



Automatic behavior composition synthesis



Giuseppe De Giacomo^a, Fabio Patrizi^a, Sebastian Sardiña^{b,*}

^a Dipartimento di Informatica e Sistemistica, Sapienza Università di Roma, Rome, Italy

^b School of Computer Science and IT, RMIT University, Melbourne, Australia

ARTICLE INFO

Article history:

Received 9 February 2011

Received in revised form 28 November 2012

Accepted 13 December 2012

Available online 2 January 2013

Keywords:

Knowledge representation and reasoning

Intelligent agents

Reasoning about actions and change

Automated planning

Synthesis of reactive systems

ABSTRACT

The behavior composition problem amounts to realizing a virtual desired module (e.g., a surveillance agent system) by suitably coordinating (and re-purposing) the execution of a set of available modules (e.g., a video camera, vacuum cleaner, a robot, etc.). In particular, we investigate techniques to synthesize a controller implementing a fully controllable target behavior by suitably coordinating available partially controllable behaviors that are to execute within a shared, fully observable, but partially predictable (i.e., non-deterministic), environment. Both behaviors and environment are represented as arbitrary finite state transition systems. The technique we propose is directly based on the idea that the controller job is to coordinate the concurrent execution of the available behaviors so as to “mimic” the target behavior. To this end, we exploit a variant of the formal notion of *simulation* to formally capture the notion of “mimicking”, and we show that the technique proposed is sound and complete, optimal with respect to computational complexity, and robust for different kind of system failures. In addition, we demonstrate that the technique is well suited for highly efficient implementation based on synthesis by model checking technologies, by relating the problem to that of finding a winning strategy in a special safety game and explaining how to actually solve it using an existing verification tool.

© 2013 Elsevier B.V. All rights reserved.

1. Introduction

In this paper, we provide a thorough investigation—from theory to implementation—of the behavior composition problem, that is, the problem of how to realize an abstract desired target behavior module by reusing and re-purposing a set of accessible modules implementing certain concrete behaviors. More concretely, we are interested in *synthesizing* a sort of controller that coordinates the available existing behaviors in order to replicate a given desired target behavior [30,79,80]. Generally speaking, a behavior stands for the logic of any artifact that is able to operate in the environment, such as devices, agents, software or hardware components, or workflows. For example, consider a painting blocks world scenario in which blocks are painted and processed by different robotic arms; different behaviors stand for different types of arms (e.g., a gripper, a painting arm, a cleaner arm, etc.), all acting in the same environment. The aim is to realize a desired (intelligent) virtual painting system by suitably “combining” the available arms.

Behavior composition is of particular interest in agents and multi-agent settings. A (desired) intelligent system may be built, for example, from a variety of existing different modules operating (that is, performing actions) on a common environment and whose logic is only partially known. These modules may, in turn, be other agents themselves. A set of RoboCup players with different capabilities can be put together to form an (abstract) more sophisticated “team” player. Similarly, a BDI (Belief–Desire–Intention) agent may implement a desired deterministic plan (which was probably obtained via

* Corresponding author.

E-mail addresses: degiacomo@dis.uniroma1.it (G. De Giacomo), patrizi@dis.uniroma1.it (F. Patrizi), sebastian.sardina@rmit.edu.au (S. Sardiña).

planning or agent communication) by appealing to the set of available user pre-defined non-deterministic plans [36,75]. In robot ecologies and ambient intelligence, advanced functionalities, such as a home surveillance agent, are achieved through the composition of many *simple* robotic devices, such as a vacuum cleaner, a lamp, or a video camera [76,17].

Our work is really a form of process synthesis as studied in Computer Science [70,1,89,51]. However, while most literature on synthesis concentrates on synthesizing a process satisfying a certain specification from scratch, behavior composition focuses on synthesizing a process (the controller) starting from available components [54]. This idea of composing and reusing components has been strongly put forward by Service Oriented Computing, under the name of “service composition” [2,42,63,86]. Indeed, service composition aims at composing complex services by orchestrating (i.e., controlling and coordinating) services that are already at disposal. When service composition takes into account the behavior of the component service, as in [20,84,16] for instance, it becomes intimately related to what we call here “behavior composition”.

When we look at behavior composition from an Artificial Intelligence perspective, the issue of actual controllability of the available behaviors becomes prominent. While one can instruct a behavior module to carry out an action, the actual outcome of the action may not always be foreseen *a priori*, though it can possibly be observed after execution. Our work here is based on revisiting a certain stream of work in service composition [13–15], called “Roman Model” in [42,86], but keeping the need of dealing with partial controllability central. In particular, we consider the problem of synthesizing a *fully controllable* target behavior from a library of available *partially controllable* behaviors that are to execute within a shared, fully observable, but *partially predictable* environment [30,79].

Technically, we abstract behaviors and the environment as finite state *transition systems*. More precisely, each available module is represented as a non-deterministic transition system (to model partial controllability); the target behavior is represented as a deterministic transition system (to model full controllability); and the environment is represented as a non-deterministic transition system (to model partial predictability). The environment’s states are fully accessible by the other transition systems. Working with finite state transition systems allows us to leverage on research in Verification and Synthesis in Computer Science [69,87,50,3,23].

Once we settle for a formal specification of the problem of concern, we develop a novel sound and complete, and optimal w.r.t. worst-case computational complexity technique to generate so-called *compositions*. The technique is directly based on the idea that a composition amounts to a controller that coordinates the concurrent execution of the available modules so as to “mimic” the desired target behavior. We capture “mimicking” through the formal notion of *simulation* [60,41]. Obviously, we need to consider that available behaviors as well as the environment are only partially controllable (i.e., non-deterministic), and therefore a special variant of the classical notion of simulation ought to be devised.

The proposed technique has several interesting features:

- The technique is *sound and complete*, in a very strong sense: it allows to synthesize a sort of meta-controller, called *controller generator*, that represents all possible compositions. While the set of possible compositions is infinite (in fact uncountable) in general, the controller generator is unique.
- The technique gives us a very precise characterization of the sources of *complexity* in the problem: it allows for computing the controller generator (i.e., an implicit representation of *all* compositions) in time exponential *only* in the number of available behaviors, but not in the number of their states. Observe that checking the existence of a composition is known to be EXPTIME-hard even for deterministic available behaviors running in a stateless environment [61].
- Due to its “universality”, the controller generator can be used to generate a sort of *lazy composition* on-the-fly, possibly adapting reactively based on runtime feedback.

In particular, we shall argue that the composition solutions obtained are *robust* to behavior failures in two ways. First, they can handle (a) temporary behavior unavailability as well as (b) unexpected behavior/environment evolution in a totally *reactive* and *on-the-fly* manner—that is, without any extra effort or “re-planning” required to continue the realization of the target behavior—if at all possible, by the very nature of the composition generator. Second, the composition solutions can be *parsimoniously refined* when a module (c) becomes permanently unavailable, or (d) unexpectedly resumes operation.

We complement the proposed technique by showing how it can be implemented by making use of *model checking* technology applied to some special *game structures* developed in the context of Synthesis in Computer Science [3,47,40,69,27]. To that end, we show how to polynomially encode behavior compositions into *safety games* of a specific form, in which each strategy for winning the game corresponds to a composition (Section 5). With that reduction at hand, one is then able to use available tools such as *TLV* [71] in order to actually compute the controller generator by symbolic model checking (Section 6).

Most results presented in this paper appeared at an earlier stage in [30,79,15,80,26]. Here we revise, extend, and combine them into a uniform and in-depth investigation which includes all the technical details and extended examples, so as to provide a fully-comprehensive and clear analysis of the problem and of our solution approach. In particular the technical contributions include:

- a notion of *composition* in the presence of *partially controllable* behaviors;

- a *simulation-based* technique working with partially controllable behaviors, which produces “universal” solutions, i.e., ones from which all possible solutions can be generated;
- *repair* procedures to incrementally refine and adapt an existing solution to various unexpected types of failures;
- an alternative, equivalent, solution technique based on *safety games* well suited for model checking based technology; and a proof-of-concept implementation of the latter in the TLV system.

The rest of the paper is organized as follows. In Section 2 we spell out our framework for behavior composition. In Section 3, we provide our technique based on simulation for synthesizing compositions, and we detail the notion of controller generator. In Section 4, we show how the approach can deal with behavior failures. Then, in Section 5, we turn to synthesis by model checking, and show how one can compute the controller generator through safety games. Based on the results of the previous sections, we show in Section 6 how to implement behavior composition in practice using existing platforms for synthesis by model checking such as TLV [71]. (The full TLV code for our running example is reported in Appendix A.) We discuss related work in various areas of Artificial Intelligence and Computer Science in Section 7, and draw conclusions in Section 8.

2. The framework

In this section, we formally define the problem of concern, by developing an abstract framework based on finite state transition systems.

Environment. We assume to have a shared fully observable *environment* which provides an abstract account of action pre-conditions and effects, and can be regarded as a means of communication among behaviors (defined below). As, in general, we have *incomplete information* about preconditions and effects (akin to an action theory), the environment can, in general, be *non-deterministic*.

Formally, an environment is a tuple $\mathcal{E} = \langle \mathcal{A}, E, e_0, \rho \rangle$, where:

- \mathcal{A} is a finite set of *shared actions*;
- E is the finite set of *environment states*;
- $e_0 \in E$ is the *environment initial state*;
- $\rho \subseteq E \times \mathcal{A} \times E$ is the *environment transition relation* among states.

When referring to environment transitions, we equivalently use notations $\langle e, a, e' \rangle \in \rho$ or $e \xrightarrow{a} e'$ (in \mathcal{E}), both denoting that performing action a in state e may lead the environment to successor state e' .

Observe that this notion of environment shares a lot of similarities with so-called “transition systems” in action languages [34]; indeed, that formalism might well be used to compactly represent the environment, in our setting.

Behaviors. A *behavior* abstracts the program of some agent (or, more in general, the logic of a device/module), in terms of (internal) states, actions and transitions. Behaviors are not intended to execute on their own but, rather, to operate within an environment (and, through this, possibly interact with other behaviors). Hence, they are equipped with the ability to test, when needed, conditions (or *guards*) on environment states.

Formally, a behavior over an environment \mathcal{E} is a tuple $\mathcal{B} = \langle B, b_0, G, F, \varrho \rangle$, where:

- B is the finite set of *behavior states*;
- $b_0 \in B$ is the *behavior initial state*;
- G is a set of *guards* over \mathcal{E} , that is, boolean functions $g : E \mapsto \{\top, \perp\}$;
- $F \subseteq B$ is the set of *behavior final states*;
- $\varrho \subseteq B \times G \times \mathcal{A} \times B$ is the *behavior transition relation*.

We freely interchange notations $\langle b, g, a, b' \rangle \in \varrho$, and $b \xrightarrow{g,a} b'$ in \mathcal{B} . A “guarded” transition $\langle b, g, a, b' \rangle \in \varrho$ denotes that: (i) action a can be executed by \mathcal{B} in state b when the environment is in a state e such that $g(e) = \top$; and (ii) the execution may lead the behavior to successor state b' . Notice that a behavior’s evolution depends on the environment it is defined over, as action executability depends on guard satisfaction.

Intuitively, behavior states model agent’s decision points: when the behavior is in a given state, the agent selects the action to be executed next among those executable¹ at that state. Executing the selected action, besides other effects, leads the behavior to a successor state, where a new set of actions become executable, and a new iteration starts. Final states are those where the behavior can be safely stopped (e.g., final states of a mechanic arm might correspond to safe configurations).

¹ Subject to environment’s current state.

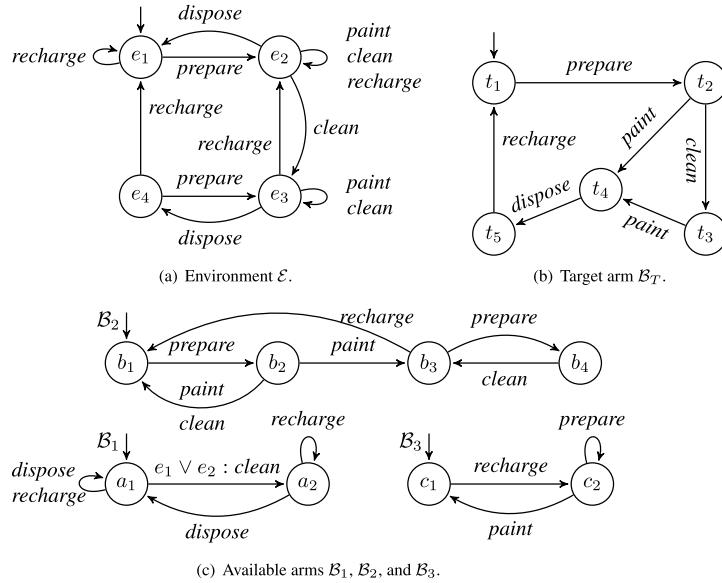


Fig. 1. The painting arms system $S = \langle B_1, B_2, B_3, \mathcal{E} \rangle$ and the target arm B_T .

We say that a behavior \mathcal{B} over environment \mathcal{E} is *deterministic* if no behavior and environment states exist, say $b \in \mathcal{B}$ and $e \in \mathcal{E}$, respectively, for which two transitions $b \xrightarrow{g_1,a} b'$ and $b \xrightarrow{g_2,a} b''$ exist such that $b' \neq b''$ and $g_1(e) = g_2(e) = \top$.

Clearly, given a *deterministic* behavior's and an environment's states, and an executable action, the next behavior state is always predictable. In other words, deterministic behaviors are *fully controllable* by appropriate action selections. In general, however, behaviors are *non-deterministic*, that is, the state resulting from an action execution is unpredictable, and, thus, so are the actions that will be available in such a state. In other words, non-deterministic behaviors are only *partially controllable*.

System and target behavior. As said above, behaviors operate within an environment (the one they are defined over) and can, through this, interact with each other. The notion of *system* introduced below allows for identifying a set of interacting behaviors over the same environment.

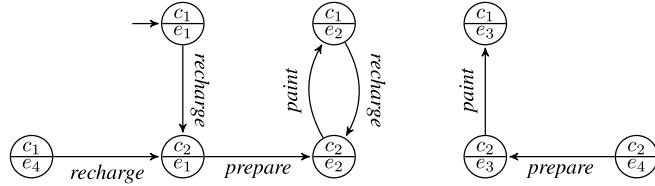
A *system* is a tuple $S = \langle B_1, \dots, B_n, \mathcal{E} \rangle$, where \mathcal{E} is an environment and B_1, \dots, B_n are pre-defined, possibly non-deterministic, *available behaviors* over \mathcal{E} . We stress that available behaviors are given and cannot be modified, though they can, of course, be (partially) controlled through action execution. The behaviors of a system model the only available implementations one can actually use to execute actions. Importantly, a behavior cannot be instructed to execute actions regardless of its (and environment's) current state, but needs to be in a state where the desired action is actually executable; external controllers must, of course, take these constraints into account when coordinating a set of behaviors.

Finally, we define the so-called *target behavior* B_T as a *deterministic* behavior over \mathcal{E} , which represents the fully controllable desired behavior to be obtained. Roughly speaking, the challenge we deal with here is to bring about the “virtual” (i.e., non-readily available) target behavior by properly “composing” the execution of available behaviors. Observe that the target is meant to be deterministic, as it is assumed that the desired system is fully known.

Example 1. In the *painting arms scenario* depicted in Fig. 1, the overall aim of the system is to process blocks. Only one block at a time can be processed: it can be cleaned or painted, but needs first to be prepared. After preparation, cleaning and painting can be performed when water and paint, stored in two different tanks, are (respectively) available. Both tanks can be charged simultaneously by pushing a button. Blocks can also be cleaned, but only in particular circumstances (i.e., environment in state e_3 , see below).

The non-deterministic environment \mathcal{E} provides a description of the dynamic domain that the behaviors interact with. Nodes and edges represent states and transitions, respectively; each edge label represents the action that triggers the transition; and the initial state has an incoming edge without source. For instance, as said, blocks can be painted or cleaned only after they have been prepared: so, from e_1 , a state where either action *paint* or *clean* is enabled (either e_2 or e_3) can only be reached by first executing *prepare*. Though not graphically represented, the environment accounts for tank states, e.g.: in e_1 and e_2 the water tank is not empty, while it is in e_3 and e_4 . Action *clean* can also be performed in e_3 , even though the water tank is empty, as in this state a cleaning tool not relying on water becomes available.

B_T describes the (deterministic) behavior of a desired (target) arm-agent module. Observe that state t_2 captures a decision point: cleaning a block is optional, as the selection of the next transition is demanded to the executor, which makes

**Fig. 2.** Enacted arm \mathcal{B}_3 .

its decisions according to internal policies—e.g., ensuring first that the block is dirty. Also, notice that \mathcal{B}_T is “conservative”, in that it always recharges the tanks after processing a block, so as to guarantee that *clean* will be executable, if needed.

The desired arm \mathcal{B}_T does not exist in reality. Nonetheless, there are three different actual arms available: \mathcal{B}_1 (states a_1, a_2), a cleaning-disposing arm able to clean and dispose blocks; \mathcal{B}_2 (states b_1, \dots, b_4), capable of preparing, cleaning, and painting blocks; and \mathcal{B}_3 (states c_1, c_2), a paint arm that can also prepare blocks for processing. All three arms are able to press the charge button (to refill the tanks). Notice that arm \mathcal{B}_2 behaves non-deterministically when it comes to painting a block. This non-determinism captures modeler’s incomplete information about \mathcal{B}_2 ’s internal logic. Observe also that arm \mathcal{B}_1 requires the environment to be in e_1 or e_2 , in order to perform *clean*, as it needs water to actually execute the action.

