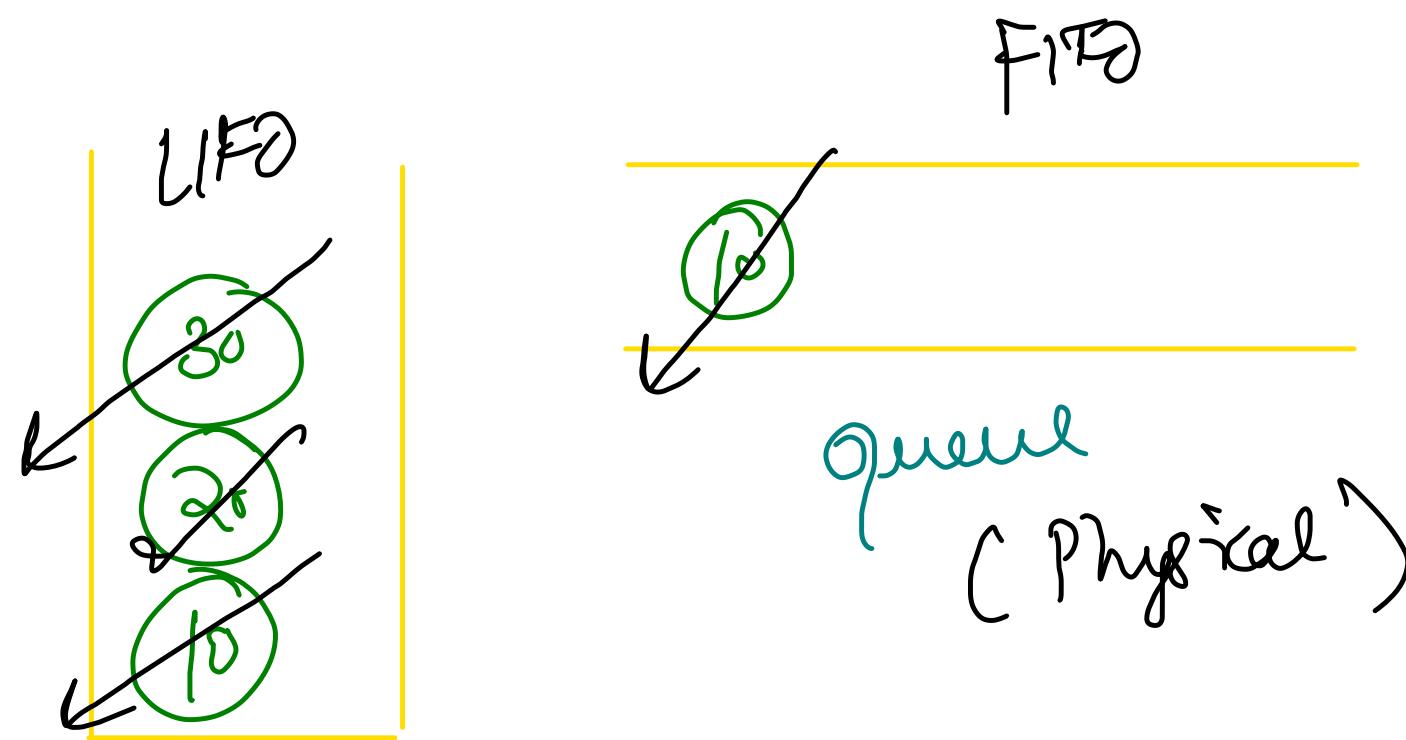
~~Dynamic Queue~~



Add → Doubling

```
void add(int val) {  
    if(size() == data.length){  
        int[] temp = new int[2 * size()];  
        |  
        int idx = front;  
        for(int j=0; j<size(); j++){  
            temp[j] = data[idx];  
            idx = (idx + 1) % data.length;  
        }  
  
        front = 0;  
        rear = size();  
        data = temp;  
    }  
  
    data[rear] = val;  
    size++;  
    rear = (rear + 1) % data.length;  
}
```

## Stack using Queue



Stack  
(logical)

- (1)  $\text{stk\_push}(10) \rightarrow O(1)$
- (2)  $\text{stk\_peek}() \rightarrow 10$   
    { 1pop, 1push }
- (3)  $\text{stk\_push}(20)$
- (4)  $\text{stk\_peek}() \rightarrow 20$   
    { 2pop, 2push }
- (5)  $\text{stk\_push}(30) \rightarrow O(N)$
- (6)  $\text{stk\_peek}() \rightarrow 30$   
    { 3pop, 3push }
- (7)  $\text{stk\_pop}()$   
    { 2pop, 1push }  
     $\rightarrow 10$
- (8)  $\text{stk\_pop}()$   
    { 1pop, 0push }

```

Queue<Integer> q;

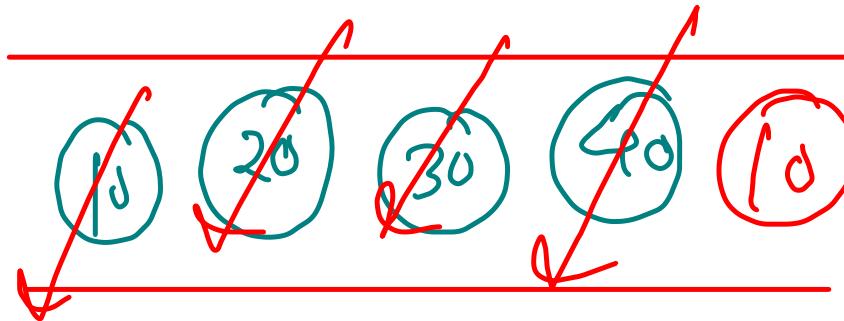
public QueueToStackAdapter() {
    q = new ArrayDeque<>();
}

int size() { → O(1) }
    return q.size();

void push(int val) { → O(1) }
    q.add(val);
}

```

Queue to Stack Adapter  
of Push Efficient



Val = → O(1) 10 20 30 40

i= → O(1)  
0 X 2  
3

Weekend  
Den

```

int pop() { → O(n)
    if(size() == 0){
        System.out.println("Stack underflow");
        return -1;
    }

    int val = 0;
    for(int i=0; i<size(); i++){
        val = q.remove();
        if(i < size())
            q.add(val);
    }
    return val;
}

```

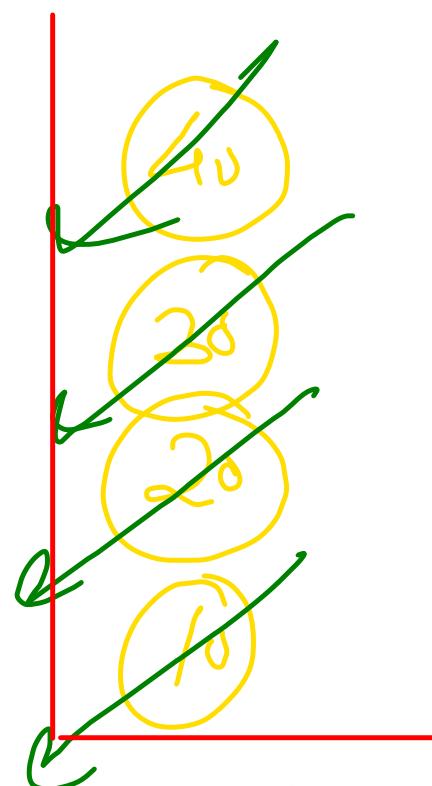
```

int top() { → O(n)
    if(size() == 0){
        System.out.println("Stack underflow");
        return -1;
    }

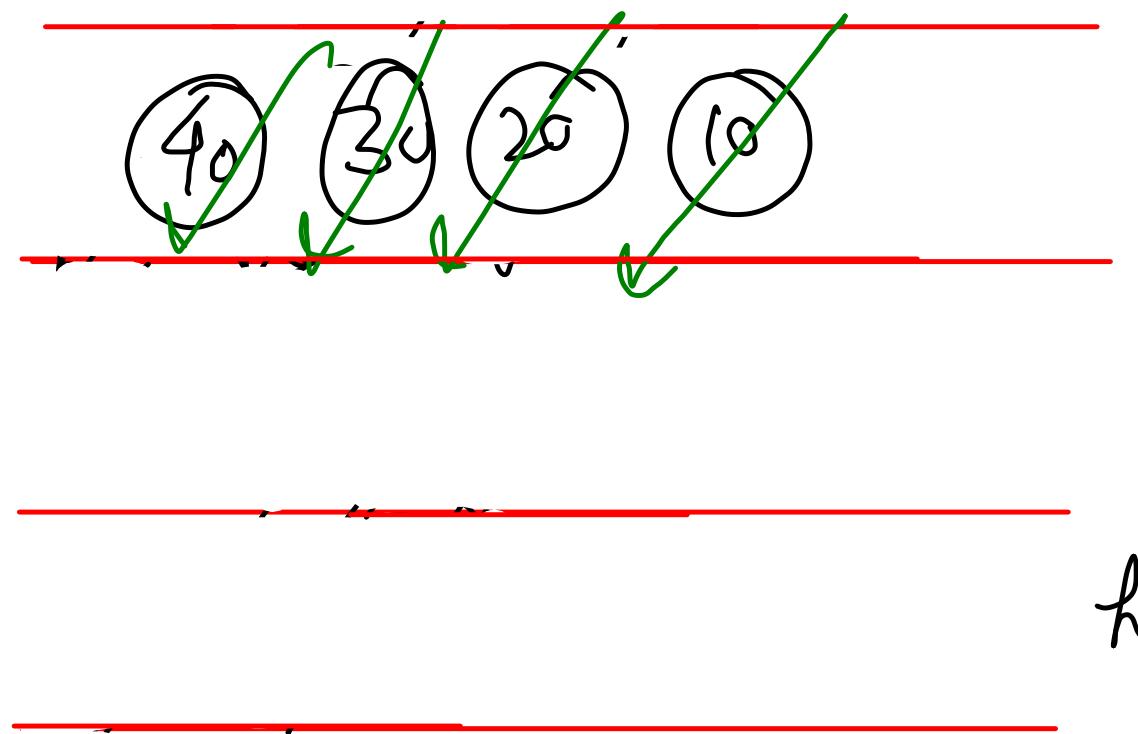
    int val = 0;
    for(int i=0; i<size(); i++){
        val = q.remove();
        q.add(val);
    }
    return val;
}

```

# Queue to Stack Adapter { Pop-Efficient }



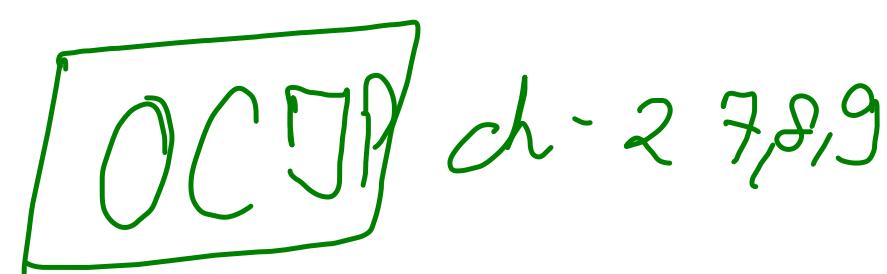
Logical  
(Stack)



Main Q

Queue  
of Actual  
Q

helper Q



ch-2 7,8,9

① q.push(40)  $\rightarrow \alpha(n)$   
 { 0.pop, 1.push }

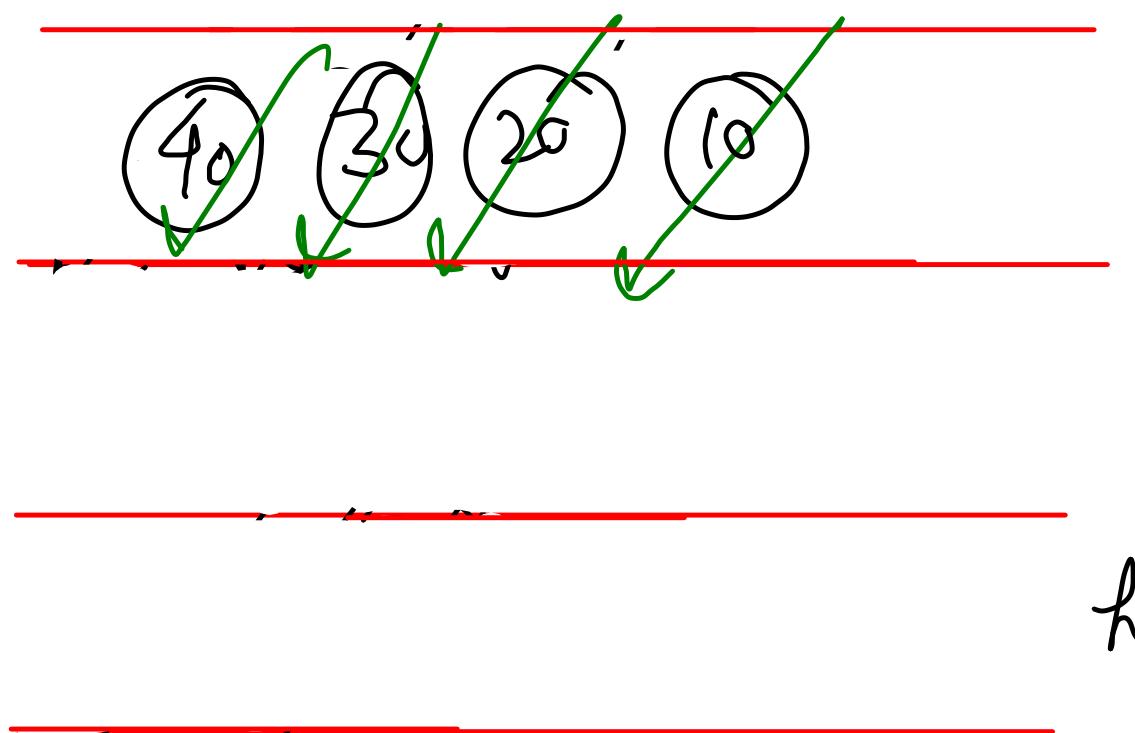
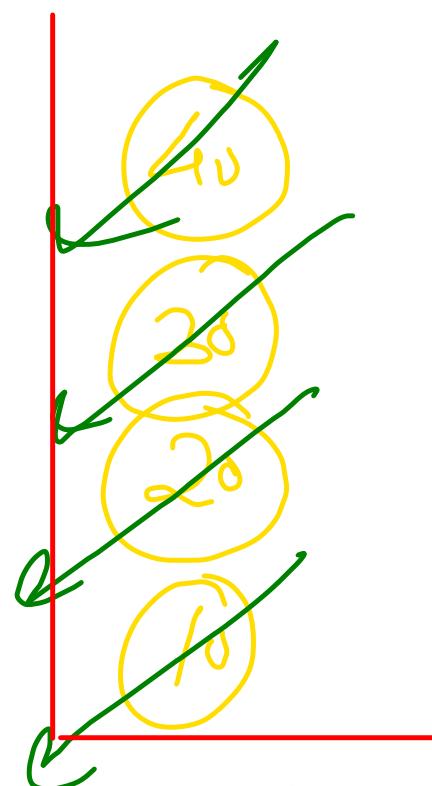
② q.push(30)  
 { 1.pop, 2.push }

③ q.push(20)  
 { 2.pop, 3.push }

④ q.push(10)  
 { 3.pop, 4.push }

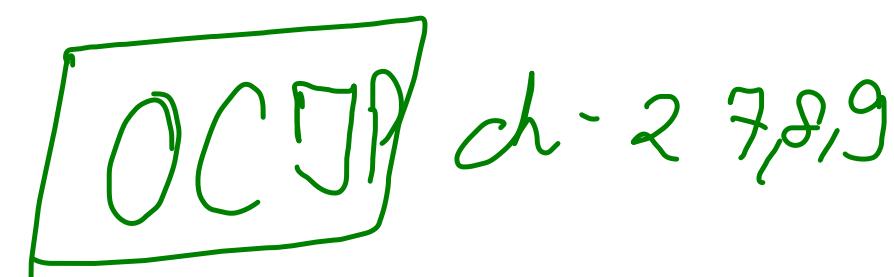
q.pop()  $\times 4$   
 $\rightarrow 80$

# Queue to Stack Adapter { Pop-Efficient }



Actual  
Queue

helper q



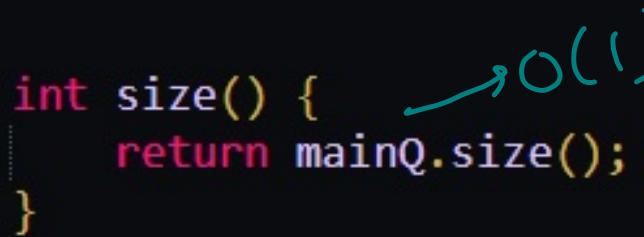
①  $q.push(10) \rightarrow \alpha(n)$   
 { 0.pop, 1.push }

②  $q.push(20)$   
 { 1.pop, 2.push }

③  $q.push(30)$   
 { 2.pop, 3.push }

④  $q.push(40)$   
 { 3.pop, 4.push }

$q.pop() \times 4$   
 ↪ 80

```
public static class QueueToStackAdapter {  
    Queue<Integer> mainQ;  
    Queue<Integer> helperQ;  
  
    public QueueToStackAdapter() {  
        mainQ = new ArrayDeque<>();  
        helperQ = new ArrayDeque<>();  
    }  
  
    int size() {   
        return mainQ.size();  
    }  
  
    void push(int val) {  
        while(size() > 0){  
            helperQ.add(mainQ.remove());  
        }  
        mainQ.add(val);  
        while(helperQ.size() > 0){  
            mainQ.add(helperQ.remove());  
        }  
    }  
}
```

$O(N)$

```
int pop() {   
    if(size() == 0){  
        System.out.println("Stack underflow");  
        return -1;  
    }  
    return mainQ.remove();  
}  
  
int top() {   
    if(size() == 0){  
        System.out.println("Stack underflow");  
        return -1;  
    }  
    return mainQ.peek();  
}
```

## Stack & Queue → Basic's

### • Stack Basic's

- Normal Stack
- Dynamic Stack
- using lh

### • Queue Basic's

- Normal Queue
- Dynamic Queue
- using lh

✓ Two stacks in Array

### • Stack using Queue

- Push efficient
- Pop Efficient

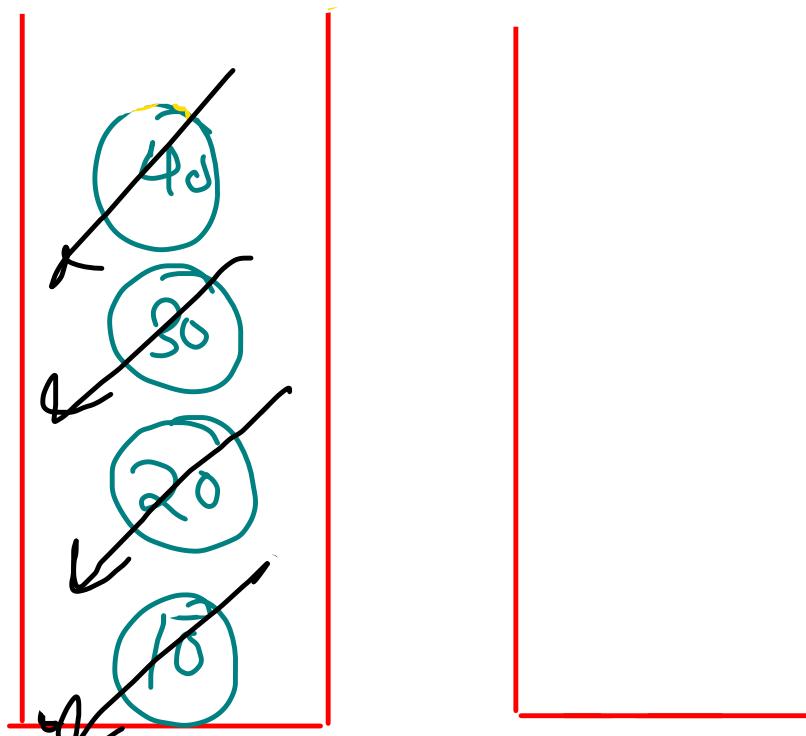
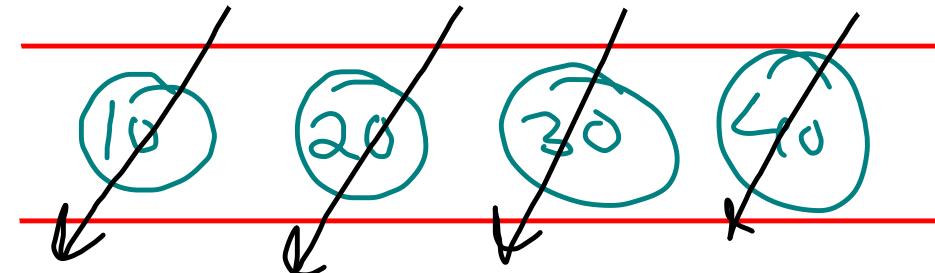
### • Queue using Stacks

