
import

```
In[2]:= data = Association@Import[FileNameJoin[{NotebookDirectory[], "data.json"}]];
```

```
In[3]:= data
```

Out[3]=

```
<| numberOfContainers → 80, ... 9 ... , solutionsStat →  
  { { 236.523, 236.523, 233.577, 233.577, 233.577, 232.983, 232.983, 231.987, 231.987,  
    230.959, 230.959, ... 129 ... , 210.266, 210.266, 210.266, 209.871, 209.871,  
    209.871, 209.871, 209.871, 209.871, 209.871, 209.871 }, ... 3 ... , { ... 1 ... } } |>
```

large output

[show less](#)

[show more](#)

[show all](#)

[set size limit...](#)

```
In[4]:= isImport = True;
```

```
In[5]:= Clear[import]
```

```
import[input_, key_, isImport_] := If[isImport, data[key], input]
```

settings

functions

```
In[7]:= getVarianteTwoArg =  
  RandomVariate@MultinomialDistribution[#1, ConstantArray[1 / #2, #2]] &;
```

initial parameters

```
In[8]:= numberOfContainers = import[7, "numberOfContainers", isImport];  
numberOfVehicles = import[2, "numberOfVehicles", isImport];  
numberOfStacks = import[2, "numberOfStacks", isImport];
```

```
In[11]:=  $\epsilon$  = 0.1;  
shareOfPairsBlocks = 0.05;
```

generate initial data

```
In[13]:= vertices1 = Range@numberOfContainers;  
vertices2 = vertices1 + numberOfContainers;
```

```

In[15]:= If[
    isImport,
    pointsVertices1 = data["pointsVertices1"];
    pointsVertices2 = data["pointsVertices2"],
    {pointsVertices1, pointsVertices2} =
        Table[RandomReal[{1, 5}, {numberOfContainers, 2}], 2];
];

In[16]:= distanceMatrix = DistanceMatrix[pointsVertices1, pointsVertices2];

In[17]:= points = Join[pointsVertices1, pointsVertices2];

In[18]:=  $\delta 1 = \delta 2 = \text{Ceiling}@\text{Mean}@\text{Flatten}@distanceMatrix;$ 

In[19]:= outArcs = MapThread[DirectedEdge, {vertices1, vertices2}];
inArcs = DeleteCases[Flatten[Outer[DirectedEdge, vertices2, vertices1]],
    i_  $\leftrightarrow$  j_ /; i - numberOfContainers == j];
startArcs = Thread[DirectedEdge[0, vertices1]];
endArcs = Thread[DirectedEdge[vertices2, 2 numberOfContainers + 1]];
arcs = Join[startArcs, inArcs, outArcs, endArcs];

In[24]:= time = Join[
    Association[#  $\rightarrow$  distanceMatrix[[#][1], #[2] - numberOfContainers] & /@ outArcs],
    Association[#  $\rightarrow$  distanceMatrix[[#][2], #[1] - numberOfContainers] & /@ inArcs],
    Association[#  $\rightarrow$  0 & /@ startArcs],
    Association[#  $\rightarrow$  0 & /@ endArcs]
];

In[25]:= If[
    isImport,
    stacks = data["stacks"],
    stacks = TakeList[RandomSample@vertices1,
        getVarianteTwoArg[numberOfContainers, numberOfStacks]]
];

In[26]:= If[
    isImport,
    pairsVertices1 = data["pairsVertices1"];
    pairsVertices2 = data["pairsVertices2"],
    {pairsVertices1, pairsVertices2} =
        RandomSample[#, Floor[shareOfPairsBlocks Length@#]] &@Subsets[#, {2}] & /@
        {vertices1, vertices2};
];

In[27]:= relationsPairsVertices1 = Flatten[Subsets[#, {2}] & /@ stacks, 1];

In[28]:= K = numberOfVehicles (Total[Max /@ distanceMatrix] + Total[Max /@ (distanceMatrixT)]);

