

# Evaluating Machine Learning Methods


## Bias of an estimator

$\theta$  true value of parameter of interest (e.g. model accuracy)

$\hat{\theta}$  estimator of parameter of interest (e.g. test set accuracy)

$$\text{Bias}[\hat{\theta}] = E[\hat{\theta}] - \theta$$

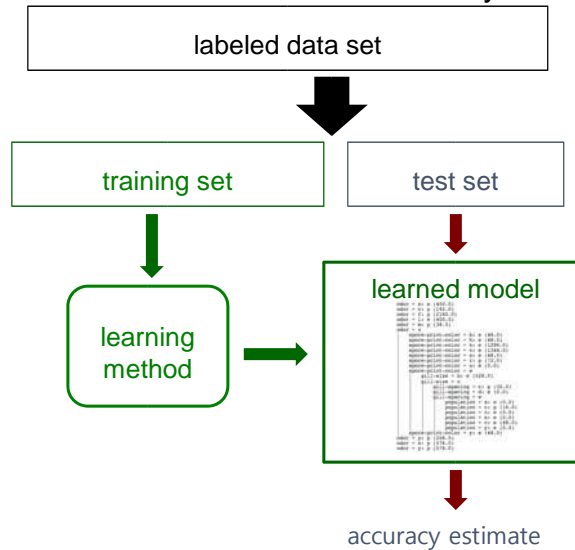
e.g. polling methodologies often have an inherent bias



| POLLSTER                                     | LIVE CALLER<br>WITH<br>CELLPHONES | INTERNET | NCPD/<br>AAPOR/<br>ROPER | POLLS<br>ANALYZED | SIMPLE<br>AVERAGE<br>ERROR | RACES<br>CALLED<br>CORRECTLY | ADVANCED<br>+/- | PREDICTIVE<br>+/- | 538<br>GRADE | BANNED<br>BY 538 | MEAN-REVERTED BIAS |
|--|-----------------------------------|----------|--------------------------|-------------------|----------------------------|------------------------------|-----------------|-------------------|--------------|------------------|--------------------|
| SurveyUSA                                    |                                   |          | ●                        | 763               | 4.6                        | 90%                          | -1.0            | -0.8              | A            |                  | D+0.1              |
| YouGov                                       |                                   | ●        |                          | 707               | 6.7                        | 93%                          | -0.3            | +0.1              | B            |                  | D+1.6              |
| Rasmussen Reports/<br>Pulse Opinion Research |                                   |          |                          | 657               | 5.3                        | 79%                          | +0.4            | +0.7              | C+           |                  | R+2.0              |
| Zogby Interactive/JZ<br>Analytics            |                                   | ●        |                          | 465               | 5.6                        | 78%                          | +0.8            | +1.2              | C-           |                  | R+0.8              |
| Mason-Dixon Polling &<br>Research, Inc.      | ●                                 |          |                          | 415               | 5.2                        | 86%                          | -0.4            | -0.2              | B+           |                  | R+1.0              |
| Public Policy Polling                        |                                   |          |                          | 383               | 4.9                        | 82%                          | -0.5            | -0.1              | B+           |                  | R+0.2              |
| Research 2000                                |                                   |          |                          | 279               | 5.5                        | 88%                          | +0.2            | +0.6              | F            | ✗                | D+1.4              |
| American Research<br>Group                   | ●                                 |          |                          | 260               | 7.6                        | 75%                          | +0.6            | +0.7              | C+           |                  | R+0.1              |
| Quinnipiac University                        | ●                                 |          | ●                        | 169               | 4.7                        | 87%                          | -0.3            | -0.4              | A-           |                  | R+0.7              |
| Marist College                               | ●                                 |          | ●                        | 146               | 5.4                        | 88%                          | -0.8            | -0.8              | A            |                  | R+0.7              |

Test sets

How can we get an unbiased estimate of the accuracy of a learned model?