In this example, all behavior states are assumed final, thus imposing no restrictions on when the execution can be stopped.

Next, we derive the notions of behavior and system *enactment*, which are abstract structures needed to formally state the composition problem and characterize its solutions.

Enacted behaviors. Behaviors and the environment mutually affect their executions. Such a “combined” evolution is formally described by *enacted behaviors*. Given a behavior $\mathcal{B} = \langle B, b_0, G, F, \varrho \rangle$ over an environment $\mathcal{E} = \langle \mathcal{A}, E, e_0, \rho \rangle$, the enacted behavior of \mathcal{B} on \mathcal{E} is a tuple $\mathcal{T}_{\mathcal{B}} = \langle S, \mathcal{A}, s_0, Q, \delta \rangle$, where:

- $S = B \times E$ is the (finite) set of $\mathcal{T}_{\mathcal{B}}$ ’s states, where for each state $s = \langle b, e \rangle \in S$, we denote b as $beh(s)$ and e as $env(s)$;
- \mathcal{A} is the same set of actions as in \mathcal{E} ;
- $s_0 \in S$ is the initial state of $\mathcal{T}_{\mathcal{B}}$, such that $beh(s_0) = b_0$ and $env(s_0) = e_0$;
- $\delta \subseteq S \times \mathcal{A} \times S$ is the enacted transition relation, where $\langle s, a, s' \rangle \in \delta$ or, equivalently, $s \xrightarrow{a} s'$ in $\mathcal{T}_{\mathcal{B}}$, if and only if:
 - $env(s) \xrightarrow{a} env(s')$ in \mathcal{E} , that is, action a is actually executable in \mathcal{E} ;
 - $beh(s) \xrightarrow{g,a} beh(s')$ in \mathcal{B} , with $g(env(s)) = \top$ for some $g \in G$, that is, action a can be performed by \mathcal{B} from its state $beh(s)$ when the environment state $env(s)$ satisfies the guard which labels the respective transition.
- $Q = \{s \in S \mid beh(s) \in F\}$ is the set of the enacted behavior’s final states.

Technically, $\mathcal{T}_{\mathcal{B}}$ is the synchronous product of the behavior and the environment, and represents all possible executions obtained from running behavior \mathcal{B} once guards are evaluated and actions are performed in \mathcal{E} . Observe that the enacted behavior non-determinism stems from both environment’s and behavior’s. Moreover, notice that action executability for a behavior is subject to: (i) its own state; (ii) guard evaluation in current environment state; and (iii) the environment state itself. In particular, even though a transition labeled with action a and outgoing from current behavior (\mathcal{B}) state exists, if, given current environment state e , no transition outgoing from e is labeled with a , then \mathcal{B} cannot execute a —as if its precondition were not satisfied. In the following, when no ambiguity arises, we simplify the notation by denoting the enacted counterpart of a behavior \mathcal{B}_i simply as \mathcal{T}_i , instead of $\mathcal{T}_{\mathcal{B}_i}$.

Example 2. The enacted behavior \mathcal{T}_3 depicted in Fig. 2 describes the evolution of arm \mathcal{B}_3 if it were to act alone in the environment. Observe that there exist some joint states that cannot be reached by \mathcal{B}_3 alone. For instance, $\langle c_1, e_4 \rangle$ can only be reached by executing action *dispose* which is not available in \mathcal{B}_3 .

Enacted system behavior. The *enacted system behavior* formally captures the concurrent, interleaved, execution of *all* available behaviors on the environment of a system. Let $\mathcal{S} = \langle \mathcal{B}_1, \dots, \mathcal{B}_n, \mathcal{E} \rangle$ be a system, where $\mathcal{E} = \langle \mathcal{A}, E, e_0, \rho \rangle$ and $\mathcal{B}_i = \langle B_i, b_{i0}, G_i, F_i, \varrho_i \rangle$ ($i = 1, \dots, n$). The enacted system behavior of \mathcal{S} is a tuple $\mathcal{T}_{\mathcal{S}} = \langle S_{\mathcal{S}}, \mathcal{A}, \{1, \dots, n\}, s_{\mathcal{S}0}, Q_{\mathcal{S}}, \delta_{\mathcal{S}} \rangle$, where:

- $S_{\mathcal{S}} = B_1 \times \dots \times B_n \times E$ is the finite set of $\mathcal{T}_{\mathcal{S}}$ states; given $s_{\mathcal{S}} = \langle b_1, \dots, b_n, e \rangle$, we denote b_i as $beh_i(s_{\mathcal{S}})$ ($i = 1, \dots, n$) and e as $env(s_{\mathcal{S}})$;
- $s_{\mathcal{S}0} \in S_{\mathcal{S}}$ is the initial state of $\mathcal{T}_{\mathcal{S}}$, such that $beh_i(s_{\mathcal{S}0}) = b_{i0}$ ($i = 1, \dots, n$) and $env(s_{\mathcal{S}0}) = e_0$;
- $Q_{\mathcal{S}} = \{s_{\mathcal{S}} \in S_{\mathcal{S}} \mid \forall i \in \{1, \dots, n\} beh_i(s_{\mathcal{S}}) \in F_i\}$ is the set of $\mathcal{T}_{\mathcal{S}}$ final states;

- $\delta_S \subseteq S_S \times \mathcal{A} \times \{1, \dots, n\} \times S_S$ is \mathcal{T}_S 's transition relation, where $\langle s_S, a, k, s'_S \rangle \in \delta_S$ or, equivalently, $s_S \xrightarrow{a,k} s'_S$ in \mathcal{T}_S , if and only if:
 - $\text{env}(s_S) \xrightarrow{a} \text{env}(s'_S)$ in \mathcal{E} ;
 - $\text{beh}_k(s_S) \xrightarrow{g,a} \text{beh}_k(s'_S)$ in \mathcal{B}_k , with $g(\text{env}(s_S)) = \top$, for some $g \in G_k$;
 - $\text{beh}_i(s_S) = \text{beh}_i(s'_S)$, for $i \in \{1, \dots, n\} \setminus \{k\}$.

The enacted system behavior \mathcal{T}_S is technically the synchronous product of: (i) the environment, and (ii) the asynchronous product of the available behaviors. Except for the presence of index k in transitions, which identifies the behavior that performs the labeling action, it is formally analogous to an enacted behavior.

Controller. We are now ready to introduce the main component of our framework: the *controller*, which models an entity able to instruct available behaviors to execute actions, as well as to activate, stop, and resume their execution. We assume the controller has *full observability* on both available behaviors and the environment, that is, it can keep track, at runtime, of their current states. Although other choices are possible, full observability is quite natural in this context, since available behaviors and environment are already suitable abstractions of *actual* modules: if details have to be hidden, this can be done directly within the exposed abstract behaviors, by resorting to non-determinism.

In order to formally define controllers, we start with the notions of *traces* and *histories*. Let $\mathcal{T}_B = \langle S, \mathcal{A}, s_0, Q, \delta \rangle$ be an enacted behavior of some (available or target) behavior B over environment \mathcal{E} . A trace for \mathcal{T}_B is a possibly infinite sequence $\tau = s^0 \xrightarrow{a^1} s^1 \xrightarrow{a^2} \dots$, such that (i) $s^0 = s_0$; and (ii) $s^j \xrightarrow{a^{j+1}} s^{j+1}$ in \mathcal{T}_B , for all $j \geq 0$. A history is just a *finite* prefix (ending with a state) $h = s^0 \xrightarrow{a^1} \dots \xrightarrow{a^\ell} s^\ell$ of a trace. We denote h 's last state s^ℓ by *last*(h), and its length ℓ by $|h|$. As finite traces are also histories, function $|\cdot|$ is also defined over them; if τ is an infinite trace, we let $|\tau| = \infty$.

Traces and histories extend immediately to enacted system behaviors, by adding index k . System traces have the form $s^0 \xrightarrow{a^1, k^1} s^1 \xrightarrow{a^2, k^2} \dots$, and system histories have the form $s^0 \xrightarrow{a^1, k^1} \dots \xrightarrow{a^\ell, k^\ell} s^\ell$. Functions $|\cdot|$ and *last* are extended in the obvious way.

Now, consider a system $S = \langle \mathcal{B}_1, \dots, \mathcal{B}_n, \mathcal{E} \rangle$ and its enacted behavior \mathcal{T}_S . Let \mathcal{H} be the set of all \mathcal{T}_S histories. A controller for S is a possibly partial function $P : \mathcal{H} \times \mathcal{A} \mapsto \{1, \dots, n\}$.² Intuitively, $P(h, a)$ identifies the available behavior, i.e., $\mathcal{B}_{P(h,a)}$, to delegate action a to, after S has evolved as described by enacted system behavior history h .

The behavior composition problem. Roughly speaking, the problem we deal with is that of synthesizing, for a given system S , a controller that *realizes* a desired target behavior, that is, a controller able to coordinate the available modules in the system so that the resulting behavior is, in fact, analogous to the target. In order to formalize this notion, we first need to define *trace realizations*. Let $S = \langle \mathcal{B}_1, \dots, \mathcal{B}_n, \mathcal{E} \rangle$ be a system, \mathcal{B}_T a target behavior, and P a controller for S . Furthermore, let τ be an enacted target behavior trace (i.e., a trace of \mathcal{T}_T) of the form $\tau = s^0 \xrightarrow{a^1} s^1 \xrightarrow{a^2} \dots$. We define the set of enacted system histories induced by controller P on trace τ , as the set $\mathcal{H}_{\tau,P} = \bigcup_{\ell \geq 0} \mathcal{H}_{\tau,P}^\ell$, where:

- $\mathcal{H}_{\tau,P}^0 = \{s_S s_0\}$;
- $\mathcal{H}_{\tau,P}^{j+1}$ is the set of all $(j+1)$ -length histories $h \xrightarrow{a^{j+1}, k^{j+1}} s_S^{j+1}$ such that:
 - $h \in \mathcal{H}_{\tau,P}^j$;
 - $\text{env}(s_S^{j+1}) = \text{env}(s^{j+1})$;
 - $k^{j+1} = P(h, a^{j+1})$, that is, at history h , action a^{j+1} in trace τ is delegated to available behavior $\mathcal{B}_{k^{j+1}}$;
 - $\text{last}(h) \xrightarrow{a^{j+1}, k^{j+1}} s^{j+1}$ in \mathcal{T}_S , that is, behavior $\mathcal{B}_{k^{j+1}}$ can actually execute action a^{j+1} .

Informally, $\mathcal{H}_{\tau,P} \subseteq \mathcal{H}$ represents the set of all possible enacted system histories that ensue when controller P processes the target trace τ . Notice that the evolution of the environment in the histories in $\mathcal{H}_{\tau,P}$ ought to respect the evolution of the environment encoded in trace τ . Also note that because the evolution of the environment is independent of which behavior executes an action, if the target can cause the environment to evolve from one state to another when performing an action, then such same action in an available behavior will also be able to cause the same evolution of the environment.

Then, we say that P realizes enacted target trace τ (recall $\tau = s^0 \xrightarrow{a^1} s^1 \xrightarrow{a^2} \dots$) if:

1. for all \mathcal{T}_S histories $h \in \mathcal{H}_{\tau,P}$: if $|h| < |\tau|$, then $P(h, a^{|h|+1}) = k$ and $\text{last}(h) \xrightarrow{a^{|h|+1}, k} s'_S$ in \mathcal{T}_S for some s'_S ;
2. if τ is finite and $s^{|\tau|} \in Q_T$ (i.e., $\text{beh}(s^{|\tau|})$ is final for \mathcal{B}_T), then all $|\tau|$ -length histories $h \in \mathcal{H}_{\tau,P}^{|\tau|}$ are such that $\text{last}(h) \in Q_S$.

² The kind of general synthesis we focus on here is that under the general assumption of *perfect recall* [32]: all what has been “seen” so far can be used to take a decision. As part of the technical contributions of this paper, we shall demonstrate later that *finite* controllers will however be sufficient for our composition framework.

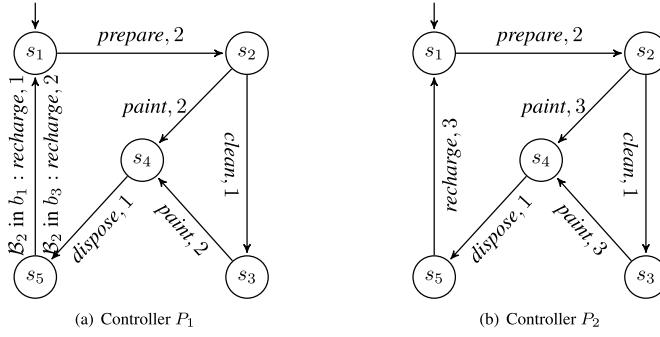


Fig. 3. Two finite state controllers.

Informally, saying that a controller realizes a target behavior trace means that: given a (possibly infinite) sequence of actions compliant with the target behavior, and a possible environment evolution resulting from the execution of such action sequence, the controller selects at each step of execution a behavior able to actually execute the action requested at that step, no matter how behaviors—which are non-deterministic—selected earlier evolved.

In addition, if the target trace finishes at a final state (for the enacted target behavior), then the whole system is brought to a legal terminating state, too. In other words, the controller is *always* able to delegate the actions so as to mimic the target behavior.

Because a deterministic behavior itself can be seen as a specification of a set of traces, we say that *a controller P realizes a target behavior \mathcal{B}_T* if and only if it realizes all traces of \mathcal{T}_T . This can be informally rephrased as the ability to delegate, step by step, all target behavior's action sequences, no matter how the environment and the available behaviors evolve.

Observe that the controller can observe the current states of the available behaviors as well as that of the environment (in fact, it can observe the whole system history up to the current state), in order to decide which behavior to select next. This makes these controllers akin to an advanced form of conditional plans and, in fact, the problem itself is related to planning [39], being both synthesis tasks. Here, though, we are not planning for choosing the next action, but for *who shall execute the next action*, whatever such action happens to be at runtime. Formally, the problem that we deal with is as follows:

Given a system $\mathcal{S} = \langle \mathcal{B}_1, \dots, \mathcal{B}_n, \mathcal{E} \rangle$ and a deterministic *target behavior* \mathcal{B}_T over \mathcal{E} , synthesize a controller P that realizes \mathcal{B}_T .

All controllers that are a solution to this problem are called *compositions* (of \mathcal{B}_T on \mathcal{E}).

Example 3. Even though compositions are, in general, functions of system histories (and actions), there are cases where they depend only on the history's last k (≥ 0) states. In such cases, they can be represented as finite state machines. In Fig. 3, for instance, two *finite state controllers* P_1 and P_2 are depicted. An edge outgoing from a state s and labeled with a pair $c : \langle a, k \rangle$ means that when the controller is in state s and action a is requested, a is delegated to behavior \mathcal{B}_k , provided condition c holds (omitted conditions are assumed true). The main difference between P_1 and P_2 is in the arm used for painting: P_1 uses \mathcal{B}_2 , while P_2 uses \mathcal{B}_3 . In addition, P_1 recharges the tanks using behavior \mathcal{B}_1 when behavior \mathcal{B}_2 is in b_1 , whereas it uses behavior \mathcal{B}_2 when \mathcal{B}_2 is in state b_1 . Controller P_2 , on the other hand, always uses \mathcal{B}_3 to recharge the tanks.