```

2Opt, 2HOpt, 4Opt functions

```

In[29]:= Clear[f]
f[x_] :=
  Total[distanceMatrix[[#1], #2]] & /@ Partition[x, 2, 1] + distanceMatrix[x[-1], x[1]]

In[31]:= Clear[inverse]
inverse[permutation_, i1_, j1_] := Module[
  {p = permutation, sortedij = Sort[{i1, j1}], i, j, oldi},
  i = sortedij[[1]];
  j = sortedij[[2]];
  If[
    j - i == Length[p] - 1,
    oldi = p[[i]]; p[[i]] = p[[j]]; p[[j]] = oldi; p,
    Join[p[[1 ;; i - 1]], Reverse[p[[i ;; j]], p[[j + 1 ;; Length@p]]]
  ]
]

In[33]:= Clear[insert]
insert[permutation_, i_, j_] := Module[
  {p = permutation, element = permutation[[j]]},
  p = Drop[p, {j}]; Insert[p, element, i]
]

In[35]:= Clear[swap]
swap[permutation_, i_, j_] := Module[
  {p = permutation, element = permutation[[i]]},
  p[[i]] = p[[j]]; p[[j]] = element; p
]

```

curing routes

```

In[37]:= (*Пары для каждого маршрута, котрые надо проверить*)
Clear[pairsForRoute]
pairsForRoute[route_] :=
  Select[relationsPairsVertices1, MemberQ[route, #1] & MemberQ[route, #2] &]

```

```

In[39]:= (*Устранение недопустимых решений*)
Clear[cureFunction]
cureFunction[routesOfTrip_] := Module[
  {routes = routesOfTrip, pairs, begin, pair, positions},
  Do[
    pairs = pairsForRoute[routes[[i]]];
    Label[begin];
    Do[
      pair = pairs[[j]];
      positions = Flatten[Position[routes[[i]], #] & /@ pair];
      If[
        positions[[1]] < positions[[2]],
        routes[[i]] = swap[routes[[i]], positions[[1]], positions[[2]]]; Goto[begin]
      ],
      {j, Length[pairs]}
    ],
    {i, Length[routes]}
  ];
  routes
]

```

find potentials

variables

```

In[41]:= varsU = u /@ Range[2 numberOfContainers];
varsUOut = u[0, #] & /@ Range[numberOfVehicles];
varsUIn = u[2 numberOfContainers + 1, #] & /@ Range[numberOfVehicles];

In[44]:= varsYPV1 = y @@@ pairsVertices1;
varsYPV2 = y @@@ pairsVertices2;

In[46]:= vars = Join[varsU, varsUOut, varsUIn, varsYPV1, varsYPV2, {umax}];

```

objfun

```

In[47]:= objfun = {Total[varsUIn - varsUOut], umax} . {0.5, 0.5};

In[48]:= c = Last@CoefficientArrays[objfun, vars];

```

constraints

```

In[49]:= cons1 = umax - varsUIn;

In[50]:= rhs1 = ConstantArray[{0, 1}, Length[cons1]];

In[51]:= cons2 = u[#[[1]]] - u[#[[2]]] & /@ relationsPairsVertices1;

```

```

In[52]:= rhs2 = ConstantArray[{ $\delta_1$ , 1}, Length[relationsPairsVertices1]];
In[53]:= cons31 = u[#[[2]]] - u[#[[1]]] - K * y[#[[1]], #[[2]]] & /@ pairsVertices1;
In[54]:= rhs31 = ConstantArray[{- $\delta_2$ , -1}, Length[pairsVertices1]];
In[55]:= cons32 = u[#[[1]]] - u[#[[2]]] + K * y[#[[1]], #[[2]]] & /@ pairsVertices1;
In[56]:= rhs32 = ConstantArray[{K -  $\delta_2$ , -1}, Length[pairsVertices1]];
In[57]:= cons41 = u[#[[2]]] - u[#[[1]]] - K * y[#[[1]], #[[2]]] & /@ pairsVertices2;
In[58]:= rhs41 = ConstantArray[{- $\delta_2$ , -1}, Length[pairsVertices2]];
In[59]:= cons42 = u[#[[1]]] - u[#[[2]]] + K * y[#[[1]], #[[2]]] & /@ pairsVertices2;
In[60]:= rhs42 = ConstantArray[{K -  $\delta_2$ , -1}, Length[pairsVertices2]];
In[61]:= lu = Join[
    ConstantArray[{0, K}, Length[varsU] + Length[varsUOut] + Length[varsUIn]],
    ConstantArray[{0, 1}, Length[varsYPV1] + Length[varsYPV2]],
    ConstantArray[{0, K}, 1]
];
In[62]:= domain = Join[
    ConstantArray[Reals, Length[varsU] + Length[varsUOut] + Length[varsUIn]],
    ConstantArray[Integers, Length[varsYPV1] + Length[varsYPV2]],
    ConstantArray[Reals, 1]
];