## Test sets

How can we get an unbiased estimate of the accuracy of a learned model?

- when learning a model, you should pretend that you don't have the test data yet (it is "in the mail")\*
- if the test-set labels influence the learned model in any way, accuracy estimates will be biased

\* In some applications it is reasonable to assume that you have access to the feature vector (i.e.  $x$ ) but not the  $y$  part of each test instance.

## Learning curves

How does the accuracy of a learning method change as a function of the training-set size?

this can be assessed by plotting *learning curves*

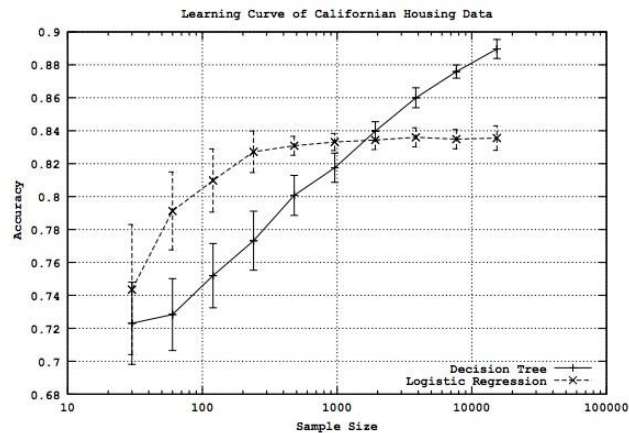
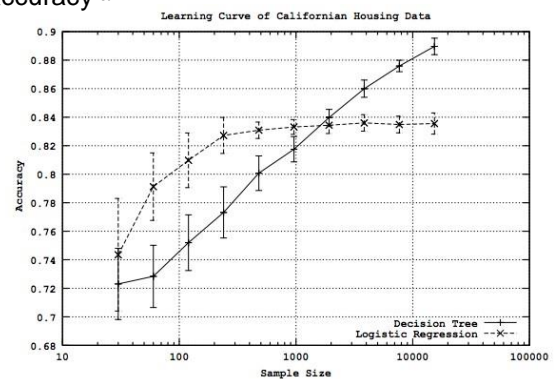


Figure from Perlich et al. *Journal of Machine Learning Research*, 2003

## Learning curves

given training/test set partition

- for each sample size  $s$  on learning curve
  - (optionally) repeat  $n$  times
    - randomly select  $s$  instances from training set
    - learn model
    - evaluate model on test set to determine accuracy  $a$
    - plot  $(s, a)$
    - or  $(s, \text{avg. accuracy and error bars})$



## Limitations of using a single training/test partition

- we may not have enough data to make sufficiently large training and test sets

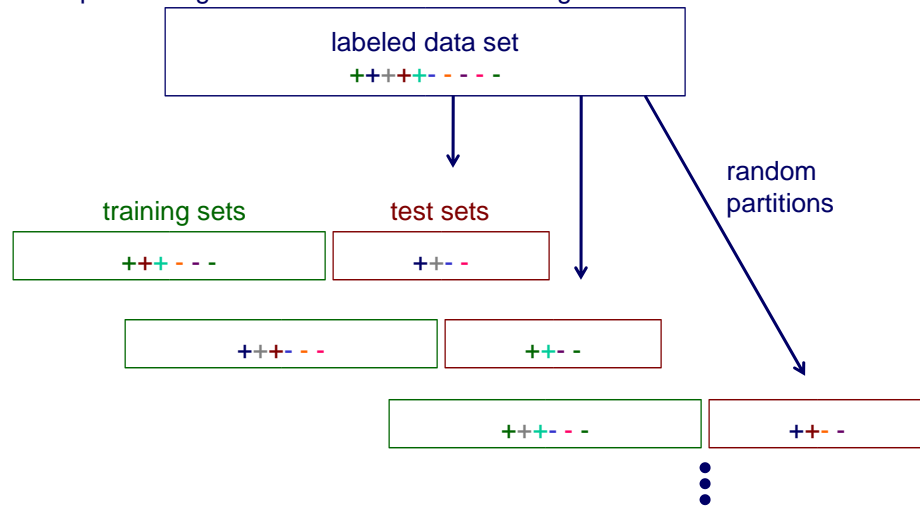
- a larger test set gives us more reliable estimate of accuracy (i.e. a lower variance estimate)
- but... a larger training set will be more representative of how much data we actually have for learning process
- a single training set doesn't tell us how sensitive accuracy is to a particular training sample

