

3.8 Order of evaluation

Precedence rules

The order in which operators are evaluated in an expression are known as **precedence rules**. Arithmetic, logical, and relational operators are evaluated in the order shown below.

Table 3.8.1: Precedence rules for arithmetic, logical, and relational operators.

Operator/Convention	Description	Explanation
()	Items within parentheses are evaluated first	In <code>(a * (b + c)) - d</code> , the <code>+</code> is evaluated first, then <code>*</code> , then <code>-</code> .
!	! (logical NOT) is next	<code>! x y</code> is evaluated as <code>(!x) y</code>
* / % + -	Arithmetic operators (using their precedence rules; see earlier section)	<code>z - 45 * y < 53</code> evaluates <code>*</code> first, then <code>-</code> , then <code><</code> .
< <= > >=	Relational operators	<code>x < 2 x >= 10</code> is evaluated as <code>(x < 2) (x >= 10)</code> because <code><</code> and <code>>=</code> have precedence over <code> </code> .
== !=	Equality and inequality operators	<code>x == 0 && x >= 10</code> is evaluated as <code>(x == 0) && (x >= 10)</code> because <code><</code> and <code>>=</code> have precedence over <code>&&</code> . <code>==</code> and <code>!=</code> have the same precedence and are evaluated left to right.
&&	Logical AND	<code>x == 5 y == 10 && z != 10</code> is evaluated as

		<code>(x == 5) ((y == 10) && (z != 10))</code> because && has precedence over .
	Logical OR	has the lowest precedence of the listed arithmetic, logical, and relational operators.

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3.8.1: Applying the precedence rules to an expression can be thought of as a 'tree'.



■ 1 2 3 4 ▶ ☒ 2x speed

$$x + 1 > y * z \parallel z == 3$$

Next comes +, then >, then ==, and finally ||.

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3.8.2: Order of evaluation.



To teach precedence rules, these questions intentionally omit parentheses; good style would use parentheses to make order of evaluation explicit.

1) Which operator is evaluated first?

! y && x

☐ &&

☒ !

Correct

! has one of the highest precedences, higher than &&, so !y is evaluated first. If y is false and x is true, the expression evaluates as (!false) && true, which is true && true, which is true.



2) Which operator is evaluated first?

w + 3 > x - y * z

☐

Correct

Arithmetic operators (+, -, *) have precedence over relational operators. Among +, -, *, the * has higher



- ☐ +
☐ -
☐ >
☒ *

precedence and thus $y * z$ is evaluated first.

- 3) In what order are the operators evaluated?

$w + 3 != y - 1 \&\& x$

- ☐ +, !=, -, &&
☐ +, -, &&, !=
☒ +, -, !=, &&

Correct

Arithmetic operators have higher precedence than equality or logical AND operators. Among + and -, evaluation is left-to-right, so + is first, then - is second. Next, the equality operators have precedence over logical AND, so != is third. && is thus fourth.

- 4) To what does this expression evaluate, given $\text{int } x = 4, \text{int } y = 7$.

$x == 3 \parallel x + 1 > y$

- ☐ true
☒ false

Correct

The arithmetic operator has highest precedence, yielding $x == 3 \parallel 5 > y$. Next is the relational operator $>$, yielding $x == 3 \parallel \text{false}$ (because $5 > 7$ is false). Next is $==$, yielding $\text{false} \parallel \text{false}$. Finally, the \parallel is evaluated, yielding false.

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Common error: Missing parentheses

A common error is to write an expression that is evaluated in a different order than expected. Good practice is to use parentheses in expressions to make the intended order of evaluation explicit. Several examples are below.

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3.8.3: Common errors in expressions.

- 1) Does $! x == 3$ evaluate as $!(x == 3)$?

- ☐ Yes
☒ No

Correct

! has precedence over $==$, so the expression evaluates as $(!x) == 3$. Using parentheses ensures an expression evaluates as a programmer desires, as in $!(x == 3)$

- 2) Does $w + x == y + z$ evaluate as $(w + x) == (y + z)$?

