

Q3,

There are 3 conditions that must be kept when dealing with 3 coloured graphs.

1. Each vertex must have at least one of the three colours, thus must satisfy the following clause by having at least one colour ($v_{\text{Red}} \vee v_{\text{White}} \vee v_{\text{Black}}$).
2. Each vertex must also not take up more than one colour at a time. The vertex must support not being at least 2 of the colours. The clauses needed to be satisfied include ($\sim v_{\text{White}} \vee \sim v_{\text{Red}}$), ($\sim v_{\text{Black}} \vee \sim v_{\text{Red}}$), ($\sim v_{\text{White}} \vee \sim v_{\text{Black}}$).

Thus every vertex in G must satisfy 4 clauses.

3. For edges, they must maintain not having the same colour as their adjacent vertex neighbours. Given 2 vertices per edge, 1 and 2, at least one vertex must not have a given colour per colour. These clauses include ($\sim v_1_{\text{White}} \vee \sim v_2_{\text{White}}$), ($\sim v_1_{\text{Red}} \vee \sim v_2_{\text{Red}}$), ($\sim v_1_{\text{Black}} \vee \sim v_2_{\text{Black}}$).

Each edge in G must satisfy 3 clauses.

Number of clauses needed for $G = 4n + 3m$