

## Portfolio:

- Stock A, 60%
- Stock B, 30%
- Stock C, 10%

Analysis that we are running on the portfolio:

In finance, a number "+10% return" is meaningless in a vacuum. It only has meaning when compared to an alternative. We evaluate a portfolio (a set of stocks) by asking three fundamental questions:

1. The Survival Test (Inflation): Did the portfolio make money *in real terms*?
  - o i.e. if your portfolio grew by 2% but inflation was 3%, you actually *lost* purchasing power.
  - o CPI (Consumer Price Index) or a **flat inflation rate** (e.g., 3%).
  - o We test whether portfolio return is greater than inflation or not.
2. The Opportunity Cost Test (S&P 500): Could the portfolio have made this money *doing nothing*?
  - o User could have just bought the entire S&P 500 (the 500 biggest US companies) with one click. If you spent hours picking specific stocks (Stock A, Stock B) but made *less* money than the S&P 500, you wasted your time.
  - o Portfolio's return must be higher than the S&P 500 return.
3. The "Skill" Test (Risk-Adjusted Return): Did portfolio take on too much danger to get this return?
  - o Making 20% is great. But if you took a risk that could have wiped you out to get it, that was "bad" investing (gambling). We need to measure if the speed was worth the bumpiness.
  - o Beta scoring. Beta>1 => more volatile than S&P 500.
  - o We test whether beta <=1.

## Fetching:

- Market data
  - o Getting price **returns** from raw data of closing prices
  - o  $(\text{today's closure price} / \text{yesterday's closure price}) - 1$

need to find:

- Portfolio Return ( $R_p$ ): The weighted average return of the user's stocks over the period.
  - o  $PR_1$ : avg return for Stock A over 1 year
  - o  $PR_2$ : avg return for Stock B over 1 year
  - o  $PR_3$ : avg return for Stock C over 1 year
  - o Percentage split:  $p_1, p_2, p_3$  (e.g. 0.6, 0.3, 0.1)
  - o  $R_p = PR_1 * p_1 + PR_2 * p_2 + PR_3 * p_3$
- Market Return ( $R_m$ ): The return of the S&P 500 over the same period.
  - o  $R_m$ : avg return of S&P 500 over 1 year
- Risk-Free Rate ( $R_f$ ): Usually the 10-Year Treasury Yield (currently ~4-4.5%). This is the return you get for taking zero risk.
  - o  $R_f$ : fixed rate, 4%, i.e. 0.04
- Beta ( $\beta$ ): A measure of how volatile the portfolio is compared to the market.
  - o Volatility of S&P 500 is defined as 1.0.
  - o Annual (individual!) volatility = daily std \*  $\sqrt{252}$ 
    - Daily std:
      - Collect closing prices
      - $(\text{today's closure price} / \text{yesterday's closure price}) - 1$

- STD of the above data
- to find the covariance between Stock A and Stock B, you multiply their deviations together for every single day, sum them up, and divide by the number of days.
- $\text{STD of portfolio} = \sqrt{\text{weights}^T * \text{CovMatrix} * \text{weights}}$

Score calculation:

1. Survival Test, Inflation (**30** points)
  - Survival gradient: if Inflation is 3% and you made 2.9%, you preserved almost all your wealth. That is infinitely better than losing -20%. So we set a "Floor" (0% return) and a "Ceiling" (a great return, e.g., 10% or Inflation + 7%).
  - Floor (<0% Return): 0 Points. (You lost nominal money. This is bad.)
  - Baseline (0% to Inflation): 1 to 15 Points. (You made money, but lost purchasing power. Better than nothing.)
  - Target (> Inflation): 16 to 30 Points. (You grew your wealth in real terms.)
  - $\text{ScoreInflation} = (\text{Rp} / 0.1) * 30\text{pts}$
2. Opportunity Cost Test, S&P 500 (**40** points)
  - $\alpha=0$ : You did exactly as well as the market expected for your risk level. This is actually a good result.
  - $\alpha>0$ : You are beating the market (great).
  - $\alpha<0$ : You are underperforming (bad).
  - Since beating the market is extremely hard, we shouldn't punish a user too hard for having an Alpha near 0.
    - We will center the score at 20 points (half credit) for an Alpha of 0.
    - Range: We will look at an Alpha range of -5% to +5%.
    - Alpha  $\leq -5\%$ : 0 Points (failed badly).
    - Alpha = 0%: 20 Points (solid, efficient investment).
    - Alpha  $\geq +5\%$ : 40 Points (amazing).
  - $\text{ScoreAlpha} = 20 + (\text{alpha} * 400); \leftarrow \text{/clamp it to be } 0..40/$
3. "Skill" Test, Risk-Adjusted Return (**30** points)
  - Sharpe  $<0$ : 0 Points.
  - Sharpe = 1.0 (Market Average): 15 Points.
  - Sharpe  $\geq 2.0$ : 30 Points.
  - Sharpe ratio measures "Return per unit of Risk."
    - $\text{Sharpe} = (\text{Rp} - \text{Rf}) / \text{StdPortfolio}$
  - $\text{ScoreSharpe} = \text{Sharpe} * 15; \leftarrow \text{/clamp it to be } 0..30/$

The score should be >65 to be Good.

Example: