

$$\omega_c = \omega_{RC} = 2\pi \times 1000 = 2000\pi \quad 6.283 \times 10^3$$

$$\omega_s = 2\pi F_s = 2\pi \times 550 = 700\pi \quad 2199.1149$$

$$T = \frac{1}{f} = \frac{1}{5000} = 0.2mS$$

$$A_p = \frac{\frac{2}{T} \tan \frac{\omega_p T}{2}}{\frac{2}{0.2m} \tan \left( \frac{2000\pi \times 0.2 \times 10^{-3}}{2} \right)} = 736.54 \text{ rad/sec} \quad 10000 \tan(0.628318)$$

$$\omega_s = \frac{2}{T} \tan \frac{\omega_s T}{2} = \frac{2}{0.2m} \tan \left( \frac{700\pi \times 0.2m}{2} \right) = 2235.3 \text{ rad/sec}$$

$$N = \frac{\log \sqrt{\frac{10^{0.145} - 1}{10^{0.145} - 1}}}{\log \frac{\omega_s}{\omega_p}} = \frac{\log \sqrt{\frac{10^{0.145} - 1}{10^{0.145} - 1}}}{\log \frac{2235.3}{736.54}} = \frac{0.6471212}{0.511836} = 0.9320879$$

$$\boxed{N \approx 1} \text{ order}$$

$$\omega_c = 1 \text{ rad/sec is } H(s) = \frac{1}{1+s}$$

$$\omega_c = \omega_p = 7265 \text{ rad/sec} \quad S \rightarrow \omega_c \rightarrow \frac{7265}{S}$$

$$H(s) = \frac{1}{s+1} \Big|_{s=\frac{7265}{S}} = \frac{1}{\frac{7265}{S} + 1} = \frac{S}{7265 + S}$$

Discrete Transformation

$$H(z) = H(s) \Big|_{s=\frac{2}{T} \left( \frac{1-z^{-1}}{1+z^{-1}} \right)}$$

$$H(z) = \frac{S}{s + 7265} \left| s = \frac{2}{0.2m} \left( \frac{1-z^{-1}}{1+z^{-1}} \right) \right.$$

$$= \frac{10^4 \left( \frac{1-z^{-1}}{1+z^{-1}} \right)}{10^4 \left( \frac{1-z^{-1}}{1+z^{-1}} \right) + 7265}$$

$$= \frac{10^4 (1-z^{-1})}{10^4 (1-z^{-1}) + 7265 (1+z^{-1})}$$

$$= \frac{10^4 (1-z^{-1})}{10^4 - 10^4 z^{-1} + 7265 + 7265 z^{-1}}$$

$$= \frac{10^4 (1-z^{-1})}{17265 - 2735 z^{-1}}$$

$$= \frac{10^4 (1-z^{-1})}{17265 (1 - 0.1584129 z^{-1})}$$

$$= \frac{0.5792065 (1-z^{-1})}{1 - 0.1584129 z^{-1}}$$