```

gurobi settings

```

In[63]:= Get[FileNameJoin[{NotebookDirectory[], "GurobiOptimization.wl"}]]
In[64]:= directory = "C:\\gurobi912\\win64\\bin\\";

```

main function

```

In[65]:= (*Сокращенных маршруты преобразуются в полные*)
Clear[fullRoutes]
fullRoutes := Table[Riffle[#[[i]], #[[i]] + numberOfContainers], {i, Length[#]}] &

In[67]:= (*Дуги маршрутов полных маршрутов*)
Clear[pairsOfFullRoutes]
pairsOfFullRoutes[routes_] := Flatten[Partition[#, 2, 1] & /@ fullRoutes[routes], 1]

```

```

In[69]:= Clear[findPotentials]
findPotentials[routes_] := Module[{
  cons5FullRoutes = fullRoutes[routes],
  cons5Pairs = pairsOfFullRoutes[routes],
  cons5, rhs5, cons6, rhs6, cons7, rhs7, m, b,
},
cons5 = u[#[[2]]] - u[#[[1]]] & /@ cons5Pairs;
rhs5 = {time[#[[1]]  $\leftrightarrow$  #[[2]], 1} & /@ cons5Pairs;
cons6 = Flatten[Table[
  If[Length[cons5FullRoutes[[i]]] == 0, {},
  {u[First[cons5FullRoutes[[i]]] - u[0, i],
  u[2 numberOfContainers + 1, i] - u[Last[cons5FullRoutes[[i]]]}
], {i, Length@cons5FullRoutes}]];
rhs6 = ConstantArray[{0, 1}, Length[cons6]];
cons7 = varsUOut;
rhs7 = {Length[#] * K, -1} & /@ routes;
m = Last@CoefficientArrays[
  Join[cons1, cons2, cons31, cons32, cons41, cons42, cons5, cons6, cons7], vars];
b = Join[rhs1, rhs2, rhs31, rhs32, rhs41, rhs42, rhs5, rhs6, rhs7];
(*LinearProgramming[c,m,b,lu,domain]*)
GurobiOptimization[Normal@c, Normal@m, b, lu, domain, directory]
]

```

target function

```

In[71]:= Clear[f]
f[routes_] := Module[{
  solution = Quiet@Check[findPotentials[routes], K],
  umax, varsUIn, varsUOut
},
If[solution == K, Return[solution]];
umax = Last[solution];
varsUIn = solution[[2 numberOfContainers + numberOfVehicles + 1
;; 2 (numberOfContainers + numberOfVehicles)]];
varsUOut = solution[[2 numberOfContainers + 1 ;; 2 numberOfContainers + numberOfVehicles]];
{Total[varsUIn - varsUOut], umax}.{0.5, 0.5}
]

```

simulated annealing

```

In[73]:= Clear[routesToAnnealing]
routesToAnnealing := Flatten[Riffle[#, 0]] &

In[75]:= Clear[routesFromAnnealing]
routesFromAnnealing[routes_] := DeleteCases[#, 0] & /@ (Split[routes, # != 0 &])

```

```

In[77]:= Clear[minimalPermut]
minimalPermut[routes_, i_, j_, mode_] :=
Module[{p = RandomReal[], permutation = routesToAnneling[routes]},
Switch[
mode,
1, MinimalBy[
{#, f[#]} & /@ (cureFunction[routesFromAnneling[#]] & /@ {inverse[permutation, i, j]},
insert[permutation, i, j], swap[permutation, i, j])), Last][[1]],
2, MinimalBy[{#, f[#]} & /@ (routesFromAnneling[#] & /@ {inverse[permutation, i, j]},
insert[permutation, i, j], swap[permutation, i, j])), Last][[1]],
3, ({#, f[#]} & /@ {routesFromAnneling@Which[p ≤ 0.5, swap[permutation, i, j],
p ≤ 0.7, inverse[permutation, i, j], True, insert[permutation, i, j]]})[[1]]
]
]

```

use cases minimalPermut

```

In[79]:= Clear[randomRoutes]
randomRoutes := NestWhile[Flatten /@ TakeList[Reverse /@ stacks,
getVarianteTwoArg[numberOfStacks, numberOfVehicles]] &, {{}}, MemberQ[{}]]