## Using multiple training/test partitions

- Two general approaches...
  - random resampling
  - cross validation

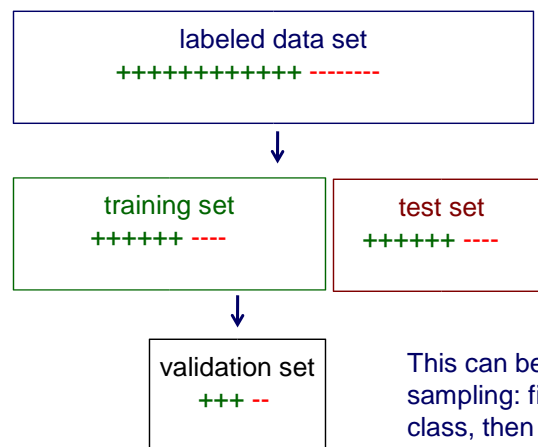
## Random Resampling

We can address the second issue by repeatedly randomly partitioning the available data into training and set sets.



## Stratified Resampling

When randomly selecting training or validation sets, we may want to ensure that class proportions are maintained in each selected set



This can be done via stratified sampling: first stratify instances by class, then randomly select instances from each class proportionally.

## Cross validation



partition data into  $n$   
subsamples

labeled data set



iteratively leave one  
subsample out for the  
test set, train on the  
rest

|           | S <sub>1</sub> | S <sub>2</sub> | S <sub>3</sub> | S <sub>4</sub> | S <sub>5</sub> |                |
|-----------|----------------|----------------|----------------|----------------|----------------|----------------|
| iteration | train on       |                |                |                | test on        |                |
| 1         |                | S <sub>2</sub> | S <sub>3</sub> | S <sub>4</sub> | S <sub>5</sub> | S <sub>1</sub> |
| 2         |                | S <sub>1</sub> | S <sub>3</sub> | S <sub>4</sub> | S <sub>5</sub> | S <sub>2</sub> |
| 3         |                | S <sub>1</sub> | S <sub>2</sub> | S <sub>4</sub> | S <sub>5</sub> | S <sub>3</sub> |
| 4         |                | S <sub>1</sub> | S <sub>2</sub> | S <sub>3</sub> | S <sub>5</sub> | S <sub>4</sub> |
| 5         |                | S <sub>1</sub> | S <sub>2</sub> | S <sub>3</sub> | S <sub>4</sub> | S <sub>5</sub> |

## Cross validation example

Suppose we have 100 instances, and we want to estimate accuracy with cross validation

| iteration | train on  | test on        | correct |
|-----------|---|----------------|---------|
| 1         | S <sub>2</sub> S <sub>3</sub> S <sub>4</sub> S <sub>5</sub> | S <sub>1</sub> | 11 / 20 |
| 2         | S <sub>1</sub> S <sub>3</sub> S <sub>4</sub> S <sub>5</sub> | S <sub>2</sub> | 17 / 20 |
| 3         | S <sub>1</sub> S <sub>2</sub> S <sub>4</sub> S <sub>5</sub> | S <sub>3</sub> | 16 / 20 |
| 4         | S <sub>1</sub> S <sub>2</sub> S <sub>3</sub> S <sub>5</sub> | S <sub>4</sub> | 13 / 20 |
| 5         | S <sub>1</sub> S <sub>2</sub> S <sub>3</sub> S <sub>4</sub> | S <sub>5</sub> | 16 / 20 |