For an example of trace realization, consider trace $\tau = \langle t_1, e_1 \rangle \xrightarrow{\text{prepare}} \langle t_2, e_2 \rangle \xrightarrow{\text{clean}} \langle t_3, e_3 \rangle \xrightarrow{\text{paint}} \langle t_4, e_3 \rangle$ of the enacted target behavior \mathcal{T}_T depicted in Fig. 4(a) (the graphical patterns of states are not relevant here). The set \mathcal{H}_{τ, P_1} of enacted system histories induced by P_1 on τ , for the enacted system behavior \mathcal{T}_S of Fig. 4(b), contains exactly the following traces:

$$\begin{aligned} h_1 &= \langle a_1, b_1, c_1, e_1 \rangle; \\ h_2 &= \langle a_1, b_1, c_1, e_1 \rangle \xrightarrow{\text{prepare}, 2} \langle a_1, b_2, c_1, e_2 \rangle; \\ h_3 &= \langle a_1, b_1, c_1, e_1 \rangle \xrightarrow{\text{prepare}, 2} \langle a_1, b_2, c_1, e_2 \rangle \xrightarrow{\text{clean}, 1} \langle a_2, b_2, c_1, e_3 \rangle; \\ h_4 &= h_3 \xrightarrow{\text{paint}, 2} \langle a_2, b_1, c_1, e_3 \rangle; \\ h_5 &= h_3 \xrightarrow{\text{paint}, 2} \langle a_2, b_3, c_1, e_3 \rangle. \end{aligned}$$

Observe that even though action *paint* may lead the environment to either state e_2 or state e_3 , the traces in \mathcal{H}_{τ, P_1} account for the latter outcome only. This is due to the fact that \mathcal{H}_{τ, P_1} only contains histories encoding the *same environment evolution* as target trace τ (and where delegations are performed as dictated by controller P_1). The case in which the environment moves to state e_2 is accounted for by another target trace, say τ' , which matches τ except for the last state, where $\text{last}(\tau') = \langle t_4, e_2 \rangle$. Notice however that in order for P_1 to be a composition, τ' must be realized as well. As for available behaviors, instead, all of their possible evolutions are accounted for in set \mathcal{H}_{τ, P_1} . For instance, h_4 and h_5 represent

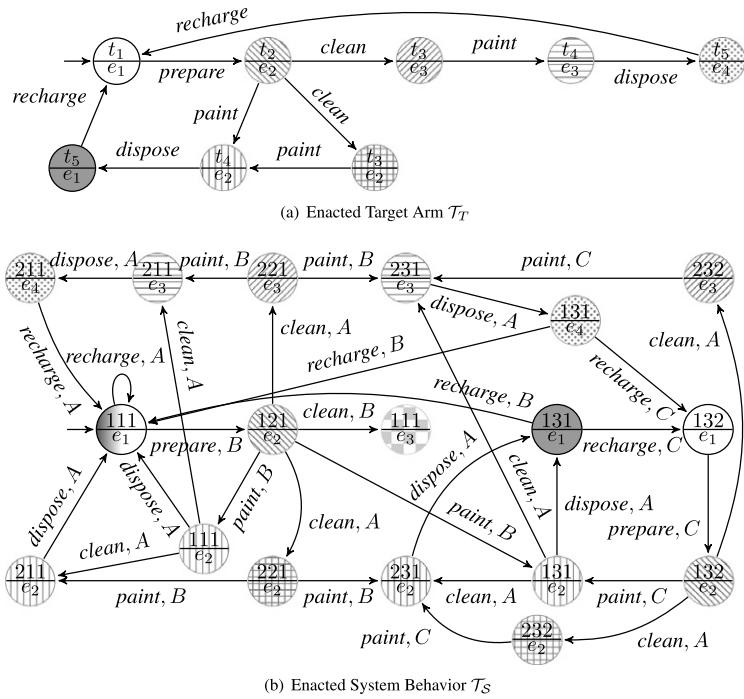


Fig. 4. The largest ND-simulation relation \preceq between the enacted target \mathcal{T}_T and (a fragment of) the enacted system \mathcal{T}_S . A state in \mathcal{T}_S ND-simulates those in \mathcal{T}_T that share its texture, e.g., $\langle \langle a_1, b_3, c_1 \rangle, e_2 \rangle \preceq \langle t_4, e_2 \rangle$. Observe that state $\langle \langle a_1, b_1, c_1 \rangle, e_1 \rangle$ is the only one with two textures—plain black and white—and hence ND-simulates both $\langle t_1, e_1 \rangle$ and $\langle t_5, e_1 \rangle$, and that state $\langle \langle a_1, b_1, c_1 \rangle, e_3 \rangle$ ND-simulates no state.

similar runs except for the fact that behavior \mathcal{B}_2 evolves differently after executing the *paint* action (either to b_1 in h_4 or to b_3 in h_5).

It can be easily seen that P_1 does realize trace τ , as well as all of the other traces of \mathcal{T}_T , thus being a composition of \mathcal{B}_T on \mathcal{E} . On the contrary, P_2 does not amount to a composition of \mathcal{B}_T . To see that, consider again the target trace τ . It turns out that set \mathcal{H}_{τ, P_2} contains the history

$$\langle a_1, b_1, c_1, e_1 \rangle \xrightarrow{\text{prepare}, 2} \langle a_1, b_2, c_1, e_2 \rangle \xrightarrow{\text{clean}, 1} \langle a_2, b_2, c_1, e_3 \rangle,$$

and that no transition $\langle a_2, b_2, c_1, e_3 \rangle \xrightarrow{\text{paint}, 3} s'_S$ exists in \mathcal{T}_S for any s'_S . Hence, P_2 does not realize τ and is not a composition.

This concludes the formal statement of the behavior composition problem. The framework just presented stands for what can be considered the “core” framework, i.e., a basic setting that incorporates all distinguishing features of the problem. However, we stress that extensions and generalization can be defined so as to obtain non-trivial variants, which can be adopted to model and solve similar problems from domains that satisfy different assumptions (see Section 8 for a discussion on this).

3. Composition via simulation

Next, we present our approach to composition synthesis. This is originally inspired by [15], where a restricted version of the composition problem was addressed, in the context of services, by taking the standard notion of *simulation relation* [60,41] as a formal tool for solution characterization. Here, the shared environment and the (devilish) non-determinism of both the available behaviors and the environment significantly sophisticate that framework, calling for a new formal setting, the one presented here, where the usual notion of simulation relation is no longer enough to fully characterize the set of solutions and, hence, to guide the solution process.

Intuitively, we say that a transition system S_1 simulates another transition system S_2 , if S_1 is able to “match”, step by step, all of S_2 moves during execution. More precisely, imagine to execute S_2 starting from its initial state. At each step of execution, S_2 performs a transition among those allowed in its (current) state. If, for all possible ways of executing S_2 , S_1 can, at each step, choose a transition that “matches” (according to some criteria, e.g., label equivalence) the one executed by S_2 then S_1 simulates S_2 . We stress that S_1 decisions are required to be made in an “online” fashion, as S_2 evolves. In other words, it is not the case that S_1 knows in advance which transitions S_2 will execute in the future.

Such an intuition is formalized in the following definition, where both non-determinism and the shared environment are taken into account.

Algorithm 1: *NDS*($\mathcal{T}_T, \mathcal{T}_S$)—Largest ND-simulation.

```

1  $\mathcal{R} := S_T \times S_S \setminus \{(s_T, s_S) \mid \text{env}(s_T) \neq \text{env}(s_S) \vee (s_T \in Q_T \wedge s_S \notin Q_S)\};$ 
2 repeat
3    $\mathcal{R} := (\mathcal{R} \setminus \mathcal{C})$ , where  $\mathcal{C}$  is the set of  $(s_T, s_S) \in \mathcal{R}$  such that there exists an action  $a \in \mathcal{A}$  and for each  $k$  there exists a transition  $s_T \xrightarrow{a} s'_T$  in  $\mathcal{T}_T$  such that either:
    (a) there is no transition  $s_S \xrightarrow{a,k} s'_S$  in  $\mathcal{T}_S$  such that  $\text{env}(s'_S) = \text{env}(s'_T)$ ; or
    (b) there exists a transition  $s_S \xrightarrow{a,k} s'_S$  in  $\mathcal{T}_S$  such that  $\text{env}(s'_S) = \text{env}(s'_T)$  but  $(s'_T, s'_S) \notin \mathcal{R}$ .
4 until ( $\mathcal{C} = \emptyset$ );
5 return  $\mathcal{R}$ ;

```

Let $\mathcal{S} = \langle \mathcal{B}_1, \dots, \mathcal{B}_n, \mathcal{E} \rangle$ be a system, \mathcal{B}_T a target behavior over \mathcal{E} , and $\mathcal{T}_S = \langle S_S, \mathcal{A}, \{1, \dots, n\}, s_{S0}, Q_S, \delta_S \rangle$ and $\mathcal{T}_T = \langle S_T, \mathcal{A}, s_{T0}, Q_T, \delta_T \rangle$ the enacted system and enacted target behaviors corresponding to \mathcal{S} and \mathcal{B}_T on \mathcal{E} , respectively. An *ND-simulation relation* of \mathcal{T}_T by \mathcal{T}_S is a relation $R \subseteq S_T \times S_S$, such that $(s_T, s_S) \in R$ implies:

1. $\text{env}(s_T) = \text{env}(s_S)$;
2. if $s_T \in Q_T$, then $s_S \in Q_S$;
3. for all $a \in \mathcal{A}$, there exists a $k \in \{1, \dots, n\}$ —also referred to as a *witness* of $(s_T, s_S) \in R$ for action a —such that for all transitions $s_T \xrightarrow{a} s'_T$ in \mathcal{T}_T :
 - (a) there exists a transition $s_S \xrightarrow{a,k} s'_S$ in \mathcal{T}_S with $\text{env}(s'_S) = \text{env}(s'_T)$;
 - (b) for all transitions $s_S \xrightarrow{a,k} s'_S$ in \mathcal{T}_S with $\text{env}(s'_S) = \text{env}(s'_T)$, it is the case that $(s'_T, s'_S) \in R$.

In words, if a pair of enacted states is in the ND-simulation (relation), then: (i) its states share the same environment component; (ii) if the target behavior is in a final state, so is the system; and (iii) for all actions the (enacted) target behavior can execute, there exists a *witness* behavior \mathcal{B}_k that can execute the same action while guaranteeing, regardless of non-determinism, preservation of the ND-simulation relation for successor target and system states.

We say that a state $s_T \in S_T$ is *ND-simulated* by a state $s_S \in S_S$ (or s_S *ND-simulates* s_T), denoted $s_T \preceq s_S$, if there exists an ND-simulation relation R of \mathcal{T}_T by \mathcal{T}_S such that $(s_T, s_S) \in R$. Observe that this is a co-inductive definition. As a result, the relation \preceq is itself an ND-simulation relation, in fact the *largest* one, in the sense that all ND-simulations are contained in \preceq .

Given \mathcal{T}_T and \mathcal{T}_S , relation \preceq can be computed by Algorithm 1 (*NDS*). Roughly speaking, the algorithm works by iteratively removing those tuples for which the requirements of the ND-simulation definition do not apply, until a fixpoint is reached. It is straightforward to prove that the algorithm reaches a fixpoint in a finite number of steps and computes the largest ND-simulation, by comparing the algorithm with the definition of ND-simulation relation and observing that no tuple is ever added to the candidate set \mathcal{R} , and that $\mathcal{C} \subseteq \mathcal{R}$.

Example 4. Fig. 4 shows a fragment of the largest ND-simulation relation for our painting blocks world example. In particular, Fig. 4(a) shows the enacted target behavior of \mathcal{B}_T and Fig. 4(b) depicts a fragment of the system enacted behavior. States in Fig. 4(b) contain, in the bottom half, the environment component, and, in the top half, a compact representation of available service (current) states: the first component of the integer string represents the subscript of the state that \mathcal{B}_1 is in, the second refers to \mathcal{B}_2 , and so on. For instance, the node labeled with $\langle 211, e_4 \rangle$ represents the system state $\langle \langle a_2, b_1, c_1 \rangle, e_4 \rangle$.

Matching graphical patterns between \mathcal{T}_T and \mathcal{T}_S states mean that such states are in ND-simulation. For example, $\langle \langle a_1, b_3, c_2 \rangle, e_2 \rangle$ of \mathcal{T}_S *ND-simulates* $\langle t_2, e_2 \rangle$ of \mathcal{T}_T ; this implies that (i) every conceivable action taken in $\langle t_2, e_2 \rangle$ can be replicated by some behavior (possibly a different one for each action) when the system is in $\langle \langle a_1, b_3, c_2 \rangle, e_2 \rangle$ and, moreover, that (ii) this property propagates to the resulting successor states.

Observe that, clearly, a \mathcal{T}_T state can be simulated by several \mathcal{T}_S 's, as is the case for, e.g., $\langle t_4, e_2 \rangle$, which is simulated by both $\langle \langle a_1, b_1, c_1 \rangle, e_2 \rangle$ and $\langle \langle a_1, b_3, c_1 \rangle, e_2 \rangle$. Also the converse may happen: $\langle \langle a_1, b_1, c_1 \rangle, e_1 \rangle$ in \mathcal{T}_S *ND-simulates* \mathcal{T}_T state $\langle t_1, e_1 \rangle$ as well as $\langle t_5, e_1 \rangle$.

The relevance of the ND-simulation relation to the composition problem addressed here is twofold. Firstly, as will be shown next, computing the largest ND-simulation relation between a target enacted behavior and a system enacted behavior is essentially equivalent to checking whether there exists a composition for the target behavior that “uses” the behaviors available in the system. Secondly, this “simulation-based” approach overcomes the main obstacles that previous solution techniques (e.g., [13]) encountered, as it enables the construction of *flexible* solutions that can take runtime information into account, at no additional (worst-case) cost.

Our first main result states that checking the existence of a composition can be reduced to checking whether the enacted target behavior's initial state is ND-simulated by the enacted system behavior's initial state, which corresponds to checking whether there exists an ND-simulation relation that includes the initial states of both.

Theorem 1. Let $\mathcal{S} = \langle \mathcal{B}_1, \dots, \mathcal{B}_n, \mathcal{E} \rangle$ be a system and \mathcal{B}_T a target behavior over \mathcal{E} . Moreover, let $\mathcal{T}_T = \langle S_T, \mathcal{A}, s_{T0}, Q_T, \delta_T \rangle$ and $\mathcal{T}_{\mathcal{S}} = \langle S_{\mathcal{S}}, \mathcal{A}, \{1, \dots, n\}, s_{S0}, Q_{\mathcal{S}}, \delta_{\mathcal{S}} \rangle$ be the enacted target behavior and the enacted system behavior for \mathcal{B}_T and \mathcal{S} , respectively. Then, a composition controller P of target \mathcal{B}_T on system \mathcal{S} exists if and only if $s_{T0} \preceq s_{S0}$.

Proof. (IF PART). First, we define P . To this end, let $h = s_S^0 \xrightarrow{a^1, k^1} \dots \xrightarrow{a^\ell, k^\ell} s_S^\ell \in \mathcal{H}$ be a $\mathcal{T}_{\mathcal{S}}$ history and $a \in \mathcal{A}$ an action. If there exists a \mathcal{T}_T history $h_T = s_T^0 \xrightarrow{a^1} \dots \xrightarrow{a^\ell} s_T^\ell$ (i.e., a history matching the actions of h) such that $s_T^\ell \preceq s_S^\ell$, and a transition $s_T^\ell \xrightarrow{a} s_T^{\ell+1}$ in \mathcal{T}_T (i.e., action a is \mathcal{B}_T -executable in s_T^ℓ), then we define $P(h, a) \in \omega_a$, where ω_a is the set of all indexes $k \in \{1, \dots, n\}$ such that for all transitions $s_T^\ell \xrightarrow{a} s_T^{\ell+1}$:

- there exists a transition $s_S^\ell \xrightarrow{a, k} s_S^{\ell+1}$ in $\mathcal{T}_{\mathcal{S}}$ with $\text{env}(s_S^{\ell+1}) = \text{env}(s_T^{\ell+1})$;
- for all transitions $s_S^\ell \xrightarrow{a, k} s_S^{\ell+1}$ in $\mathcal{T}_{\mathcal{S}}$ with $\text{env}(s_S^{\ell+1}) = \text{env}(s_T^{\ell+1})$, $s_T^{\ell+1} \preceq s_S^{\ell+1}$.

Because $s_T^\ell \preceq s_S^\ell$, we know that $\omega_a \neq \emptyset$. In all other cases, namely, when h_T does not exist or a is not \mathcal{B}_T -executable, $P(h, a)$ undefined.

Next, we prove that P is indeed a composition, that is, we show that every \mathcal{T}_T trace is realized by P . To this end, we consider any \mathcal{T}_T trace $\tau = s_T^0 \xrightarrow{a^1} s_T^1 \xrightarrow{a^2} \dots (s_T^0 = s_{T0})$ and prove the following claim first:

(†) for every $\mathcal{T}_{\mathcal{S}}$ history $h = s_S^0 \xrightarrow{a^1, k^1} \dots \xrightarrow{a^\ell, k^\ell} s_S^\ell \in \mathcal{H}_{\tau, P}$, with $0 \leq \ell < |\tau|$, it is the case that $s_T^\ell \preceq s_S^\ell$.

Since $\mathcal{H}_{\tau, P} = \bigcup_{\ell \geq 0} \mathcal{H}_{\tau, P}^\ell$, we prove (†) by induction on ℓ as follows:

- Let $\mathcal{H}_{\tau, P}^0 = \{s_{S0}\}$. Clearly, $s_{T0} \preceq s_{S0}$ and (†) holds trivially.
- Take $h^{\ell+1} = s_S^0 \xrightarrow{a^1, k^1} \dots \xrightarrow{a^\ell, k^\ell} s_S^\ell \xrightarrow{a^{\ell+1}, k^{\ell+1}} s_S^{\ell+1} \in \mathcal{H}_{\tau, P}^{\ell+1}$, where $s_S^0 = s_{S0}$. By the definition of $\mathcal{H}_{\tau, P}^{\ell+1}$, $s_S^\ell \xrightarrow{a^{\ell+1}, k^{\ell+1}} s_S^{\ell+1}$ in $\mathcal{T}_{\mathcal{S}}$, $\text{env}(s_T^{\ell+1}) = \text{env}(s_S^{\ell+1})$ and $P(h^\ell, a^{\ell+1}) = k^{\ell+1}$. By the induction hypothesis, we know that $s_T^\ell \preceq s_S^\ell$. Then, by the way P was defined above, it follows that $s_T^{\ell+1} \preceq s_S^{\ell+1}$.

Next, take any $h \in \mathcal{H}_{\tau, P}$ such that $|h| < |\tau|$. Because of the way each $\mathcal{H}_{\tau, P}^i$ is constructed, h ought to be of the form $h = s_S^0 \xrightarrow{a^1, k^1} \dots \xrightarrow{a^\ell, k^\ell} s_S^\ell$, that is, h has to match all actions in τ . From (†) above, we have that $s_T^\ell \preceq s_S^\ell$. Then, by definition of ND-simulation, the fact that $a^{\ell+1}$ is \mathcal{B}_T -executable in s_T^ℓ , and the way P is defined above, there exists a transition $s_S^\ell \xrightarrow{a^{\ell+1}, k} s_S^{\ell+1}$, where $k = P(h, a^{\ell+1})$ and $k \in \{1, \dots, n\}$. In addition, if τ is finite, then for every $h \in \mathcal{H}_{\tau, P}^{|\tau|}$ we have, due to (†) above, that $s_T^{|\tau|} \preceq \text{last}(h)$, which in turns implies that if $s_T^{|\tau|} \in Q_T$ (i.e., \mathcal{T}_T is final in enacted state $s_T^{|\tau|}$), then $\text{last}(h) \in Q_{\mathcal{S}}$. Then, P realizes τ and P is a composition.