```

```

In[81]:= initialRoutes = randomRoutes

```

```

Out[81]= {{24, 62, 69, 77, 14, 45, 37, 47, 26, 33, 38, 49, 3, 70, 12, 67, 5, 54},
{32, 65, 39, 16, 64, 55, 7, 10, 11, 6, 72, 60, 56, 27, 78, 75, 57, 58, 18, 34,
71, 41, 19, 53, 48, 66, 8, 29, 80}, {25, 42, 4, 59, 21, 28, 52, 43, 40, 73, 22},
{9, 51, 76, 31, 35, 68, 36}, {15, 2, 74, 61, 17, 30, 23, 79, 1, 50, 46, 20, 44, 13, 63}}

```

```

In[82]:= random = RandomSample[Range[numberOfContainers + numberOfVehicles - 1], 2]

```

```

Out[82]= {37, 81}

```

```

In[83]:= minimalPermut[initialRoutes, random[[1]], random[[2]], 1] // AbsoluteTiming

```

```

Out[83]= {3.70804,
{{24, 62, 69, 77, 14, 45, 37, 47, 26, 33, 38, 49, 3, 70, 12, 67, 5, 54}, {32, 65, 39, 16, 64,
55, 7, 10, 11, 6, 72, 60, 56, 27, 78, 75, 57, 20, 79, 1, 50, 46, 15, 2, 74, 61, 17, 30, 23},
{68, 36, 9, 51, 76, 31, 35}, {43, 40, 73, 22, 25, 42, 4, 59, 21, 28, 52},
{41, 19, 53, 48, 66, 8, 29, 80, 58, 18, 34, 71, 44, 13, 63}}, 231.737}}

```

```

In[84]:= minimalPermut[initialRoutes, random[[1]], random[[2]], 2] // AbsoluteTiming

```

```

Out[84]= {2.76852,
{{24, 62, 69, 77, 14, 45, 37, 47, 26, 33, 38, 49, 3, 70, 12, 67, 5, 54}, {32, 65, 39, 16, 64,
55, 7, 10, 11, 6, 72, 60, 56, 27, 78, 75, 57, 20, 46, 50, 1, 79, 23, 30, 17, 61, 74, 2, 15},
{36, 68, 35, 31, 76, 51, 9}, {22, 73, 40, 43, 52, 28, 21, 59, 4, 42, 25},
{80, 29, 8, 66, 48, 53, 19, 41, 71, 34, 18, 58, 44, 13, 63}}, 231.737}}

```

```
In[85]:= minimalPermut[initialRoutes, random[[1]], random[[2]], 3] // AbsoluteTiming
Out[85]= {0.809619,
  {{24, 62, 69, 77, 14, 45, 37, 47, 26, 33, 38, 49, 3, 70, 12, 67, 5, 54}, {32, 65, 39, 16, 64,
    55, 7, 10, 11, 6, 72, 60, 56, 27, 78, 75, 57, 20, 18, 34, 71, 41, 19, 53, 48, 66, 8, 29, 80},
    {25, 42, 4, 59, 21, 28, 52, 43, 40, 73, 22}, {9, 51, 76, 31, 35, 68, 36},
    {15, 2, 74, 61, 17, 30, 23, 79, 1, 50, 46, 58, 44, 13, 63}}, 231.737}}
```

simulated annealing function

```
In[86]:= Clear[simulatedAnnealing]
simulatedAnnealing[routes_, maxIteration_,
  initialTemperature_, endTemperature_, a_, mode_] := Module[
  {currentRoutes = routes, t = initialTemperature,
    randomChoice, p, currentf, fy, history = {}, candidate,
    listToChoose = Range[numberOfContainers + numberOfVehicles - 1]},
  AppendTo[history, {currentRoutes, f[currentRoutes]}];
  Do[
    randomChoice = RandomSample[listToChoose, 2];
    candidate = minimalPermut[currentRoutes, randomChoice[[1]], randomChoice[[2]], mode];
    fy = candidate[[2]];
    currentf = f[currentRoutes];
    If[
      fy ≤ currentf,
      currentRoutes = candidate[[1]],
      p = Exp[(- (fy - currentf)) / t];
      If[RandomReal[] ≤ p, currentRoutes = candidate[[1]]]
    ];
    AppendTo[history, {currentRoutes, currentf}];
    t = t * a;
    If[t ≤ endTemperature, Break[]],
    {i, maxIteration}];
  history
]
```