accuracy =  $73/100 = 73\%$

## Cross validation

- 10-fold cross validation is common, but smaller values of  $n$  are often used when learning takes a lot of time
- in *leave-one-out* cross validation,  $n = \#$  instances
- in *stratified* cross validation, stratified sampling is used when partitioning the data
- CV makes efficient use of the available data for testing
- note that whenever we use multiple training sets, as in CV and random resampling, we are evaluating a learning method as opposed to an individual learned model

## Confusion matrices / contingency tables

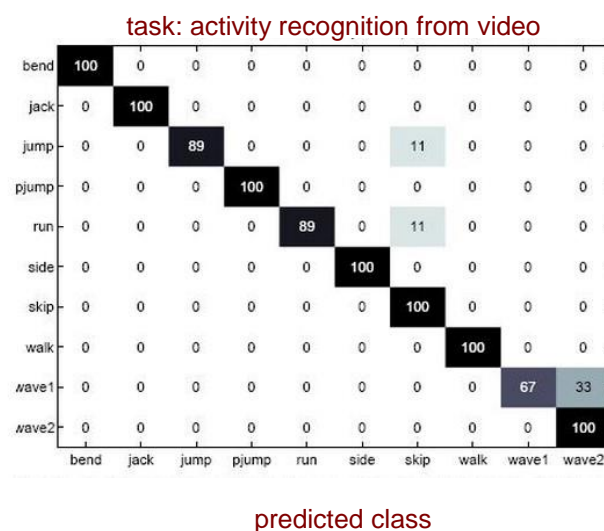
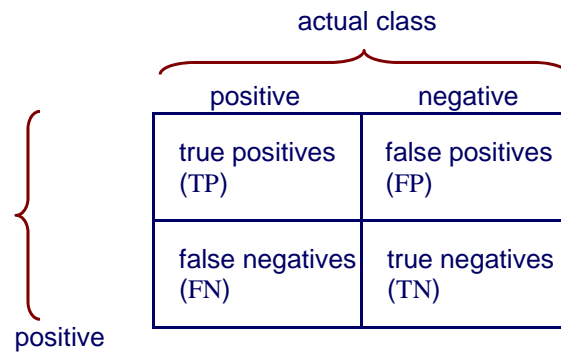


figure from vision.jhu.edu

## Confusion matrix for 2-class problems



A confusion matrix for a 2-class problem. The matrix is a 2x2 grid with blue borders. Above the grid, a red bracket spans both columns, labeled 'actual class'. Below the grid, a red bracket spans both rows, labeled 'positive'. The columns are labeled 'positive' and 'negative' above the grid. The rows are labeled 'true positives (TP)' and 'false negatives (FN)' on the left side of the grid. The cells contain: top-left 'true positives (TP)', top-right 'false positives (FP)', bottom-left 'false negatives (FN)', and bottom-right 'true negatives (TN)'.

|                      |                      |
|----------------------|----------------------|
| actual class         |                      |
| positive             | negative             |
| true positives (TP)  | false positives (FP) |
| false negatives (FN) | true negatives (TN)  |

predicted  
class

negative

$$\text{accuracy} = \frac{TP + TN}{TP + FP + FN + TN}$$

## Is accuracy perfect?

accuracy may not be useful measure in cases where

- there is a large class skew
- Is 98% accuracy good when 97% of the instances are negative?
- there are differential misclassification costs – say, getting a positive wrong costs more than getting a negative wrong
- Consider a medical domain in which a false positive results in an extraneous test but a false negative results in a failure to treat a disease
- we are most interested in a subset of high-confidence predictions