(ONLY-IF PART). Let P be a controller for \mathcal{S} that is a composition of \mathcal{B}_T on \mathcal{E} . From P , we build a relation $R \subseteq S_T \times S_{\mathcal{S}}$ that is an ND-simulation such that $\langle s_{T0}, s_{S0} \rangle \in R$. The definition of R is as follows: $\langle s_T, s_{\mathcal{S}} \rangle \in R$ if and only if there exists a \mathcal{T}_T trace $\tau = s_T^0 \xrightarrow{a^1} s_T^1 \xrightarrow{a^2} \dots$ and an (induced) $\mathcal{T}_{\mathcal{S}}$ history $h \in \mathcal{H}_{\tau, P}$ such that $s_T = s_T^{|h|}$ and $s_{\mathcal{S}} = \text{last}(h)$.

Next, we show that R is an ND-simulation relation (page 114). Consider then a pair $\langle s_T, s_{\mathcal{S}} \rangle \in R$. By R 's definition, there exists a \mathcal{T}_T trace of the form $\tau = s_T^0 \xrightarrow{a^1} \dots \xrightarrow{a^\ell} s_T \dots$ and an ℓ -length $\mathcal{T}_{\mathcal{S}}$ history (induced by τ and P) $h \in \mathcal{H}_{\tau, P}^\ell$ such that $h = s_S^0 \xrightarrow{a^1, k^1} \dots \xrightarrow{a^\ell, k^\ell} s_{\mathcal{S}}$.

First, due to the way set $\mathcal{H}_{\tau, P}^\ell$ is constructed, $\text{env}(s_T) = \text{env}(s_{\mathcal{S}})$ holds, as only system histories matching the evolution of the environment as in trace τ are considered. Second, because P is a composition, P realizes τ as well as its $|h|$ -length trace prefix $\tau|_{|h|}$. It follows then that if $\text{last}(\tau|_{|h|}) = s_T \in Q_T$, then $s_{\mathcal{S}} \in Q_{\mathcal{S}}$.

It remains to prove that the third requirement of ND-simulation holds. To that end, consider an action $a \in \mathcal{A}$ that is \mathcal{B}_T -executable in s_T , that is, there exists $s_T \xrightarrow{a} s_T^*$ in \mathcal{B}_T . Take now trace $\tau^* = \tau|_{\ell} \xrightarrow{a} s_T^*$. Clearly, $h \in \mathcal{H}_{\tau^*, P}^\ell$, that is, h can be induced by P when realizing trace τ^* . Since P is a composition, it realizes trace τ^* and hence there exists $k_a \in \{1, \dots, n\}$ such that $P(h, a) = k_a$ and $s_{\mathcal{S}} \xrightarrow{a, k_a} s_{\mathcal{S}}^*$ in $\mathcal{T}_{\mathcal{S}}$. Next consider any transition $s_T \xrightarrow{a} s'_T$ in \mathcal{T}_T . Because the evolution of the environment is independent of that of the behaviors, there must exist $s_{\mathcal{S}} \xrightarrow{a, k_a} s'_{\mathcal{S}}$ with $\text{env}(s'_{\mathcal{S}}) = \text{env}(s'_T)$ and hence condition 3(a) of ND-simulation definition applies. Moreover, $\tau' = \tau|_{\ell} \xrightarrow{a} s'_T$ is a legal trace of \mathcal{T}_T and history $h \xrightarrow{a, k_a} s'_{\mathcal{S}} \in \mathcal{H}_{\tau', P}^{\ell+1}$. Hence, by definition of R above, $R(s'_T, s'_{\mathcal{S}})$ holds, that is, requirement 3(b) of the ND-simulation definition is satisfied, with $k_a = P(h, a)$ being indeed a witness of $s_T \preceq s_{\mathcal{S}}$ for action a . \square

Theorem 1 provides a straightforward method for checking the existence of a composition, namely: (i) compute the largest ND-simulation relation between \mathcal{T}_T and $\mathcal{T}_{\mathcal{S}}$, and (ii) check whether $\langle s_{T0}, s_{S0} \rangle$ is in such a relation.

As for computational complexity considerations, observe that algorithm *NDS* described above computes the largest ND-simulation relation \preceq between \mathcal{T}_T and \mathcal{T}_S in polynomial time, with respect to the size of \mathcal{T}_T and \mathcal{T}_S . Since the number of states in \mathcal{T}_S is exponential in the number of available behaviors $\mathcal{B}_1, \dots, \mathcal{B}_n$, we get that the largest ND-simulation relation \preceq can be computed in exponential time in the *number of available behaviors*. Hence, as formally stated in the next theorem, this technique is a notable improvement with respect to the ones based on reduction to PDL [30,79], which are exponential also in the *number of states* of both the behaviors and the environment.³ Considering that the composition problem is EXPTIME-hard [61], the upper bound we get is indeed tight, that is, roughly speaking, this is the best we can hope for.

Theorem 2. *Checking for the existence of compositions by computing the largest ND-simulation relation \preceq can be done in polynomial time in the number of states of the available behaviors, of the environment, and of the target behavior, and in exponential time in the number of available behaviors.*

Once the ND-simulation relation is computed, the problem of “synthesizing” a controller that is a composition arises. Next, we show how, from the largest ND-simulation relation, we can build a finite state program, i.e., a *controller generator*, that returns, at each step, the set of all available behaviors capable of performing the requested action, while guaranteeing the possibility of delegating to available services all (target-compliant) requests that can be issued in the future.

Formally, let $\mathcal{S} = \langle \mathcal{B}_1, \dots, \mathcal{B}_n, \mathcal{E} \rangle$ be a system, \mathcal{B}_T a target behavior over \mathcal{E} , and $\mathcal{T}_S = \langle \mathcal{S}_S, \mathcal{A}, \{1, \dots, n\}, s_{S0}, Q_S, \delta_S \rangle$ and $\mathcal{T}_T = \langle \mathcal{T}_T, \mathcal{A}, s_{T0}, Q_T, \delta_T \rangle$ the enacted system behavior and the enacted target behavior corresponding, respectively, to \mathcal{S} and \mathcal{B}_T . The controller generator (CG) of \mathcal{S} for \mathcal{B}_T is a tuple $CG = \langle \Sigma, \mathcal{A}, \{1, \dots, n\}, \partial, \omega \rangle$, where:

1. $\Sigma = \{ \langle s_T, s_S \rangle \in S_T \times S_S \mid s_T \preceq s_S \}$ is the set of CG states, formed by all pairs of \mathcal{T}_T and \mathcal{T}_S state belonging to the largest ND-simulation relation; given $\sigma = \langle s_T, s_S \rangle$ we denote s_T by $com_T(\sigma)$ and s_S by $com_S(\sigma)$.
2. \mathcal{A} is the finite set of shared actions.
3. $\{1, \dots, n\}$ is the finite set of available behavior indexes.
4. $\partial \subseteq \Sigma \times \mathcal{A} \times \{1, \dots, n\} \times \Sigma$ is the *transition relation*, where $\langle \sigma, a, k, \sigma' \rangle \in \partial$, or $\sigma \xrightarrow{a,k} \sigma'$ in CG , if and only if:
 - there exists a transition $com_T(\sigma) \xrightarrow{a} com_T(\sigma')$ in \mathcal{T}_T ;
 - there exists a transition $com_S(\sigma) \xrightarrow{a,k} com_S(\sigma')$ in \mathcal{T}_S ;
 - for all $\sigma'' \in S_T \times S_S$ such that $com_S(\sigma) \xrightarrow{a,k} com_S(\sigma'')$ in \mathcal{T}_S , $com_T(\sigma) \xrightarrow{a} com_T(\sigma'')$ in \mathcal{T}_T , and $env(com_T(\sigma'')) = env(com_S(\sigma''))$, it is the case that $\langle com_T(\sigma''), com_S(\sigma'') \rangle \in \Sigma$ (i.e., k is a witness of $com_T(\sigma) \preceq com_S(\sigma)$ for action a).
5. $\omega : \Sigma \times \mathcal{A} \mapsto 2^{\{1, \dots, n\}}$ is the *output function* defined as

$$\omega(\sigma, a) = \{k \mid \exists \sigma' \in \Sigma \text{ s.t. } \sigma \xrightarrow{a,k} \sigma' \text{ is in } CG\}.$$

Roughly speaking, the CG is a finite state transducer that, given an action a (compliant with the target behavior), outputs, through function ω , the set of *all* available behaviors that can perform a next, according to the largest ND-simulation relation \preceq . Observe that computing the CG from relation \preceq is easy, as it involves checking *local* conditions only. In fact, one could directly compute the CG by *enriching* relation \preceq , during computation, with information about actions, indices, and transitions.

By Theorem 1, if there exists a composition of \mathcal{B}_T , then $s_{T0} \preceq s_{S0}$ and CG does include state $\sigma_0 = \langle s_{T0}, s_{S0} \rangle$. In such a case, we can build actual controllers, called *generated controllers*, that are compositions of \mathcal{B}_T , by picking up, at each step, one available behavior among those returned by output function ω . Notice that full-observability of available behavior states is a crucial assumption here, as both ω and ∂ depend on the current states of both the environment and all system behaviors, which, due to non-determinism, cannot be known with certainty, i.e., can be *reconstructed*, by just looking at the action history. As a result, after each action execution, in order to obtain ω 's output, the new states of the system and of the environment need to be known. Of course, more complex scenarios where available behavior states are only partially observable can be considered, though this is out of the scope of this paper.

Formally, controllers that are compositions can be *generated* from the CG as follows.⁴ Firstly, in analogy with behavior and system traces, we define CG *traces* and *histories*: a trace for CG is a possibly infinite sequence $\sigma^0 \xrightarrow{a^1,k^1} \sigma^1 \xrightarrow{a^2,k^2} \dots$, such that each transition $\sigma^j \xrightarrow{a^{j+1},k^{j+1}} \sigma^{j+1}$ is in CG, for all $j \geq 0$ ⁵; consequently, a history for CG is a finite prefix of a trace. Functions *last* and $|\cdot|$ over CG histories are defined as usual. For technical convenience, given a CG trace $\tau_{CG} = \sigma^0 \xrightarrow{a^1,k^1} \sigma^1 \xrightarrow{a^2,k^2} \dots$, we define the corresponding projected system trace as the sequence $proj_S(\tau_{CG}) = com_S(\sigma^0) \xrightarrow{a^1,k^1} com_S(\sigma^1) \xrightarrow{a^2,k^2} \dots$, intuitively obtained from τ_{CG} by taking only the system component of each state. Clearly, by definition of CG, if $\sigma^0 = \langle s_{T0}, s_{S0} \rangle$ then

³ Though in light of the result in here, a better complexity analysis involving the specific PDL satisfiability procedures could be carried out.

⁴ We stress that as a composition exists if and only if $\sigma_0 = \langle s_{T0}, s_{S0} \rangle \in \Sigma$ (Theorem 1), constructing a composition makes sense only if this condition holds.

⁵ Observe that we do not require $\sigma^0 = \langle s_{T0}, s_{S0} \rangle \doteq \sigma_0$ as, in general, the CG does not include σ_0 .

$\text{proj}_S(\tau_{CG})$ is a legal \mathcal{T}_S trace. Also, from τ_{CG} we define the corresponding projected target trace $\text{proj}_T(\tau_{CG}) = \text{com}_T(\sigma^0) \xrightarrow{a^1} \text{com}_T(\sigma^1) \xrightarrow{a^2} \dots$ that can be easily proven to be a legal \mathcal{T}_T trace if $\sigma^0 = \langle s_{T0}, s_{S0} \rangle$. Similarly, we can derive from each CG history h_{CG} a projected system history and a projected target history, which are, respectively, a \mathcal{T}_T history and a \mathcal{T}_S history, if $\sigma^0 = \langle s_{T0}, s_{S0} \rangle$.

Next, let \mathcal{H}_{CG} be the set of all CG histories, and consider a selection function

$$CGP : \mathcal{H}_{CG} \times \mathcal{A} \mapsto \{1, \dots, n\}$$

such that $CGP(h_{CG}, a) \in \omega(\text{last}(h_{CG}), a)$, for all $h_{CG} \in \mathcal{H}_{CG}$ and $a \in \mathcal{A}$, if $\omega(\text{last}(h_{CG}), a)$ is non-empty, while it is left unconstrained if $\omega(\text{last}(h_{CG}), a)$ is empty.

Finally, assuming that CG includes $\sigma_0 = \langle s_{T0}, s_{S0} \rangle$, for each CG history $h_{CG} = \sigma^0 \xrightarrow{a^1, k^1} \dots \xrightarrow{a^\ell, k^\ell} \sigma^\ell$ such that $\sigma^0 = \sigma_0$, consider the corresponding projected system history:

$$\text{proj}_S(h_{CG}) = \text{com}_S(\sigma^0) \xrightarrow{a^1, k^1} \dots \xrightarrow{a^\ell, k^\ell} \text{com}_S(\sigma^\ell).$$

For a given selection function CGP , a generated controller is any function $P_{CGP} : \mathcal{H} \times \mathcal{A} \mapsto \{1, \dots, n\}$ such that for every \mathcal{T}_S history $h \in \mathcal{H}$ and action $a \in \mathcal{A}$, if $h = \text{proj}_S(h_{CG})$ for some CG history h_{CG} , then $P_{CGP}(h, a) = CGP(h_{CG}, a)$.

The following results relate CGs to compositions and show that, given a CG containing σ_0 , one gets *all and only* controllers that are compositions by considering all possible resolutions of the non-determinism of function CGP . Notably, while each specific composition may be an infinite state program, the controller generator, which in fact includes them all, is always finite.

Theorem 3. Let S , \mathcal{B}_T , \mathcal{T}_S and \mathcal{T}_T be as above, and let $CG = \langle \Sigma, \mathcal{A}, \{1, \dots, n\}, \partial, \omega \rangle$ be the controller generator of S for \mathcal{B}_T . If $\sigma_0 = \langle s_{T0}, s_{S0} \rangle \in \Sigma$, then:

1. every generated controller obtained from CG as shown above is a composition of \mathcal{B}_T on \mathcal{E} ;
2. every controller that is a composition of \mathcal{B}_T on \mathcal{E} can be obtained from CG as shown above.

Proof. To prove the first claim, we show that for every target trace $\tau \in \mathcal{H}_T$ and controller P_{CGP} defined as above, there exists a controller P , defined as in the (IF PART) of Theorem 1, such that $\mathcal{H}_{\tau, P} = \mathcal{H}_{\tau, P_{CGP}}$. Since P is proven to realize τ , by looking at the definition of *trace realization*, this is enough to prove that P_{CGP} realizes τ as well.

Let $\mathcal{H}_{\tau, P_{CGP}}^\ell \subseteq \mathcal{H}_{\tau, P_{CGP}}$ be the set of system histories $h = s_S^0 \xrightarrow{a^1, k^1} \dots \xrightarrow{a^\ell, k^\ell} s_S^\ell$ induced by τ and P_{CGP} . Also, let $\mathcal{H}_{\tau, P}^\ell \subseteq \mathcal{H}_{\tau, P}$ be the analogous set for τ and P . We prove, by induction, the existence of P (defined as in the (IF PART) of Theorem 1) such that $\mathcal{H}_{\tau, P_{CGP}}^\ell = \mathcal{H}_{\tau, P}^\ell$, for every $\ell \geq 0$. Since, for every controller C , $\mathcal{H}_{\tau, C} = \bigcup_{\ell \geq 0} \mathcal{H}_{\tau, C}^\ell$, we get that $\mathcal{H}_{\tau, P_{CGP}} = \mathcal{H}_{\tau, P}$.

For the base case ($\ell = 0$), no matter how P is defined, $\mathcal{H}_{\tau, P_{CGP}}^0 = \mathcal{H}_{\tau, P}^0 = \{s_{S0}\}$. By induction hypothesis, assume $\mathcal{H}_{\tau, P_{CGP}}^\ell = \mathcal{H}_{\tau, P}^\ell$, and consider a system history $h = s_S^0 \xrightarrow{a^1, k^1} \dots \xrightarrow{a^\ell, k^\ell} s_S^\ell \in \mathcal{H}_{\tau, P_{CGP}}^\ell$. Because h is an induced history, for $i = 1, \dots, \ell$, we have $k^i = P_{CGP}(h|_{i-1}, a^i)$, where $h|_j = s_S^0 \xrightarrow{a^1, k^1} \dots \xrightarrow{a^{j-1}, k^{j-1}} s_S^j$. In particular $k^\ell = P_{CGP}(h|_{\ell-1}, a^\ell)$ is defined, and therefore, by P_{CGP} definition, there exists a CG history $\tilde{h}_{CG} = \langle \tilde{s}_T^0, s_S^0 \rangle \xrightarrow{a^1, k^1} \dots \xrightarrow{a^{\ell-1}, k^{\ell-1}} \langle \tilde{s}_T^{\ell-1}, s_S^{\ell-1} \rangle$ such that $\text{proj}_S(\tilde{h}_{CG}) = h|_{\ell-1}$. In principle, \tilde{h}_{CG} can be any, as long as $\text{proj}_S(\tilde{h}_{CG}) = h|_{\ell-1}$. In particular, it could be unrelated to τ . But because \tilde{h}_{CG} is a history for CG, it is such that $\langle \tilde{s}_T^i, s_S^i \rangle \in \Sigma$ ($i = 0, \dots, \ell - 1$), hence $\tilde{s}_T^i \leq s_S^i$ and therefore $\text{env}(\tilde{s}_T^i) = \text{env}(s_S^i)$. In turn, h being induced by τ , $\text{env}(s_S^i) = \text{env}(s_T^i)$, and hence $\text{env}(\tilde{s}_T^i) = \text{env}(s_S^i) = \text{env}(s_T^i)$ ($i = 0, \dots, \ell - 1$). Finally, \mathcal{B}_T being deterministic and having $\tilde{s}_T^0 = s_T^0 = s_{T0}$, we get $\text{beh}(\tilde{s}_T^i) = \text{beh}(s_T^i)$. So, we conclude that $\text{proj}_T(\tilde{h}_{CG}) = \tau|_{\ell-1}$. Based on this and the fact that $\text{proj}_S(\tilde{h}_{CG}) = h|_{\ell-1}$, we also have that \tilde{h}_{CG} is unique, for fixed h .