main

results

```
In[88]:= initialRoutes = import[randomRoutes, "initialRoutes", isImport]
Out[88]= {{24, 62, 69, 77, 14, 45, 37, 47, 26, 33, 38, 49, 3, 70, 12, 67, 5, 54, 32, 65, 39},
  {16, 64, 55, 7, 10, 11, 6, 72, 60, 56, 27, 78, 75, 57, 58, 18, 34, 71,
    41, 19, 53, 48, 66, 8, 29, 80}, {25, 42, 4, 59, 21, 28, 52, 43, 40, 73, 22},
  {9, 51, 76, 31, 35, 68, 36, 15, 2, 74, 61, 17, 30, 23}, {79, 1, 50, 46, 20, 44, 13, 63}}
```



```
In[89]:= f[initialRoutes]
```

```
Out[89]= 231.737
```

```
In[90]:= solution = If[isImport, data["solution"],
    simulatedAnnealing[initialRoutes, 800, 0.025, 10-10, 0.99, 1]]];
```

```
In[91]:= finalRoute = solution[[-1, 1]]
```

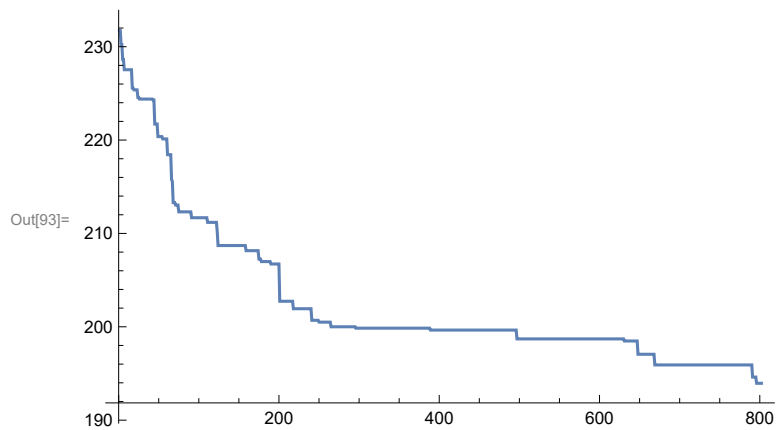
```
Out[91]= {{40, 38, 77, 14, 45, 79, 1, 15, 19, 50, 46, 2, 74, 61, 17, 32, 71, 9, 23, 51, 76, 31, 35},
    {43, 24, 73, 22, 25, 62, 42, 4, 37, 20, 44, 13, 49, 47, 59, 3, 70, 5, 30, 12, 65, 69, 8, 36, 39},
    {16, 64, 75, 57, 55, 41, 7, 10, 58, 11, 56, 6, 18, 34, 63, 67},
    {27, 78, 72, 54, 60, 26, 48, 33, 66, 29, 80}, {21, 28, 52, 53, 68}}
```

```
In[92]:= finalRouteF = solution[[-1, 2]]
```

```
Out[92]= 193.948
```

