

Question-3

~~low 42 36 33~~

M:	low	42	37	29	35	40	32
H:	M:	36	35	32	38	39	42
H:	H:	33	44	40	36	44	37

$$\bar{Y}_1 = 36.5714, \quad \bar{Y}_2 = 36.5714, \quad \bar{Y}_3 = 39.857$$

$$\bar{Y} = 37.666$$

$\rightarrow H_0 =$ All the α_i are the same.

$H_1 =$ not all the α_i are equal.

$$SS_A \quad n=7, \quad m=3$$

$m = \text{number of groups}$

$$SS_A = \sum_{i=1}^m n_i (\bar{Y}_i - \bar{Y})^2$$

$$= 7 \left\{ 2(36.5714 - 37.666)^2 + (39.857 - 37.666)^2 \right\}$$

$$= \underline{50.377}$$

$$F = \frac{\frac{SS_A}{m-1}}{\frac{SS_E}{N-m}} = \frac{\frac{50.377}{3-1}}{\frac{340.2781}{18}}$$

$$= \frac{25.1885}{19.4599} = 1.3324$$

$$SS_E = \sum_{i=1}^m \sum_{j=1}^{n_i} (Y_{ij} - \bar{Y}_i)^2$$

$$SS_T = \sum_{i=1}^m \sum_{j=1}^{n_i} (Y_{ij} - \bar{Y})^2$$

$$= (42 - 37.666)^2 + (41 - 37.666)^2 + (37 - 37.666)^2 \\ + (29 - 37.666)^2 + (35 - 37.666)^2 + (40 - 37.666)^2 \\ + (32 - 37.666)^2 + (36 - 37.666)^2 + (35 - 37.666)^2 \\ + (32 - 37.666)^2 + (38 - 37.666)^2 + (39 - 37.666)^2 \\ + (42 - 37.666)^2 + (34 - 37.666)^2 + (33 - 37.666)^2 \\ + (44 - 37.666)^2 + (40 - 37.666)^2 + (36 - 37.666)^2 \\ + (44 - 37.666)^2 + (37 - 37.666)^2 + (45 - 37.666)^2$$

$$SS_T = 390.6555$$

$$SS_E = SS_T - SSA$$

$$= 390.6555 - 50 \cdot 377$$

$$= 340.2781$$

$$f_{0.05, 20, 18} = 3.5546$$

प्रश्न 1

F (विद्यमान) < (क्रा. 3)

Patadin Max सान दिजेरु राना

Moxibac

let $n = \text{number of zeros} = 13$

$m = 11$ $h = 4$ $\text{one} = 12$

$$R_{un} = R = 10$$

$$E(R) = \mu = \frac{2mn}{m+n} + 1$$

$$V(R) = \sigma^2 = \frac{13.48}{19.48} \cdot \frac{(11-1)(12-2)}{m+n-1}$$

$$= \frac{(13.48-1)(13.48-2)}{25-1}$$

$$= 5.9696$$

$$\sigma = 2.4432$$

hence $R < \mu$ so,

$$p \text{ value} : 2\phi\left(\frac{(R-\mu)}{\sigma}\right) \\ = 2\phi\left(\frac{10-13.48}{2.4432}\right)$$

$$= 2\phi(-1.4243)$$

$$= 2 \times (0.0778)$$

$$= \boxed{0.1556}$$

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$P > 0.05$ so

null rejected

Moxibac

Question - 10

H_0 : The sample is random.

H_1 : The sample is not random.

sorted data:-

45 75 88 96 99 99

100 105 110 111 117 121

(122) 126 132 133 142 142

143 150 153 154 155 161

211

Now, Median = 122.

here, is, $x_i < \text{median}$; $x_i = 0$

otherwise $x_i = 1$

0 0 0 1 0 0 0 0 0 1 1

1 1 0 0 0 1 1 1 1 0 1

0 1

$$V(T) = \sigma^2 = \frac{mn(n+m+1)}{12}$$

$$= \frac{8 \times 7 (8+7+1)}{12}$$

$$= 74.6667$$

$$p \text{ value} = P(\Phi(T) \leq 66)$$

$$= P(\Phi \leq \frac{66 - 64}{74.6667})$$

$$= P(\Phi \leq 0.026785)$$

$$\approx 0.5080$$

$$p \text{ value} > 0.05.$$

so, we cannot reject the null

hypothesis.

$$P \text{ value} > 0.05$$



so, we cannot reject null hypothesis.