- Push efficient
- Pop efficient

✓ Duplicate Brackets

✓ Balanced Brackets

# Queue Using Stack



Actual  
Stack

HelperStack

Push Efficient

Logical Queue

push(10) → O(1)

push(20) → O(1)

push(30) → O(1)

push(40) → O(1)

peek() → 10

↳ helper { N pop, O(N) push }

pop() → 10

↳ { N pop, (n-1) push }

push() → 20

{ N pop, n-1 push }  
O(n)

pop() → 30

{ n pop, N-1 push }

pop() → 40

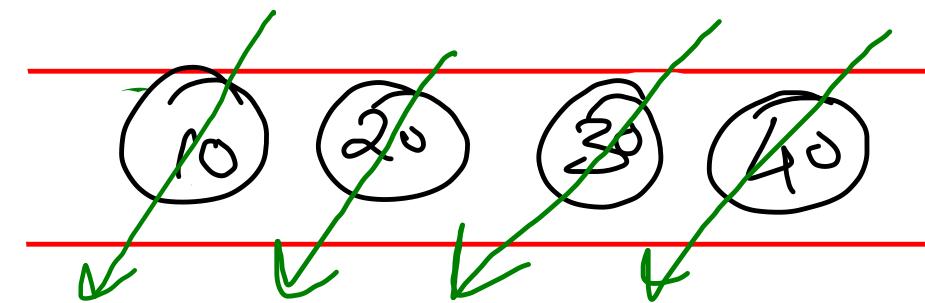
pop() → Queue Underflow

Dynamic

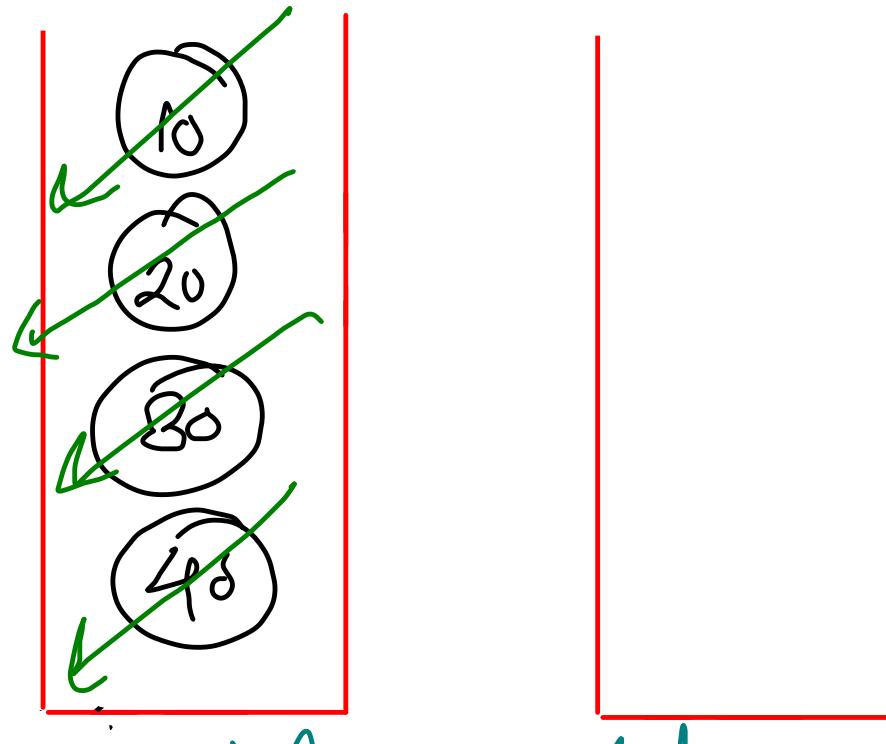
```
public static class StackToQueueAdapter {  
    Stack<Integer> mainS;  
    Stack<Integer> helperS;  
  
    public StackToQueueAdapter() {  
        mainS = new Stack<>();  
        helperS = new Stack<>();  
    }  
  
    int size() { → O(1)  
        return mainS.size();  
    }  
  
    void add(int val) { → O(1)  
        mainS.push(val);  
    }  
}
```

```
int remove() { → O(N)  
    if(mainS.size() == 0){  
        System.out.println("Queue underflow");  
        return -1;  
    }  
  
    while(mainS.size() > 0)  
        helperS.push(mainS.pop());  
  
    int val = helperS.pop();  
    while(helperS.size() > 0)  
        mainS.push(helperS.pop());  
  
    return val;  
}  
  
int peek() { → O(N)  
    if(mainS.size() == 0){  
        System.out.println("Queue underflow");  
        return -1;  
    }  
  
    while(mainS.size() > 0)  
        helperS.push(mainS.pop());  
  
    int val = helperS.peek();  
    while(helperS.size() > 0)  
        mainS.push(helperS.pop());  
  
    return val;  
}
```

Queue using Stack { Pop Efficient }

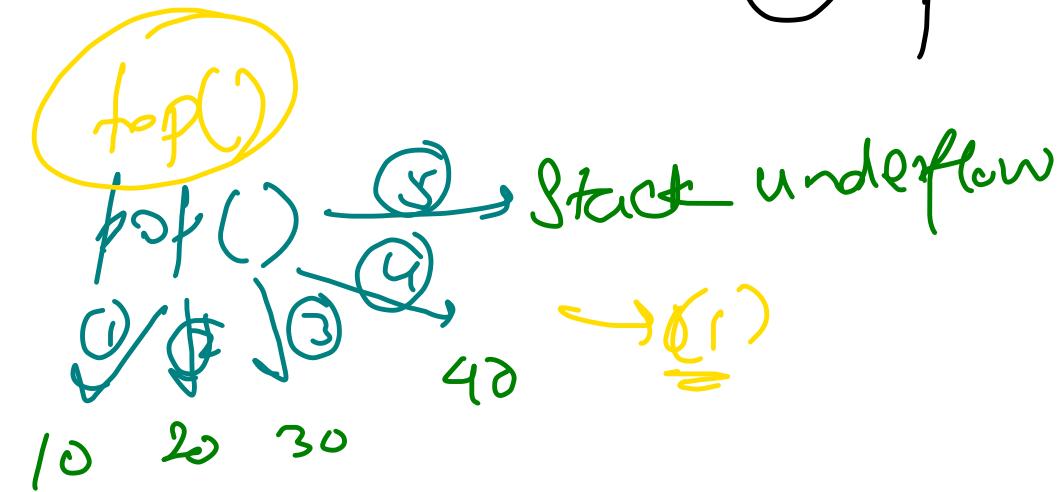


# Logical (Quesn)



(Actual)

- ① push (10)
  - ② push (20)
    - { insert At Bv from }
    - { 1 pop, 2 push }
  - ③ push (30)
    - { 2 pop, 3 push }
  - ④ push (40)  $\{ O(n) \}$ 
    - { 3 pop, 4 push }



```
Stack<Integer> mainS;
Stack<Integer> helpers;

public StackToQueueAdapter() {
    mainS = new Stack<>();
    helpers = new Stack<>();
}

int size() { → O(1)
    return mainS.size();
}

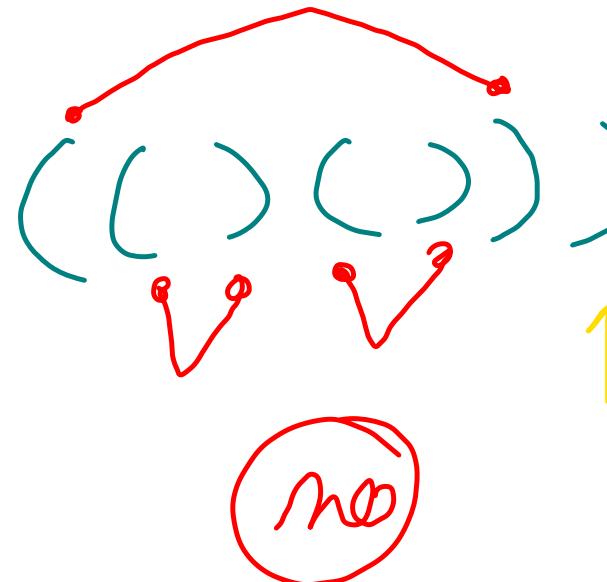
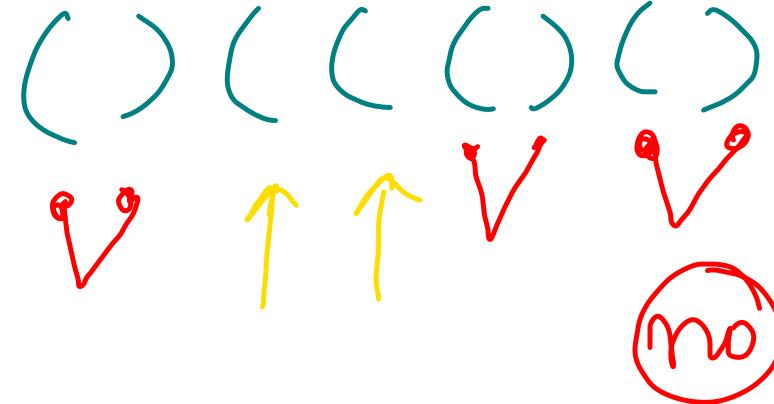
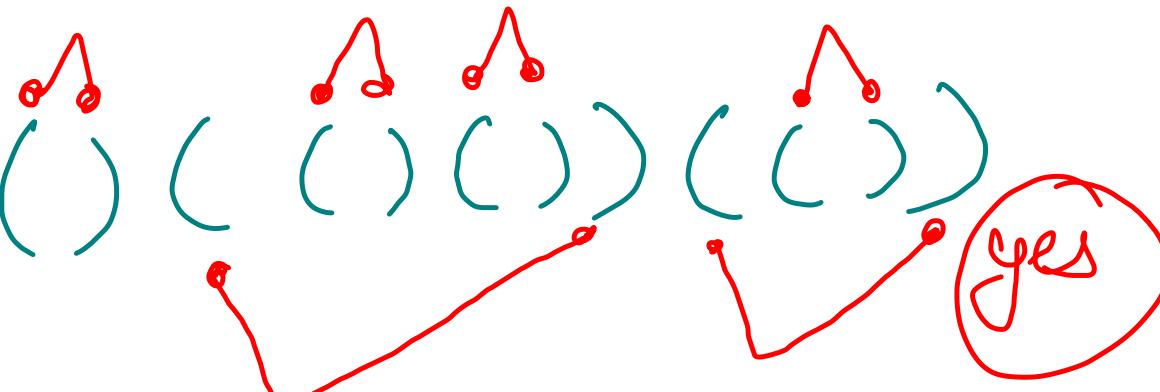
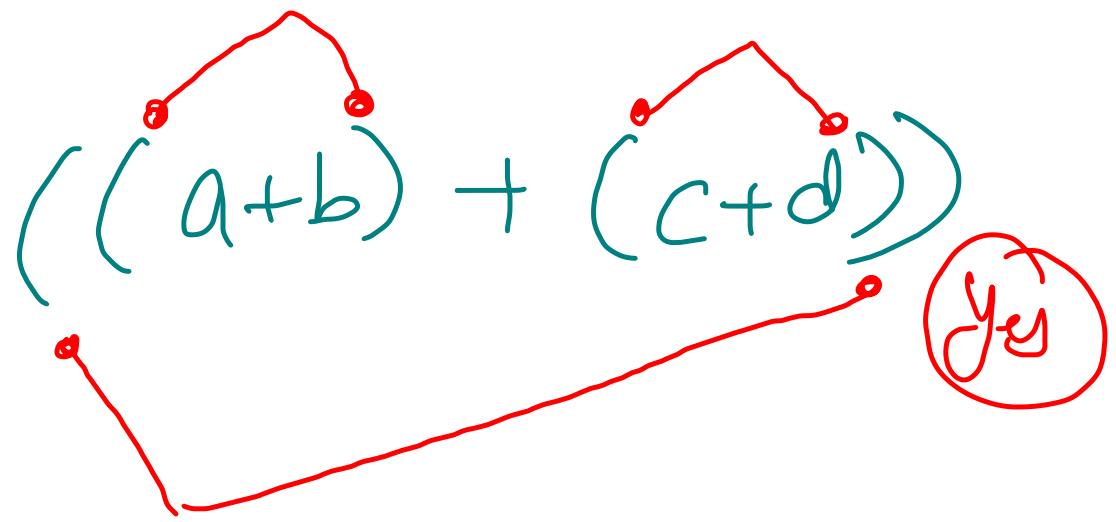
void add(int val) { → O(N)
    while(mainS.size() > 0){
        helpers.push(mainS.pop());
    }
    mainS.push(val);
    while(helpers.size() > 0){
        mainS.push(helpers.pop());
    }
}
```

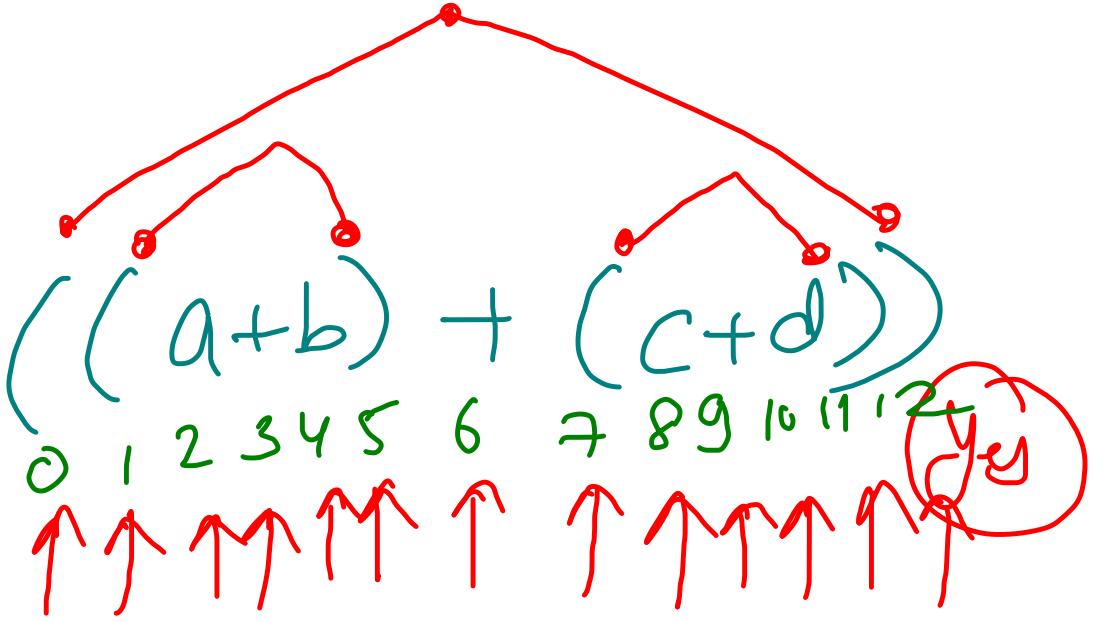
```
int remove() { → O(1)
    if(size() == 0){
        System.out.println("Queue underflow");
        return -1;
    }
    return mainS.pop();
}

int peek() { → O(1)
    if(size() == 0){
        System.out.println("Queue underflow");
        return -1;
    }
    return mainS.peek();
}
```