By definition of induced history, given h , $k^\ell = P_{CGP}(h|_{\ell-1}, a^\ell) = CGP_{CGP}(\tilde{h}_{CG}, a^\ell) \in \omega(\langle s_T^{\ell-1}, s_S^{\ell-1} \rangle, a^\ell)$. So, observing the definition of CG and ω , it is easily seen that the sequence $h_{CG} = \langle s_T^0, s_S^0 \rangle \xrightarrow{a^1, k^1} \dots \xrightarrow{a^\ell, k^\ell} \langle s_T^\ell, s_S^\ell \rangle$ is a CG history, in particular, such that $\text{proj}_S(h_{CG}) = h$ and $\text{proj}_T(h_{CG}) = \tau|_\ell$.

Next, we prove that all possible extensions of h , obtained by *realizing* action $a^{\ell+1}$ in τ (if any), according to P_{CGP} , are also possible under P , and vice versa. In other words, we prove that $\mathcal{H}_{\tau, P_{CGP}}^{\ell+1} = \mathcal{H}_{\tau, P}^{\ell+1}$. Two cases are possible: either (i) $\tau = \tau|_\ell$ (i.e., τ is finite); or (ii) not. In case (i), we trivially obtain $\mathcal{H}_{\tau, P_{CGP}}^{\ell+1} = \mathcal{H}_{\tau, P}^{\ell+1} = \emptyset$. For case (ii), observe that $s_T^\ell \leq s_S^\ell$ as $\langle s_T^\ell, s_S^\ell \rangle \in \Sigma$ —and that $a^{\ell+1}$ is \mathcal{B}_T -executable in s_S^ℓ (this trivially comes from $a^{\ell+1}$ position in τ). In addition, h_{CG} is proved, above, a CG history such that $\text{proj}_S(h_{CG}) = h$. Therefore, by definition of generated controller, $P_{CGP}(h, a^{\ell+1}) = k^{\ell+1} \in \omega(\langle s_T^\ell, s_S^\ell \rangle, a^{\ell+1}) \neq \emptyset$.

On the other hand, consider the construction of P in the (IF PART) of Theorem 1. Given h , $\tau|_\ell$ matches (by construction) all actions in h , and is such that $s_T^\ell = \text{last}(\tau|_\ell) \preceq \text{last}(h) = s_S^\ell$ (as proven above). So, $P(h, a^{\ell+1}) \in \omega_{a^{\ell+1}} \neq \emptyset$. But then, observing that $\omega(\langle s_T^\ell, s_S^\ell \rangle, a^{\ell+1}) = \omega_{a^{\ell+1}}$, no matter which index P_{CGP} returns, P can choose the same index, say $k^{\ell+1}$, from $\omega_{a^{\ell+1}}$ so that $k^{\ell+1} = P_{CGP}(h, a^{\ell+1}) = P(h, a^{\ell+1})$. Clearly, given h , $a^{\ell+1}$ and $k^{\ell+1}$, every possible system history of the

form $\hat{h} = h \xrightarrow{a^{\ell+1}, k^{\ell+1}} s^{\ell+1}$ is such that $\hat{h} \in \mathcal{H}_{\tau, P}^{\ell+1}$ if and only if $\hat{h} \in \mathcal{H}_{\tau, P_{CGP}}^{\ell+1}$. Since h is arbitrarily chosen, we ultimately get $\mathcal{H}_{\tau, P}^{\ell+1} = \mathcal{H}_{\tau, P_{CGP}}^{\ell+1}$.

We prove the second part by showing that for all \mathcal{T}_T traces, all decisions made by P along an arbitrary history induced by τ and P are compliant with the definition of generated controller.

Let $\tau = s_T^0 \xrightarrow{a^1} s_T^1 \xrightarrow{a^2} \dots$ be a \mathcal{T}_T trace, and $h = s_S^0 \xrightarrow{a^1, k^1} \dots \xrightarrow{a^\ell, k^\ell} s_S^\ell \in \mathcal{H}_{\tau, P}$ a generic history induced by τ and P . Since P is a composition, by (ONLY-IF PART) of Theorem 1, we get that $k^i = P(h|_i, a^{i+1})$ is a witness of $s_T^i \preceq s_S^i$ for a^{i+1} , for $i = 0, \dots, \ell - 1$. Then, $h_{CG} = \langle s_T^0, s_S^0 \rangle \xrightarrow{a^1, k^1} \dots \xrightarrow{a^\ell, k^\ell} \langle s_T^\ell, s_S^\ell \rangle$ is a CG-history. Indeed, by definition of ω , for every a that is \mathcal{B}_T -executable in s_T , $\omega(s_T, s_S, a)$ contains all (and only) the witnesses of $s_T \preceq s_S$ for a . So, this will be true, in particular, for $\omega(s_T^i, s_S^i, a^{i+1})$.

Since every prefix of a history is a history itself, and ℓ being arbitrary, the argument above proves that for every prefix of h , say $h|_j$ ($j = 0, \dots, \ell - 1$), there exists an h_{CG} prefix $h_{CG}|_j$, which is a CG-history, such that $\text{proj}_S(h_{CG}|_j) = h|_j$. But then, $P_{CGP}(h|_j, a^{j+1}) = CGP(h_{CG}|_j) \in \omega(s_T^j, s_S^j, a^{j+1})$. As $k^j \in \omega(s_T^j, s_S^j, a^{j+1})$, we get that P_{CGP} can behave in the same way as P , along h , by properly picking, at every step, an element from the set returned by ω . Since ℓ was arbitrarily chosen, this result extends to all histories $h \in \mathcal{H}_{\tau, P}$. \square

We close this section by observing that compositions can be generated *just-in-time*, based on both the CG and observability of behavior and environment states. Intuitively, the CG is analogous to a sort of “meta-plan” or a stateful non-deterministic “complete universal plan”, which keeps all the existing plans at its disposal and selects the one to follow for next action, possibly with contingent decisions.⁶

Example 5. The CG can decide how to delegate actions, as requests from target arm \mathcal{B}_T come in. For instance, if a *clean* action is requested after a block has been prepared, the CG knows it ought to delegate such a request to arm \mathcal{B}_A , so as to stay within the ND-simulation relation. While physically possible, delegating *clean* to arm \mathcal{B}_B would bring the enacted system into state $\langle (a_1, b_1, c_1), e_3 \rangle$ which is known not to be in ND-simulation with the (enacted) target.

4. On behavior failures

In discussing the behavior composition problem, we have, so far, assumed implicitly that all (available) component modules are fully reliable, i.e., that they are always available, and behave “correctly”, relative to their specification. However, there are many situations and domains in which full reliability of components might not be an adequate assumption. For example, in multi-agent complex and highly dynamic domains, one can rely neither on total availability nor on reliability of the existing modules, which may stop being available due to a variety of reasons, e.g.: devices may break down, agents may decide to stop cooperating, communication with agents may drop, exogenous events may change the state of the environment, and many others; also, behaviors may possibly re-appear into the system at some later stage, thus creating new “composition opportunities” for the controller.

Generally speaking, behavior and environment specifications can be seen as contracts, and failures, such as those described above, can be interpreted as “breaches” of such contracts. In this section, we identify some classes of failures and propose respective procedures to “repair” the controller under execution when the failure occurred. Specifically, we identify five core ways of breaking contracts⁷:

- (a) A behavior *temporarily freezes*, that is, it stops responding and remains still, then eventually resumes in the same state it was in. As a result, while frozen, the controller cannot delegate actions to it.
- (b) A behavior unexpectedly and arbitrarily (i.e., without respecting its transition relation) *changes its current state*. The controller can in principle keep delegating actions to it, but it must take into account the behavior’s new state.
- (c) The *environment* unexpectedly and arbitrarily (i.e., without respecting its transition relation) changes its current state. The controller has to take into account that this affects both the target and the available behaviors.
- (d) A behavior dies, that is, it becomes *permanently unavailable*. The controller has to completely stop delegating actions to it.
- (e) A behavior that was assumed dead unexpectedly *resumes operation* starting in a certain state. The controller can exploit this opportunity by delegating actions to the resumed behavior, again.

Previous composition techniques (e.g., [14,30,79]) do not address these cases, as they assume that controllers always deal with fully reliable modules. Consequently, upon any of the above failures, we are only left with the (default) option of

⁶ As stated, we defined controllers to be as general as possible. Note that since traces are unbounded in nature, it is not immediate that finite controller are enough. Indeed, the notion of simulation includes a local condition on states as well as a transition condition that captures how states evolve over time.

⁷ Obviously, we assume an infrastructure that is able to distinguish between these failures.

“re-planning” from scratch for a whole new controller, if any. What we shall prove in this section is that the simulation-based technique presented in Section 3 is *intrinsically robust*, in the sense of being able to deal with unexpected failures by suitably *refining* the solution at hand, either *on-the-fly* (for cases (a), (b), and (c)), or *parsimoniously* (for cases (d) and (e)), thus avoiding full re-planning.

4.1. Reactive adaptability

We start by showing that Theorem 3 provides us with a sound and complete technique for dealing with failure cases (a), (b) and (c), without requiring any re-planning step. As a matter of fact, once we have the controller generator, actual compositions can be generated “*just-in-time*”, as (target compliant) actions are requested. In other words, one can *delay the choice* performed by the selection function CGP until run-time, when contingent information, such as actual behavior availability, can be taken into account. This ability provides the executor with great flexibility, as, in a sense, it can “switch” compositions online, as needed. A controller generated in this manner is referred to as a *just-in-time (JIT) generated controller*, and is denoted as CGP_{JIT} . Below, we discuss the effectiveness of JIT generated controllers in cases (a), (b) and (c).

Freezing of behaviors. A JIT generated controller CGP_{JIT} fully addresses temporary behavior freezing, i.e., failure case (a). Indeed, if a behavior is temporarily frozen, the CGP_{JIT} simply stops delegating actions to it, and continues with any other possible choice.⁸ Obviously, if no other choices are possible, the CGP_{JIT} is left with no other option than waiting for the frozen behavior to come back.

State change of behaviors and environment. JIT generated controllers also address unexpected changes in the internal state of behaviors and/or of the environment, that is, failure cases (b) and (c).⁹ To understand this, let us denote by $\mathcal{T}_S(z_S)$ the variant of the enacted system behavior whose initial state is z_S instead of s_{S0} . Similarly, let us denote by $\mathcal{T}_T(z_T)$ the enacted target behavior whose initial state is z_T instead of s_{T0} . Next, suppose that the state of the enacted system behavior changes, unexpectedly, to state \hat{s}_S , due to a change of the state of a behavior (or a set of behaviors) and/or of the environment. Then, if s_T is the state of the target when the failure happened, one should recompute the composition with the system starting in \hat{s}_S and the target starting from \hat{s}_T , where \hat{s}_T is just s_T with its environment state replaced by the one in \hat{s}_S (note $\hat{s}_T = s_T$ for failures of type (b)). Observe, though, that ND-simulation relations are *independent* from the initial states of both the target and the system enacted behaviors. Therefore, the largest ND-simulation relation between $\mathcal{T}_T(\hat{s}_T)$ and $\mathcal{T}_S(\hat{s}_S)$ is, in fact, relation \preceq , that we already computed. This implies that we can still use the very same controller generator CG (and the same just-in-time generated controller CGP_{JIT} as well), with the guarantee that all compositions of the system variant for the target variant, if any, are still captured by the CG (and CGP_{JIT} too). Put it all together, we only need to check whether $\hat{s}_T \preceq \hat{s}_S$, and, if so, continue to use CGP_{JIT} (now from 0-length CG history $h_{CG}^0 = (\hat{s}_T, \hat{s}_S)$).

Example 6. Upon an unexpected change in the system, in the environment or any available behavior, the CG can react/adapt to the change immediately. For instance, referring to Fig. 4, suppose the target is in state t_3 , the environment in state e_3 , and the available behaviors B_1 , B_2 , and B_3 , are in their states a_2 , b_2 , and c_1 , respectively. That is, \mathcal{T}_T is in $\langle t_3, e_3 \rangle$, and \mathcal{T}_S is in $\langle a_2, b_2, c_1, e_3 \rangle$. Suppose that, unexpectedly, the environment happens to change to state e_2 —someone has recharged the water tank. All that is needed in this case is to check whether the new states of \mathcal{T}_T and \mathcal{T}_S , namely $\langle t_3, e_2 \rangle$ and $\langle a_2, b_2, c_1, e_2 \rangle$, respectively, are still related according to relation \preceq . Since they are, the CG continues the realization of the target from such (new) enacted states.

Computing reactive compositions on-the-fly. Observe that a JIT generated controller CGP_{JIT} can be computed *on-the-fly* by storing only the ND-simulation relation \preceq . In fact, at each point, the only information required for the next choice is $\omega(\sigma, a)$, where $\sigma \in \Sigma$ (recall $\Sigma = \preceq$) is formed by the current state of the enacted target behavior and that of the enacted system behavior. Now, in order to compute $\omega(\sigma, a)$ we only need to know \preceq .

4.2. Parsimonious refinement

As seen above, failure cases (a), (b), and (c), do not need any particular effort to be dealt with. However, when considering cases (d) and (e), things change significantly: a simple reactive approach is no longer sufficient, and more complex refinement techniques are required. Concretely, suppose that the current composition that is being executed—from an ND-simulation relation—becomes suddenly invalid, due to a disruption in the available system (e.g., a behavior becomes unavailable). While the current ND-simulation relation behind the composition is no longer sound, it may not be necessary to recompute the new ND-simulation relation (and a corresponding composition, if any) “from scratch”. As a matter of fact, we shall show here that the ND-simulation at hand can be *refined* in an intelligent manner, so as to re-use previous computation effort. Technically, using the current ND-simulation relation and the nature of the disruption, one can identify *upper*

⁸ If more information is at hand, the CGP_{JIT} may use it to choose in an informed way, though this is out of the scope of this paper.

⁹ Although hardly as meaningful as the ones above, unforeseen changes in the target state can be accounted for in a similar way.

Algorithm 2: NDSP($\mathcal{T}_T, \mathcal{T}_S, \mathcal{R}_{\text{init}}, \mathcal{R}_{\text{sure}}$).

```

1  $\mathcal{R} := \mathcal{R}_{\text{init}} \setminus \mathcal{R}_{\text{sure}}$ ;
2  $\mathcal{R} := \mathcal{R} \setminus \{(s_T, s_S) \mid (\text{env}(s_T) \neq \text{env}(s_S)) \vee (s_T \in Q_T \wedge s_S \notin Q_S)\}$ ;
3 repeat
4    $\mathcal{R} := (\mathcal{R} \setminus \mathcal{C})$ , where  $\mathcal{C}$  is the set of  $(s_T, s_S) \in \mathcal{R}$  such that there exists an action  $a \in \mathcal{A}$  such that for each  $k$  there is a transition  $s_T \xrightarrow{a} s'_T$  in  $\mathcal{T}_T$  such that either:
    (a) there is no transition  $s_S \xrightarrow{a,k} s'_S$  in  $\mathcal{T}_S$  such that  $\text{env}(s'_T) = \text{env}(s'_S)$ ; or
    (b) there exists a transition  $s_S \xrightarrow{a,k} s'_S$  in  $\mathcal{T}_S$  such that  $\text{env}(s'_T) = \text{env}(s'_S)$ 
        but  $(s'_T, s'_S) \notin \mathcal{R} \cup \mathcal{R}_{\text{sure}}$ .
5 until ( $\mathcal{C} = \emptyset$ );
6 return  $\mathcal{R} \cup \mathcal{R}_{\text{sure}}$ ;

```

and *lower* bounds for the new ND-simulation relation that needs to be computed due to the disruption. The upper bound will rule out tuples that are known *not* to be in the new ND-simulation, whereas the lower bound will provide those tuples that ought to be in such relation.

To that end, we define a new algorithm, namely Algorithm 2 (*NDSP*), that instead of computing the largest ND-simulation relation from scratch (as done by Algorithm 1), it does so by leveraging on *known* lower ($\mathcal{R}_{\text{init}}$) and upper ($\mathcal{R}_{\text{sure}}$) bounds. More specifically, the algorithm—a (generalized) parametric version of Algorithm 1—computes the largest ND-simulation relation between \mathcal{T}_T and \mathcal{T}_S that is contained in the initial relation $\mathcal{R}_{\text{init}} \subseteq S_T \times S_S$ and assuming that such resulting relation contains relation $\mathcal{R}_{\text{sure}} \subseteq S_T \times S_S$. Of course, not every upper and lower bounds are reasonable. We will present below a set of results that tells us how to use such algorithm in order to refine or adapt an existing (ND-simulation) relation at hand. As one can observe, the *NDSP* algorithm works the same way as algorithm *NDS*, except that: (i) instead of starting from $S_T \times S_S$, it takes the initial set $\mathcal{R}_{\text{init}}$ as input; and (ii) neglects all pairs contained in $\mathcal{R}_{\text{sure}}$ for removal, as they are assumed to be (*surely*) included in the ND-simulation relation that is being computed. As expected, when $\mathcal{R}_{\text{init}} = S_T \times S_S$ and $\mathcal{R}_{\text{sure}} = \emptyset$, algorithm *NDSP* behaves exactly as *NDS* does. Indeed, this is a special case of the next result, which identifies sufficient conditions on the new parameters to guarantee that the outputs of *NDSP* and *NDS* match.