## Other performance metrics

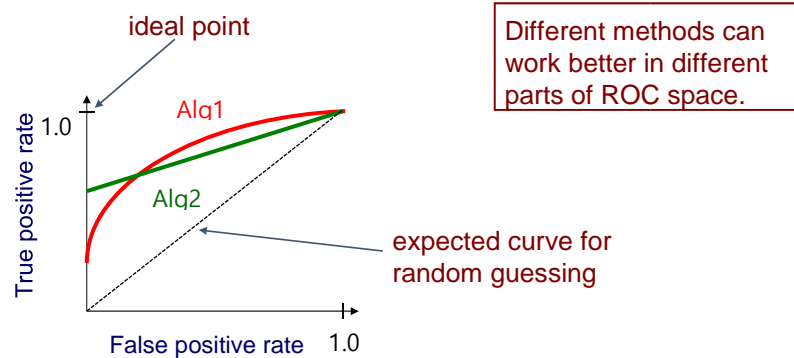
error  $\square 1 - \text{accuracy}$

|                 | actual class                                |   |
|-----------------|---|---|
| predicted class | positive                                    | negative                                    |
|                 | true positives (TP)<br>false negatives (FN) | false positives (FP)<br>true negatives (TN) |

$$\text{true positive rate (recall)} = \frac{\text{TP}}{\text{actual pos TP} + \text{FN}}$$

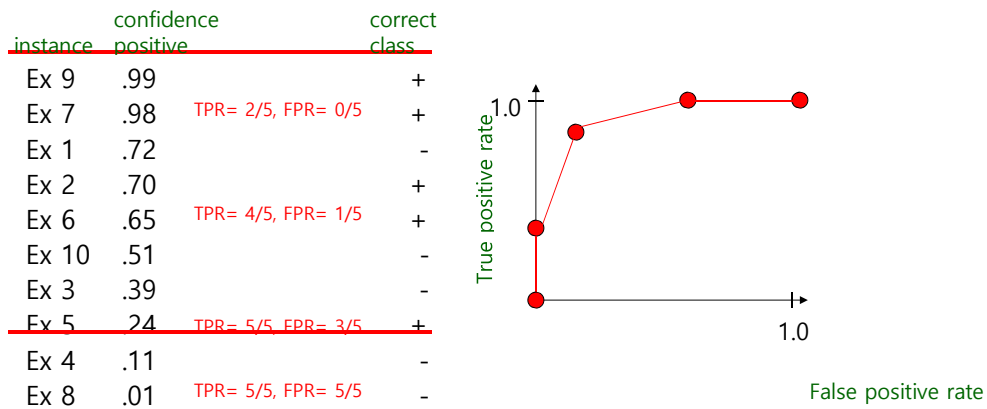
## ROC curve

A Receiver Operating Characteristic (ROC) curve plots the TP-rate vs. the FP-rate as a threshold on the confidence of an instance being positive is varied



$$\text{false positive rate} = \frac{\text{FP}}{\text{actual neg}} = \frac{\text{FP}}{\text{TN} + \text{FP}}$$

