

Peck  $\rightarrow$  getFirst()

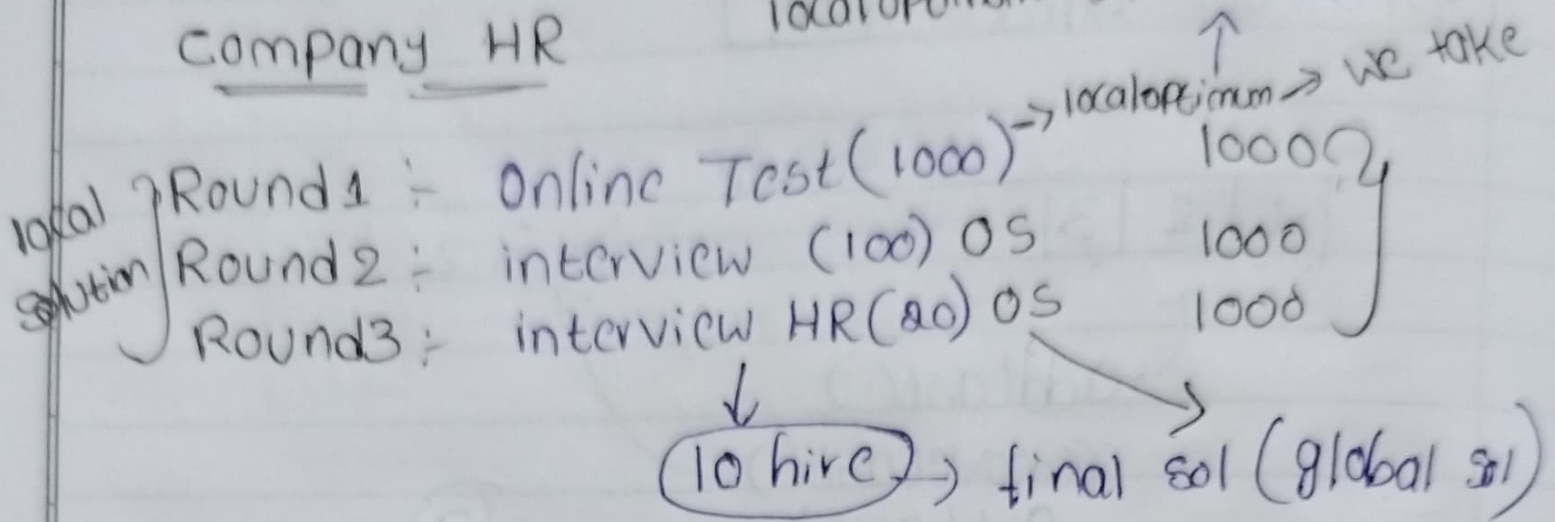
## Greedy Approach

### Introduction to Greedy

Company HR

local optimum (OS)

Time  $\uparrow$   
resource  $\uparrow$



Def: Greedy algorithms are the problem-solving

Technique where we can make the locally optim-

-Um choice at each stage & hope to

Expt. No.: .....

achieve a global optimum (final sol)

- 1) optimization  $\rightarrow$  Min. Max  $\rightarrow$  final sol
    - Sorting
    - Binary Search
    - Quick Sort
    - Merge Sort
  - 2)
  - 3) No fixed rule
  - 4) not realize
- They have fixed rules

Pros

Simple & Easy  
Good enough TC

Cons

A lot of time, global optimum is not achieved

DropAct: Might not give the global optimum in all cases.

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### Activity Selection

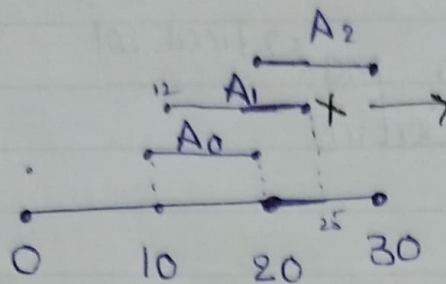
You are given  $n$  activities with their start and end times. Select the maximum number of activities that can be performed by a single person, assuming that a person can only work on a single activity at a time. Activities are sorted according to end time.