target function value

```
In[93]:= ListLinePlot[solution[All, 2]]
```



```
In[94]:= Clear[listLinePlot]
```

```
listLinePlot[fullSolution_, step_, n_] := ListLinePlot[
    points[#[[step, 1, n]]] & /@
    If[n ≠ numberOfVehicles + 1, fullSolution[step, 1, n], fullSolution[step, 1]],
    PlotRange → {{1, 5}, {1, 5}},
    PlotLegends → If[n ≠ numberOfVehicles + 1, StringJoin[ToString[n], " vehicle"],
        (StringJoin[ToString[#[[step, 1, n]], " vehicle"] & /@ Range[numberOfVehicles])],
    Epilog → PointSize[Large], ImageSize → 500, Mesh → All
]
```

```

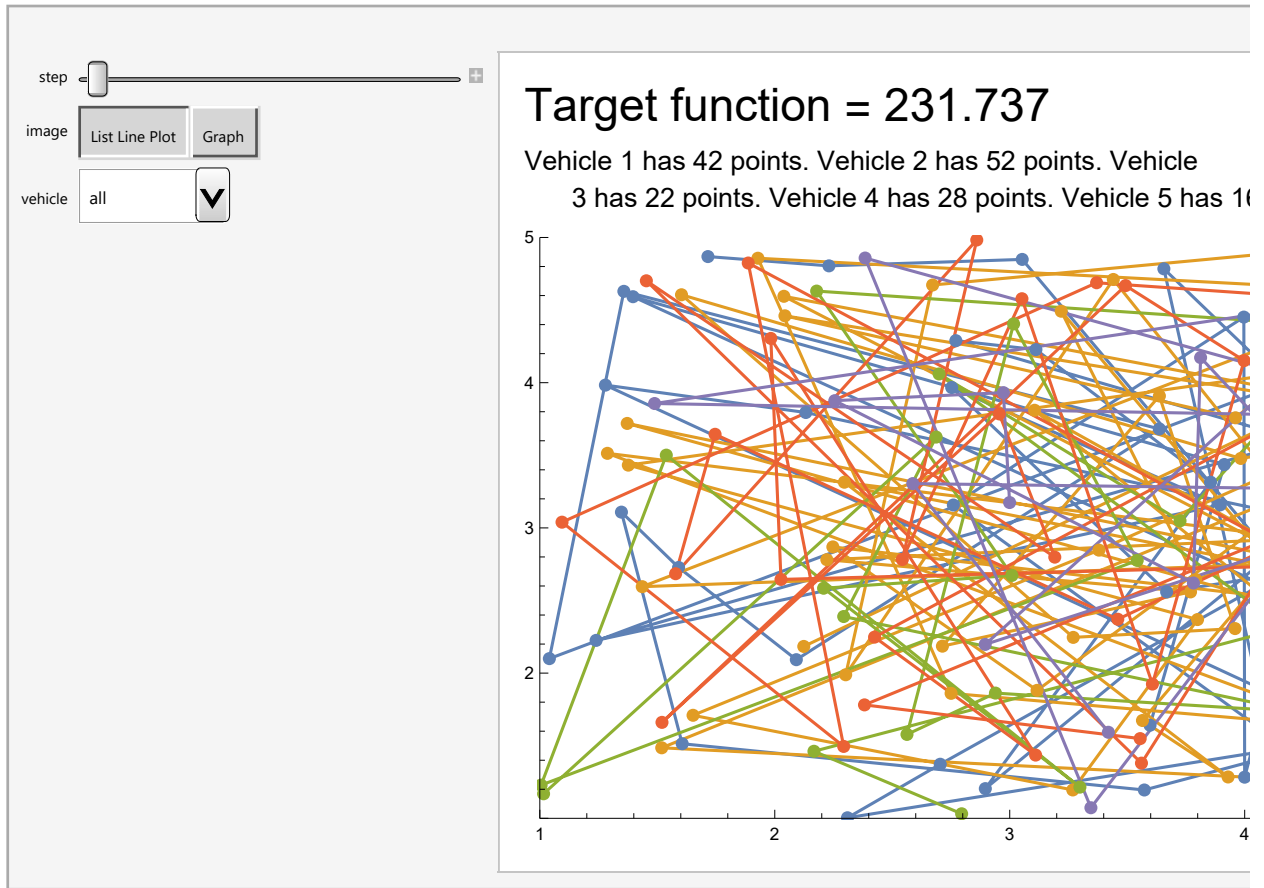
In[96]:= Clear[graph]
graph[fullSolution_, step_, n_] := Module[{edgesPairs, edgesStyle,
  c = Table[Hue[i / numberOfVehicles, 1, 1], {i, numberOfVehicles}]],
  If[
    n ≠ numberOfVehicles + 1,
    edgesPairs = DirectedEdge @@@ Partition[fullSolution[[step, 1, n]], 2, 1],
    edgesPairs = DirectedEdge @@@ Partition[#, 2, 1] & /@ fullSolution[[step, 1]]
  ];
  If[
    n ≠ numberOfVehicles + 1,
    edgesStyle = Flatten[Table[edgesPairs[[j]] → c[[n]], {j, Length[edgesPairs]}]],
    edgesStyle = Flatten[
      Table[edgesPairs[[i, j]] → c[[i]], {i, numberOfVehicles}, {j, Length[edgesPairs[[i]]}}]
    ];
  Graph[Flatten@edgesPairs, EdgeStyle → edgesStyle, VertexLabels → "Name",
    VertexCoordinates → Table[i → points[[i]], {i, 1, Length[points]}], ImageSize → 500]
]

In[98]:= Clear[manipulate]
manipulate[solution_, plot_] := Module[{fullSolution},
  fullSolution = {fullRoutes[#[[1]], #[[2]]] & /@ solution;
  Manipulate[Column[{
    Text[Style["Target function = " <> ToString[solution[[step, 2]], 24]],
    Text[Style[StringJoin[MapIndexed["Vehicle " <> ToString[#[2[[1]]] <> " has " <>
      ToString[Length[#[1]]] <> " points. " &, fullSolution[[step, 1]]], 14]],
    Switch[image, 1, listLinePlot[fullSolution, step, vehicle], 2,
      graph[fullSolution, step, vehicle]]
  }], {step, 1, Length[solution], 1}, {image, {1 → "List Line Plot", 2 → "Graph"}},
  {vehicle, Join[{numberOfVehicles + 1 → "all"},
    Table[m → (ToString[m] <> " vehicle"), {m, 1, numberOfVehicles}]]}]
]