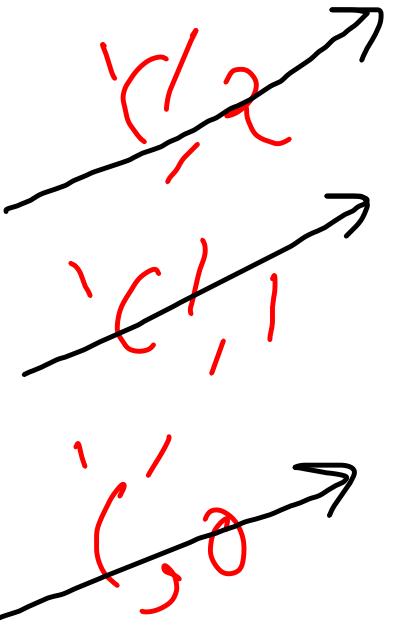
break till 10:00 PM

# Balanced Brackets

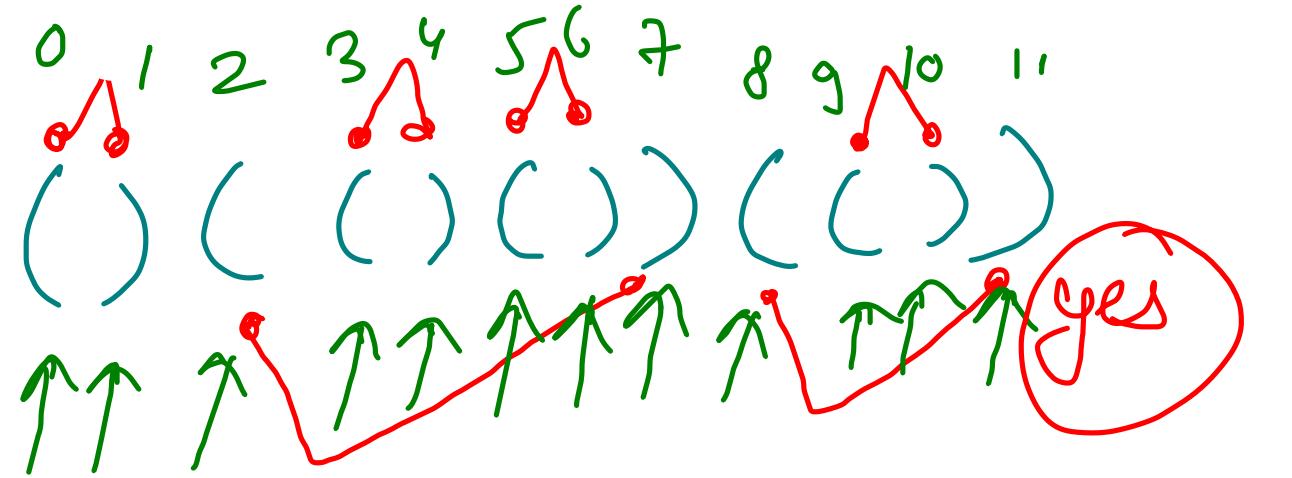




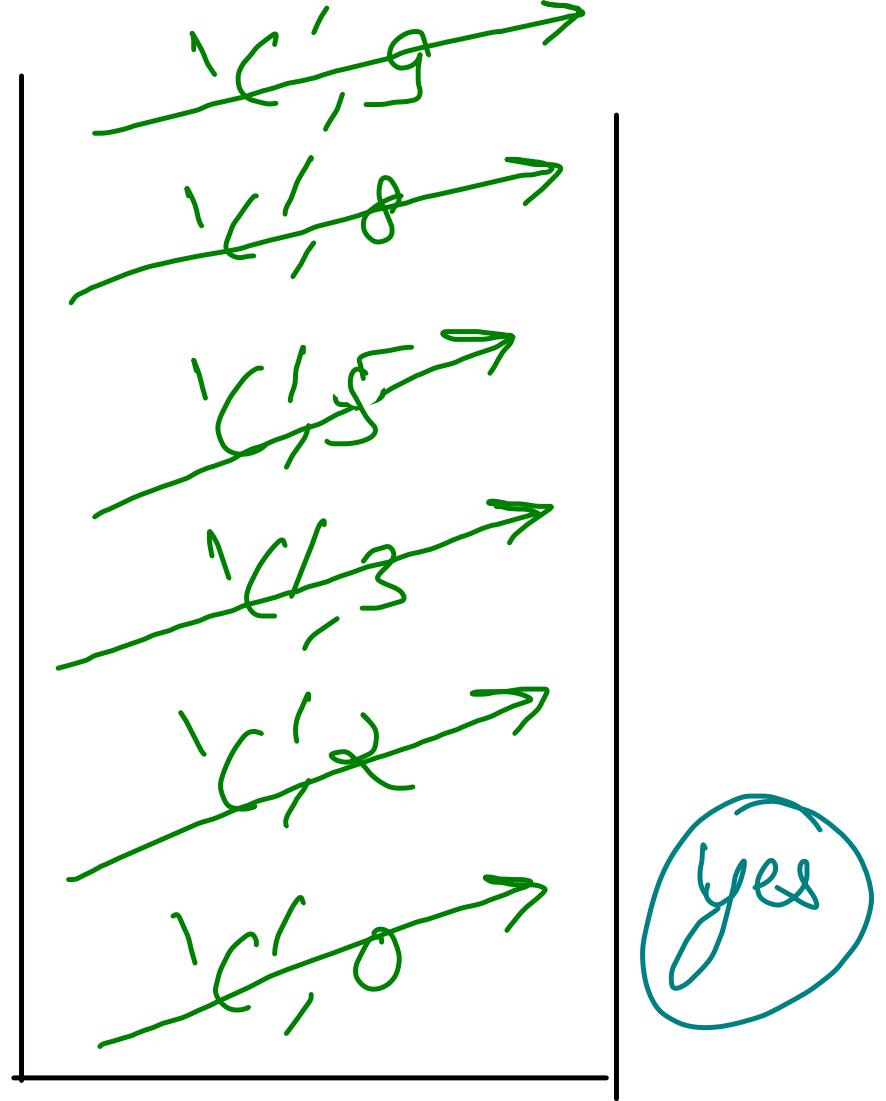
unbalanced char index  
Stack overflow

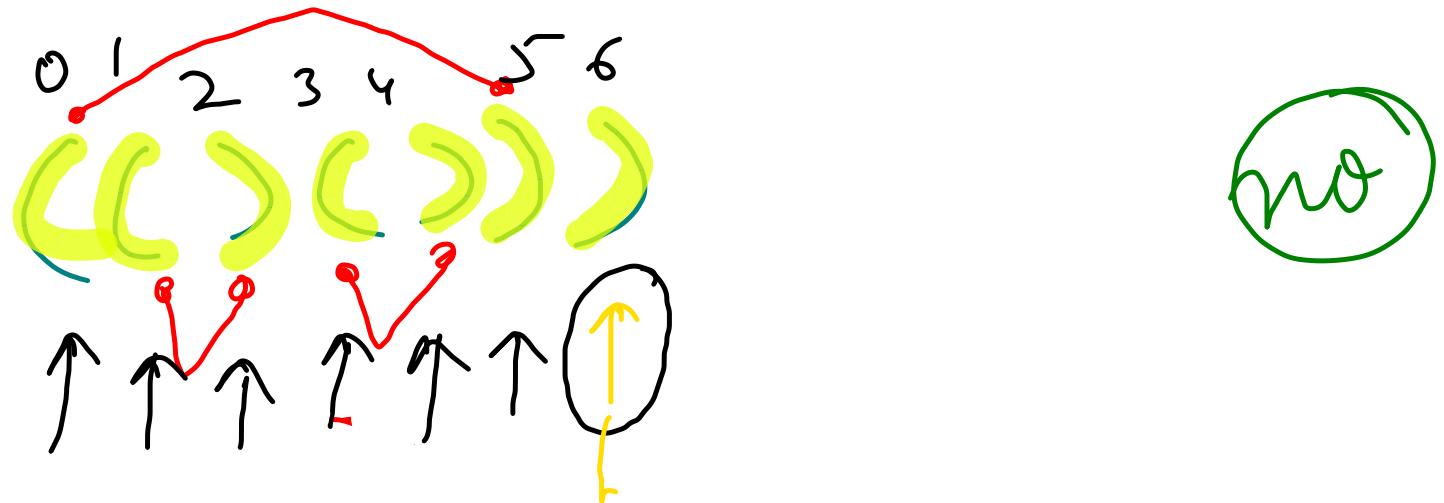


- ① opening braces  $\Rightarrow$  push
- ② closing braces  $\rightarrow$   $stk \cdot top() == 'C'$   
 $\Rightarrow stk.pop()$
- ③ neither opening nor closing  
(a-z, 0-9, +, -, /, \*)



- ① opening braces  $\Rightarrow$  push
- ② closing braces  $\rightarrow$   $8t_k \cdot f_{push}() = 'C'$   
 $\Rightarrow 8t_k \cdot f_{pop}()$
- ③ neither opening nor closing  
 $(a-z, 0-9, +, -, /, *, )$

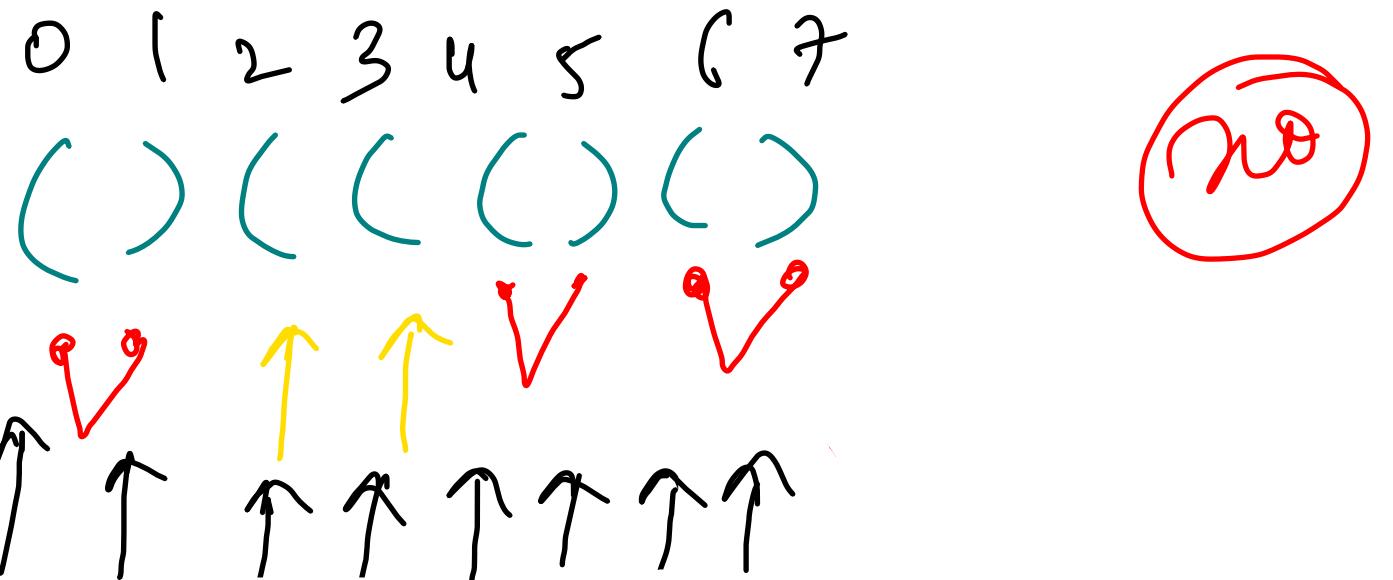




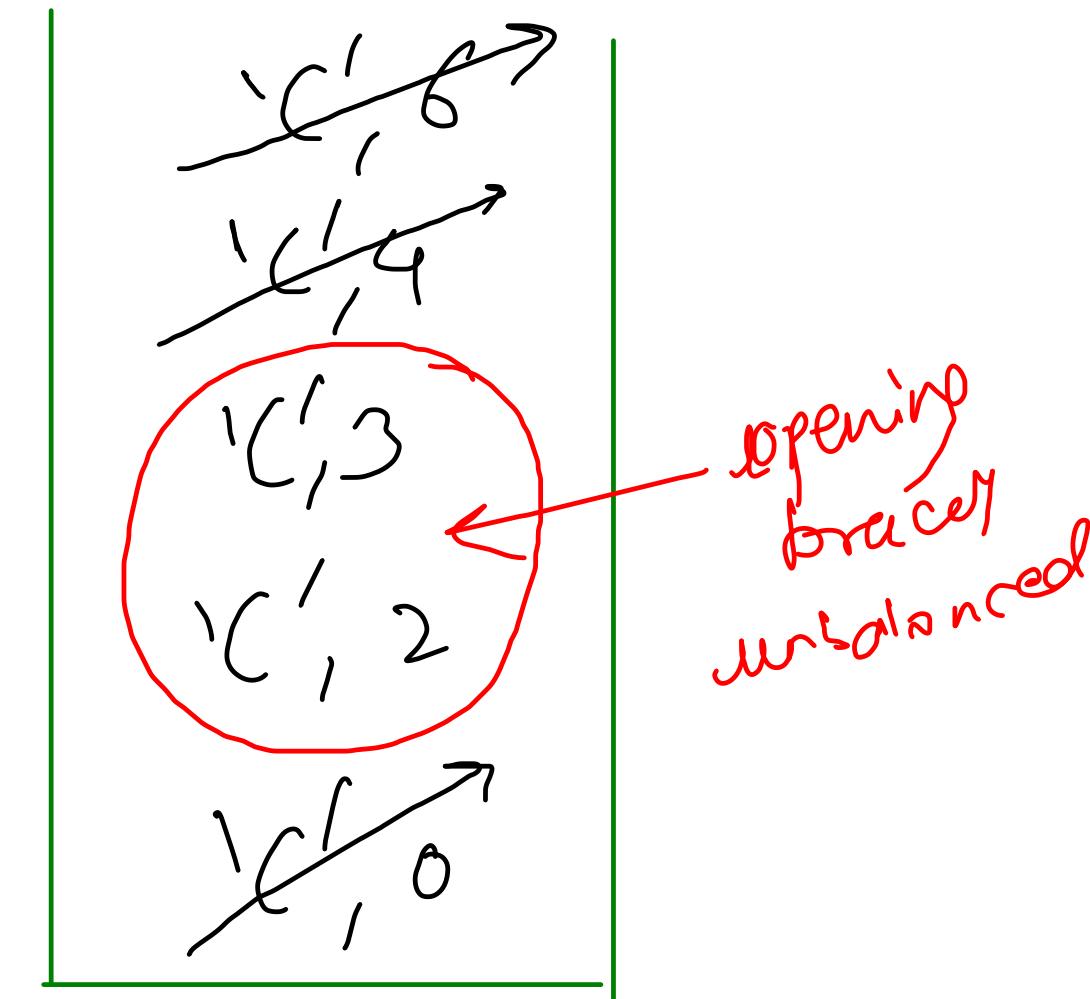
- ① opening braces  $\Rightarrow$  push
- ② closing braces  $\Rightarrow$   $stack.pop() = 'C'$   
 $\Rightarrow stack.pop()$   
 $stack.size = 0 \Rightarrow$  no
- ③ neither opening nor closing  
 $(a-z, 0-9, +, -, /, *)$

$'\rangle'$   
*unbalanced*

~~'C', 3~~  
~~'C', 1~~  
~~'C', 0~~

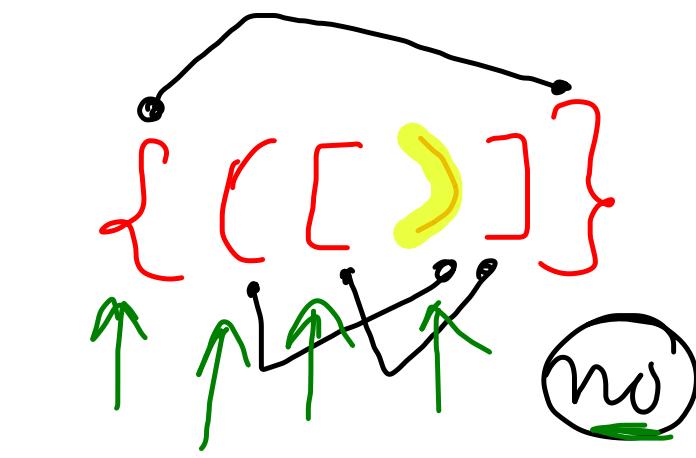
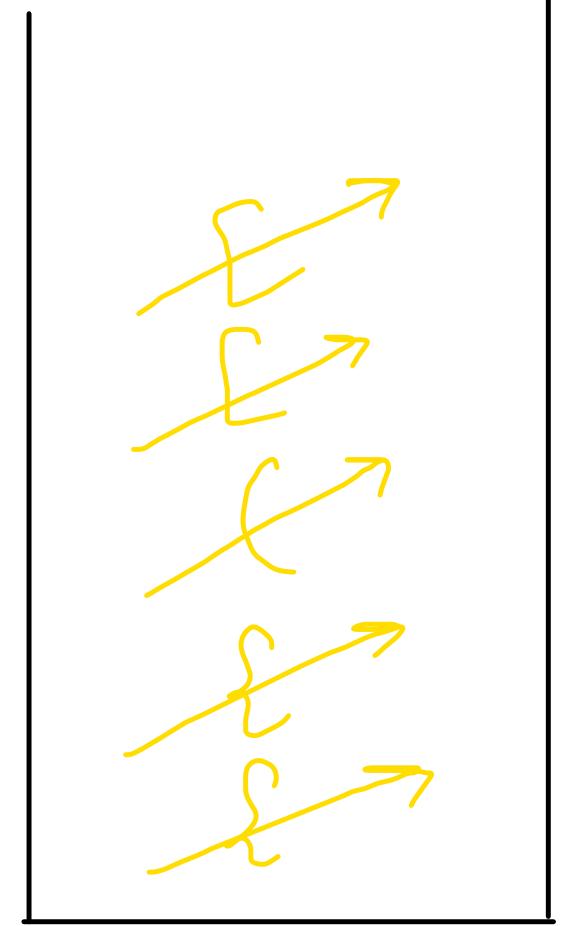
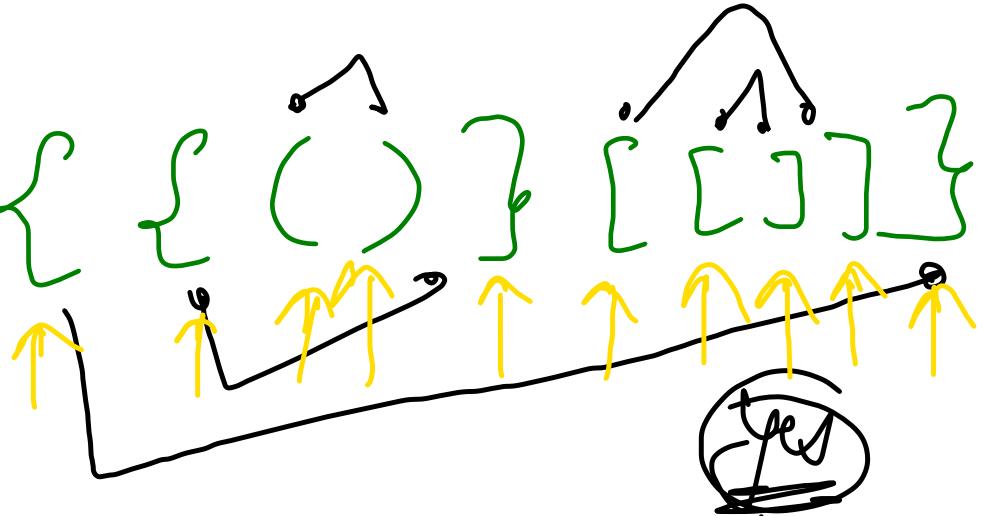
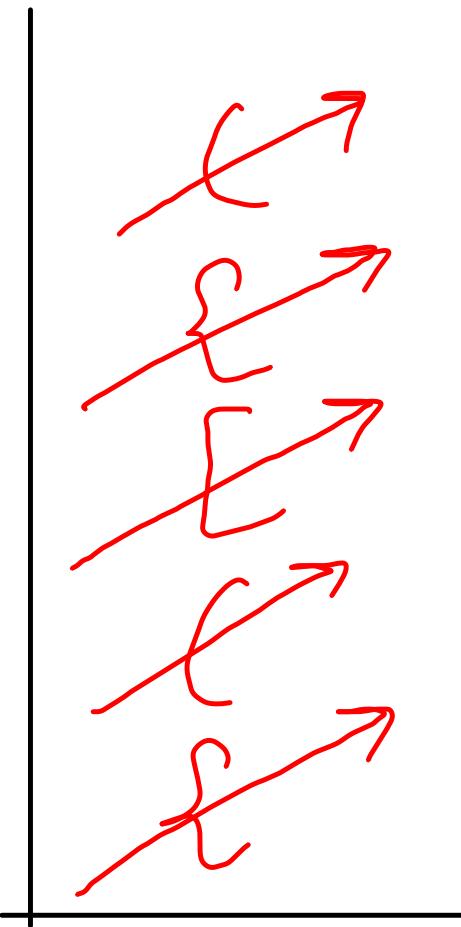
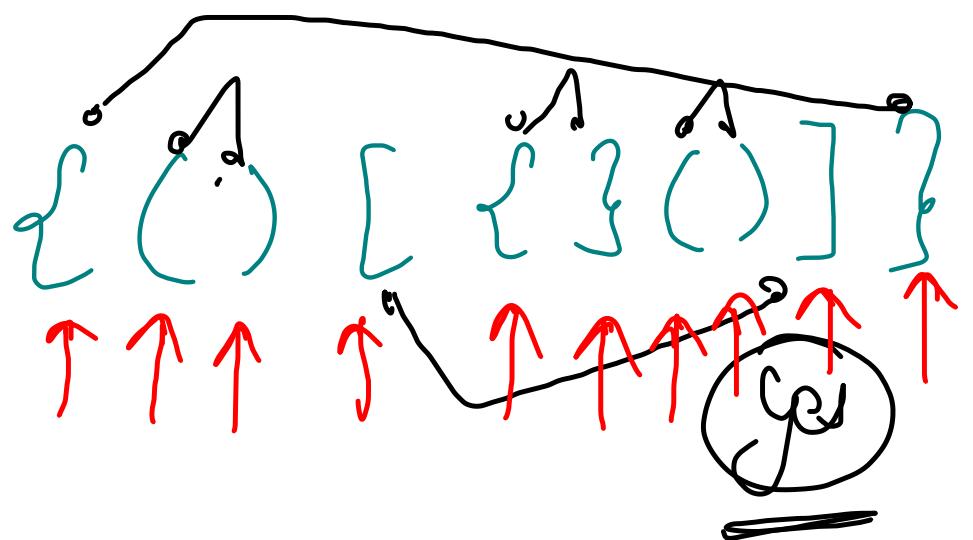


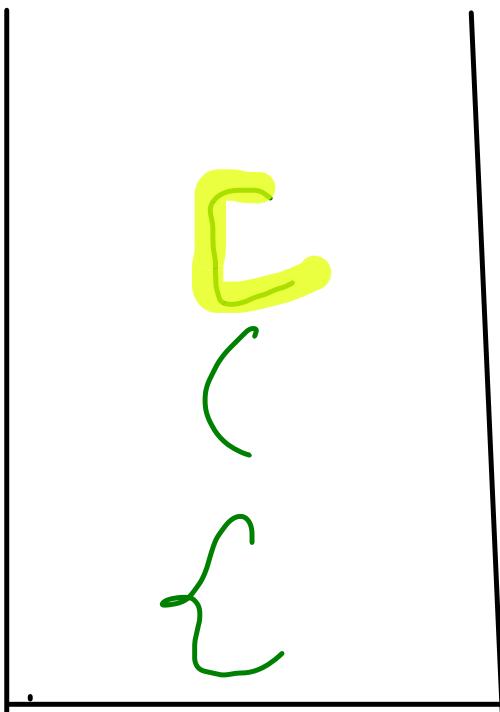
- ① opening braces  $\Rightarrow$  push
  - ② closing braces  $\rightarrow$   $stk \cdot top() == \text{Same type}$   
 $\Rightarrow stk.pop()$   
 $\text{diff type, size} \Rightarrow \text{no}$
  - ③ neither opening nor closing  
 $(a-z, 0-9, +, -, /, *)$   
do nothing
- After traversal
- if  $stk.size = 0$   
return true  
return false;  $\text{no}$  ' $'$  unbalanced



