

Bit Manipulation

Decimal \rightarrow 0-9

Binary \rightarrow 0's & 1's

Convert D to B

$$(4)_{10} \rightarrow (?)_2$$

$$\begin{array}{r} 2 \mid 4 \rightarrow 0 \\ 2 \mid 2 \rightarrow 0 \\ \hline 1 \end{array} \rightarrow 100$$

$$\begin{array}{r}
 1 \ 0 \ 0 \\
 \swarrow \downarrow \searrow \\
 1 \times 2^2 \quad 0 \times 2^1 \\
 4 + 0 + 0 = 4
 \end{array}$$

Bit-wise Operators

Binary AND &

Binary OR |

Binary XOR ^

Binary one's complement

Binary left shift <<

Binary right shift >>

Binary AND &

== ==

$$586 \quad A=0101 \quad B=01$$

Rules

Output

$$0 \& 0 \rightarrow 0$$

$$0 \& 1 \rightarrow 0$$

$$1 \& 0 \rightarrow 0$$

$$1 \& 1 \rightarrow 1$$

101

110

$$\underline{100} = (4)_{10}$$

Binary OR

Rules

OR		OUTPUT	
0	1	0	0

0	1	1	1
---	---	---	---

1	1	0	1
---	---	---	---

1	1	1	1
---	---	---	---

$$516 \quad A = 101, \quad B = 110$$

$$\begin{array}{r} 101 \\ 110 \\ \hline 111 \end{array} \rightarrow (7)_{10}$$

~~1 1~~ ↓ ↓

$$1 \times 2^2 \quad 1 \times 2^1 \quad 1 \times 2^0$$

$$4 + 2 + 1 = 7$$

Binary XOR

Rules

OR		OUTPUT	
0	^	0	0

0	^	1	1
---	---	---	---

1	^	0	1
---	---	---	---

1	^	1	0
---	---	---	---

$$5 \wedge 6 \quad A = 101, \quad B = 110$$

$$101$$

$$\begin{array}{r} 110 \\ \hline 011 \end{array}$$

$$= (3)_{10}$$

Binary ones Complement

Rules

$$\sim 5 \quad A = 0101$$

$$\sim 0 \quad 1$$

$$\sim 1 \quad 0$$

$$\begin{array}{r} 101 \\ \hline 010 \end{array} \rightarrow (2)_{10}$$

(LSB) → Least Significant Bit

(MSB) → Most Significant Bit

$5 \rightarrow \underline{00000} \underline{101}$
 MSB LSB

(1) 00000 101

↓
 - 5

11111 010
 ↓
 (-6)₁₀

2's complement

↓
 1's complement ($\sim n$) (magnitude)

↓
 add 1

000000101 → 1's comp

+ 1
 ——————
 00000110

$\sim 5 = (-6)_{10}$

↓
 - 6

Binary Left Shift <<

Rules

$a << b (2)$

000, 101

$a = \boxed{000} / 101100$

0 1 0 ! - -

0 1 0 1 1 0 0 - -

$5 < 2 = (10100)_2 \rightarrow$

~~17~~

$$a \ll b = a * 2^b$$

$$5 \ll 2 = 5 * 2^2$$

$$\leftarrow 5 * 4 = 20$$

Binary Right Shift >>

Rules

$\gg 2$

~~6 >> 1~~

$A = 000110$

$0\ 0\ 1\ 00\ 1\ 00$

$6 \gg 1$

~ 001001

000110

$$6 \gg 1 = (3)_{10}$$

~ 000101

$$a \ll b = a * 2^b$$

$$a \gg b = a / 2^b$$

$$6 / 2^1 = 3$$

2) Check if a number is odd or Even

$$0 = 000 \quad \text{LSB}$$

$$1 = 001 \quad \text{odd} \quad \text{even}$$

$$2 = 010 \quad \text{LSB} \rightarrow 1 \quad \text{LSB} \rightarrow 0$$

$$3 = 011 \quad \text{LSB} \rightarrow 1 \quad \text{LSB} \rightarrow 0$$

$$4 = 100 \quad n 80 \rightarrow 0$$

$$5 = 101 \quad n 81 \rightarrow 1$$

$$6 = 011 \quad \text{Ex: } 3$$

$$\text{Ex: } 4$$

$$100$$

$$8001$$

$$\overline{000}$$

$$(0)_{10}$$

$$\downarrow$$

$$\text{even}$$

~~17~~

011

$$8 \frac{001}{00} \rightarrow (1)_{10} \rightarrow \text{odd}$$

$$\begin{array}{r} 1001 \\ \hline 8 | 0001 \\ \hline 0001 \end{array} \rightarrow (1)_{10} \neq 0$$

↓ odd

Operations

3) Get i-th bit 0 0 0 0 1 1 1 i=2

$$\frac{8[0\ 0\ 0\ 0\ 1\ 0\ 0]}{0\ 0\ 0\ 0\ 0\ 1\ 0\ 0} = 0 \rightarrow \text{ith}$$

For example

$$\begin{array}{r}
 0\ 0\ 0\ 0\ 1\ 0\ 1\ 1 \\
 0\ 0\ 0\ 0\ 0\ 1\ 0\ 0 \\
 \hline
 0\ 0\ 0\ 0\ 0\ 0\ 0\ 0
 \end{array}$$

↓
 = 0 → i^{th} bit 0

$\& \text{ (1} \ll i)$ → bit zero

→ #0 bit one

$$\text{Ex: } n = 10^1, i = 2$$

16 10

zero → Answer

2) Set ith bit

$$\begin{array}{r} 0000 \quad 10 \\ \downarrow \\ 0000 \quad 1110 \end{array} \quad i=2$$

Note: set ith bit to 1

$$\text{number} = \underline{10} \quad i=2$$

$$n1(1 \ll i) = \begin{array}{r} 00 \\ 01001 \\ \hline 1110 \end{array}$$

3) Clear ith bit

$$\begin{array}{r} 10 = 1010 \quad i=1 \\ \downarrow \\ 1000 \quad (8) \end{array} \quad \begin{array}{r} 1 \ll i \\ \downarrow \\ \sim(1 \ll i) \end{array}$$

$$\begin{array}{r} 1010 \\ 8 \begin{array}{r} 1101 \\ \hline 1000 \end{array} = (8)_{10} \end{array} \quad \begin{array}{r} \sim(1 \ll i) \Rightarrow \sim(0010) \\ 1101 \end{array}$$

Note: In short

$$n = 10, \rightarrow (1010)_{10}$$

$$\begin{array}{r} i=1 \quad \sim(0010) \\ 1 \ll i \quad 1101 \end{array} \quad \begin{array}{r} 1010 \\ 8 \begin{array}{r} 1101 \\ \hline 1000 \end{array} = (8)_{10} \end{array}$$

$$\begin{array}{r} 0001 \\ 0010 \rightarrow \end{array}$$

Update ith bit \rightarrow + ith

val = 0 or 1

$i + (\text{clear, set})$

Clear $nB = 0$



$nB << i$

$0 << i (0) \text{ in}$

$\Rightarrow \underline{n}$

Set $nB = 1$



$(nB << i) \text{ in}$



ith bit set

$i > 2^j$



$(i > 2^j) \text{ in}$

$(8) \text{ 0001}$

$(3100)_{\text{in}} \oplus (i > 2^j)_{\text{in}}$

1011

0101

0101

$1011, 0$

$(3100)_{\text{in}}$

$(8) = \underline{1001}$

1011

$i > 2^j$