Question : 9

H_0 : has no effect.

H_1 : has effect.

	19	31	39	45	47	66	78	81
<u>RANK</u>	1	3	5	7	8	13	14	15
	28	36	44	49	52	52	60	
<u>RANK</u>	2	4	6	9	10.5	10.5	12	

Ranks: 1 2 3 4 5 6 7

→ $T = 66$ [Treatment group as rank sum]

$$n = 8 \quad m = 7$$

$$E(T) = \mu = \frac{48 \times (8+7+1)}{2} = 64$$

$$\sum \text{rank}_i = 6 + 1.5 + 18 + 12 + 19 + 10 + 8.5 + 15 + 6 + 17 + 16 + 13 + 11 = \underline{148}$$

$$T_- = \sum_{i=1}^n i I_i = \underline{148}$$

$$E(T_-) = \frac{n(n+1)}{4} = \frac{18 \times 19}{4} = 85.5$$

$$V(T_-) = \frac{n(n+1)(2n+1)}{24}$$

$$= \frac{18 \times 19 \times (18 \times 2 + 1)}{24}$$

$$= 527.25$$

$$P \text{ value} = P(T_- > t) \quad t = \underline{148}$$

$$= 1 - P(T_- \leq t)$$

$$= 1 - P\left(T_- \leq \frac{148 - 85.5}{527.25}\right)$$

$$= 1 - P(Z \leq 0.11854)$$

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$$1 - 0.5478 \quad \text{Moxibac}$$

$$= 0.4522$$

Question - 8

signed rank test

$$H_0: m = m_0$$

$$H_1: m < m_0$$

-5 -1 2 8 -25 1 5 -12 -16
-9 -8 -18 -5 -22 4 -21 -15 -11

absolute difference are:

5 1 2 8 25 1 5 12 16
9 8 18 5 22 4 21 15 21

1	2	3	4	5	6	7	8	9	10	11	12
1	1	2	4	5	5	5	8	8	9	9	11

12	15	16	18	21	22	25
12	13	14	15	16	14	13

1.5 1.5 3 4 ~~5.5~~ ~~5.5~~ 7.5 7.5

rank

1.5 1.5 3 4 6 6 8.5 8.5
10 11 12 13 14 15 16 17 18

Question - 7

standard value

$$n = 18$$

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$$\text{Median} = 0$$

(-5)	-1	+2	+8	-25	+1	+5	-12	-16
-9	-8	-18	-5	-22	+4	-21	-15	-11

$$1, 1, 0, 0, 1, 0, 0, -1, 1$$

$$1, 1, -1, -1, 1, 0, -1, 1, 1$$

$$\sum_{i=1}^n I_i = 13$$

Under the null, $\sum_{i=1}^n I_i \sim \text{binomial}(18, \frac{1}{2})$

thus, $p\text{value} = P\left(\sum_{i=1}^{18} I_i \leq 13\right)$

$$\Rightarrow \left({}^{18}C_{13} + {}^{18}C_{12} + {}^{18}C_{11} + {}^{18}C_{10} + {}^{18}C_9 + {}^{18}C_8 + {}^{18}C_7 + {}^{18}C_6 + {}^{18}C_5 + {}^{18}C_4 + {}^{18}C_3 + {}^{18}C_2 + {}^{18}C_1 + {}^{18}C_0 \right) \times \left(\frac{1}{2}\right)^{18}$$

$$P \Rightarrow 0.984558$$

Patadin Max

$$P > 0.05$$

so,

Null cannot be reject.

Moxibac

$$\chi^2_{\text{obj}} = \frac{(20 - 33.26)^2}{33.26} + \frac{(38 - 30.884)^2}{30.884} \\ + \frac{(28 - 21.856)^2}{21.856} + \frac{(50 - 36.74)^2}{36.74} \\ + \frac{(27 - 34.116)^2}{34.116} + \frac{(18 - 24.144)^2}{24.144} \\ = 16.4867.$$

$$\chi^2_{0.05, 2} = 5.991$$

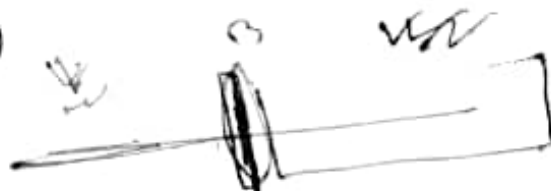
$$\chi^2_{\text{obj}} > \chi^2_{0.05, 2}$$

we reject the null hypothesis.

