



ALGORITHMS AND DATA STRUCTURES

ASSIGNMENT 2: Operations on Binary Search Trees.

PART II: Recursion, Binary Search Trees.

1. Background.

The Abstract Data Type (ADT) `myBinarySearchTrees<T1, T2>` allows to store nodes with the format (T1 key, T2 value). Whereas T2 can be any datatype (e.g., an Integer, a String, a `myPlayer`, etc.), the datatype T1 is constrained to have a total order relationship \leq (i.e., two elements T1 elem_i and T1 elem_j can be compared and sorted).

The ADT `myBinarySearchTrees<T1, T2>` supports the set of operations we have seen in the lectures, and it is specified in the interface `myBinarySearchTree.java`.

1. `//public myBinarySearchTree<T1, T2> create_from_binary_search_node(
myBinarySearchNode<T1, T2> n);`
2. `public boolean my_is_empty();`
3. `public myBinarySearchNode<T1, T2> my_root();`
4. `public myBinarySearchTree<T1, T2> my_left_tree() throws myException;`
5. `public myBinarySearchTree<T1, T2> my_right_tree() throws myException;`
6. `public myBinarySearchNode<T1,T2> my_find(T1 key);`
7. `public myBinarySearchTree<T1, T2> my_insert(T1 key, T2 info);`
8. `public myBinarySearchTree<T1, T2> my_remove(T1 key);`
9. `public int my_length();`
10. `public int my_node_count();`
11. `public int my_leaf_count();`
12. `public myList<T2> my_inorder();`
13. `public myList<T2> my_preorder();`
14. `public myList<T2> my_postorder();`
15. `public myBinarySearchNode<T1, T2> my_maximum() throws myException;`
16. `public myBinarySearchNode<T1, T2> my_minimum() throws myException;`

All the operations are implemented in the class `myBinarySearchTreeImpl.java`.

2. Goal of the Assignment.

In this assignment the ADT `myBinarySearchTrees<T1, T2>` has been extended with 3 new operations:

17. `public int my_count_at_level(int level);`
This operation receives as an input the level of the tree we are looking for, and returns the amount of nodes placed on that level.
18. `public boolean my_is_balanced();`
A binary tree is balanced when the length of its two subtrees (left subtree and right subtree) do not differ in more than 1 unit, and the proper left subtree and right subtree are balanced trees as well).
This operation returns if the tree is balanced or not.
19. `public int my_count_smaller_nodes(T1 key);`
This operation receives as an input a key, and returns the amount of nodes in the tree with smaller key values.
20. `public int my_find_node_at_level(T1 key);`
This operation receives as an input a key, and returns the level were the node is located.

Exercise: Implement the 4 methods in the class `myBinarySearchTreeImpl.java` using recursion. *Note: You can reuse any of the other 16 defined operations if you want.*

3. Marking Scheme and Submission Date.

- **Total marks:** 10 (2.5 for each operation).
- **Submission instructions:** Submit to Blackboard the file `myBinarySearchTreeImpl.java`!
- **Submission deadline:** Sunday 7th May, 11:59pm.