Teacher's Signature \_\_\_\_\_



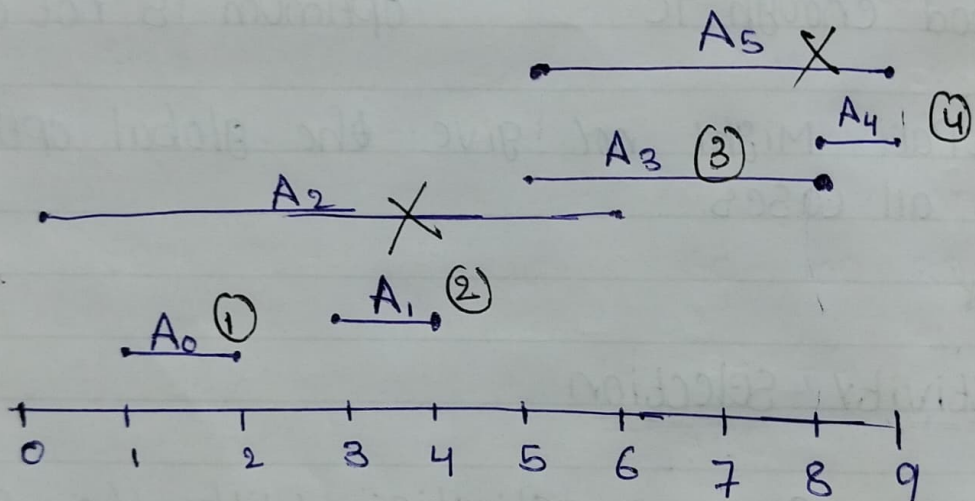
Start =  $[10, 12, 20]$   
 end =  $[20, 25, 30]$

Ans = 2 ( $A_0$  &  $A_2$ )



### Approach

Start =  $[1, 3, 0, 5, 8, 5]$   
 end =  $[2, 4, 6, 7, 9, 9]$

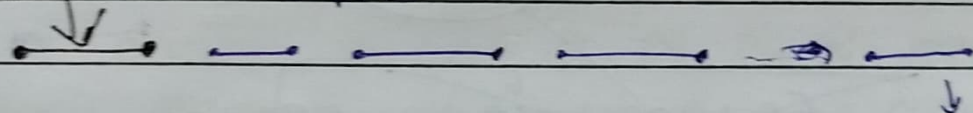


- 1) ~~end~~ end basis sort
- 2)  $A_0$  (is the first activity)  
 ↳ end time  
 → then non-overlap disjoint
- 3) where start time  $\geq$  last choicen end time

Count ++;

Activity Selection \*\* (Appit & Commu)

MATH logic

Sol A  $\xrightarrow{A_0}$  .....  $\rightarrow n$ Sol B  $\xrightarrow{K}$  .....  $\rightarrow n_1$ Where Note Sol B Start with Null then second to  $K$  to  $n_1$  (Non-overlap) $n_1 > n$  $n_1 = n \rightarrow \text{optimal}$  $n_1 - 1 + 1$ Fractional knapsack

Ex: Given the weights and values of  $N$  items, put these items in a knapsack of capacity  $W$  to get the maximum total value in the knapsack.

Value =  $[60, 100, 120]$  $W = 50$ Weight =  $[10, 20, 30]$ 

Given data



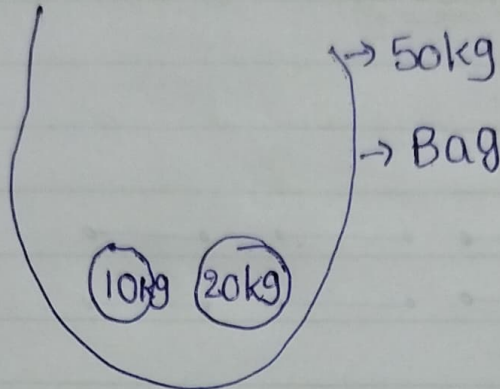
Weights ↓

Value ↑

N items

↓  
Profit

knapsack →



W = 50

Ans: 240

~~$60 + 100 + \frac{120}{30} \times 20$~~  wrong

~~$60 + 100 + \frac{120}{20} \times 30$~~

$50 - 20 + 10$

$50 - 30$

$50 - 20$  remain

but we have

30kg

$$\begin{aligned} &= 60 + 100 + \frac{4}{30} \times 120 \\ &= 60 + 100 + 80 \\ &= 180 + 60 \\ &= 240 \end{aligned}$$