Lemma 4. Consider a system $\mathcal{S} = \{\mathcal{B}_1, \dots, \mathcal{B}_n, \mathcal{E}\}$ and a target behavior \mathcal{B}_T , and let \mathcal{T}_S and \mathcal{T}_T be their respective enacted behaviors. If $\mathcal{R}_{\text{sure}} \subseteq \text{NDS}(\mathcal{T}_T, \mathcal{T}_S) \subseteq \mathcal{R}_{\text{init}}$, then $\text{NDSP}(\mathcal{T}_T, \mathcal{T}_S, \mathcal{R}_{\text{init}}, \mathcal{R}_{\text{sure}}) = \text{NDS}(\mathcal{T}_T, \mathcal{T}_S)$.

Proof. Let \mathcal{R}_1^i and \mathcal{R}_2^i be the sets representing \mathcal{R} in algorithms *NDS* and *NDSP*, respectively, after the i -th repeat-loop iteration. Similarly, define \mathcal{C}_1^i and \mathcal{C}_2^i . Moreover, assume that *NDSP* and *NDS* require n_2 and n_1 , respectively, repeat-loop iterations (clearly, $n_2 \leq n_1$).

First, let us prove, by induction on i , that $\mathcal{R}_2^i \cup \mathcal{R}_{\text{sure}} \subseteq \mathcal{R}_1^i$. It is obvious that $\mathcal{R}_2^0 \cup \mathcal{R}_{\text{sure}} \subseteq \mathcal{R}_1^0$ (observe $\mathcal{R}_{\text{init}} \subseteq S_T \times S_S$). Suppose now that $\mathcal{R}_2^r \cup \mathcal{R}_{\text{sure}} \subseteq \mathcal{R}_1^r$, with $r < n_1$. Let $\pi = (s_T, s_S) \in \mathcal{R}_2^{r+1} \cup \mathcal{R}_{\text{sure}}$, but $\pi \notin \mathcal{R}_1^{r+1}$. Since neither \mathcal{R}_1^r nor \mathcal{R}_2^r are ever expanded along iterations, it is the case that $\pi \notin \mathcal{R}_{\text{sure}}$ (otherwise $\pi \in \text{NDS}(\mathcal{T}_T, \mathcal{T}_S)$ and $\pi \in \mathcal{R}_1^{r+1}$, as $\text{NDS}(\mathcal{T}_T, \mathcal{T}_S) \subseteq \mathcal{R}_1^{r+1}$), and thus $\pi \in \mathcal{R}_2^{r+1}$, $\pi \in \mathcal{R}_2^r$, and $\pi \in \mathcal{R}_1^r$. Because $\pi \notin \mathcal{R}_1^{r+1}$, π was deleted at the r -th loop iteration of *NDS*, that is, $\pi \in \mathcal{C}_1^r$. This means that there exists an action $\hat{a} \in \mathcal{A}$ such that for each k there is a transition $s_T \xrightarrow{\hat{a}} s'_T$ in \mathcal{T}_T such that either (a) or (b) of step 3 of *NDS* holds. If case (a) holds, then also $\pi \in \mathcal{C}_2^r$ trivially holds. If case (b) applies for some k , then there exists a tuple $\pi'_k = (s'_T, s'_S)$ such that $s_S \xrightarrow{\hat{a}, k} s'_S$ in \mathcal{T}_S , but $\pi'_k \notin \mathcal{R}_1^r$. By induction hypothesis, $\pi'_k \notin \mathcal{R}_2^r \cup \mathcal{R}_{\text{sure}}$. Thus, action \hat{a} and tuple π'_k do indeed satisfy the requirement of the step 4 of *NDSP*. Hence, $\pi \in \mathcal{C}_2^r$. We conclude that if either (a) or (b) of *NDS*' step 3 hold then $\pi \in \mathcal{C}_2^r$ and, consequently, $\pi \notin \mathcal{R}_2^{r+1}$. Contradiction. Therefore, $\mathcal{R}_2^{r+1} \cup \mathcal{R}_{\text{sure}} \subseteq \mathcal{R}_1^{r+1}$ and $\text{NDSP}(\mathcal{T}_T, \mathcal{T}_S, \mathcal{R}_{\text{init}}, \mathcal{R}_{\text{sure}}) \subseteq \text{NDS}(\mathcal{T}_T, \mathcal{T}_S)$.

Next, we prove that $\text{NDS}(\mathcal{T}_T, \mathcal{T}_S) \subseteq \text{NDSP}(\mathcal{T}_T, \mathcal{T}_S, \mathcal{R}_{\text{init}}, \mathcal{R}_{\text{sure}})$. To that end, we shall prove, by induction on i , that $\text{NDS}(\mathcal{T}_T, \mathcal{T}_S) \subseteq \mathcal{R}_2^i \cup \mathcal{R}_{\text{sure}}$. Since $\text{NDS}(\mathcal{T}_T, \mathcal{T}_S) \subseteq \mathcal{R}_{\text{init}}$, $\text{NDS}(\mathcal{T}_T, \mathcal{T}_S) \subseteq \mathcal{R}_2^0 \cup \mathcal{R}_{\text{sure}}$. Next, suppose that $\text{NDS}(\mathcal{T}_T, \mathcal{T}_S) \subseteq \mathcal{R}_2^r \cup \mathcal{R}_{\text{sure}}$, for some $r < n_2$, and let $\pi = (s_T, s_S) \in \text{NDS}(\mathcal{T}_T, \mathcal{T}_S)$ but $\pi \notin \mathcal{R}_2^{r+1} \cup \mathcal{R}_{\text{sure}}$. By induction hypothesis, $\pi \in \mathcal{R}_2^r \cup \mathcal{R}_{\text{sure}}$, and π was therefore removed from \mathcal{R}_2 in the r -th iteration of the *NDSP* algorithm. This means that there exists an action $\hat{a} \in \mathcal{A}$ such that for each k there is a transition $s_T \xrightarrow{\hat{a}} s'_T$ in \mathcal{T}_S such that either (a) or (b) of the fourth step in *NDSP* holds. In particular, if case (b) applies for some k , then there exists a tuple $\pi'_k = (s'_T, s'_S)$ such that $s_S \xrightarrow{\hat{a}, k} s'_S$ in \mathcal{T}_S , but $\pi'_k \notin \mathcal{R}_2^r \cup \mathcal{R}_{\text{sure}}$. By the induction hypothesis, $\pi'_k \notin \text{NDS}(\mathcal{T}_T, \mathcal{T}_S)$ and thus $\pi'_k \notin \mathcal{R}_1^{n_1}$. However, since $\pi \in \text{NDS}(\mathcal{T}_T, \mathcal{T}_S)$, $\pi \in \mathcal{R}_1^{n_1}$. But, by using the same action \hat{a} , together with the corresponding $\pi'_k \notin \mathcal{R}_1^{n_1}$ tuples, π is a candidate to be removed from set $\mathcal{R}_1^{n_1}$, i.e., $\pi \in \mathcal{C}_1^{n_1}$. Then, algorithm *NDS* requires more than n_1 , a contradiction. Hence, $\pi \in \mathcal{R}_2^r \cup \mathcal{R}_{\text{sure}}$ and $\text{NDS}(\mathcal{T}_T, \mathcal{T}_S) \subseteq \text{NDSP}(\mathcal{T}_T, \mathcal{T}_S, \mathcal{R}_{\text{init}}, \mathcal{R}_{\text{sure}})$ follows. \square

Next, we introduce convenient notations to shrink and expand systems and ND-simulation relations. Given a system $\mathcal{S} = \{\mathcal{B}_1, \dots, \mathcal{B}_n, \mathcal{E}\}$ and a set of behavior indexes $W \subseteq \{1, \dots, n\}$, we denote by $\mathcal{S}(W)$ the system derived from \mathcal{S} by

keeping only the behaviors \mathcal{B}_i such that $i \in W$ (note $\mathcal{S} = \mathcal{S}(\{1, \dots, n\})$). Also, for an enacted target behavior \mathcal{T}_T over \mathcal{E} , we denote by \preceq_W the largest ND-simulation relation of \mathcal{T}_T by $\mathcal{T}_{\mathcal{S}(W)}$. Finally, given a further set of indexes $U \subseteq \{1, \dots, n\}$ such that $W \cap U = \emptyset$, we denote by $\preceq_W \otimes U$ the relation obtained from \preceq_W , by (trivially) putting back into the system all \mathcal{B}_i such that $i \in U$. Formally, this latter operation can be defined as follows (without loss of generality, assume $W = \{1, \dots, \ell\}$ and $U = \{\ell + 1, \dots, m\}$):

$$\begin{aligned} \preceq_W \otimes U = \{ & \langle s_T, s' \rangle \mid s' = \langle b_1, \dots, b_\ell, b_{\ell+1}, \dots, b_m, e \rangle \text{ such that } \langle s_T, \langle b_1, \dots, b_\ell, e \rangle \rangle \in \preceq_W \text{ and } b_i \text{ is a state of } \mathcal{B}_i, \\ & \text{for } i \in \{\ell + 1, \dots, m\} \} \end{aligned}$$

Intuitively, adding a set of behaviors to a system can only extend, and never reduce, the capabilities of the system. Indeed, the additional behaviors do not constrain in any way those already present, while, in general, make the system able to execute more actions. In particular, if a system can simulate a target behavior (on some environment), we expect it to have the same ability, and possibly more, after introducing additional behaviors. The next result proves this intuition, i.e., that when “putting back” a set of behaviors U into system $\mathcal{S}(W)$, by extending \preceq_W as shown above, we are guaranteed to obtain an ND-simulation relation for the (expanded) system $\mathcal{S}(W \cup U)$, though not necessarily the largest one.

Lemma 5. Given a system $\mathcal{S} = \{\mathcal{B}_1, \dots, \mathcal{B}_n, \mathcal{E}\}$, a target behavior \mathcal{B}_T and its respective enacted behavior \mathcal{T}_T over \mathcal{E} , let $W, U \subseteq \{1, \dots, n\}$ be such that $W \cap U = \emptyset$. The following hold:

- $\preceq_W \otimes U \subseteq \preceq_{W \cup U}$;
- $\preceq_W \otimes U$ is an ND-simulation relation of \mathcal{T}_T by $\mathcal{T}_{\mathcal{S}(W \cup U)}$.

Proof. Without loss of generality, consider $W = \{1, \dots, \ell\}$, and $U = \{\ell + 1, \dots, m\}$. Suppose that $\langle \langle t, e \rangle, \langle b_1, \dots, b_\ell, b_{\ell+1}, \dots, b_m, e' \rangle \rangle \in \preceq_W \otimes U$. Due to the definition of operation \otimes , it is the case that $\langle t, e \rangle \preceq_W \langle b_1, \dots, b_\ell, e' \rangle$. This means that $e = e'$ and that for each $a \in \mathcal{A}$, there exists index $k_a \in W$ satisfying the requirements of the ND-simulation relation definition for system $\mathcal{S}(W)$. Then, $\langle t, e \rangle \preceq_{W \cup U} \langle b_1, \dots, b_\ell, b_{\ell+1}, \dots, b_m, e' \rangle$. Indeed, $e = e'$, and for every $a \in \mathcal{A}$, the same index k_a would also satisfy the requirements of the ND-simulation definition for system $\mathcal{S}(W \cup U)$ —the new behaviors are not used and they cannot either remove or inhibit other behaviors capabilities. This shows that $\preceq_W \otimes U$ is an ND-simulation relation of \mathcal{T}_T by $\mathcal{T}_{\mathcal{S}(W \cup U)}$ and, hence, $\preceq_W \otimes U \subseteq \preceq_{W \cup U}$, as $\preceq_{W \cup U}$ is the largest ND-simulation relation of \mathcal{T}_T by $\mathcal{T}_{\mathcal{S}(W \cup U)}$. \square

As it turns out, adding new behaviors has a minimal impact on the ND-simulation relation, that can be recomputed through simple projection operations. Unfortunately, this is not the case when behaviors become unavailable. As discussed below, this has, in general, a disruptive impact on the ND-simulation relation, which, in order to be recomputed, requires more than just *local* changes. To see this, let $F \subseteq W$ be the set of indexes of those behaviors that become permanently unavailable, and denote by $\preceq_{W|F}$ the relation obtained from \preceq_W by *projecting out*, that is dropping, the terms/arguments corresponding to (failed) behaviors \mathcal{B}_i such that $i \in F$. In general, the so-obtained relation just contains (possibly properly) the new largest ND-simulation after failure. Specifically, we have:

Lemma 6. For \mathcal{S} and \mathcal{T}_T as above, let $W, F \subseteq \{1, \dots, n\}$ be such that $F \subseteq W$. The following holds:

- $\preceq_{(W \setminus F)} \subseteq \preceq_{W|F}$;
- $\preceq_{W|F}$ may not be an ND-simulation relation of \mathcal{T}_T by $\mathcal{T}_{\mathcal{S}(W \setminus F)}$.

Proof. By Lemma 5, $\preceq_{(W \setminus F)} \otimes F \subseteq \preceq_{(W \setminus F) \cup F}$, that is, $\preceq_{(W \setminus F)} \otimes F \subseteq \preceq_W$. By projecting out F on both relations, we get $\preceq_{(W \setminus F)} \otimes F|_F \subseteq \preceq_{W|F}$. Then, since $\preceq \otimes X|_X = \preceq$ for any \preceq and X , $\preceq_{(W \setminus F)} \subseteq \preceq_{W|F}$ follows.

It is immediate to find cases where the containment is proper, and hence the second part follows. \square

Notice that even though \preceq_W is the largest ND-simulation relation when all behaviors in W are active, the projected relation $\preceq_{W|F}$ is not necessarily even an ND-simulation relation for the (contracted) system $\mathcal{S}(W \setminus F)$.

In light of these results, we next show how to deal with failure cases (d) and (e).

Permanent unavailability. When a behavior becomes permanently unavailable (cf. case (d)), one cannot wait for it to resume. Instead, one can either continue to executing the composition (controller) and just “hope for the best”, i.e., that the failed behavior will not be actually required (because, e.g., some actions occurring in the target behavior are not executed at runtime), or one can “refine” the current composition so as to continue guaranteeing the full realization of the target behavior.

Assume that, at some point, while a composition built from an ND-simulation relation is executing, a set of available behaviors become unavailable. Clearly, the current composition is no longer sound (as some required behaviors might be unavailable), the ND-simulation relation is no longer useful, and one is required to recompute a new one (and a corresponding

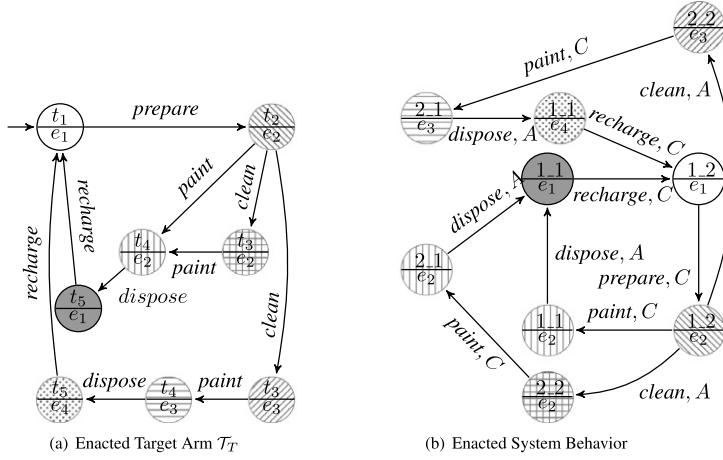


Fig. 5. An ND-simulation relation between enacted target behavior \mathcal{T}_T and enacted system behavior $\mathcal{T}_{S((1,3))}$.

composition) in order to keep executing the target behavior. Of course, the new ND-simulation relation can always be computed “from scratch”, by considering only the set of currently available behaviors. However, from the computational point of view this might not be the best solution, as it does not take advantage of what has been previously computed. In the following, we propose a different approach, based on the above results, that aims at minimizing the required computational effort by *refining*, rather than recomputing, the ND-simulation relation at hand.