## Plotting an ROC curve



## ROC curve example

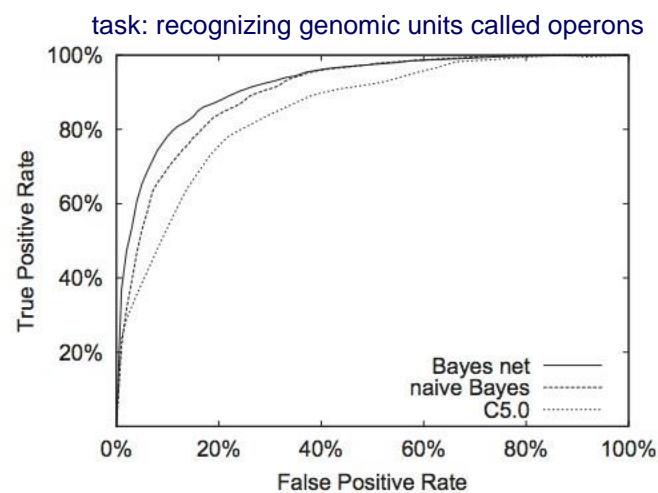
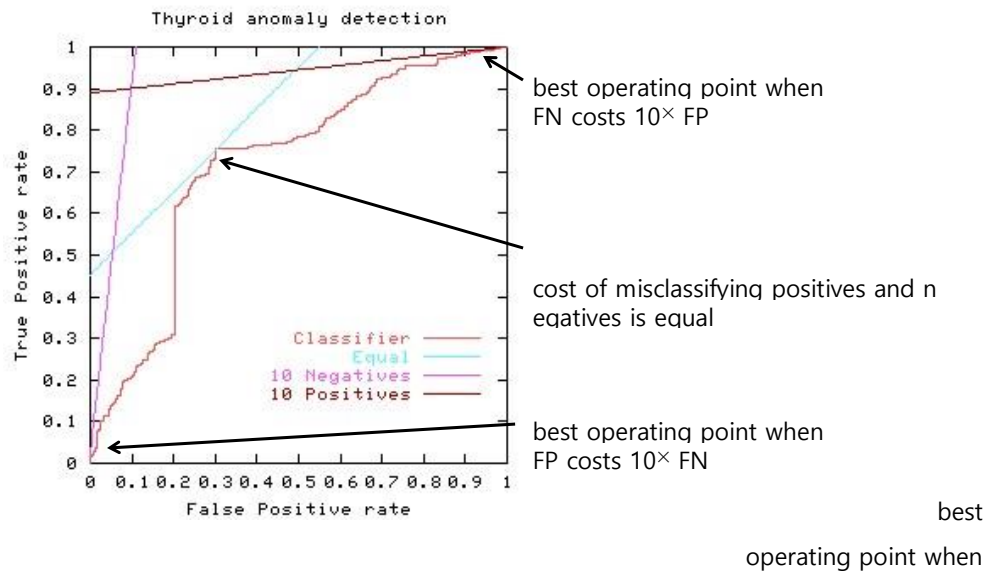


figure from Bockhorst et al., *Bioinformatics* 2003

Plotting an ROC example



The best operating point depends on the relative costs of FN and FP misclassifications