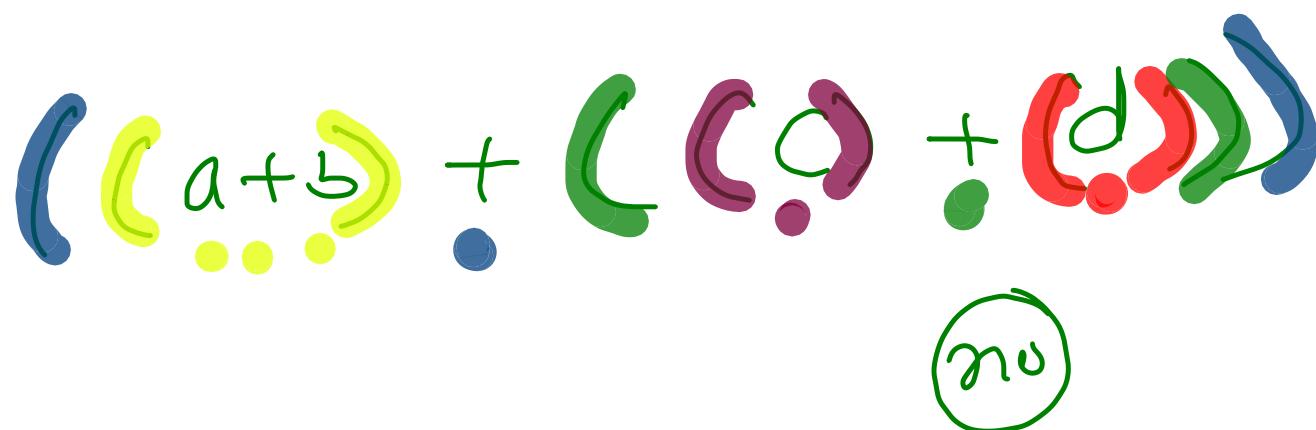
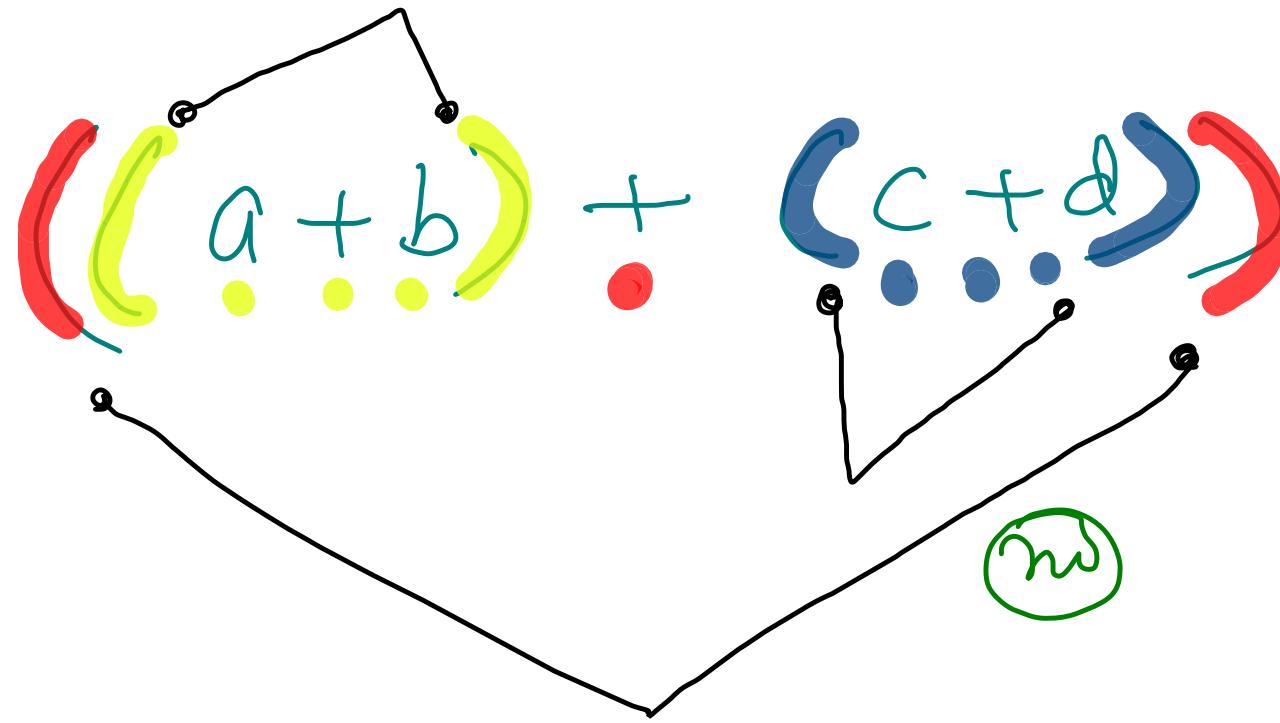
```
Stack<Character> stk = new Stack<>();  
for(int i=0; i<s.length(); i++){  
    char ch = s.charAt(i);  
  
    if(ch == ')'){  
        if(stk.isEmpty() || stk.peek() != '('){  
            return false;  
        }  
        stk.pop();  
    } else if(ch == '}'){  
        if(stk.isEmpty() || stk.peek() != '{'){  
            return false;  
        }  
        stk.pop();  
    } else if(ch == ']'){  
        if(stk.isEmpty() || stk.peek() != '['){  
            return false;  
        }  
        stk.pop();  
    } else {  
        stk.push(ch);  
    }  
  
return (stk.size() == 0) ? true : false;
```

$\mathcal{O}(N)$

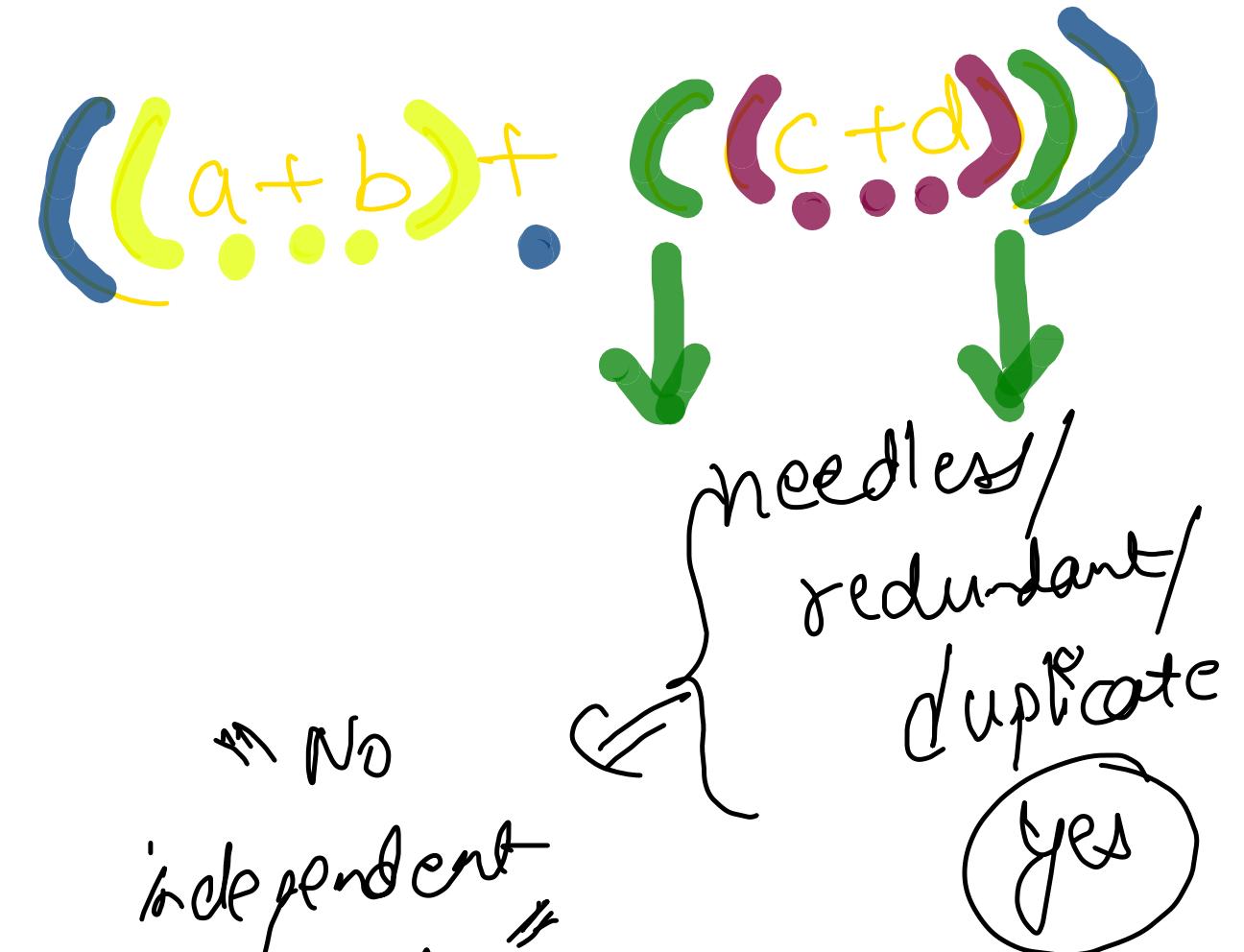


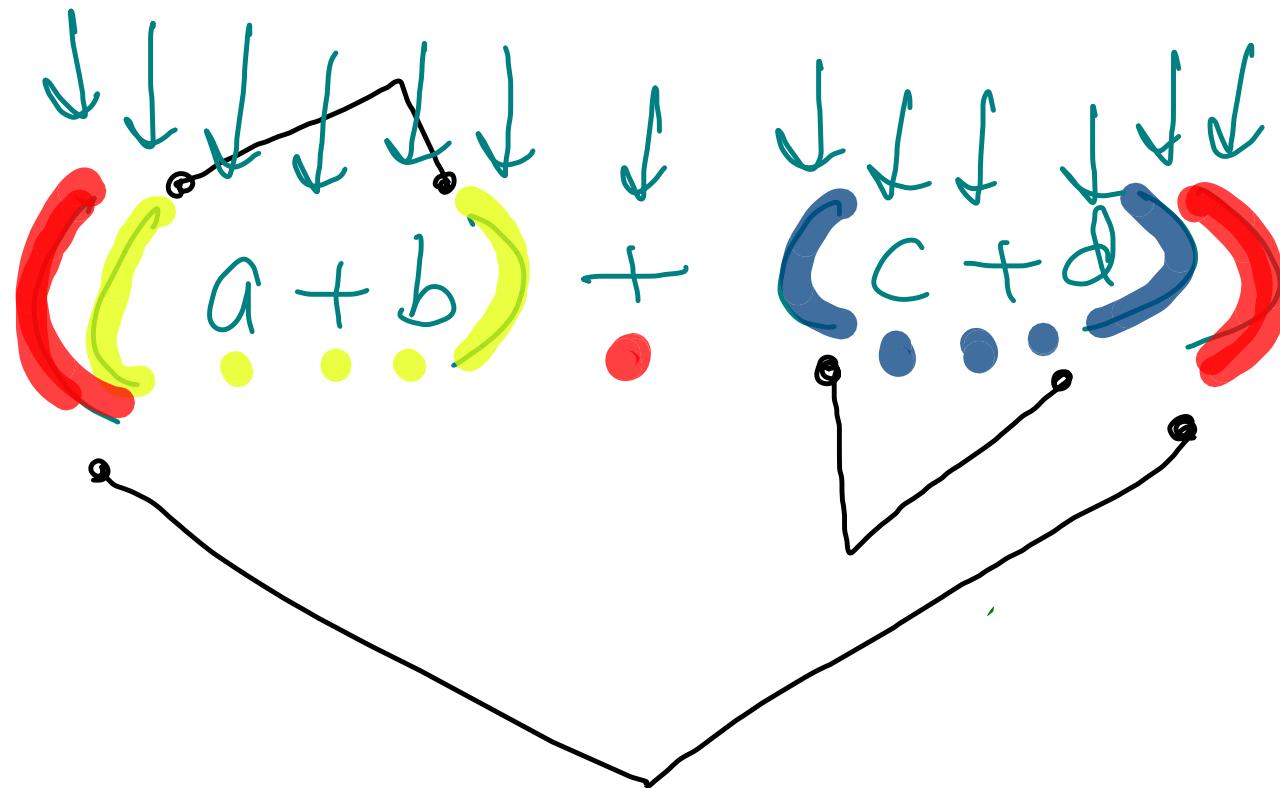
$$(a + [b + c] + d)$$


Redundant / Duplicate / Needless / Extra Brackets

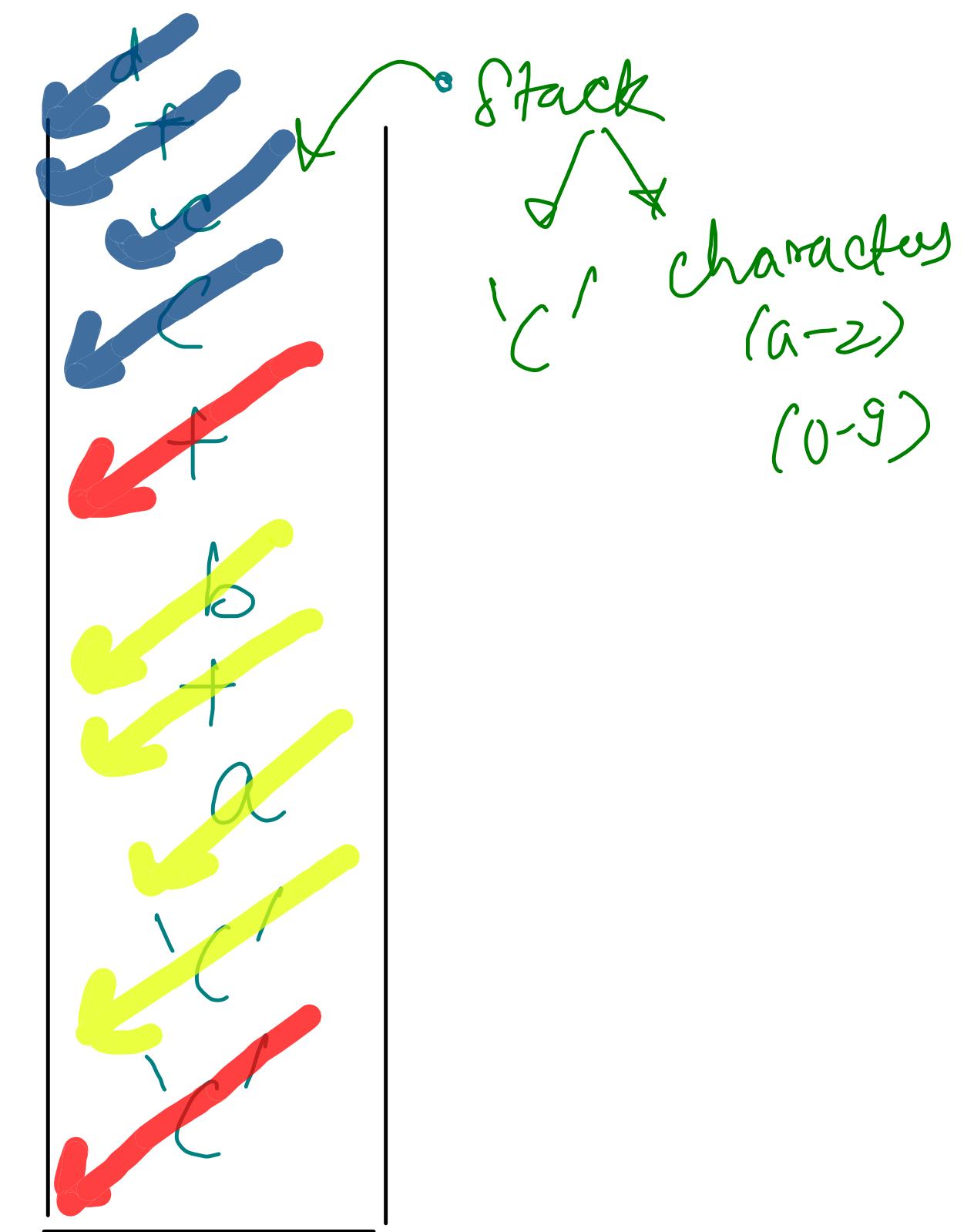


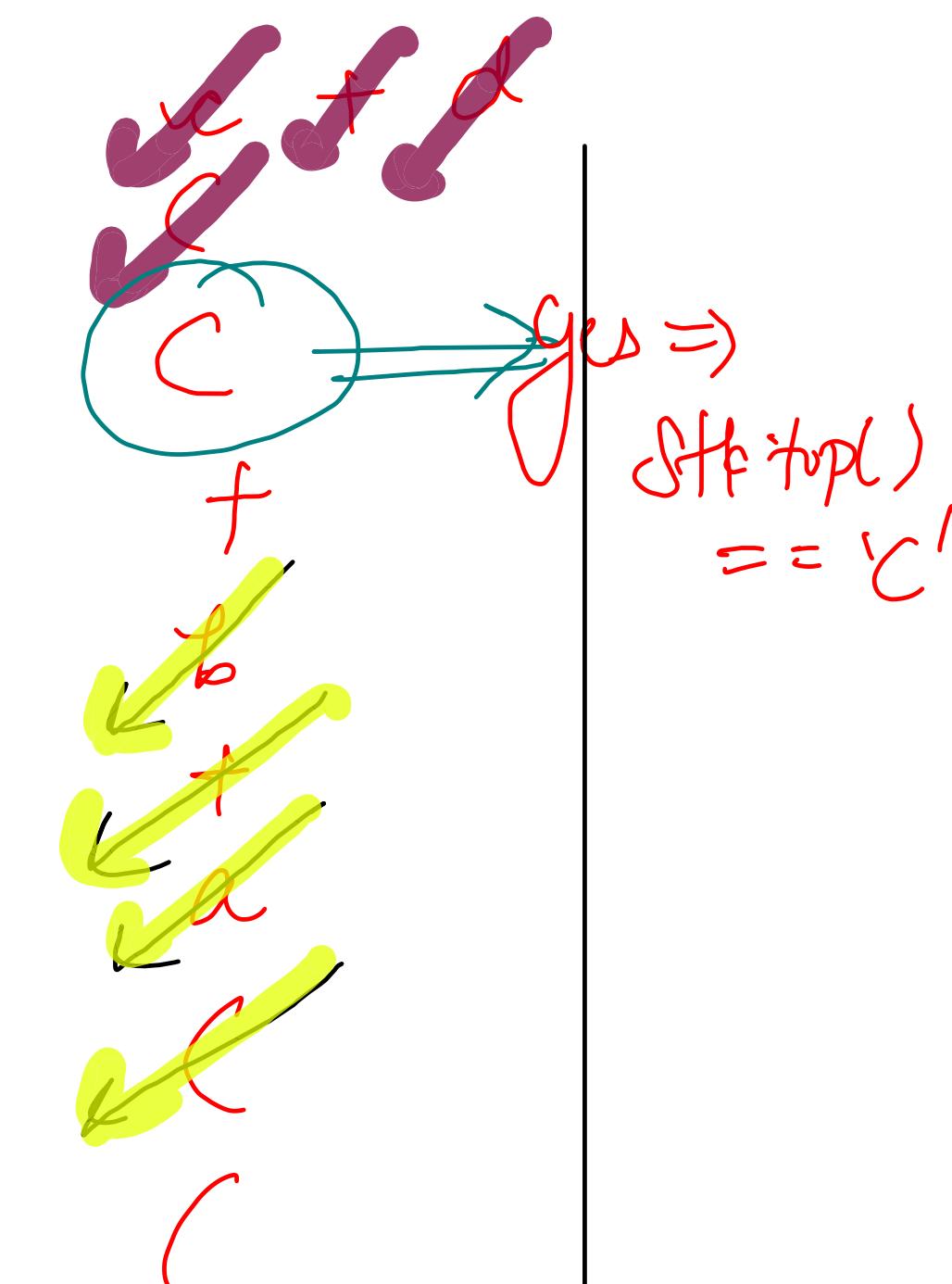
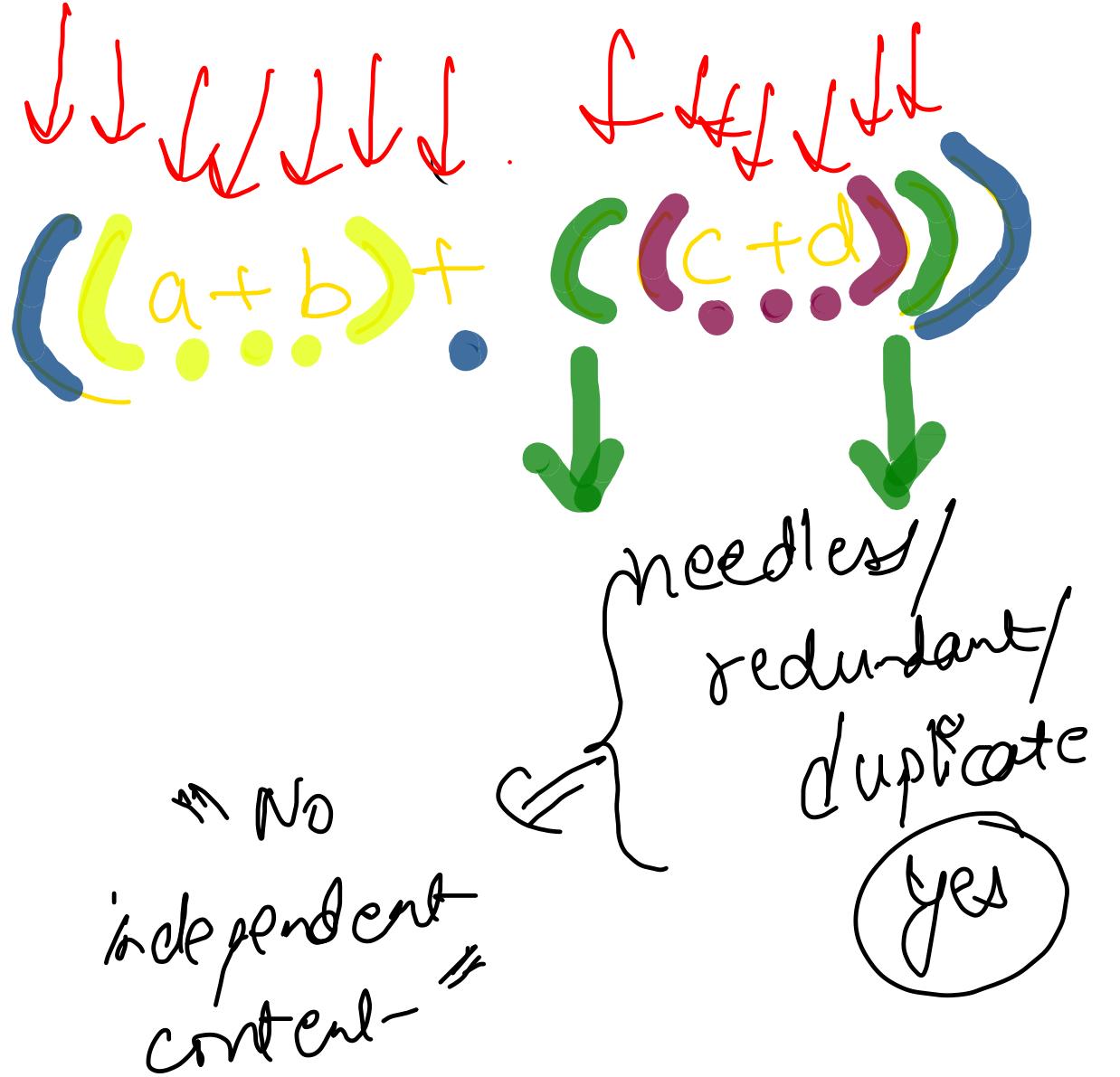
↑ No  
independent  
content - //