Lemma 6 essentially says that, when some behaviors become unavailable, in order to compute the new ND-simulation relation, it is enough to execute the *NDSP* algorithm by instantiating $\mathcal{R}_{\text{init}}$ with the relation obtained by projecting out the failed components from the current ND-simulation relation. This yields, in general, substantially less algorithm iterations than *NDS*. Indeed, as behaviors become unavailable, the effort to obtain the new largest ND-simulation relation is *systematic* and *incremental*, in that no tuples that were previously discarded are considered again. This, along with Lemma 4 leads to the following

Theorem 7. Consider S , B_T and \mathcal{T}_T as above. Let $W \subseteq \{1, \dots, n\}$ contain the indexes of the behaviors currently working in S and let $F \subseteq W$ contain the indexes of the behaviors that, at a given point, become permanently unavailable. Then, for every relation β such that $\beta \subseteq \preceq_{(W \setminus F)}$, the following holds:

$$\preceq_{(W \setminus F)} = \text{NDSP}(\mathcal{T}_T, \mathcal{T}_{S(W \setminus F)}, \preceq_W|_F, \beta).$$

Proof. Direct consequence of Lemmas 4 and 6. \square

Example 7. Suppose that arm B_T (Fig. 1) is being successfully realized by means of controller P_1 (Fig. 3). Assume that arm B_2 breaks down in state b_3 , just after painting a block. With B_2 out, controller P_1 cannot guarantee B_T realization anymore—yet, interestingly, this can now be done by controller P_2 on the new (unexpected) sub-system. To handle such a failure case, first, behavior B_2 is projected out from the ND-simulation relation $\preceq_{\{1,2,3\}}$, thus getting $\preceq_{\{1,2,3\}|_{\{2\}}}$; then, the new largest ND-simulation relation is computed with *NDSP* starting from relation $\preceq_{\{1,2,3\}|_{\{2\}}}$, thus obtaining $\preceq_{\{1,3\}}$ —from which a new CG and a corresponding composition can be derived. The result is shown in Fig. 5, where the enacted target behavior is the same as in Fig. 4(b), reported here for convenience. Like in Example 4, matching filling patterns individuate pairs in the ND-simulation relation. Observe that tuple $\langle\langle t_3, e_3\rangle, \langle\langle a_2, b_1, c_1\rangle, e_3\rangle\rangle$ belongs to relation $\preceq_{\{1,2,3\}|_{\{2\}}}$, but is filtered out by the *NDSP* algorithm (the original tuple $\langle\langle t_3, e_3\rangle, \langle\langle a_2, b_2, c_1\rangle, e_3\rangle\rangle \in \preceq_{\{1,2,3\}}$ relied on B_2 for maintaining the ND-simulation).

Resumed behaviors. Consider now the situation where the operating behaviors are those with indexes in W , and others, supposed to be permanently unavailable, become unexpectedly available (cf. case (e)). Let U be the set of indexes of such behaviors, with $U \cap W = \emptyset$. As already observed, this never reduces the capabilities of the whole system but could enhance it with more choices, or, differently said, after behaviors in U become available again, the system can still realize *at least* the same executions as before. However, if one wants to exploit the further capabilities brought by the resumed behaviors, the new largest ND-simulation relation $\preceq_{(W \cup U)}$ must be computed. In doing so, one can leverage on the fact that $\preceq_{(W \cup U)}$ contains relation $\preceq_W \otimes U$ (cf. Lemma 5) and completely neglect, for potential filtering, tuples in $\preceq_W \otimes U$. That is, such tuples can be provided in input to the *NDSP* algorithm as the “sure set”.

Theorem 8. Consider \mathcal{S} , \mathcal{B}_T and \mathcal{T}_T as above. Let $W \subseteq \{1, \dots, n\}$ contain the indexes of the behaviors currently working in \mathcal{S} , and $U \subseteq \{1, \dots, n\}$, with $W \cap U = \emptyset$, the indexes of those that were assumed permanently unavailable but have unexpectedly resumed. Then, for every set α such that $\preceq_{(W \cup U)} \subseteq \alpha$, the following holds:

$$\preceq_{(W \cup U)} = NDSP(\mathcal{T}_T, \mathcal{T}_{\mathcal{S}(W \cup U)}, \alpha, \preceq_W \otimes U).$$

Proof. Consequence of Lemmas 4 and 5. \square

As it turns out, this requires, in general, less iterations than those required for computing the ND-simulation relation from scratch, as tuples considered by NDS are not processed by $NDSP$. Observe that even if new behaviors not appearing in $\{1, \dots, n\}$ are included in U , the thesis of Lemma 5 still holds. Therefore, if the system is enriched with new behaviors, one can use the largest ND-simulation relation previously computed, in order to save computational efforts, when computing the new ND-simulation relation.

Reusing previously computed ND-simulations. Theorems 7 and 8 essentially show that, by using algorithm $NDSP$, when a behavior resumes or becomes unavailable and a new ND-simulation relation needs to be re-computed, one can take advantage of the ND-simulation relation previously computed. In fact, such theorems can be combined so as to reuse not only the last ND-simulation relation computed, but all those computed in the past (assuming they have been stored).

To see this, let $\mathcal{W} \subseteq 2^{\{1, \dots, n\}}$, such that $\{1, \dots, n\} \in \mathcal{W}$, be a set of sets of behavior indices, and assume that the largest ND-simulation relation for each set in \mathcal{W} has been already computed and stored. For $W \notin \mathcal{W}$, in order to compute the (largest) ND-simulation relation \preceq_W , one can first define the following sets:

$$\bar{\alpha} = \bigcap_{\{W' \in \mathbb{D}_W^{\mathcal{W}}\}} \preceq_{W'}|_{(W' \setminus W)};$$

$$\bar{\beta} = \bigcup_{\{W' \in \mathbb{E}_W^{\mathcal{W}}\}} \preceq_{W'} \otimes (W \setminus W');$$

where $\mathbb{D}_W^{\mathcal{W}}$ and $\mathbb{E}_W^{\mathcal{W}}$ stand for the set of *tightest* supersets and subsets, respectively, of W in \mathcal{W} , namely:

$$\mathbb{D}_W^{\mathcal{W}} = \{W' \in \mathcal{W} \mid W \subseteq W' \wedge \forall V \in \mathcal{W}. W \subseteq V \rightarrow V \not\subseteq W'\};$$

$$\mathbb{E}_W^{\mathcal{W}} = \{W' \in \mathcal{W} \mid W' \subseteq W \wedge \forall V \in \mathcal{W}. V \subseteq W \rightarrow W' \not\subseteq V'\}.$$

Then, by applying Theorems 7 and 8, \preceq_W can be computed as follows:

$$\preceq_W = NDSP(\mathcal{T}_T, \mathcal{T}_{\mathcal{S}(W)}, \bar{\alpha}, \bar{\beta}).$$

Clearly, by using $NDSP(\mathcal{T}_T, \mathcal{T}_{\mathcal{S}(W)}, \bar{\alpha}, \bar{\beta})$ to compute \preceq_W , the computations already carried out are *maximally reused* to devise other ND-simulation relations, as $\bar{\alpha}$ and $\bar{\beta}$ are the tightest sets one can obtain starting from the ND-simulation relations for sets in \mathcal{W} . Of course, once computed \preceq_W , CGP_{JIT} can be immediately computed on-the-fly, as before.

We close this section by noting that the kind of failures considered can be seen as *core* classes of breach-of-contract, with respect to the specification. Other forms of failures are clearly conceivable [88,64,55], which assume additional information at hand—e.g., a module may announce unavailability duration and/or the state (or possible states) it will join back—and that can be exploited for failure reaction, thus opening interesting research directions. However, covering a wider range of failure cases is out of the scope of the present paper, and we limit our attention only to the classes presented above.

5. Simulation and safety games

In previous sections, we have shown that the behavior composition problem can be reduced to the problem of finding an ND-simulation relation between two transition systems that, together, describe the original problem instance. Moreover, we have discussed optimization approaches to obtain computational benefits, when computing a new ND-simulation relation in response to different type of failures. In the rest of the paper, we adopt a more pragmatic perspective, and focus on finding effective ways for actually computing an ND-simulation relation. Concretely, we will demonstrate how controller generators can be synthesized by applying model checking techniques.

We begin by laying down the theoretical bases for actually solving the behavior composition problem, and show that an ND-simulation relation can be constructed by resorting to infinite games. In particular, we argue that constructing an ND-simulation relation is equivalent to building a *winning strategy in a safety game* (cf. [5,6,69]).¹⁰ The main motivation behind the use of game structures is the availability of software tools, such as *TLV* [71], *LILY* [44], *ANZU* [45], and *Mocha* [4], which provide (i) effective procedures for strategy computation; and (ii) convenient languages for representing the problem instance in a modular and high-level manner. In fact, the next section explains in detail how to solve behavior composition problem instances using the *TLV* system.

¹⁰ Safety games are those where some condition—the invariant property—needs to always be maintained, in our case: \mathcal{T}_S is always able to “locally” (i.e., state-by-state) mimic \mathcal{T}_T .

5.1. Safety-game structures

We consider the notion of *game structure* proposed in [69], specialize it to *safety games* (see, e.g., [5]), and adapt literature results [5,6] to solve the resulting problem. Roughly speaking, a safety-game structure represents a game played by two players, *system* and *controller*,¹¹ where, at each turn, the former moves and the latter replies. Moves are subject to constraints (i.e., only some moves/replies are allowed in a given game state). Intuitively, the controller's objective is to always be able to reply to system's moves so as to satisfy a given (goal) property, while the system tries to avoid this.

Throughout the rest of the paper, we assume to deal with infinite-play (though finite state) games, possibly obtained by introducing fake loops, as customary, e.g., in LTL verification. Infinite plays are assumed for technical convenience only, so as to handle all plays—finite or infinite—in a uniform way. This assumption, however, does not limit the power of game structures (for technical details about plays, see below).

A safety-game structure (\square -GS, for short) is a tuple $G = (\mathcal{V}, \mathcal{X}, \mathcal{Y}, \Theta, \rho_s, \rho_c, \square\varphi)$, where:

- $\mathcal{V} = \{v_1, \dots, v_n\}$ is the finite set of *state variables*, which range over finite domains V_1, \dots, V_n , respectively. Set \mathcal{V} is partitioned into sets $\mathcal{X} = \{v_1, \dots, v_m\}$ (the *system variables*) and $\mathcal{Y} = \{v_{m+1}, \dots, v_n\}$ (the *controller variables*). A *valuation* of variables in \mathcal{V} is a total function $val : \mathcal{V} \longrightarrow \bigcup_{i=1}^n V_i$ such that $val(v_i) \in V_i$, for each $i \in \{1, \dots, n\}$. For convenience, we represent valuations as vectors $\vec{s} = \langle s_1, \dots, s_n \rangle \in V$, where $V = V_1 \times \dots \times V_n$ and $s_i = val(v_i)$, for each $i \in \{1, \dots, n\}$. Consequently, (sub)valuations of variables in \mathcal{X} (resp. \mathcal{Y}) are represented by vectors $\vec{x} \in X$ ($\vec{y} \in Y$), with $X = V_1 \times \dots \times V_m$ ($Y = V_{m+1} \times \dots \times V_n$). A *game state* is a valuation $\vec{s} = \langle s_1, \dots, s_n \rangle \in V$, and its sub-vectors $\vec{x} = \langle s_1, \dots, s_m \rangle \in X$ and $\vec{y} = \langle s_{m+1}, \dots, s_n \rangle \in Y$ are the corresponding *system* and *controller* states, respectively. By a slight abuse of notation, we shall also write $\vec{s} = \langle \vec{x}, \vec{y} \rangle$.
- Θ is a formula representing the initial states of the game. Technically, it is a boolean combination of expressions of the form $(v_i = s_i)$, where $v_i \in \mathcal{V}$, for some $i \in \{1, \dots, n\}$, and $s_i \in V_i$. Each of such expressions is an assignment constraint, satisfied by state $\vec{s} = \langle s_1, \dots, s_n \rangle$ if $val(v_i) = s_i$. In general, not all variables in \mathcal{V} are required to occur in Θ . Given a game state $\langle \vec{x}, \vec{y} \rangle \in V$, we write $\langle \vec{x}, \vec{y} \rangle \models \Theta$ if $\langle \vec{x}, \vec{y} \rangle$ satisfies, in the obvious way, the boolean combination of assignment constraints specified by Θ .
- $\rho_s \subseteq X \times Y \times X$ is the *system transition relation*, which relates each game state to its possible successor system states.
- $\rho_c \subseteq X \times Y \times X \times Y$ is the *controller transition relation*, relating each game state together with one its successor system states (i.e., move), to possible successor controller states.
- $\square\varphi$ is the goal formula, representing the invariant property to be guaranteed, where φ has the same form as Θ above.

The above definition is completed by enforcing the infinite-play game assumption, informally stated above, by requiring that for each game state $\langle \vec{x}, \vec{y} \rangle \in V$:

- there exists an $\vec{x}' \in X$ such that $\rho_s(\vec{x}, \vec{y}, \vec{x}')$; and
- for all \vec{x}' such that $\rho_s(\vec{x}, \vec{y}, \vec{x}')$, there exists a $\vec{y}' \in Y$ such that $\rho_c(\vec{x}, \vec{y}, \vec{x}', \vec{y}')$.

In the rest of the paper, when no ambiguity arises, we will use “game structure” or simply “game” to refer to a safety-game structure. The idea behind game structures is that, with the game in some state $\vec{s} = \langle \vec{x}, \vec{y} \rangle$, the system *moves*, by choosing \vec{x}' such that $\rho_s(\vec{x}, \vec{y}, \vec{x}')$, and the controller then *replies*, by choosing \vec{y}' such that $\rho_c(\vec{x}, \vec{y}, \vec{x}', \vec{y}')$. Each pair of system move and subsequent controller reply defines a game transition from $\vec{s} = \langle \vec{x}, \vec{y} \rangle$ to state $\vec{s}' = \langle \vec{x}', \vec{y}' \rangle$. Note that the controller is allowed to *observe* the system move before replying, as witnessed by the presence of \vec{x}' in $\rho_c(\vec{x}, \vec{y}, \vec{x}', \vec{y}')$.

With the formal notion of games at hand, let us next define the corresponding dynamics and the notion of *winning* in a game. A game state $\langle \vec{x}, \vec{y} \rangle$ is a *successor* of a state $\langle \vec{x}', \vec{y}' \rangle$ iff $\rho_s(\vec{x}', \vec{y}', \vec{x})$ and $\rho_c(\vec{x}, \vec{y}, \vec{x}', \vec{y}')$. A game play starting from state $\langle \vec{x}_0, \vec{y}_0 \rangle \in V$ is an infinite sequence of states $\eta = \langle \vec{x}_0, \vec{y}_0 \rangle \langle \vec{x}_1, \vec{y}_1 \rangle \dots$ such that for each $j \geq 0$, $\langle \vec{x}_{j+1}, \vec{y}_{j+1} \rangle$ is a successor of $\langle \vec{x}_j, \vec{y}_j \rangle$. Clearly, by the infinite-play assumption, every game always admits at least a play. Intuitively, plays capture (infinite) sequences of game states obtained by alternating system moves and controller replies. A play is said to be winning (for the controller) if it satisfies the winning condition $\square\varphi$, that is, $\langle \vec{x}_i, \vec{y}_i \rangle \models \varphi$, for all $i \geq 0$. The intuition is that the play remains within a set of *safe* states, i.e., which satisfy the invariant property.

A (controller) strategy is a partial function $f : (X \times Y) \times X^+ \mapsto Y$ such that for every (finite) sequence of game states $\lambda : \langle \vec{x}_0, \vec{y}_0 \rangle \dots \langle \vec{x}_n, \vec{y}_n \rangle$ and for every system state $\vec{x}' \in X$ such that $\rho_s(\vec{x}_n, \vec{y}_n, \vec{x}')$, it is the case that $\rho_c(\vec{x}_n, \vec{y}_n, \vec{x}'), f(\langle \vec{x}_0, \vec{y}_0 \rangle, \vec{x}_1 \dots \vec{x}_n \vec{x}')$ holds. A play $\eta = \langle \vec{x}_0, \vec{y}_0 \rangle \langle \vec{x}_1, \vec{y}_1 \rangle \dots$ is *compliant with a strategy* f if $\vec{y}_\ell = f(\langle \vec{x}_0, \vec{y}_0 \rangle, \vec{x}_1 \dots \vec{x}_\ell)$, for all $\ell > 0$, that is, intuitively, all controller replies in the play match those the strategy prescribes. A strategy f is *winning from a state* \vec{s} if all plays starting from \vec{s} and compliant with f are winning. A strategy f is winning for a game G if f is winning from all of G 's initial states. We say that a game is *winning* (for the controller) if there exists a winning strategy for it, and that a game state is *winning* if there exists a winning strategy from that state. The winning set of a game G is the set of all winning states of that game.

¹¹ To avoid confusion with our previous notation, we adopt a notation different from that of [69], in which the players are the *environment* (our system) and the *system* (our controller).

Algorithm 3: WIN—Computes a safety-game structure's winning set.

```

1  $W' := \{\langle \vec{x}, \vec{y} \rangle \in V \mid \langle \vec{x}, \vec{y} \rangle \models \varphi\}$ ;
2 repeat
3    $W := W'$ ;                                     // current candidate set
4    $W' := W \cap \pi(W)$ ;                      // compute next candidate set
5 until ( $W = W'$ );
6 return  $W$ ;

```

Intuitively, a game is winning if the controller can *control* the game evolution, through a winning strategy that affects only \mathcal{Y} variables, so as to guarantee that the winning condition φ holds along all game plays, no matter how the system moves happen to be. In order to prove that a game is winning, one thus needs to prove the existence of a winning strategy, which is clearly equivalent to showing that the set of game's initial states is a subset of the winning set.

Next, we show how one can compute the winning set of a given safety-game structure $G = \langle \mathcal{V}, \mathcal{X}, \mathcal{Y}, \Theta, \rho_s, \rho_c, \square \varphi \rangle$. The key ingredient is the following operator $\pi : 2^V \longrightarrow 2^V$ (see [5]):

$$\pi(P) \doteq \{\langle \vec{x}, \vec{y} \rangle \in V \mid \forall \vec{x}' . \rho_s(\vec{x}, \vec{y}, \vec{x}') \rightarrow \exists \vec{y}' . \rho_c(\vec{x}, \vec{y}, \vec{x}', \vec{y}') \wedge \langle \vec{x}', \vec{y}' \rangle \in P\}.$$

Intuitively, given a set of game states $P \subseteq V$, $\pi(P)$ denotes the set of P 's *controllable predecessors*, that is, the set of all game states from which the controller can force the play to reach a state in P , *no matter how* the system happens to move. Using this operator, Algorithm 3 [5] can be applied to compute the set of all G 's winning states, as proven below.