```

In[100]:= `manipulate[solution, listLinePlot]`

Out[100]=



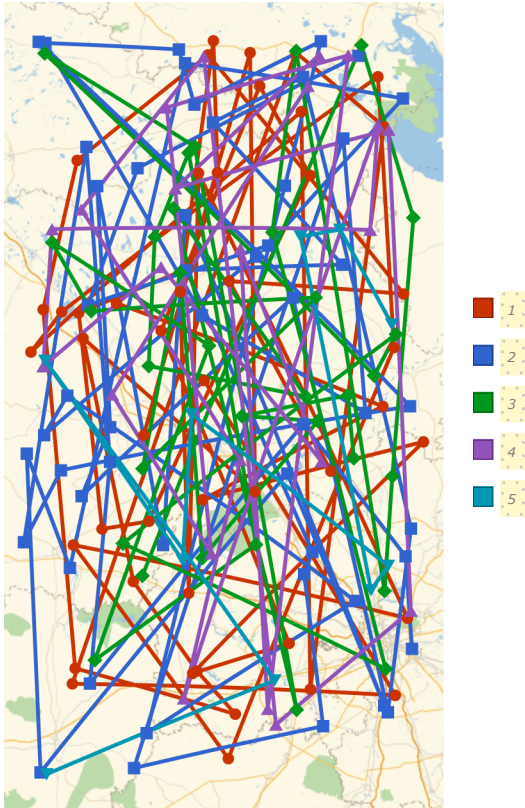
Loading from Wolfram Research server... (59%)
Remaining time 16s

map vizualization

In[101]:= `newPoints = {#[[1]] + 54, #[[2]] + 33} & /@ points;`

```
In[102]:= GeoListPlot[Map[GeoPosition[newPoints[##]] &, fullRoutes[finalRoute]], Joined → True]
```