no redundant  
braces





$O(N)$  Time,  $O(N)$  auxiliary space (Stack)

```
Stack<Character> stk = new Stack<>();
for(int i=0; i<str.length(); i++){
    char ch = str.charAt(i);

    if(ch == ')'){
        if(stk.peek() == '('){
            // No Independent braces
            System.out.println("true");
            return;
        }

        while(stk.peek() != '('){
            stk.pop();
        }

        stk.pop(); // ')' is balanced, hence pop
    } else stk.push(ch);
}

System.out.println("false");
```

## Lecture ④ { Wednesday }

- Next Greater to Right

HW

NGE to Left

NSE to Right

NSE to Left

- Stock Span

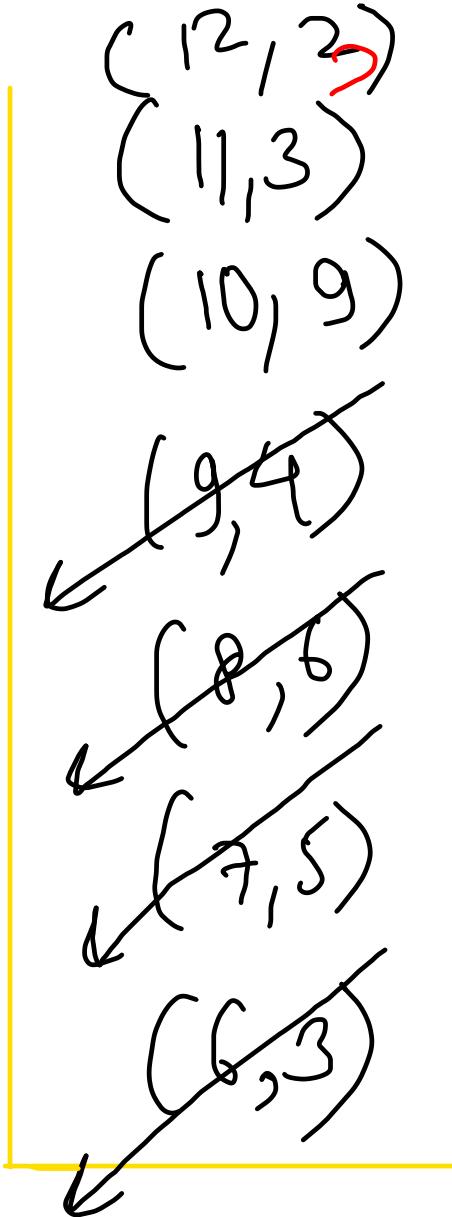
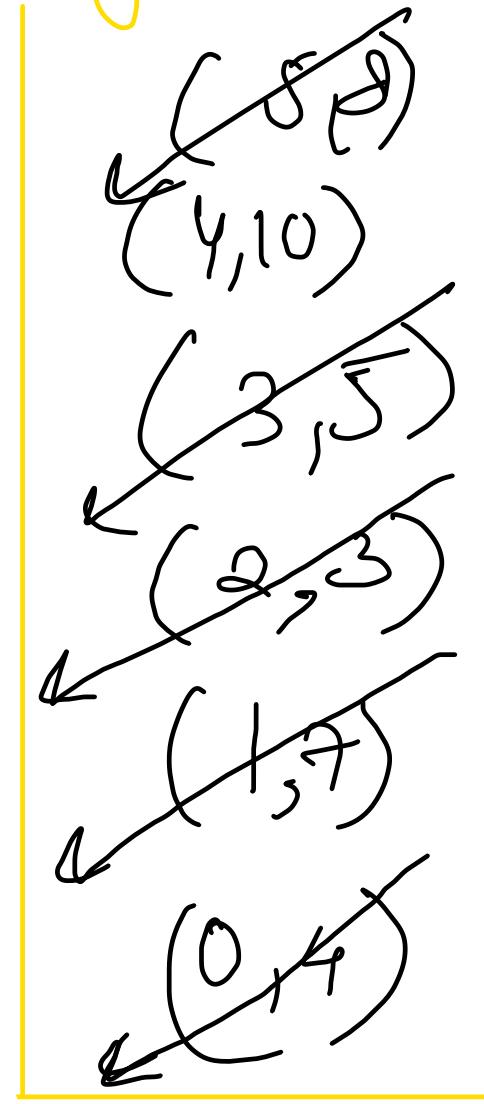
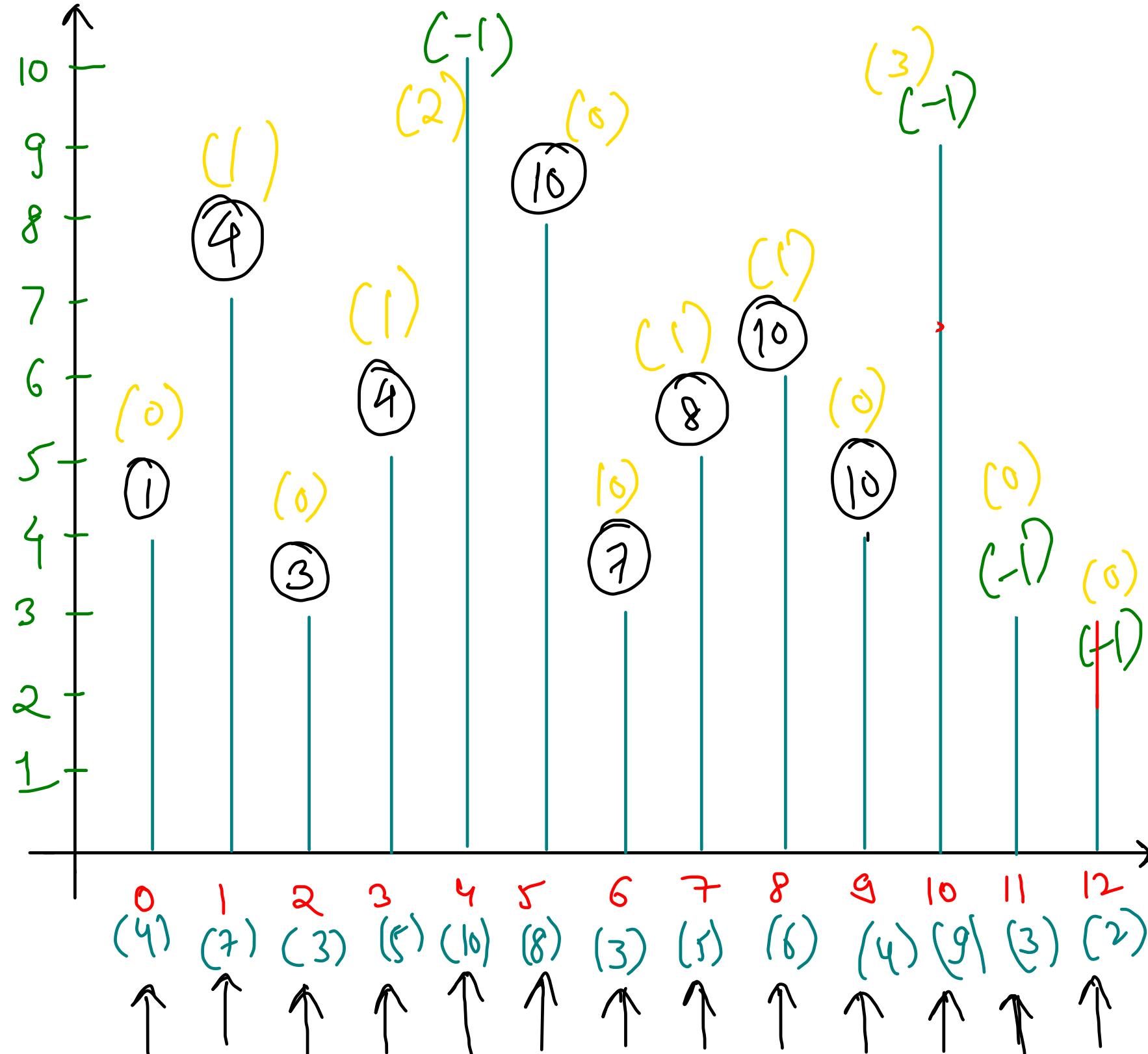
- Largest Histogram

- Sliding window  
maximum



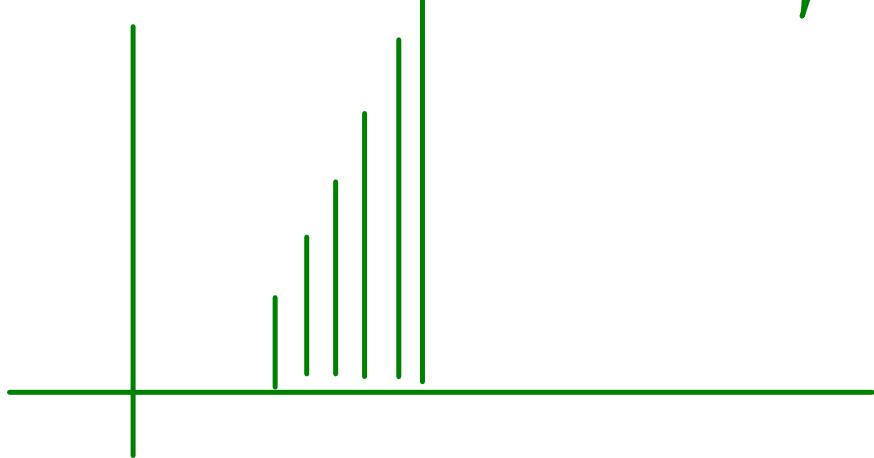
Interview Specific Problems

# Next Greater Element to the right



→ for those whose elements NGE doesn't exist

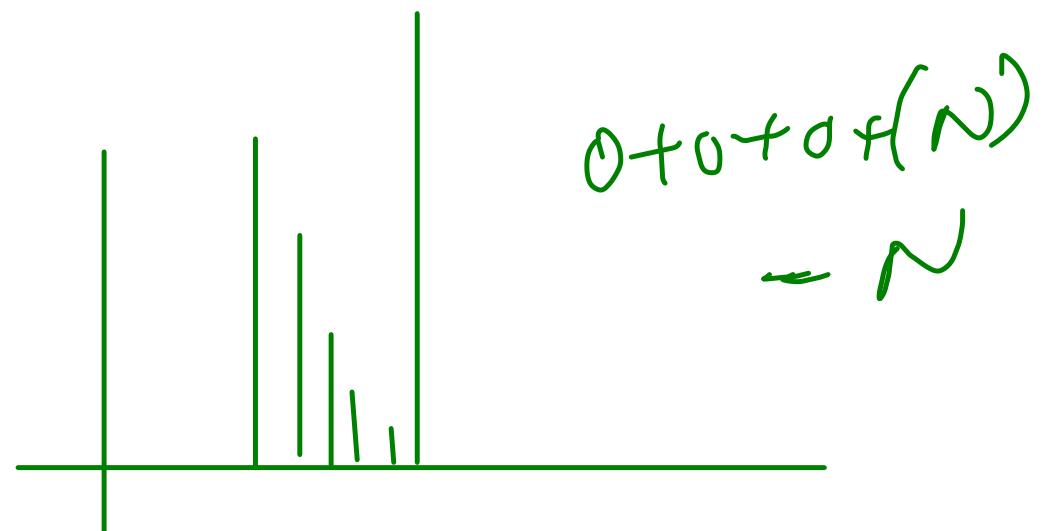
$$1+1+1+1+1+1+1 = N$$



$O(N)$  Time Comp

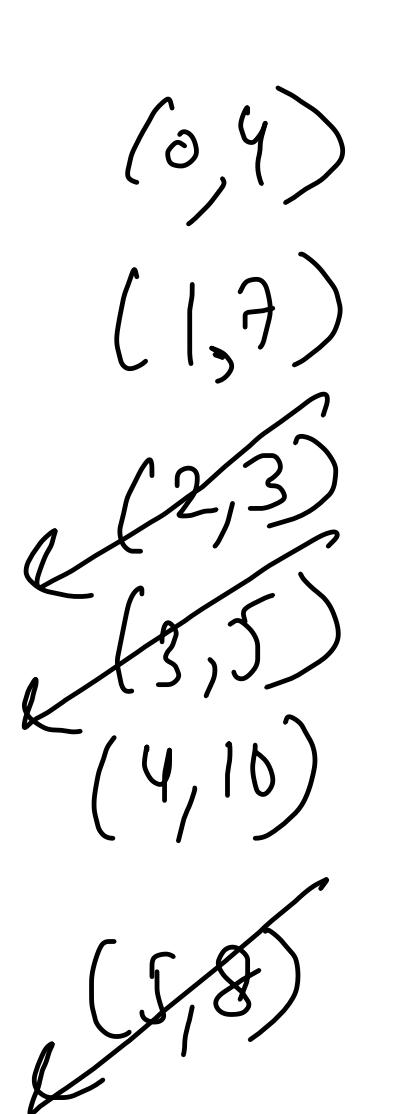
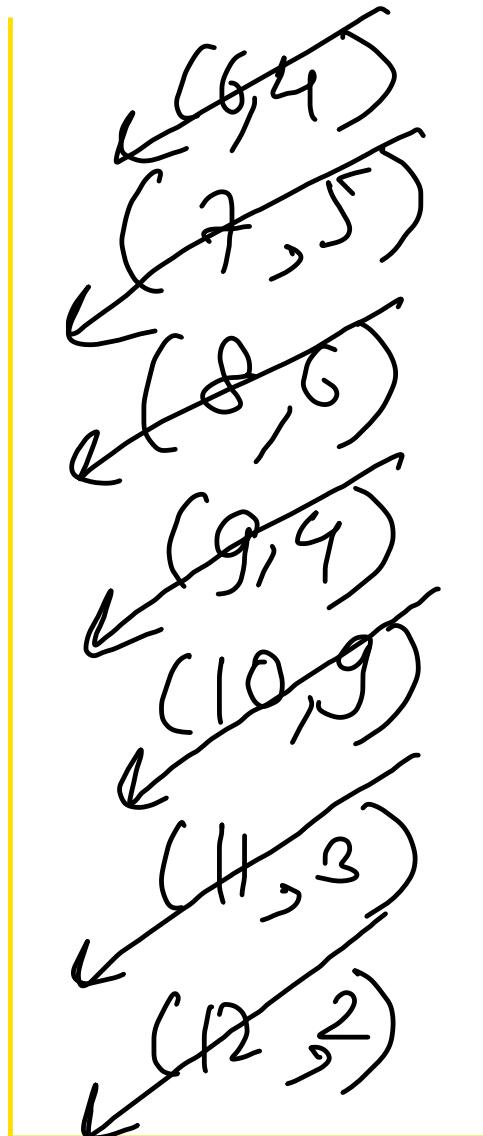
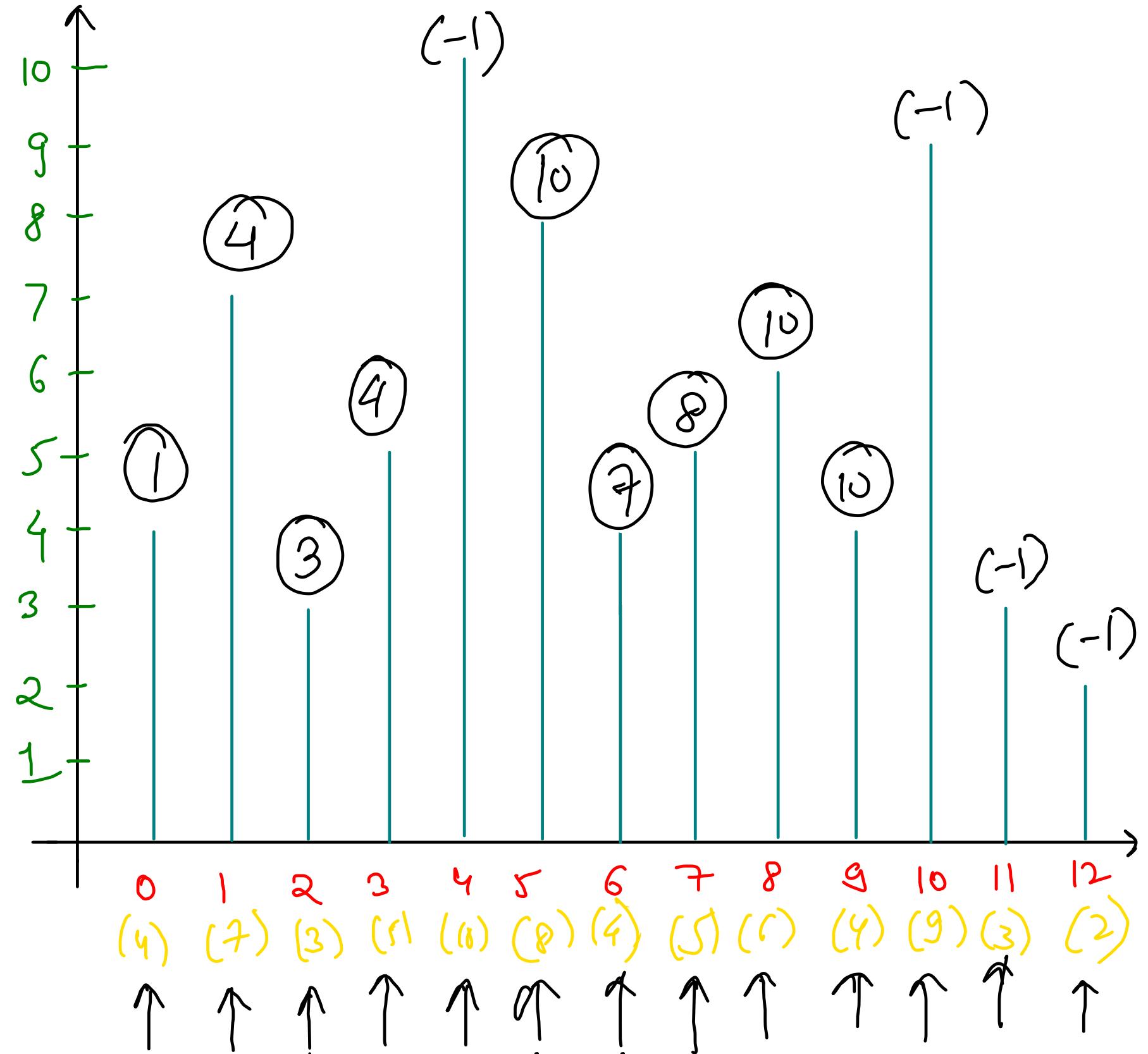
$O(N)$  auxiliary space {stack}

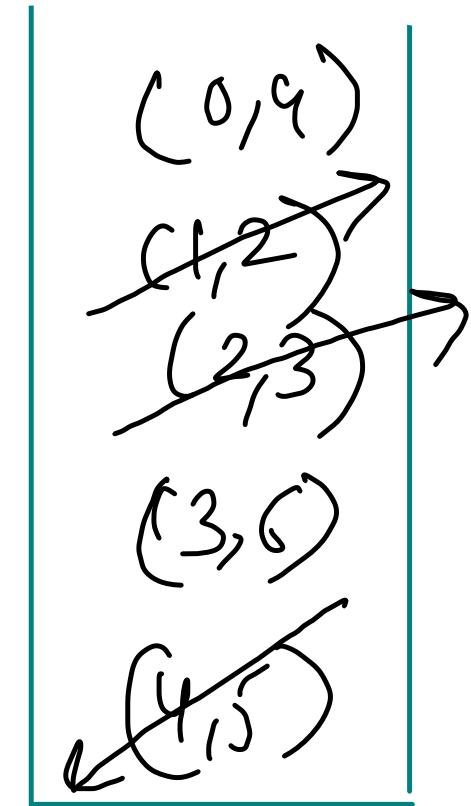
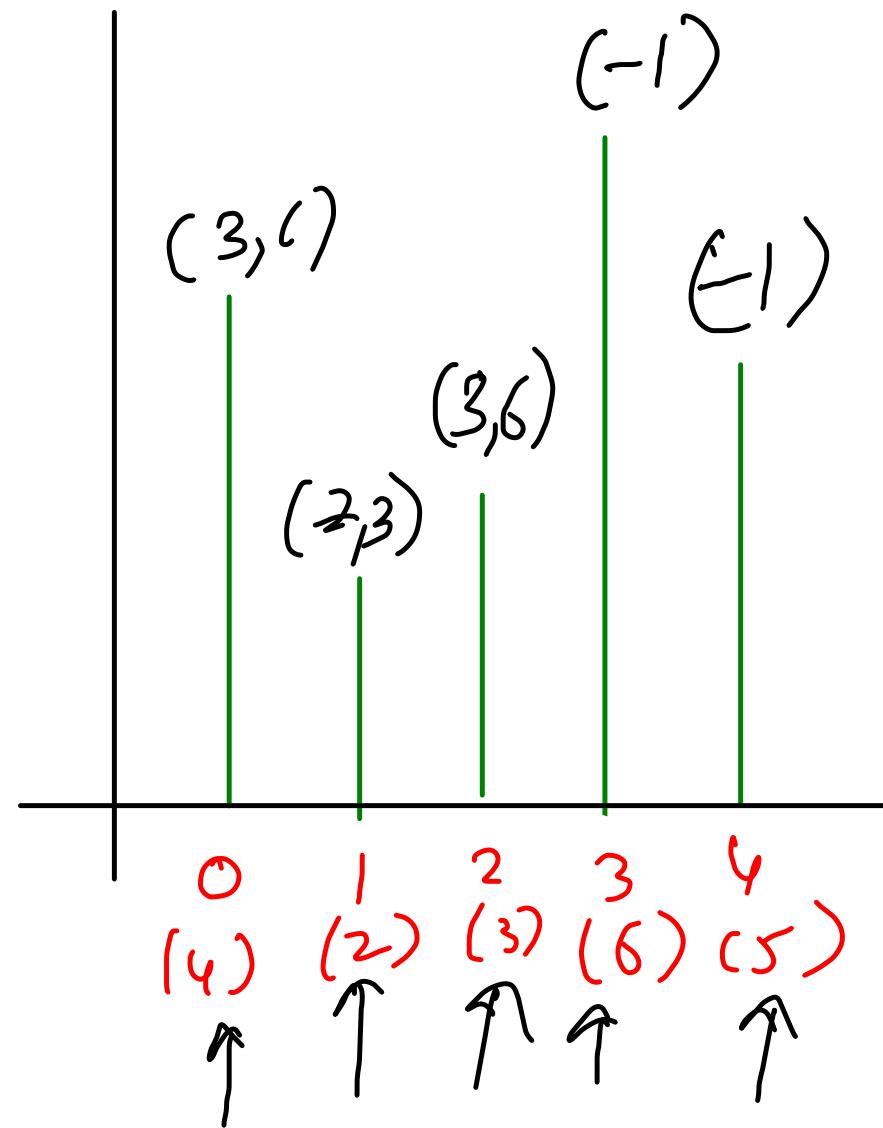
$O(N)$  output space {nge array}



$$O(O+O+f(N)) = N$$

Next greater to the right (2nd approach)





```

int[] nge = new int[arr.length];
Arrays.fill(nge, -1);

Stack<Integer> stk = new Stack<>();
for (int i = arr.length - 1; i >= 0; i--) {
    // pop smaller or equal elements to the right (in the stack)
    while (stk.size() > 0 && arr[i] >= arr[stk.peek()]) {
        stk.pop();
    }

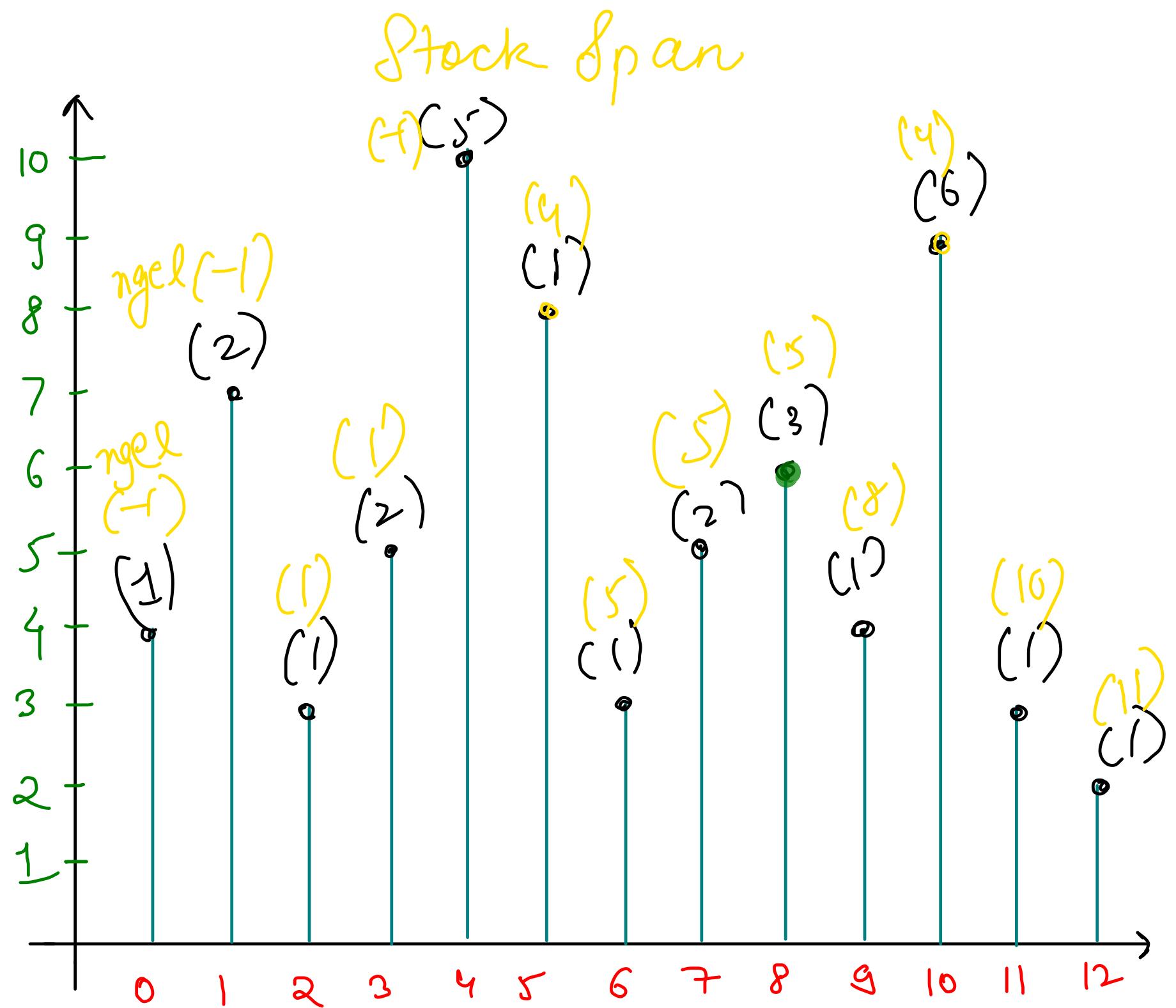
    if(stk.size() > 0)
        nge[i] = arr[stk.peek()];

    // push ourself to find our nge to the right
    stk.push(i);
}

return nge;

```

$\rightarrow O(N)$



nge

- ① nge to the right / left
- ②  $nge[i] = \text{index value}$

stock span  $[i]$

= diff b/w 1st and nge[i]'s index

```

public static int[] solve(int[] arr){
    int[] stock = new int[arr.length];

    Stack<Integer> stk = new Stack<>();
    for (int i = 0; i < arr.length; i++) {
        while (stk.size() > 0 && arr[i] >= arr[stk.peek()]) {
            stk.pop();
        }

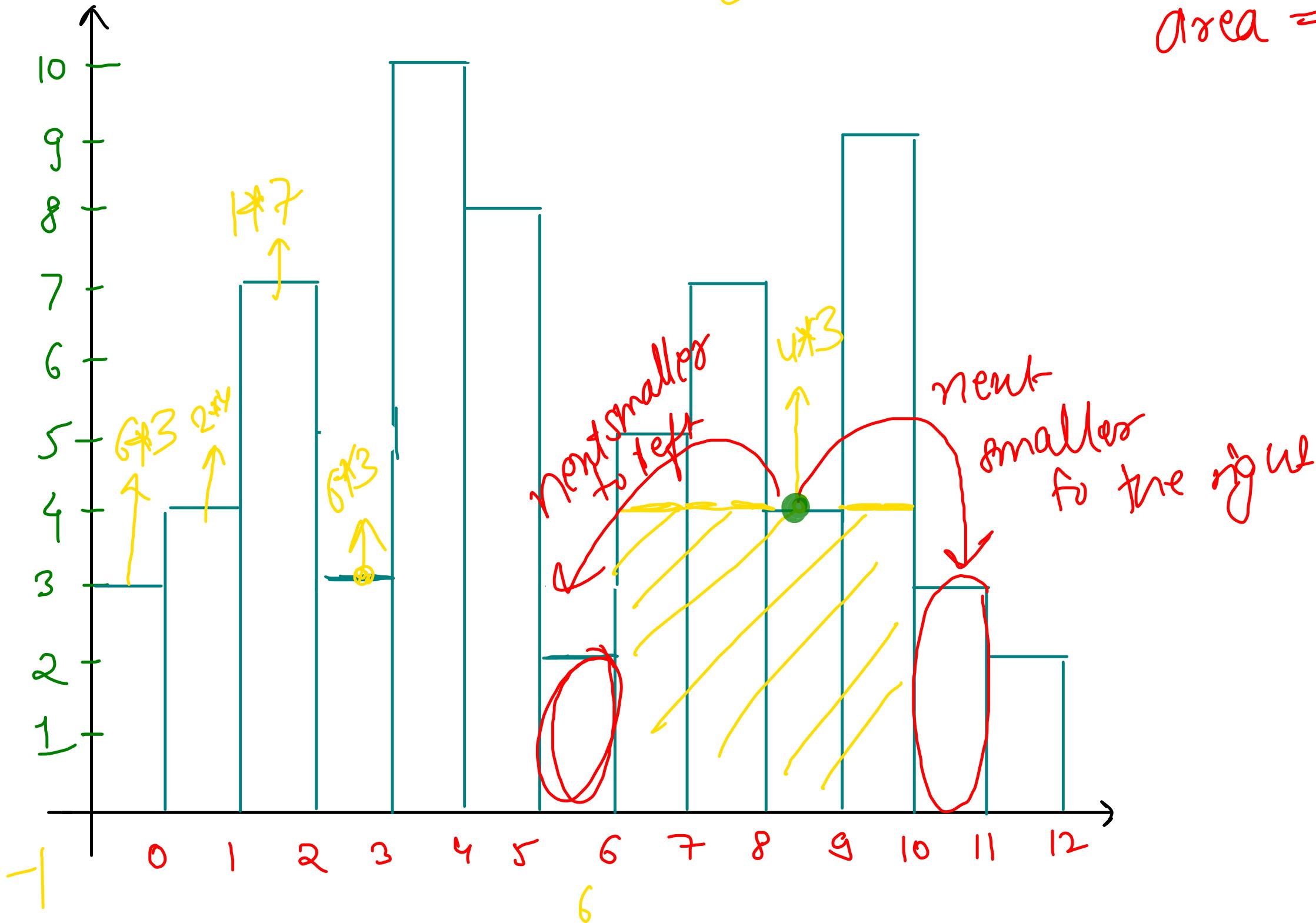
        if(stk.size() > 0)
            stock[i] = (i - stk.peek());
        else stock[i] = (i + 1);

        stk.push(i);
    }
    return stock;
}

```

$\Theta(N)$  Time Complexity  
 $O(N)$  extra space  
{Stack}

# Max Area Histogram



$$\text{area} = \begin{cases} \text{inxr}[i] \\ - \text{nsl}[i] \\ - 1 \end{cases}$$

length  
height  
 $\text{inxr}[i]$

```

public static int[] nsr(int[] arr) {
    int[] nse = new int[arr.length];
    Arrays.fill(nse, arr.length);

    Stack<Integer> stk = new Stack<>();
    for (int i = arr.length - 1; i >= 0; i--) {
        while (stk.size() > 0 && arr[i] <= arr[stk.peek()]) {
            stk.pop();
        }

        if(stk.size() > 0)
            nse[i] = stk.peek();

        stk.push(i);
    }
    return nse;
}

```

```

public static int[] nsr(int[] arr){
    int[] nse = new int[arr.length];
    Arrays.fill(nse, -1);

    Stack<Integer> stk = new Stack<>();
    for (int i = 0; i < arr.length; i++) {
        while (stk.size() > 0 && arr[i] <= arr[stk.peek()]) {
            stk.pop();
        }

        if(stk.size() > 0)
            nse[i] = stk.peek();

        stk.push(i);
    }
    return nse;
}

```

```

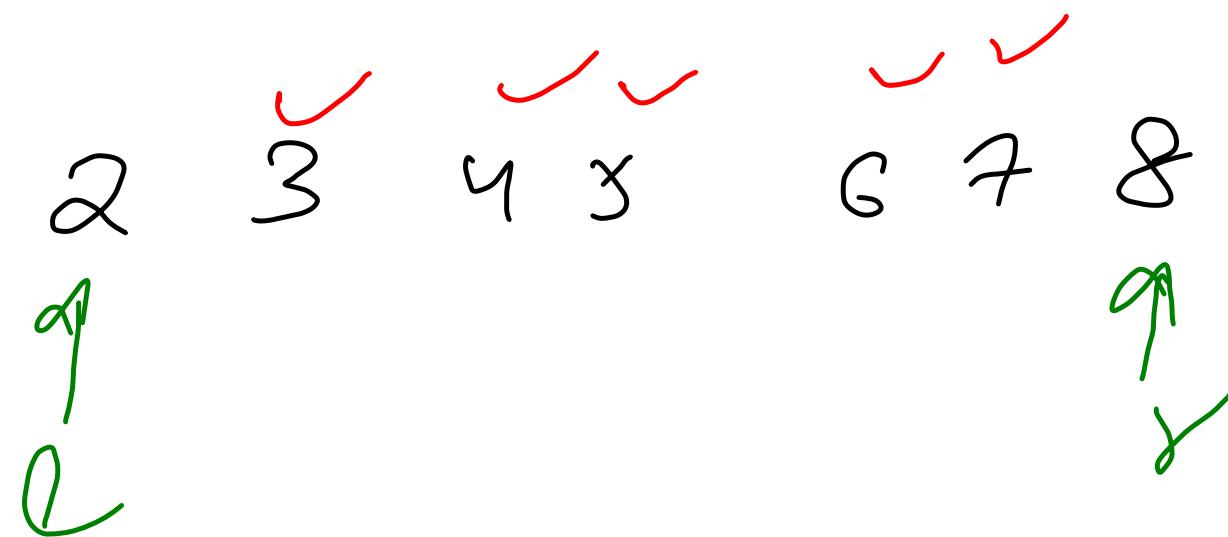
// code
int[] ns1 = ns1(arr); → O(N)
int[] nsr = nsr(arr); → O(N)

int maxArea = 0;
for(int i=0; i<arr.length; i++){ → O(N)
    int currArea = (nsr[i] - ns1[i] - 1) * arr[i];
    maxArea = Math.max(maxArea, currArea);
}

System.out.println(maxArea);