Question 7

$$H_0: m = m_0 \rightarrow m$$

$$H_1: m < m_0$$



Conclusion

There are no any effect of medicine.

$$\chi^2_{0.05, 2} = \underline{5.991}$$

$$\chi^2_{\text{obj}} < \chi^2_{0.05, 2}$$

We cannot reject the null hypothesis

Question: 6

Q

6

	Nonsmo	Moderate smoke	Heavy smoker	Total
Hypertension	20 (33.26)	38 (30.884)	28 (21.856)	86
No Hypertension	50 (36.74)	27 (34.116)	18 (24.1436)	95
total	70	65	46	181

$$\chi^2 = \sum_{i=1}^n \sum_{j=1}^c \frac{(O_{ij} - E_{ij})^2}{E_{ij}}$$

H_0 : There is ^{no} relation between hypertension and smokers.

H_1 : there is ~~not~~ a relation between hypertension and smoker.

$$F_{0.95, m-1, (n-1)(m-1)}$$

$$\Rightarrow F_{0.95, 3, 6} = \cancel{2.888} \quad \underline{4.76}$$

Always in both case.

Null rejected.

Question - 5 -

	obj. freq.	probability	<u>Expected freq</u>
White	141	$\frac{1}{4}$	141
pink	291	$\frac{1}{2}$	282
red	132	$\frac{1}{4}$	141
total = 564			

H_0 : The distribution fits the data.

H_1 : The distribution does not fit the data.

$$\chi^2 = \sum_{i=1}^n \frac{(O_{ij} - E_i)^2}{E_i}$$

$$= \frac{(141-141)^2}{141} + \frac{(291-282)^2}{282} + \frac{(132-141)^2}{141}$$

$$= \frac{27}{94} + \frac{27}{47} = \underline{0.86170}$$

Question - 4

2 factor ANOVA

Hypothesis for method:

H_0 : All α_i are zero.

H_1 : Not all are zero.

" for storage condition:

(B) H_0 : All β_i are zero.

H_1 : Not all β_i are zero.

	A	B	C	D
1	1.35	1.13	1.06	0.98
2	1.40	1.23	1.26	1.22
3	1.49	1.43	1.40	1.35

$$\bar{Y} = 1.2775$$

Y_{11}	Y_{12}	Y_{13}	Y_{14}
1.413	1.2633	1.24	1.1833

$$\bar{Y}_{1.} = 1.13$$

$$\bar{Y}_{2.} = 1.2775$$

$$\bar{Y}_{3.} = 1.4275$$

$$SS_A = n \sum_{i=1}^m \left\{ (1.13 - 1.2775)^2 + (1.2775 - 1.2775)^2 + (1.4275 - 1.2775)^2 \right\}$$

$$= 0.17405$$

$$m=4$$

$$SS_B = m \sum_{j=1}^n (Y_{.j} - \bar{Y})^2$$

$$= 3 \times \left\{ (1.413 - 1.2775)^2 + (1.2633 - 1.2775)^2 + (1.24 - 1.2775)^2 + (1.1833 - 1.2775)^2 \right\}$$

$$= 0.08652$$

$$SS_T = \sum_{i=1}^n \sum_{j=1}^m (\bar{Y}_{ij} - \bar{Y})^2$$

$$= (1.35 - 1.2775)^2 + (1.13 - 1.2775)^2 + (1.06 - 1.2775)^2 + (0.98 - 1.2775)^2 + (1.40 - 1.2775)^2 + (1.23 - 1.2775)^2 + (1.26 - 1.2775)^2 + (1.22 - 1.2775)^2 + (1.49 - 1.2775)^2 + (1.43 - 1.2775)^2 + (1.40 - 1.2775)^2 + (1.35 - 1.2775)^2$$