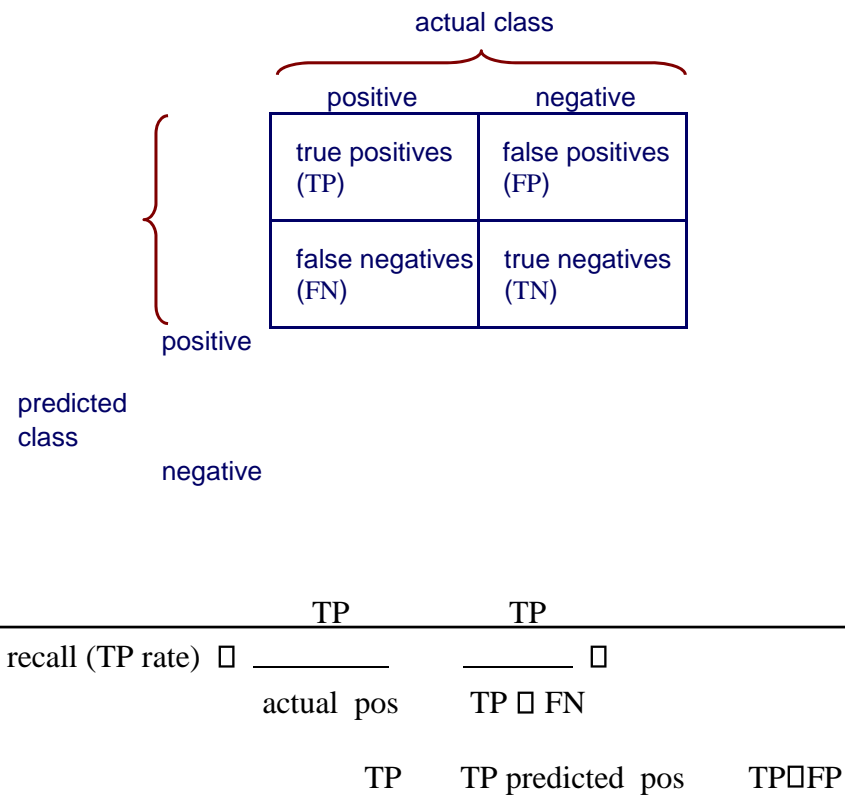
## ROC curve

Does a low false-positive rate indicate that most positive predictions (i.e. predictions with confidence > some threshold) are correct?

suppose our TPR is 0.9, and FPR is 0.01

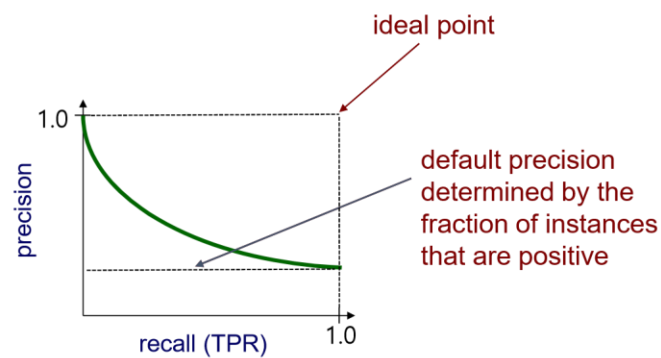
| fraction of instances that are positive | fraction of positive predictions that are correct |
|---|---|
| 0.5                                     | 0.989   |
| 0.1                                     | 0.909   |
| 0.01                                    | 0.476   |
| 0.001                                   | 0.083   |

## Other performance metrics



## Precision / recall curve

A *precision/recall curve* plots the precision vs. recall (TP-rate) as a threshold on the confidence of an instance being positive is varied



precision (positive predictive value)  $\square$   $\square$

Precision / recall curve example

predicting patient risk for VTE

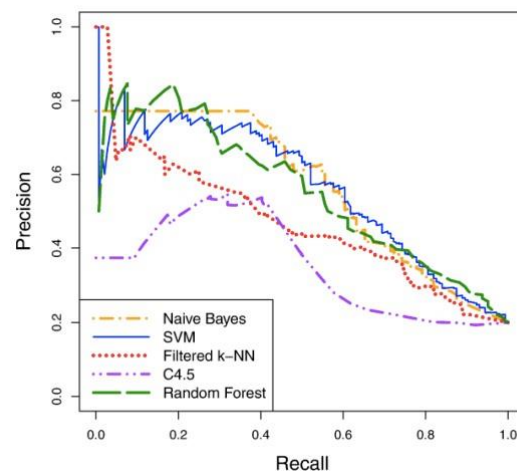


figure from Kawaler et al., *Proc. of AMIA Annual Symposium*, 2012

## How do we get one ROC/PR curve when we do CV?

### Approach 1

- make assumption that confidence values are comparable across folds
- pool predictions from all test sets
- plot the curve from the pooled predictions

### Approach 2 (for ROC curves)

- plot individual curves for all test sets
- view each curve as a function
- plot the average curve for this set of functions

## Comments...

### Both

- allow predictive performance to be assessed at various levels of confidence
- assume binary classification tasks
- sometimes summarized by calculating *area under the curve* (*AUC*)

### ROC curves

- insensitive to changes in class distribution (ROC curve does not change if the proportion of positive and negative instances in the test set are varied)
- can identify optimal classification thresholds for tasks with differential misclassification costs

### Precision/recall curves

- show the fraction of predictions that are false positives
- well suited for tasks with lots of negative instances