Out[]:=



statistics

```
In[ ]:= Clear[statistic]
statistic[n_, iteration_, mode_] :=
  Quiet@Module[{initialRoutes = randomRoutes, solutions = {}, solution},
    Do[solution = simulatedAnnealing[initialRoutes, iteration, 0.55, 10-10, 0.99, mode];
      AppendTo[solutions, solution[[All, 2]]],
      {i, n}];
  solutions]

In[ ]:= solutionsStat = If[isImport, data["solutionsStat"], statistic[5, 150, 1]];
```

```

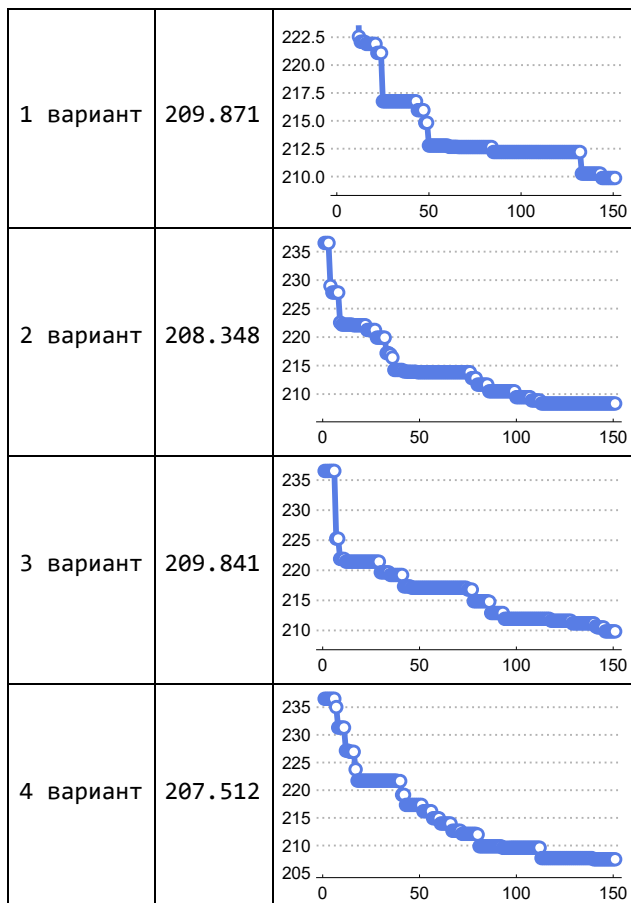
In[ ]:= Clear[plotStatistic]
plotStatistic[solutions_] :=
  Quiet@Module[{initialRoutes = randomRoutes, values = {}, graphics = {},
    solution, stat, colors, str, n = Length@solutions},
    Do[
      AppendTo[values, Last@solution];
      AppendTo[graphics, ListLinePlot[solution, PlotTheme → "Business"]],
      {solution, solutions}];
    stat = {Max[values], Mean[values], Min[values]};
    colors = Permutations[{Magenta, LightGray, LightGray}];
    str = StringJoin[ToString[#], " вариант"] & /@ Range[n];
    If[n > 2,
      values = Join[values, stat];
      graphics = Join[graphics, ListLinePlot[ConstantArray[#, n] & /@ stat,
        PlotTheme → "Business", PlotStyle → #] & /@ colors];
      str = Join[str, {"Худший", "Средний", "Лучший"}];
    ];
    Grid[Transpose@{str, values, graphics}, Frame → All]
  ]

```

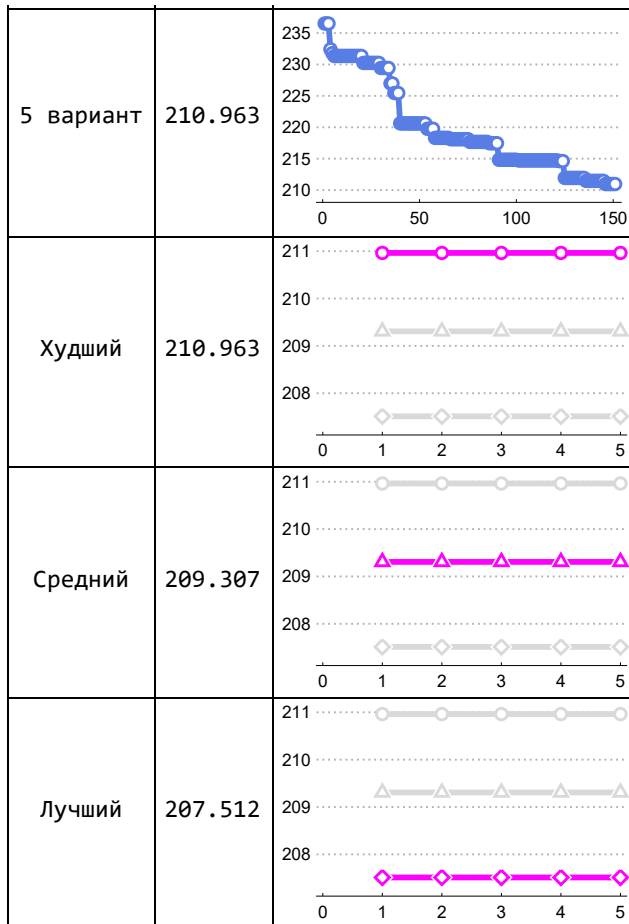
```

In[ ]:= plotStatistic[solutionsStat]

```



Out[]:=



```

In[ ]:= (*Export[FileNameJoin[{NotebookDirectory[], "data.json"}], {
  "numberOfContainers" -> numberOfContainers,
  "numberOfVehicles" -> numberOfVehicles,
  "numberOfStacks" -> numberOfStacks,
  "pointsVertices1" -> pointsVertices1,
  "pointsVertices2" -> pointsVertices2,
  "stacks" -> stacks,
  "pairsVertices1" -> pairsVertices1,
  "pairsVertices2" -> pairsVertices2,
  "initialRoutes" -> initialRoutes,
  "solution" -> solution,
  "solutionsStat" -> solutionsStat
}];*)

```