$$\Rightarrow SS_T = 0.272375$$

$$SS_E = SS_T - (SS_A + SS_B) = 0.011805$$

$$F_A = \frac{SS_A / (m-1)}{SS_E / (n-1)(m-1)}$$

$$= 22.90$$

$$F_B = 7.50$$

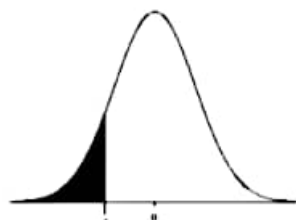
Patadin Max

$$F_{0.95, 2, 8} = 3.4131$$

Moxibac

cum. prob	$t_{.50}$	$t_{.75}$	$t_{.90}$	$t_{.95}$	$t_{.99}$	$t_{.995}$	$t_{.9975}$	$t_{.999}$	$t_{.9995}$	$t_{.9999}$	$t_{.99995}$
one-tail	0.50	0.25	0.20	0.15	0.10	0.05	0.025	0.01	0.005	0.001	0.0005
two-tails	1.00	0.50	0.40	0.30	0.20	0.10	0.05	0.02	0.01	0.002	0.001
df											
1	0.000	1.000	1.376	1.963	3.078	6.314	12.71	31.82	63.66	318.31	636.62
2	0.000	0.816	1.061	1.386	1.886	2.920	4.303	6.965	9.925	22.327	31.599
3	0.000	0.765	0.978	1.250	1.638	2.353	3.182	4.541	5.841	10.215	12.924
4	0.000	0.741	0.941	1.190	1.533	2.132	2.776	3.747	4.604	7.173	8.610
5	0.000	0.727	0.920	1.156	1.476	2.015	2.571	3.365	4.032	5.893	6.869
6	0.000	0.718	0.906	1.134	1.440	1.943	2.447	3.143	3.707	5.208	5.959
7	0.000	0.711	0.896	1.119	1.415	1.895	2.365	2.998	3.499	4.785	5.408
8	0.000	0.706	0.889	1.108	1.397	1.860	2.306	2.896	3.355	4.501	5.041
9	0.000	0.703	0.883	1.100	1.383	1.833	2.262	2.821	3.250	4.297	4.781
10	0.000	0.700	0.879	1.093	1.372	1.812	2.228	2.764	3.169	4.144	4.587
11	0.000	0.697	0.876	1.088	1.363	1.796	2.201	2.718	3.106	4.025	4.437
12	0.000	0.695	0.873	1.083	1.356	1.782	2.179	2.681	3.055	3.930	4.318
13	0.000	0.694	0.870	1.079	1.350	1.771	2.160	2.650	3.012	3.852	4.221
14	0.000	0.692	0.868	1.076	1.345	1.761	2.145	2.624	2.977	3.787	4.140
15	0.000	0.691	0.866	1.074	1.341	1.753	2.131	2.602	2.947	3.733	4.073
16	0.000	0.690	0.865	1.071	1.337	1.746	2.120	2.583	2.921	3.686	4.015
17	0.000	0.689	0.863	1.069	1.333	1.740	2.110	2.567	2.898	3.646	3.965
18	0.000	0.688	0.862	1.067	1.330	1.734	2.101	2.552	2.878	3.610	3.922
19	0.000	0.688	0.861	1.066	1.328	1.729	2.093	2.539	2.861	3.579	3.883
20	0.000	0.687	0.860	1.064	1.325	1.725	2.086	2.528	2.845	3.552	3.850
21	0.000	0.686	0.859	1.063	1.323	1.721	2.080	2.518	2.831	3.527	3.819
22	0.000	0.686	0.858	1.061	1.321	1.717	2.074	2.508	2.819	3.505	3.792
23	0.000	0.685	0.858	1.060	1.319	1.714	2.069	2.500	2.807	3.485	3.768
24	0.000	0.685	0.857	1.059	1.318	1.711	2.064	2.492	2.797	3.467	3.745
25	0.000	0.684	0.856	1.058	1.316	1.708	2.060	2.485	2.787	3.450	3.725
26	0.000	0.684	0.856	1.058	1.315	1.706	2.056	2.479	2.779	3.435	3.707
27	0.000	0.684	0.855	1.057	1.314	1.703	2.052	2.473	2.771	3.421	3.690
28	0.000	0.683	0.855	1.056	1.313	1.701	2.048	2.467	2.763	3.408	3.674
29	0.000	0.683	0.854	1.055	1.311	1.699	2.045	2.462	2.756	3.396	3.659
30	0.000	0.683	0.854	1.055	1.310	1.697	2.042	2.457			