```

$O(N)$  time Complexity  
 $O(N)$  extra space of Stack, ns1, nsr }



$$[2, 8] \Rightarrow 8 - 2 + 1 = 7 \Rightarrow r - l + 1$$

$$(2, 8] \Rightarrow 8 - 2 \Rightarrow r - l$$

$$[2, 8) \Rightarrow 8 - 2 \Rightarrow r - l$$

$$(2, 8) \Rightarrow 8 - 2 - 1 \Rightarrow r - l - 1$$

# Today's Questions

largest area Histogram

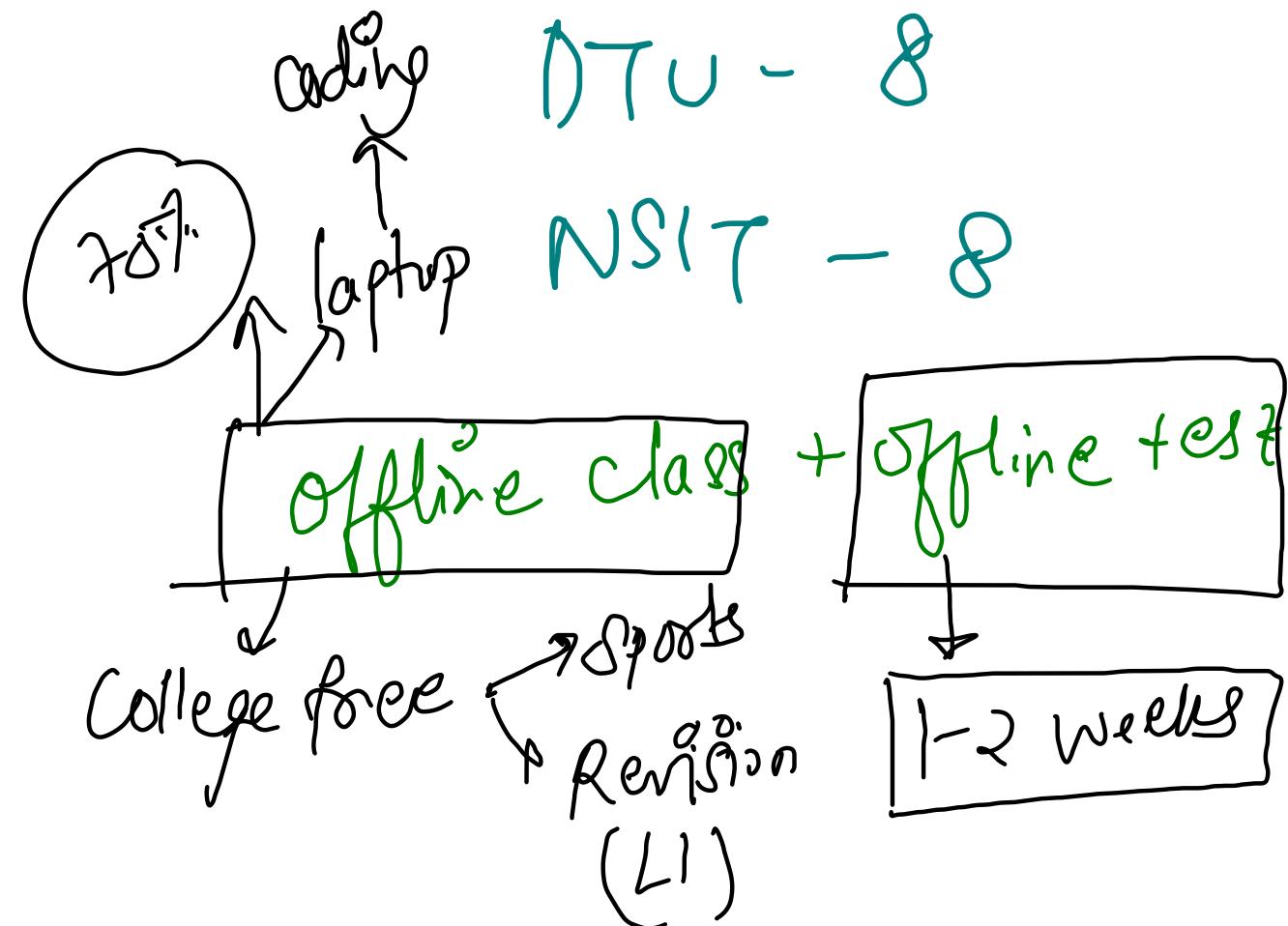
offline

sliding window Maximum

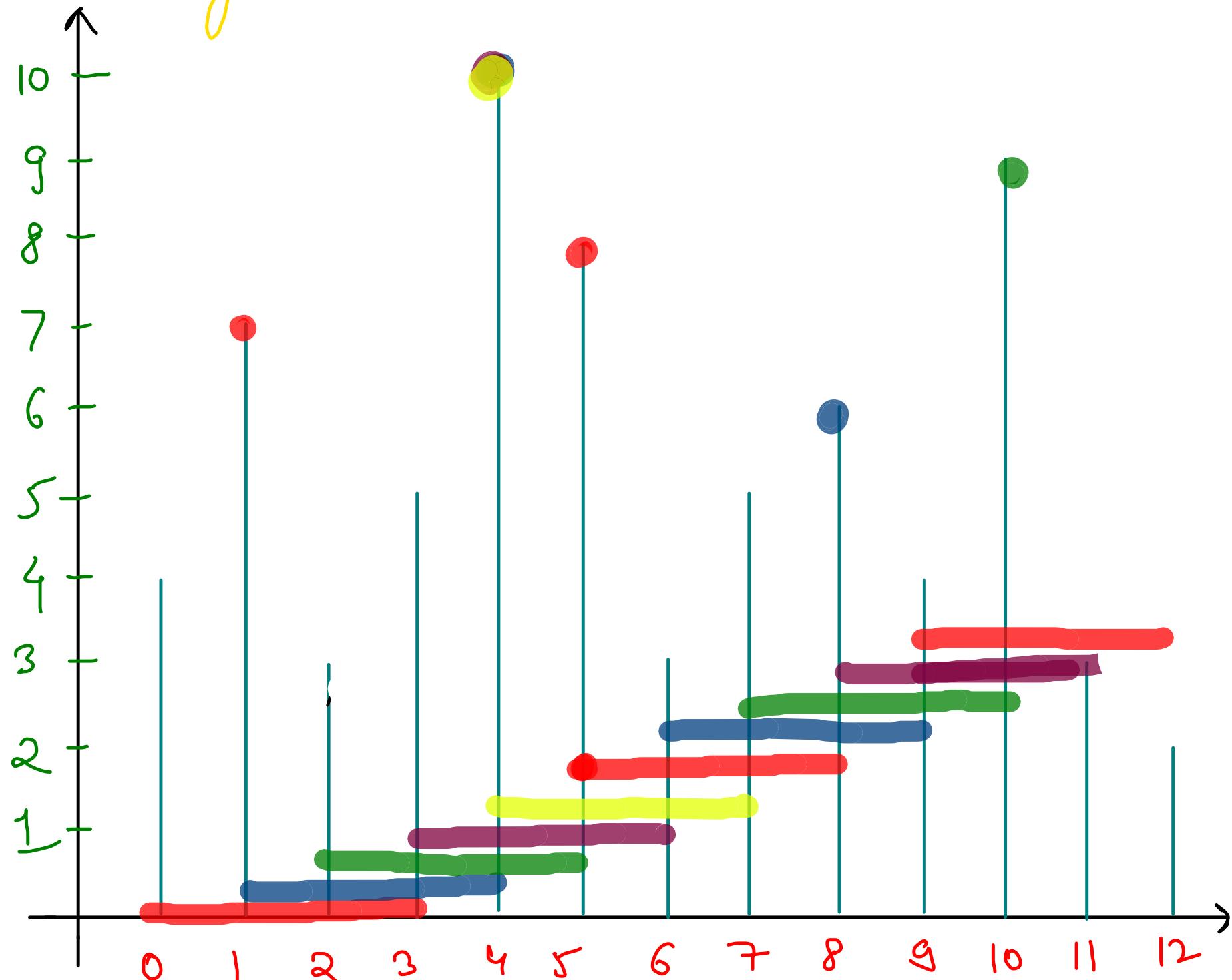
MIIT - 14

- Celebrity Problem
- Minimum Stack
  - with Extra Space
  - w/o Extra Space
- Smallest No following pattern

MA17 - 21



# Sliding Window Maximum



Window = 4

$[0, 3] \Rightarrow 7$

$[1, 4] \Rightarrow 10$

$[2, 5] \Rightarrow 10$

$[3, 6] \Rightarrow 10$

$[4, 7] \Rightarrow 10$

$[5, 8] \Rightarrow 8$

$[6, 9] \Rightarrow 6$

$[7, 10] \Rightarrow 9$

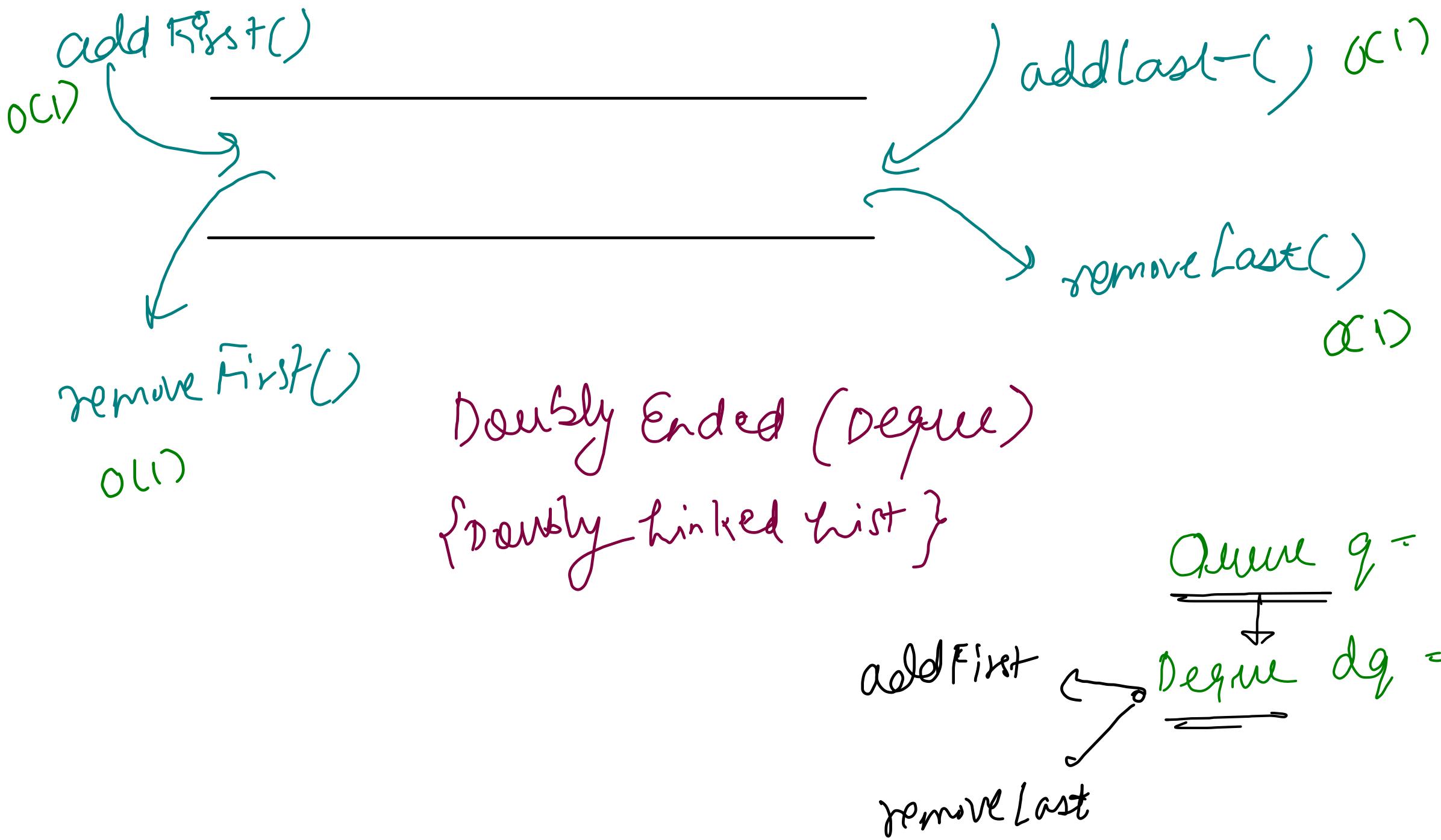
$[8, 11] \Rightarrow 9$

$[9, 12] \Rightarrow 9$

① Brute force  
 $O(n*k)$   
 nested loops

② Using Doubly Ended Queue (Deque)

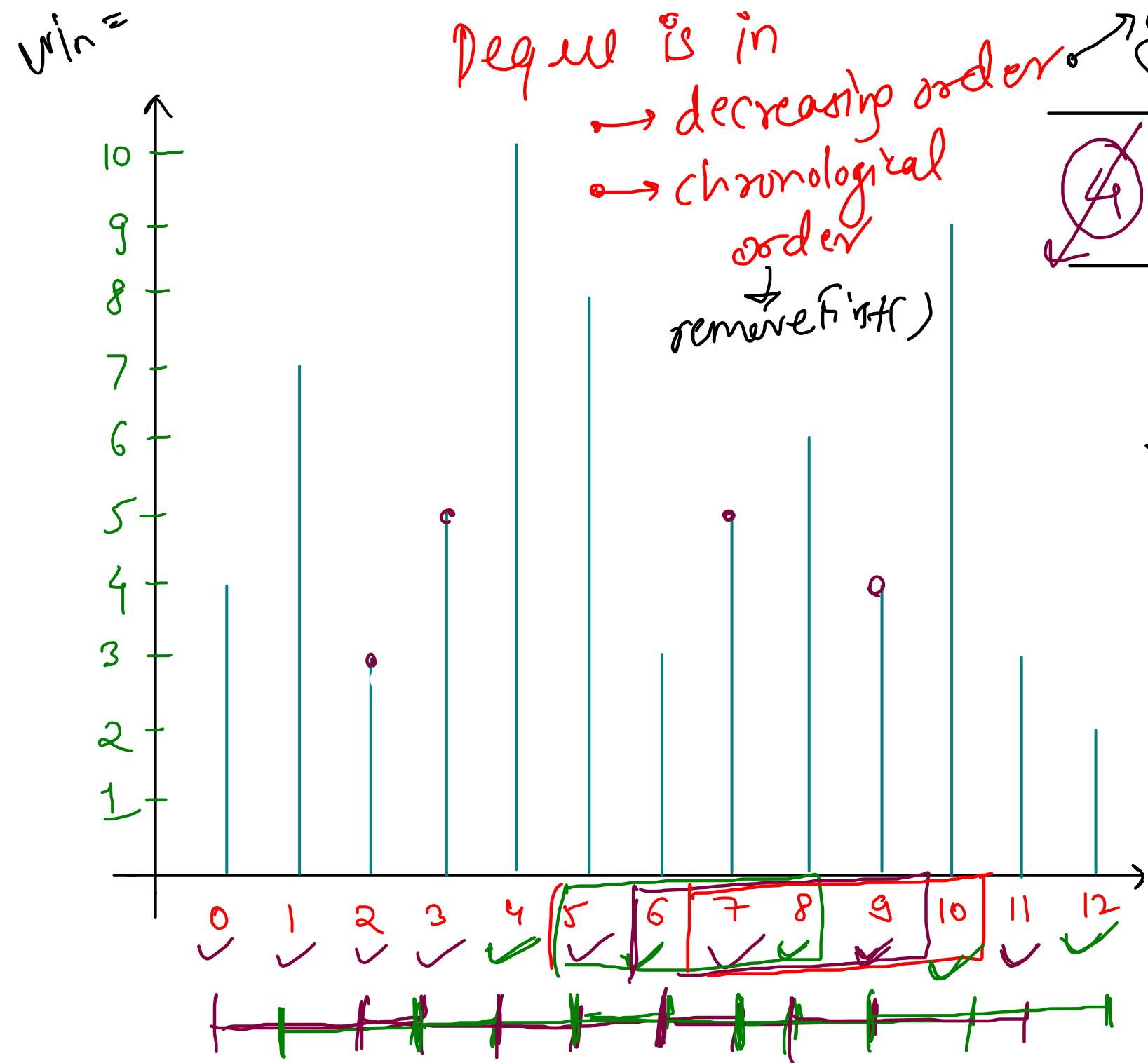
③ Using Stack (NGE)



Queue  $q = \text{new ArrayQueue}();$

Degree  $dg = \text{new ArrayDegree}();$

addFirst      removeLast



$\{7, 10, 10, 10, 10, 8, 6, 9, 9, 9\}$

# getFirst → maximum of curr win down  
which got excluded  
from the window

① removeFirst

Smaller than  
ourself  
(can't be  $\max^m$   
of any window)

② removeLast

We may find the  $\max^m$   
of upcoming windows

```

public int[] maxSlidingWindow(int[] nums, int k) {
    int[] res = new int[nums.length - k + 1];
    int idx = 0;

    Deque<Integer> q = new ArrayDeque<>();

    for(int i=0; i<nums.length; i++){
        // removeFirst -> when front element is excluded from current window
        if(q.size() > 0 && q.getFirst() <= i - k){
            q.removeFirst();
        }

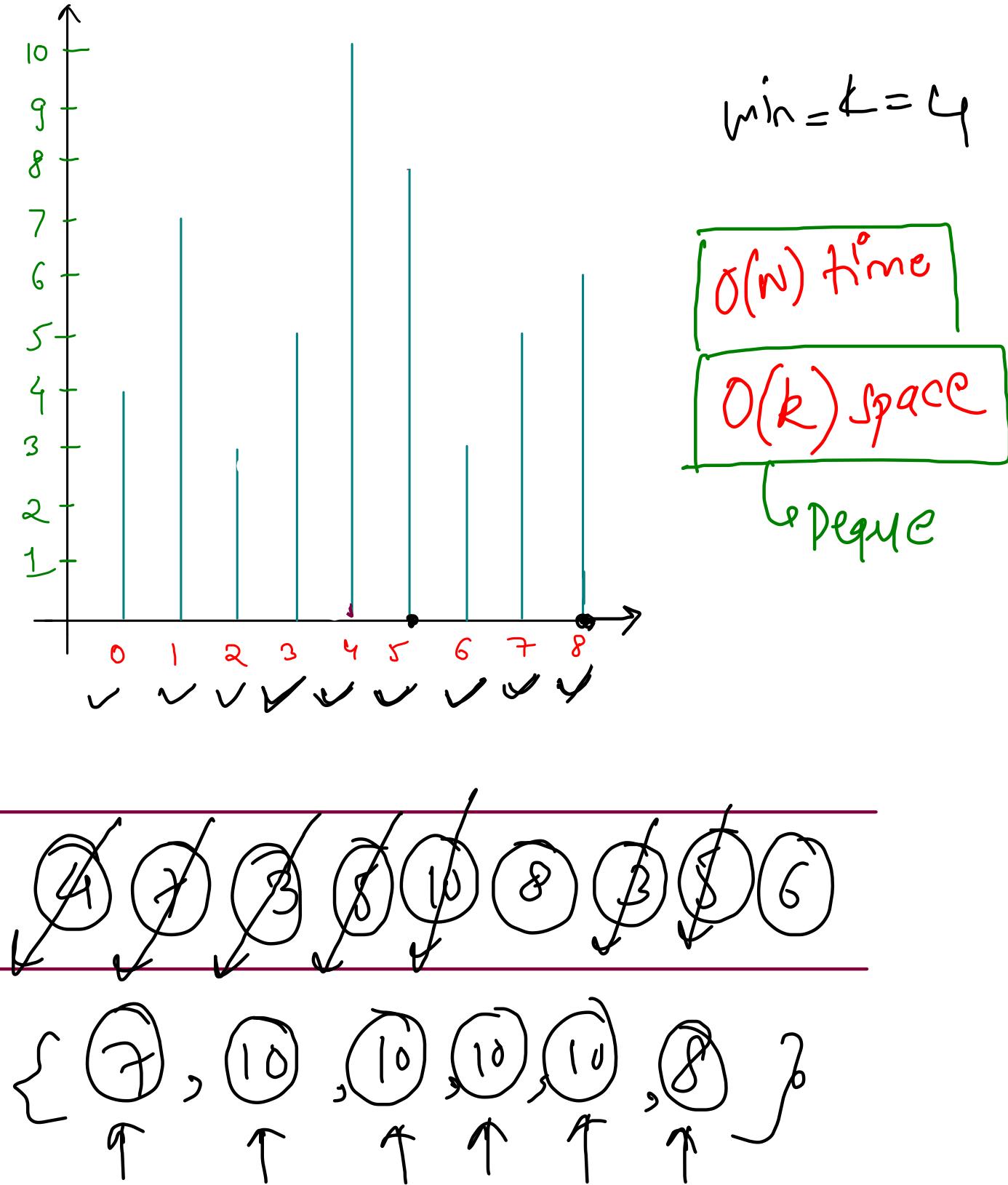
        // removeLast -> smaller than our current element
        while(q.size() > 0 && nums[q.getLast()] < nums[i]){
            q.removeLast();
        }

        // addLast -> We may be answer of current or upcoming windows
        q.addLast(i);

        if(i >= k - 1){
            // current window's maximum is at front of deque
            res[idx++] = nums[q.getFirst()];
        }
    }

    return res;
}

```



# Celebrity Problem

	0	1	2	3
0	0	0	1	0
1	0	0	1	1
2	0	0	0	0
3	1	0	1	0

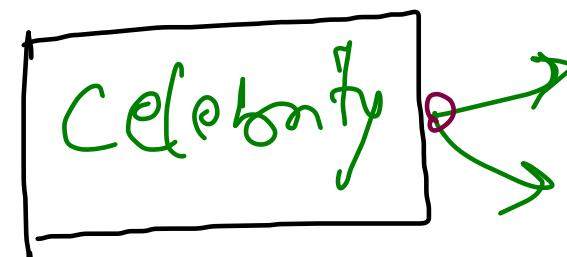
Boolean matrix  
 $\text{mat}[i][j]$

$\rightarrow 1$

$i^{\text{th}}$  person knows  $j^{\text{th}}$  person

$\rightarrow 0$

$i^{\text{th}}$  person doesn't know  
 $j^{\text{th}}$  person



Who knows nobody  
All know him/her

- ① No celebrity (T/F)
- ② More than 1 celebrity (T/F)