- ☒ Yes
☐ No

Correct

+ has precedence over $==$, so $w + x$ and $y + z$ are each evaluated before the $==$. However, good practice is to write $(w + x) == (y + z)$ to make the intended order explicit.

3) Does `w && x == y && z` evaluate as `(w && x) == (y && z)`?

- ☐ Yes
☒ No

Correct

`==` has precedence over `&&`. Thus, perhaps surprisingly, the expression evaluates as `(w && (x == y)) && z`, which almost certainly was not the programmer's intent. This example illustrates why consistently using parentheses can reduce bugs.

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3.8.4: Order of evaluation.

Which illustrates the actual order of evaluation via parentheses?

1) `! green == red`

- ☒ `(!green) == red`
☐ `!(green == red)`
☐ `(!green =) = red`

Correct

Spacing doesn't matter; `!` has precedence. Lack of parentheses causes common errors.

2) `bats < birds || birds < insects`

- ☐ `((bats < birds) || birds < insects)`
☐ `bats < (birds || birds) < insects`
☒ `(bats < birds) || (birds < insects)`

Correct

The comparisons occur first. The parentheses make that clear.

3) `! (bats < birds) || (birds < insects)`

- ☐ `! ((bats < birds) || (birds < insects))`
☒ `(! (bats < birds)) || (birds < insects)`
☐ `((!bats) < birds) || (birds < insects)`

Correct

The items within parentheses are evaluated first. Then, `!` has precedence over `||` so is evaluated next.

4) `(num1 == 9) || (num2 == 0) && (num3 == 0)`

Correct

☒ (num1 == 9) ||
((num2 == 0) &&
(num3 == 0))

☐ ((num1 == 9) ||
(num2 == 0)) &&
(num3 == 0)

☐ (num1 == 9) ||
(num2 == (0 &&
num3) == 0)

Items within parentheses are evaluated first. && has precedence over ||.

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Common error: Math expression for range

A common error often made by new programmers is to write expressions like `(16 < age < 25)`, as one might see in mathematics.

The meaning, however, almost certainly is not what the programmer intended. Suppose age is presently 28. The expression is evaluated left-to-right, so evaluation of `16 < age` yields true. Next, the expression `true < 25` is evaluated; clearly not the programmer's intent. However, true is actually 1, and evaluating `1 < 25` will yield true. Thus, the above expression evaluates to true, even for ages greater than 25.

Thus, `16 < age < 25` is actually the same as `(16 < age) < 25`, which evaluates to `(true) < 25` for any age over 16, which is the same as `(1) < 25`, which evaluates to true. The correct way to do such a comparison is: `(age > 16) && (age < 25)`.

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3.8.5: Expression for detecting a range.

- 1) A programmer erroneously wrote an expression as: `0 < x < 10`. Rewrite the expression using logical AND. Use parentheses.

(0 < x)

Check

Show answer

Answer

&& (x < 10)

If `0 < x AND x < 10`, then x must be between 0 and 10, as intended by the math expression `0 < x < 10`.

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Common error: Bitwise rather than logical operators

Logical AND is `&&` and not just `&`, and logical OR is `||` and not just `|`. `&` and `|` represent **bitwise operators**, which perform AND or OR on corresponding individual bits of the operands.

A common error is to use a bitwise operator instead of a logical operator, typing `&` instead of `&&`, or typing `|` instead of `||`. A bitwise operator may yield different behavior than expected.

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3.8.6: Bitwise vs. logical operators.



Indicate if the expression correctly uses logical operators.

1) `(x > 5) & (y > 3) & (z != 0)`

☐ Yes

☒ No

Correct

A single `&` is not logical AND, but rather bitwise AND, which has different behavior.



2) `(x == 0) || (y == 0) | (z == 0)`

☐ Yes

☒ No

Correct

The second operator uses just one `|` rather than `||`.



3) `((x == y) && (y == z)) || (w == 0)`

☒ Yes

☐ No

Correct

Logical AND was used, and logical OR was also used.



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