Table of Standard Normal Probabilities for Negative Z-scores



z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
-3.4	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0002
-3.3	0.0005	0.0005	0.0005	0.0004	0.0004	0.0004	0.0004	0.0004	0.0004	0.0003
-3.2	0.0007	0.0007	0.0006	0.0006	0.0006	0.0006	0.0006	0.0005	0.0005	0.0005
-3.1	0.0010	0.0009	0.0009	0.0009	0.0008	0.0008	0.0008	0.0008	0.0007	0.0007
-3.0	0.0013	0.0013	0.0013	0.0012	0.0012	0.0011	0.0011	0.0011	0.0010	0.0010
-2.9	0.0019	0.0018	0.0018	0.0017	0.0016	0.0016	0.0015	0.0015	0.0014	0.0014
-2.8	0.0026	0.0025	0.0024	0.0023	0.0023	0.0022	0.0021	0.0021	0.0020	0.0019
-2.7	0.0035	0.0034	0.0033	0.0032	0.0031	0.0030	0.0029	0.0028	0.0027	0.0026
-2.6	0.0047	0.0045	0.0044	0.0043	0.0041	0.0040	0.0039	0.0038	0.0037	0.0036
-2.5	0.0062	0.0060	0.0059	0.0057	0.0055	0.0054	0.0052	0.0051	0.0049	0.0048
-2.4	0.0082	0.0080	0.0078	0.0075	0.0073	0.0071	0.0069	0.0068	0.0066	0.0064
-2.3	0.0107	0.0104	0.0102	0.0099	0.0096	0.0094	0.0091	0.0089	0.0087	0.0084
-2.2	0.0139	0.0136	0.0132	0.0129	0.0125	0.0122	0.0119	0.0116	0.0113	0.0110
-2.1	0.0179	0.0174	0.0170	0.0166	0.0162	0.0158	0.0154	0.0150	0.0146	0.0143
-2.0	0.0228	0.0222	0.0217	0.0212	0.0207	0.0202	0.0197	0.0192	0.0188	0.0183
-1.9	0.0287	0.0281	0.0274	0.0268	0.0262	0.0256	0.0250	0.0244	0.0239	0.0233
-1.8	0.0359	0.0351	0.0344	0.0336	0.0329	0.0322	0.0314	0.0307	0.0301	0.0294
-1.7	0.0446	0.0436	0.0427	0.0418	0.0409	0.0401	0.0392	0.0384	0.0375	0.0367
-1.6	0.0548	0.0537	0.0526	0.0516	0.0505	0.0495	0.0485	0.0475	0.0465	0.0455
-1.5	0.0668	0.0655	0.0643	0.0630	0.0618	0.0606	0.0594	0.0582	0.0571	0.0559
-1.4	0.0808	0.0793	0.0778	0.0764	0.0749	0.0735	0.0721	0.0708	0.0694	0.0681
-1.3	0.0968	0.0951	0.0934	0.0918	0.0901	0.0885	0.0869	0.0853	0.0838	0.0823
-1.2	0.1151	0.1131	0.1112	0.1093	0.1075	0.1056	0.1038	0.1020	0.1003	0.0985
-1.1	0.1357	0.1335	0.1314	0.1292	0.1271	0.1251	0.1230	0.1210	0.1190	0.1170
-1.0	0.1587	0.1562	0.1539	0.1515	0.1492	0.1469	0.1446	0.1423	0.1401	0.1379
-0.9	0.1841	0.1814	0.1788	0.1762	0.1736	0.1711	0.1685	0.1660	0.1635	0.1611
-0.8	0.2119	0.2090	0.2061	0.2033	0.2005	0.1977	0.1949	0.1922	0.1894	0.1867
-0.7	0.2420	0.2389	0.2358	0.2327	0.2296	0.2266	0.2236	0.2206	0.2177	0.2148
-0.6	0.2743	0.2709	0.2676	0.2643	0.2611	0.2578	0.2546	0.2514	0.2483	0.2451
-0.5	0.3085	0.3050	0.3015	0.2981	0.2946	0.2912	0.2877	0.2843	0.2810	0.2776
-0.4	0.3446	0.3409	0.3372	0.3336	0.3300	0.3264	0.3228	0.3192	0.3156	0.3121
-0.3	0.3821	0.3783	0.3745	0.3707	0.3669	0.3632	0.3594	0.3557	0.3520	0.3483
-0.2	0.4207	0.4168	0.4129	0.4090	0.4052	0.4013	0.3974	0.3936	0.3897	0.3859
-0.1	0.4602	0.4562	0.4522	0.4483	0.4443	0.4404	0.4364	0.4325	0.4286	0.4247
-0.0	0.5000	0.4960	0.4920	0.4880	0.4840	0.4801	0.4761	0.4721	0.4681	0.4641