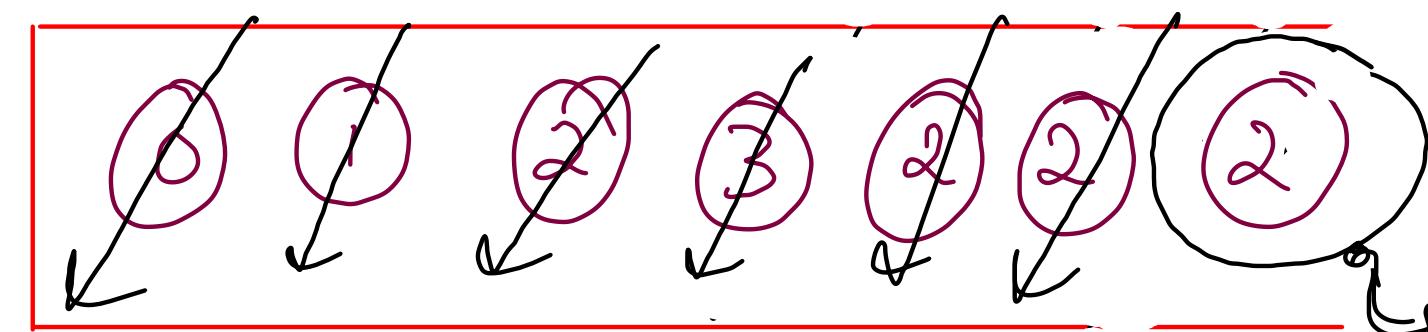
↳ Assumption

$(x, y)$  b.p. are celebrity

$$T(n) = T(n-1) + OCD$$

$O(n)$

(2 pop,  
1 push)



col == 1  
row == 0  
stk.size() == 1  
↑ confirmation

	0	1	2	3
0	0	0	1	0
1	0	0	1	1
2	0	0	1	0
3	1	0	1	0

Possible Celebrities

→ Potential celebrity

{ $x$ ,  $y$ }

if  $\text{mat}[x][y] = 1 \rightarrow x \text{ knows } y$   
 $\Rightarrow x \text{ can't be celebrity}$

else  $\text{mat}[x][y] = 0 \rightarrow x \text{ doesn't know } y$   
 $\Rightarrow y \text{ can't be a celebrity}$

$O(n)$  time,  $O(n)$  extra space (stack)

```
stack<Integer> potentialCeleb = new Stack<>();
for(int i=0; i<arr.length; i++)
    potentialCeleb.push(i);

while(potentialCeleb.size() > 1){
    int y = potentialCeleb.pop();
    int x = potentialCeleb.pop();

    if(arr[x][y] == 1){
        // x knows y -> x can't be a celebrity
        potentialCeleb.push(y); // y may or may not be a celebrity
    } else {
        // x does not know y -> y can't be a celebrity
        potentialCeleb.push(x); // x may or may not be a celebrity
    }
}
```

```
// Confirmation
int x = potentialCeleb.pop();

// Its row should be 0 (x should know nobody)
for(int j=0; j<arr.length; j++){
    if(j == x) continue; ← mat(i)(j)
    if(arr[x][j] == 1) {
        System.out.println("none"); // No celebrity
        return;
    }
}

// Its column should be 1 (Everybody knows x)
for(int i=0; i<arr.length; i++){
    if(i == x) continue; ← mat(i)(i)
    if(arr[i][x] == 0){
        System.out.println("none");
        return;
    }
}

System.out.println(x);
```

# Minimum Stack { with extra space }

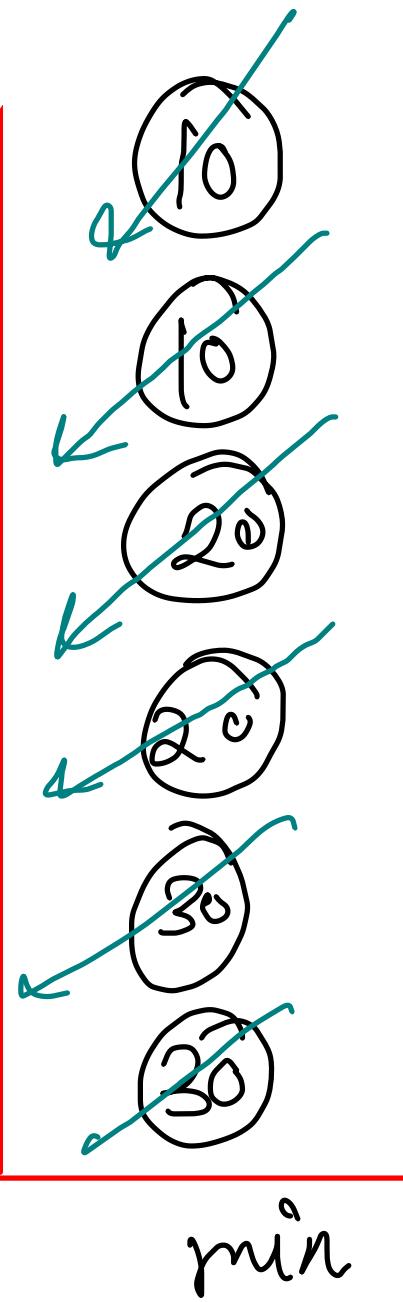
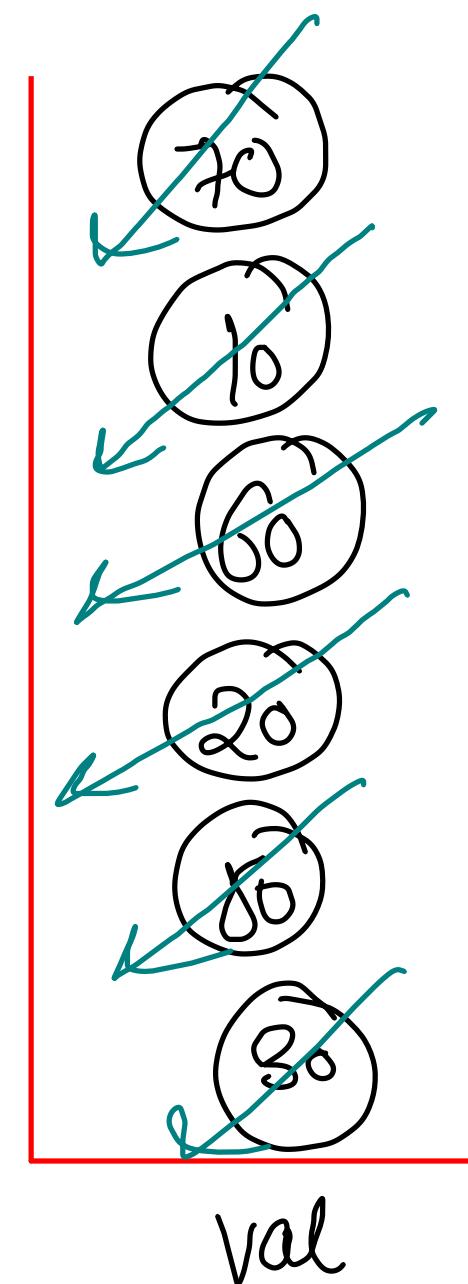
push(30)  
push(50)  
push(20)  
push(60)  
push(10)  
push(70)

peek()  $\Theta(1)$

min()  $\Theta(1)$

30  
50  
20  
60  
10  
70

pop()  $\Theta(1)$

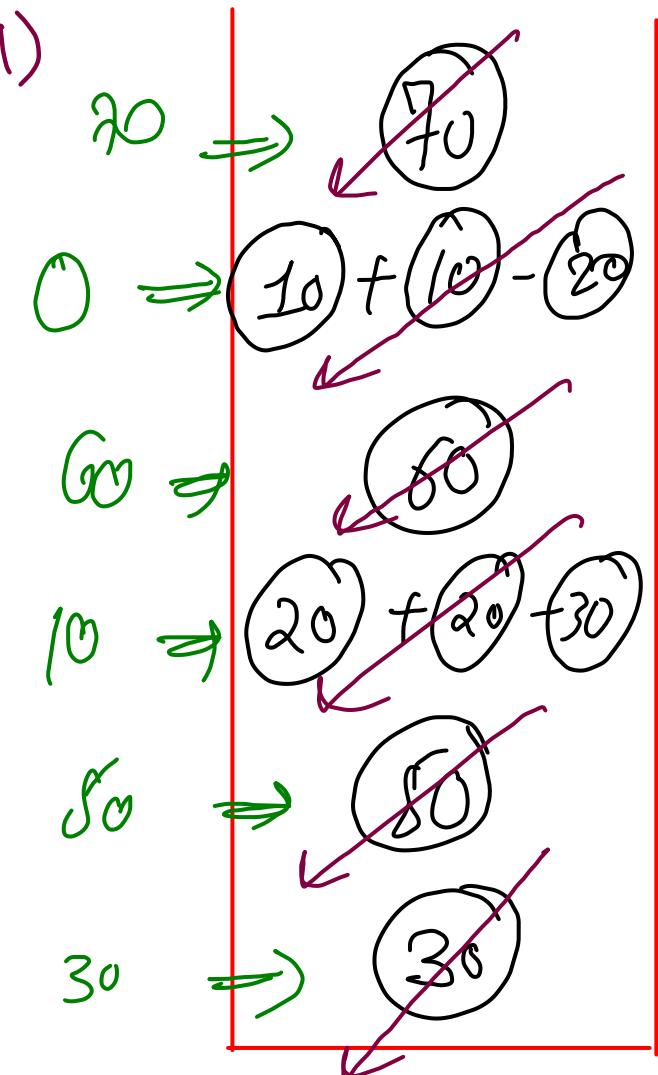
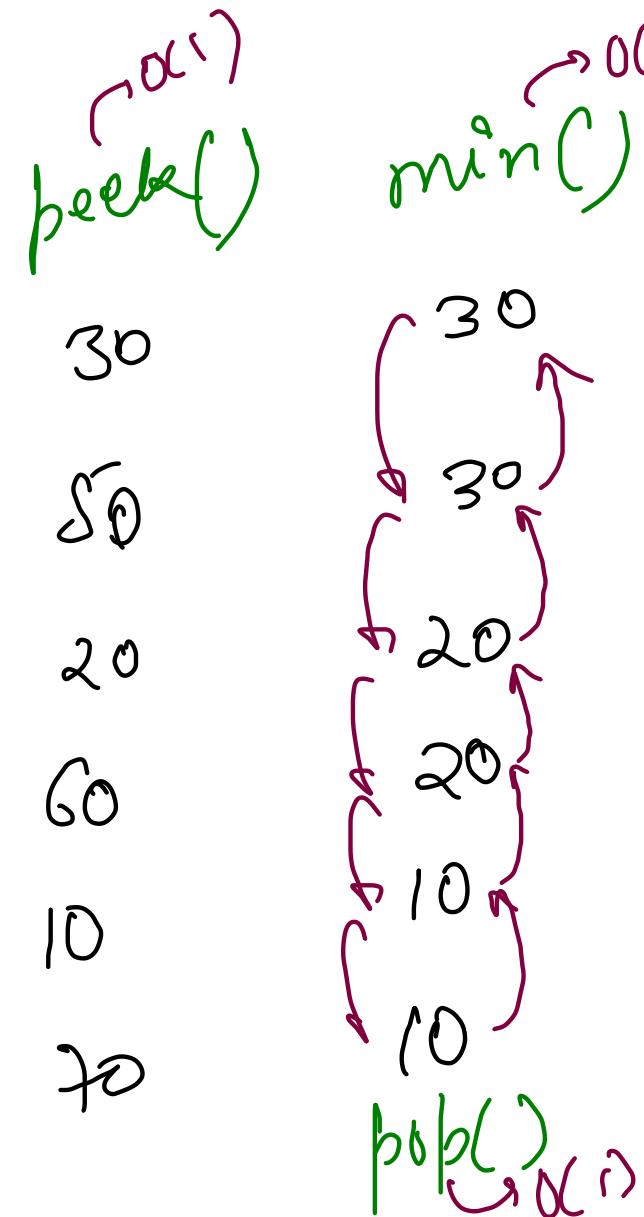


```
public static class MinStack {  
    Stack<Integer> allData;  
    Stack<Integer> minData;  
  
    public MinStack() {  
        allData = new Stack<>();  
        minData = new Stack<>();  
        minData.push(Integer.MAX_VALUE);  
    }  
  
    int size() {  
        return allData.size();  
    }  
  
    void push(int val) {  
        allData.push(val);  
        minData.push(Math.min(minData.peek(), val));  
    }  
  
    int pop() {  
        if(size() == 0){  
            return -1; // underflow  
        }  
  
        minData.pop();  
        return allData.pop();  
    }  
}
```

```
int top() {  
    if(size() == 0){  
        return -1; // underflow  
    }  
  
    return allData.peek();  
}  
  
int min(){  
    if(size() == 0){  
        return -1; // underflow  
    }  
  
    return minData.peek();  
}
```

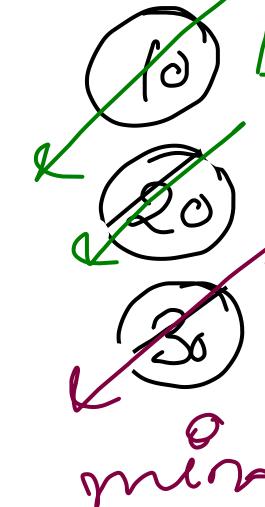
{ without extra space }

- ✓ push(30)  $\Theta(1)$
- ✓ push(50)  $\Theta(1)$
- ✓ push(20)  $\Theta(1)$
- ✓ push(60)  $\Theta(1)$
- ✓ push(10)  $\Theta(1)$
- ✓ push(70)  $\Theta(1)$



Decryption

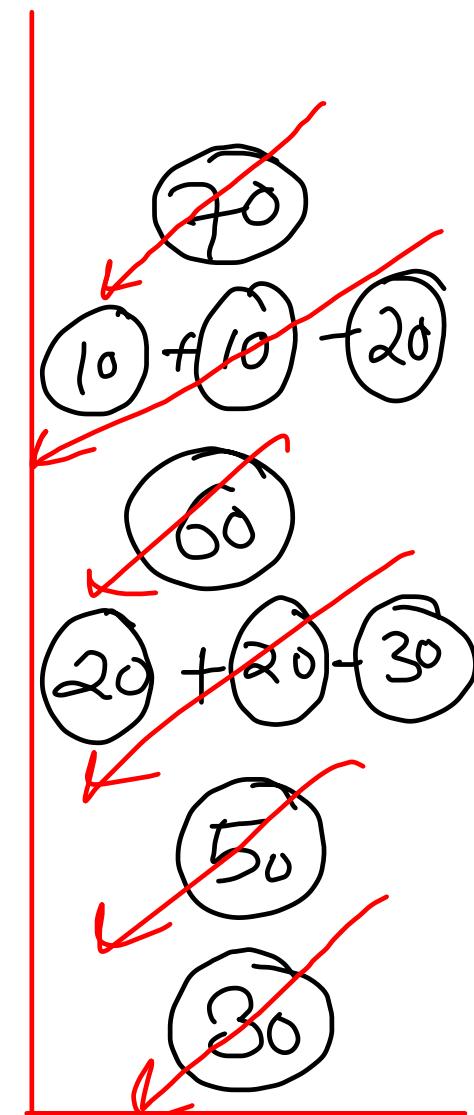
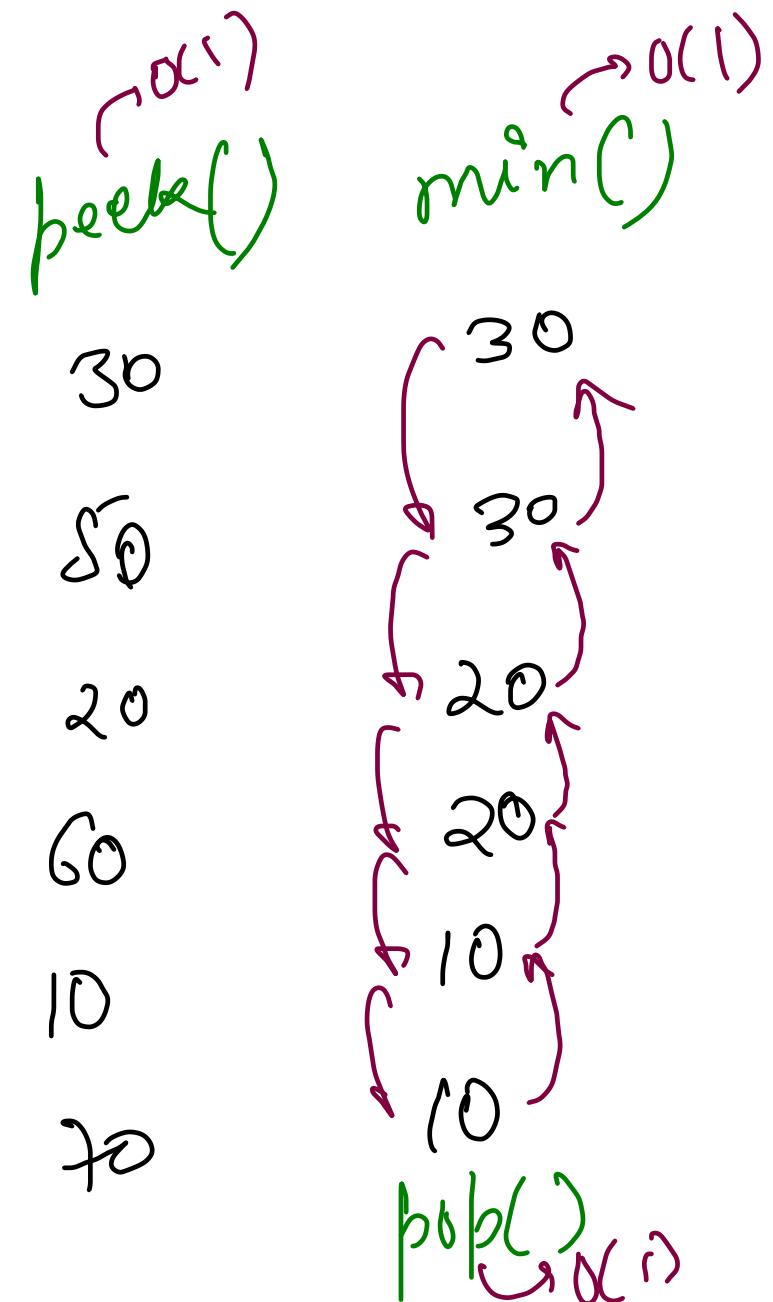
$$\text{top} = \frac{\text{min} + \text{mh} - \text{prev}}{\text{prev} = 2 * \text{min} - \text{top}}$$



min  $\Theta(1)$   
Encryption ( $y/n$ )  
Encrypt  $\Rightarrow$  minimum node  
 $\text{val} + (\text{val} - \text{min})$  in integer Range  
 $20 + (20 - 30) < 20$

without extra space

- ✓ push(70)  $O(1)$
- ✓ push(50)  $O(1)$
- ✓ push(20)  $O(1)$
- ✓ push(60)  $O(1)$
- ✓ push(10)  $O(1)$
- ✓ push(30)  $O(1)$



encrypt

val &  $\min$

$$\text{val} + \frac{\text{val} - \min}{-\text{ve}}$$

+  
min

decryptn

prev  
=  $2 * \min$   
- top

O(1) extra space

```
Stack<Long> stk = new Stack<>();
long min = Long.MAX_VALUE;

public void push(int val) {
    if(stk.size() == 0){
        stk.push(1L * val);
        min = (long)val;
    } else if(val < min){
        stk.push(2L * val - min);
        min = (long)val;
    } else {
        stk.push(1L * val);
    }
}
```

O(1)

$$2L \Rightarrow 2^{16} \text{ long}$$

$$2L = (\text{long})^2$$

```
public void pop() {
    if(stk.size() == 0) return;

    // check if top is encrypted value
    if(stk.peek() < min){
        // decrypt the previous min
        min = 2L * min - stk.pop();
    } else {
        stk.pop();
    }
}

public int top() {
    if(stk.size() == 0) return -1;

    // check if top is encrypted value
    if(stk.peek() < min) return (int)min;
    long top = stk.peek();
    return (int)top;
}

public int getMin() {
    if(stk.size() == 0) return -1;
    return (int)min;
}
```

O(1)

O(1)

O(1)