Code Approach

Min Absolute Difference Pairs

Given two arrays A and B of equal length n. Pair each element of array A to an element in array B, such that sum S of absolute differences of all the pairs is minimum

$$A = [1, 2, 3]$$

$$\text{Ans} = 0$$

$$B = [2, 1, 3]$$

→ logic

for Ex:  $a=5, b=5$  (or)  $a=1, b=2$

$$|a-b| = |5-5| = 0$$

$$|1-2| = -1 \rightarrow +1$$

$$|6-a| = |6-5| = 0$$

$$|2-1| = 1$$

→ Case 1:  $|1-2| + |2-1| + |3-3| = 1 + 1 + 0 = 2$

Case 2:  $|1-3| + |2-1| + |3-2| = 2 + 1 + 1 = 4$

Case 3:  ~~$|2-3|$~~   $|1-1| + |2-2| + |3-3| = 0+0+0=0$   
Min

### Greedy Approach

Sort A & B

Ex:  $A = [1, 2, 3]$

$B = [2, 1, 3]$

$A = [1, 2, 3]$

$B = [1, 2, 3]$  then we do  $|1-1| + |2-2| + |3-3|$   
 $= 0$

### Max Length chain of pairs

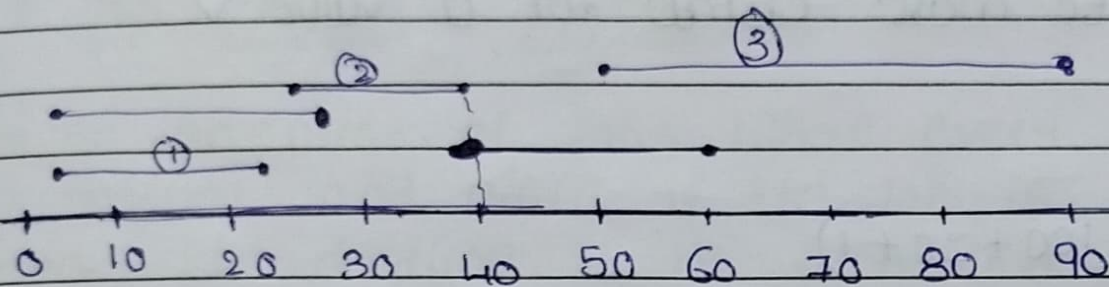
You are given  $n$  pairs of numbers. In every pair, the first number is always smaller than the second number. A pair  $(c, d)$  can come after pair  $(a, b)$  if  $b < c$ . Find the longest chain which can be formed from a given set of pairs.

Pairs =

$(5, 24)$	$(5, 28)$	$(50, 90)$
$(39, 60)$	$(27, 40)$	Ans = 3



Expt. No.: .....



Note! overlapping No

Approach

1) Sort (at last element are 24, 60, 28, 40, 90)

2) ~~Store~~ first pair

for (int i = 1; i < n; i++) ?

if (first > end select last) ?

last → update  
ans++

Teacher's Signature \_\_\_\_\_



## Indian Coins

We are given an infinite supply of denominations [1, 2, 5, 10, 20, 50, 100, 500, 2000]. Find min no. of coins/notes to make change for a value  $V$ .

$$V = 121$$

$$\text{ans} = 3(100 + 20 + 1)$$

$$V = 590$$

$$\text{ans} = 4(500 + 50 + 20 + 20)$$

### Approach

1) ~~Sort~~ [1, 2, 5, 10, 20, 50, 100, ...]

1) Sort descending (200, 500, 100, 50, 20, 10, 5, 2, 1)

$$\text{Amount} = 590$$

$$\text{count} = 0$$

for (int  $i = 0$ ;  $i < n$ ;  $i++$ )?

if (coin[ $i$ ] < amount)?

while (coin[ $i$ ] < amount)?

count++

$$590 - 500 = 90 - 50 = 40$$

↓

20

↓

20

amount = amount - coin[Ci]

8

3

### Job Sequence problem

Given an array of jobs where every job has a deadline and profit if the job is finished before the deadline. It is also given that every job takes a single unit of time. So the minimum possible deadline for any job is 1. Maximize the total profit if only one job can be scheduled at a time.

Job A = 4, 20

Job B = 1, 10

Ans = C, A

Job C = 1, 40

Job D = 1, 30

① A time = 1, profit = 20

② B, A time = 2, profit = 10 + 20 = 30

③ ~~B, A~~ C, A time = 2, profit = 40 + 20 = 60 ✓

④ D, A time = 1, profit = 30 + 20 = 50



Another way of solving this

				$J_1$	$J_2$	$J_3$	$J_4$	
A	B	C	D	$P_j$	20	10	40	30
				$D_j$	4	1	1	1

$$\begin{array}{ccccccc}
 0 & \underline{J_3} & 1 & - & 2 & - & 3 & \underline{J_1} & 4 \\
 (\text{ms}) & 9 & 10 & & 11 & & 12 & 1 & 
 \end{array}$$

$J_3 + J_1 = 40 + 20 = 60$

Approach

Step 1: base sort (That means sort the Profit's)

Step 2: time =  $\phi$

array

Ans

1	4	
---	---	--

Step 3:

```
for (int i=0; i<jobs; i++)
{
```

```
    if (job(deadline) > time) ?
```

~~add ans~~

add

time++

y y