Table of Standard Normal Probabilities for Positive Z-scores



z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.0	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990
3.1	0.9990	0.9991	0.9991	0.9991	0.9992	0.9992	0.9992	0.9992	0.9993	0.9993
3.2	0.9993	0.9993	0.9994	0.9994	0.9994	0.9994	0.9994	0.9995	0.9995	0.9995
3.3	0.9995	0.9995	0.9995	0.9996	0.9996	0.9996	0.9996	0.9996	0.9996	0.9997
3.4	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9998

**Note that the probabilities given in this table represent the area to the LEFT of the z-score.
The area to the RIGHT of a z-score = 1 – the area to the LEFT of the z-score**

DF2	DF1 $\alpha = 0.05$																		
	1	2	3	4	5	6	7	8	9	10	12	15	20	24	30	40	60	120	Inf
1	161.45	199.5	215.71	224.58	230.16	233.99	236.77	238.88	240.54	241.88	243.91	245.95	248.01	249.05	250.1	251.14	252.2	253.25	254.31
2	18.513	19	19.164	19.247	19.296	19.33	19.353	19.371	19.385	19.396	19.413	19.429	19.446	19.454	19.462	19.471	19.479	19.487	19.496
3	10.128	9.5521	9.2766	9.1172	9.0135	8.9406	8.8867	8.8452	8.8123	8.7855	8.7446	8.7029	8.6602	8.6385	8.6166	8.5944	8.572	8.5494	8.5264
4	7.7086	6.9443	6.5914	6.3882	6.2561	6.1631	6.0942	6.041	5.9988	5.9644	5.9117	5.8578	5.8025	5.7744	5.7459	5.717	5.6877	5.6581	5.6281
5	6.6079	5.7861	5.4095	5.1922	5.0503	4.9503	4.8759	4.8183	4.7725	4.7351	4.6777	4.6188	4.5581	4.5272	4.4957	4.4638	4.4314	4.3985	4.365
6	5.9874	5.1433	4.7571	4.5337	4.3874	4.2839	4.2067	4.1468	4.099	4.06	3.9999	3.9381	3.8742	3.8415	3.8082	3.7743	3.7398	3.7047	3.6689
7	5.5914	4.7374	4.3468	4.1203	3.9715	3.866	3.787	3.7257	3.6767	3.6365	3.5747	3.5107	3.4445	3.4105	3.3758	3.3404	3.3043	3.2674	3.2298
8	5.3177	4.459	4.0662	3.8379	3.6875	3.5806	3.5005	3.4381	3.3881	3.3472	3.2839	3.2184	3.1503	3.1152	3.0794	3.0428	3.0053	2.9669	2.9276
9	5.1174	4.2565	3.8625	3.6331	3.4817	3.3738	3.2927	3.2296	3.1789	3.1373	3.0729	3.0061	2.9365	2.9005	2.8637	2.8259	2.7872	2.7475	2.7067
10	4.9646	4.1028	3.7083	3.478	3.3258	3.2172	3.1355	3.0717	3.0204	2.9782	2.913	2.845	2.774	2.7372	2.6996	2.6609	2.6211	2.5801	2.5379
11	4.8443	3.9823	3.5874	3.3567	3.2039	3.0946	3.0123	2.948	2.8962	2.8536	2.7876	2.7186	2.6464	2.609	2.5705	2.5309	2.4901	2.448	2.4045
12	4.7472	3.8853	3.4903	3.2592	3.1059	2.9961	2.9134	2.8486	2.7964	2.7534	2.6866	2.6169	2.5436	2.5055	2.4663	2.4259	2.3842	2.341	2.2962
13	4.6672	3.8056	3.4105	3.1791	3.0254	2.9153	2.8321	2.7669	2.7144	2.671	2.6037	2.5331	2.4589	2.4202	2.3803	2.3392	2.2966	2.2524	2.2064
14	4.6001	3.7389	3.3439	3.1122	2.9582	2.8477	2.7642	2.6987	2.6458	2.6022	2.5342	2.463	2.3879	2.3487	2.3082	2.2664	2.2229	2.1778	2.1307
15	4.5431	3.6823	3.2874	3.0556	2.9013	2.7905	2.7066	2.6408	2.5876	2.5437	2.4753	2.4034	2.3275	2.2878	2.2468	2.2043	2.1601	2.1141	2.0658
16	4.494	3.6337	3.2389	3.0069	2.8524	2.7413	2.6572	2.5911	2.5377	2.4935	2.4247	2.3522	2.2756	2.2354	2.1938	2.1507	2.1058	2.0589	2.0096
17	4.4513	3.5915	3.1968	2.9647	2.81	2.6987	2.6143	2.548	2.4943	2.4499	2.3807	2.3077	2.2304	2.1898	2.1477	2.104	2.0584	2.0107	1.9604
18	4.4139	3.5546	3.1599	2.9277	2.7729	2.6613	2.5767	2.5102	2.4563	2.4117	2.3421	2.2686	2.1906	2.1497	2.1071	2.0629	2.0166	1.9681	1.9168
19	4.3807	3.5219	3.1274	2.8951	2.7401	2.6283	2.5435	2.4768	2.4227	2.3779	2.308	2.2341	2.1555	2.1141	2.0712	2.0264	1.9795	1.9302	1.878
20	4.3512	3.4928	3.0984	2.8661	2.7109	2.599	2.514	2.4471	2.3928	2.3479	2.2776	2.2033	2.1242	2.0825	2.0391	1.9938	1.9464	1.8963	1.8432
21	4.3248	3.4668	3.0725	2.8401	2.6848	2.5727	2.4876	2.4205	2.366	2.321	2.2504	2.1757	2.096	2.054	2.0102	1.9645	1.9165	1.8657	1.8117
22	4.3009	3.4434	3.0491	2.8167	2.6613	2.5491	2.4638	2.3965	2.3419	2.2967	2.2258	2.1508	2.0707	2.0283	1.9842	1.938	1.8894	1.838	1.7831
23	4.2793	3.4221	3.028	2.7955	2.64	2.5277	2.4422	2.3748	2.3201	2.2747	2.2036	2.1282	2.0476	2.005	1.9605	1.9139	1.8648	1.8128	1.757
24	4.2597	3.4028	3.0088	2.7763	2.6207	2.5082	2.4226	2.3551	2.3002	2.2547	2.1834	2.1077	2.0267	1.9838	1.939	1.892	1.8424	1.7896	1.733
25	4.2417	3.3852	2.9912	2.7587	2.603	2.4904	2.4047	2.3371	2.2821	2.2365	2.1649	2.0889	2.0075	1.9643	1.9192	1.8718	1.8217	1.7684	1.711
26	4.2252	3.369	2.9752	2.7426	2.5868	2.4741	2.3883	2.3205	2.2655	2.2197	2.1479	2.0716	1.9898	1.9464	1.901	1.8533	1.8027	1.7488	1.6906
27	4.21	3.3541	2.9604	2.7278	2.5719	2.4591	2.3732	2.3053	2.2501	2.2043	2.1323	2.0558	1.9736	1.9299	1.8842	1.8361	1.7851	1.7306	1.6717
28	4.196	3.3404	2.9467	2.7141	2.5581	2.4453	2.3593	2.2913	2.236	2.19	2.1179	2.0411	1.9586	1.9147	1.8687	1.8203	1.7689	1.7138	1.6541
29	4.183	3.3277	2.934	2.7014	2.5454	2.4324	2.3463	2.2783	2.2229	2.1768	2.1045	2.0275	1.9446	1.9005	1.8543	1.8055	1.7537	1.6981	1.6376
30	4.1709	3.3158	2.9223	2.6896	2.5336	2.4205	2.3343	2.2662	2.2107	2.1646	2.0921	2.0148	1.9317	1.8874	1.8409	1.7918	1.7396	1.6835	1.6223
40	4.0847	3.2317	2.8387	2.606	2.4495	2.3359	2.249	2.1802	2.124	2.0772	2.0035	1.9245	1.8389	1.7929	1.7444	1.6928	1.6373	1.5766	1.5089
60	4.0012	3.1504	2.7581	2.5252	2.3683	2.2541	2.1665	2.097	2.0401	1.9926	1.9174	1.8364	1.748	1.7001	1.6491	1.5943	1.5343	1.4673	1.3893
120	3.9201	3.0718	2.6802	2.4472	2.2899	2.175	2.0868	2.0164	1.9588	1.9105	1.8337	1.7505	1.6587	1.6084	1.5543	1.4952	1.429	1.3519	1.2539
Inf	3.8415	2.9957	2.6049	2.3719	2.2141	2.0986	2.0096	1.9384	1.8799	1.8307	1.7522	1.6664	1.5705	1.5173	1.4591	1.394	1.318	1.2214	1