The algorithm essentially computes a fixpoint, starting from the set of all game states that satisfy the goal formula φ . After the first iteration, W' (the next “candidate” set) contains all those game states that satisfy φ , and from which the controller has a strategy to force, in one step, the game to a state that satisfies φ . The process is then iterated, by refining the current candidate set W , ruling out all those states that are not controllable predecessors of W . At the end of the n -th iteration, W contains all those game states from which the controller has a strategy to make the game traverse n states satisfying φ , independently of system moves. When a fixpoint is reached, n can be replaced by ∞ . Termination of the algorithm is evident, as no new states are ever added to W . The following theorem, which shows that the obtained set is indeed the winning set, rephrases previous results from [5] and [6] within our game framework.

Theorem 9. Let $G = \langle \mathcal{V}, \mathcal{X}, \mathcal{Y}, \Theta, \rho_s, \rho_c, \square \varphi \rangle$ be a safety-game structure as above, and let W be obtained by running Algorithm 3 on G . Given a game state $\langle \vec{x}_0, \vec{y}_0 \rangle \in V$, there exists a winning strategy from $\langle \vec{x}_0, \vec{y}_0 \rangle$ if and only if $\langle \vec{x}_0, \vec{y}_0 \rangle \in W$.

Proof. (IF PART) When the algorithm returns, it is the case that $W' = W$. Being $W' = W \cap \pi(W)$, we have that $W = W \cap \pi(W)$ and therefore $W \subseteq \pi(W)$. Hence, by definition of $\pi(W)$, the following holds:

$$\forall \langle \vec{x}, \vec{y} \rangle \in W, \quad \forall \vec{x}' \in X . \rho_s(\vec{x}, \vec{y}, \vec{x}') \rightarrow \Phi(\vec{x}, \vec{y}, \vec{x}') \neq \emptyset, \tag{1}$$

where $\Phi(\vec{x}, \vec{y}, \vec{x}') = \{\vec{y}' \mid \rho_c(\vec{x}, \vec{y}, \vec{x}', \vec{y}') \wedge \langle \vec{x}', \vec{y}' \rangle \in W\}$ represents, informally, the set of all “good” moves when the system has just played \vec{x}' from game state $\langle \vec{x}, \vec{y} \rangle$.

Using set Φ , we consider next any strategy $f(\langle \vec{x}, \vec{y} \rangle, \lambda)$ satisfying the following constraint (here $\ell \geq 1$):

$$f(\langle \vec{x}_0, \vec{y}_0 \rangle, \vec{x}_1 \cdots \vec{x}_\ell) \in \Phi(\vec{x}_{\ell-1}, \vec{y}_{\ell-1}, \vec{x}_\ell), \quad \text{whenever } \Phi(\vec{x}_{\ell-1}, \vec{y}_{\ell-1}, \vec{x}_\ell) \neq \emptyset,$$

where $\vec{y}_{\ell-1} = f(\langle \vec{x}_0, \vec{y}_0 \rangle, \vec{x}_1 \cdots \vec{x}_{\ell-1})$, when $\ell > 1$ (when $\ell = 1$, $\vec{y}_{\ell-1} = \vec{y}_0$).

Next, let us prove that strategy f is indeed a winning strategy from the initial game state. To that end, all we have to do is to show that for any game play $\eta = \langle \vec{x}_0, \vec{y}_0 \rangle \langle \vec{x}_1, \vec{y}_1 \rangle \dots$ from game state $\langle \vec{x}_0, \vec{y}_0 \rangle$ and compliant with strategy f , it is the case that $\langle \vec{x}_i, \vec{y}_i \rangle \in W$, for all $i \geq 0$. Observe that for any game state $\langle \vec{x}, \vec{y} \rangle \in W$, it is the case that $\langle \vec{x}, \vec{y} \rangle \models \varphi$. This is because the algorithm starts exactly with the game states that satisfy φ (line 1) and only removes states from the candidate set (line 4). So, let us prove that $\langle \vec{x}_i, \vec{y}_i \rangle \in W$, for all $i \geq 0$, by induction on the index i . The base case when $i = 0$ is trivial, as $\langle \vec{x}_0, \vec{y}_0 \rangle \in W$ holds by assumption.

Next, suppose that for $\langle \vec{x}_i, \vec{y}_i \rangle \in W$, for all $i \leq k$, for some $k \geq 0$. Because η is a game play, it is the case that $\rho_s(\vec{x}_k, \vec{y}_k, \vec{x}_{k+1})$. Also, by the induction hypothesis, $\langle \vec{x}_k, \vec{y}_k \rangle \in W$. Therefore, by applying Eq. (1), we have that $\Phi(\vec{x}_k, \vec{y}_k, \vec{x}_{k+1}) \neq \emptyset$. From this—together with the fact that $\vec{y}_k = f(\langle \vec{x}_0, \vec{y}_0 \rangle, \vec{x}_1 \cdots \vec{x}_k)$ when $k > 0$, as play η is compliant with f —it follows that $f(\langle \vec{x}_0, \vec{y}_0 \rangle, \vec{x}_1 \cdots \vec{x}_{k+1}) = \vec{y}_{k+1} \in \Phi(\vec{x}_k, \vec{y}_k, \vec{x}_{k+1})$, and by definition of set Φ , $\langle \vec{x}_{k+1}, \vec{y}_{k+1} \rangle \in W$ follows.

(ONLY-IF PART) Let W_i be the version of W at i -th iteration (at line 5), where $1 \leq i \leq N$, assuming the algorithm terminates in N iterations and hence it returns W_N . We show, by induction on index i , that for any game state $\langle \vec{x}, \vec{y} \rangle$, if $\langle \vec{x}, \vec{y} \rangle \notin W_i$, and hence $\langle \vec{x}, \vec{y} \rangle \notin W_N$, then the system can always force from state $\langle \vec{x}, \vec{y} \rangle$ to reach, in at most i steps, a state $\langle \vec{x}', \vec{y}' \rangle$ such that $\langle \vec{x}', \vec{y}' \rangle \not\models \varphi$.

For the base case, suppose that $\langle \vec{x}, \vec{y} \rangle \notin W_1$. Due to lines 1 and 3 of Algorithm 3, set W_1 is exactly those and only those states that satisfy φ , that is, $\langle \vec{x}, \vec{y} \rangle \not\models \varphi$, and the claim follows trivially. Now, assume the claim holds for all $i \leq k$ and consider a game state $\langle \vec{x}, \vec{y} \rangle \notin W_{k+1}$. If $\langle \vec{x}, \vec{y} \rangle \notin W_k$, then the game state was removed at some previous iteration $j \leq k$, and by the induction hypothesis, the system can force all plays to violate the goal in at most k (and hence $k+1$) steps. So,

suppose on the other hand that $\langle \vec{x}, \vec{y} \rangle \in W_k$, that is, the game state was removed at the $k+1$ iteration (in line 4). From line 4 in the algorithm, we know that $W_{k+1} = W_k \cap \pi(W_k)$. Since $\langle \vec{x}, \vec{y} \rangle \in W_k$ but $\langle \vec{x}, \vec{y} \rangle \notin W_{k+1}$, it follows that $\langle \vec{x}, \vec{y} \rangle \notin \pi(W_k)$. By definition of π , there the system has a move $\vec{x}' \in X$, with $\rho_s(\vec{x}, \vec{y}, \vec{x}')$, such that for all controller replies $\vec{y}' \in Y$ with $\rho_c(\vec{x}, \vec{y}, \vec{x}', \vec{y}')$, it is the case that $\langle \vec{x}', \vec{y}' \rangle \notin W_k$. By the induction hypothesis, the system can always force from game state $\langle \vec{x}', \vec{y}' \rangle$ to reach, in at most k steps, a state that violates φ . Thus, by playing \vec{x}' from the initial state $\langle \vec{x}, \vec{y} \rangle$, the system is always able to force violating φ in at most $k+1$ steps.

Now, suppose that there exists a winning strategy f from state $\langle \vec{x}_0, \vec{y}_0 \rangle$, but on the contrary, that $\langle \vec{x}_0, \vec{y}_0 \rangle \notin W$, or what is the same, that $\langle \vec{x}_0, \vec{y}_0 \rangle \notin W_N$. By our reasoning above, the system can always force the game to violate φ in at most N steps. This implies that there exists a game play $\eta = \langle \vec{x}_0, \vec{y}_0 \rangle \langle \vec{x}_1, \vec{y}_1 \rangle \dots$ (i.e., starting from $\langle \vec{x}_0, \vec{y}_0 \rangle$) and compliant with f such that for some $i < N$, $\langle \vec{x}_i, \vec{y}_i \rangle \not\models \varphi$ applies. Hence, f would not be a winning strategy from $\langle \vec{x}_0, \vec{y}_0 \rangle$, a contradiction is reached, and it follows then that $\langle \vec{x}_0, \vec{y}_0 \rangle \in W$ must apply. \square

Importantly, once the winning set is computed, it can be used to define a winning strategy [5,6]. To see this, assume that $\eta = \langle \vec{x}_0, \vec{y}_0 \rangle \dots \langle \vec{x}_n, \vec{y}_n \rangle$ is the prefix of a play executed up to some point. For each next system move $\vec{x}' \in X$ (such that $\rho_s(\vec{x}_n, \vec{y}_n, \vec{x}')$), one can define $f(\langle \vec{x}_0, \vec{y}_0 \rangle, \vec{x}_1 \dots \vec{x}_n \vec{x}') = \vec{y}'$, by taking any reply \vec{y}' such that $\langle \vec{x}', \vec{y}' \rangle \in W$ (and $\rho_c(\vec{x}_n, \vec{y}_n, \vec{x}', \vec{y}')$). Indeed, such a condition guarantees that the controller has a winning strategy from $\langle \vec{x}', \vec{y}' \rangle$, informally meaning that it can force the (future extension of the) play to maintain φ .

5.2. From composition to safety games

Next, we show how the behavior composition problem can be reduced in practice to the problem of *synthesizing a winning strategy in a safety-game structure*. In order to do so, we need to identify which place each component of a composition problem—target behavior, available behaviors, environment, and composition controller—occupies in the game representation, that is, players controller and system need to be defined for the particular setting. Generally speaking, when composing behaviors, a controller can be seen as a strategy, i.e., a function of system histories that returns decisions, so, from this perspective, it seems very natural to represent the composition as the (synthesized strategy for) controller player, and all other components combined together as the system player.

Let $\mathcal{S} = \langle \mathcal{B}_1, \dots, \mathcal{B}_n, \mathcal{E} \rangle$ be a system and \mathcal{B}_T a target behavior over \mathcal{E} , where $\mathcal{B}_i = \langle B_i, b_{i0}, G_i, F_i, Q_i \rangle$, for $i = 1, \dots, n, T$, and $\mathcal{E} = \langle \mathcal{A}, E, e_0, \rho \rangle$. We derive a safety-game structure $G_{(\mathcal{S}, \mathcal{B}_T)} = \langle \mathcal{V}, \mathcal{X}, \mathcal{Y}, \Theta, \rho_s, \rho_c, \Box \varphi \rangle$ that captures the relationship between the target behavior and the system, as follows:

1. $\mathcal{V} = \{b_1, \dots, b_n, e, b_T, a, \text{ind}\}$, where:
 - b_i ranges over B_i , for each $i \in \{1, \dots, n, T\}$;
 - e ranges over E ;
 - a ranges over $\mathcal{A} \cup \{\#\}$;
 - ind ranges over $\{1, \dots, n\} \cup \{\#\}$.

Here, $V = B_1 \times \dots \times B_n \times E \times B_T \times (\mathcal{A} \cup \{\#\}) \times \{1, \dots, n, \#\}$ is the set of all possible valuations.

2. $\mathcal{X} = \{b_1, \dots, b_n, e, b_T, a\}$ is the set of player system variables, and $X = B_1 \times \dots \times B_n \times E \times B_T \times (\mathcal{A} \cup \{\#\})$ represents the set of all possible valuations.

3. $\mathcal{Y} = \{\text{ind}\}$ is the (singleton) set of player controller variables, and $Y = \{1, \dots, n, \#\}$ represents the set of all possible valuations.

4. $\Theta = (\text{ind} = \#) \wedge (a = \#) \wedge \bigwedge_{i \in \{1, \dots, n, T\}} b_i = b_{i0} \wedge e = e_0$;

5. $\rho_s \subseteq X \times Y \times X$ is such that $\langle \langle b_1, \dots, b_n, e, b_T, a \rangle, \text{ind}, \langle b'_1, \dots, b'_n, e', b'_T, a' \rangle \rangle \in \rho_s$ iff $a' \in \{\#\} \cup \{\hat{a} \mid e' \xrightarrow{\hat{a}} e'' \text{ in } \mathcal{E}, b'_T \xrightarrow{g'_T, \hat{a}} b''_T \text{ in } \mathcal{B}_T, g'_T(e') = \top\}$ and one of the following three cases applies:

- (a) $\text{ind} = \#$ and $b'_i = b_{i0}$, for each $i \in \{1, \dots, n, T\}$, and $e' = e_0$;
- (b) $\text{ind} \neq \#$ and

i. there exists a transition $b_T \xrightarrow{g_T, a} b'_T$ in \mathcal{B}_T such that $g_T(e) = \top$;

ii. there exists a transition $b_{\text{ind}} \xrightarrow{g_{\text{ind}}, a} b'_{\text{ind}}$ in \mathcal{B}_{ind} such that $g_{\text{ind}}(e) = \top$;

iii. $b_i = b'_i$, for all $i \in \{1, \dots, n\} \setminus \{\text{ind}\}$;

iv. there exists a transition $e \xrightarrow{a} e'$ in \mathcal{E} ; or

- (c) $\text{ind} \neq \#, e' = e$ and $b'_i = b_i$, for each $i \in \{1, \dots, n, T\}$, and at least one of the following conditions applies:

i. there is no transition $b_T \xrightarrow{g_T, a} b''_T$ in \mathcal{B}_T such that $g_T(e) = \top$;

ii. there is no transition $b_{\text{ind}} \xrightarrow{g_{\text{ind}}, a} b'_{\text{ind}}$ in \mathcal{B}_{ind} such that $g_{\text{ind}}(e) = \top$; or

iii. there is no transition $e \xrightarrow{a} e''$ in \mathcal{E} .

6. $\langle \langle b_1, \dots, b_n, e, b_T, a \rangle, \text{ind}, \langle b'_1, \dots, b'_n, e', b'_T, a' \rangle, \text{ind}' \rangle \in \rho_c$ iff $\text{ind}' \neq \#$.

7. Formula φ is defined depending on current system, target, and environment state, current requested action and current behavior selection¹²:

$$\varphi(b_1, \dots, b_n, e, b_T, a, ind) \doteq \left(validReq \rightarrow \bigwedge_{i=1}^n \neg fail_i \right) \wedge \left(final_T \rightarrow \bigwedge_{i=1}^n final_i \right),$$

where

- $validReq \doteq \bigvee_{\langle b_T, g_T, a, b'_T \rangle \in Q_T} g_T(e) = \top$;
- $fail_i \doteq ind = i \wedge \bigwedge_{\langle b_i, g_i, a, b'_i \rangle \in Q_i} g_i(e) = \perp$, for each $i \in \{1, \dots, n\}$;
- $final_i \doteq \bigvee_{b \in F_i} (b_i = b)$, for each $i \in \{1, \dots, n, T\}$.

Intuitively, the system player represents all possible evolutions of \mathcal{S} generated by legal executions of \mathcal{B}_T , which are indeed the only evolutions relevant to our problem. Each complete valuation of variables in \mathcal{V} captures the current state of the system (variables b_1, \dots, b_n , and e), that of the target behavior (variable b_T), the action to be performed next (variable a), and the available behavior selected to perform the action (variable ind). For technical convenience, a special value \sharp is used for both the action request and the delegation, to represent a request for “no action” ($a = \sharp$) and the initial distinguished states of the game ($ind = \sharp$).

As for the evolution of the game, the player system’s transition relation ρ_s accounts for the synchronous evolution of the system and the target behavior. Condition 5(a) states that initial game states—those where $ind = \sharp$ —evolve to states encoding \mathcal{S} ’s and \mathcal{B}_T ’s initial states. Condition 5(b) encodes the evolution of system \mathcal{S} when the controller has performed a valid action delegation. Basically, the new state of player system encodes the correct evolution of the target (condition 5(b)i), the selected available behavior (condition 5(b)ii), the non-selected behaviors (condition 5(b)iii), and the environment (condition 5(b)iv). Condition 5(c), on the other hand, accounts for the cases in which there is no valid behavior delegation possible, either because the current action being requested is not target-compatible (condition 5(c)i), cannot be handled by any available behavior (condition 5(c)ii), or is not allowed in the environment (condition 5(c)iii). In these cases, all behaviors and the environment are forced to stay still. Note that condition 5(c) accounts for the case of an “empty” action request, that is, when $a = \sharp$. Finally, the next requested action a' can either be \sharp —denoting no request—or one that conforms with the target behavior logic. Observe that in a certain game state, transition function ρ_s may allow several different system player’s moves, thus reflecting the non-determinism coming from the available behaviors, the environment, as well as from target action requests.

The rules for controller player’s moves are simpler, as such player is allowed to arbitrarily assign any available behavior index in any of its moves (condition 6).

To fully comply with our definition of safety-game structures given in Section 5.1, we need to show that $G_{\langle \mathcal{S}, \mathcal{B}_T \rangle}$ satisfies the infinite-play assumption. For legibility, from now on, when $\vec{x}_i = \langle b_{1i}, \dots, b_{ni}, e_i, b_{Ti}, a_i \rangle$ is a system player state in $G_{\langle \mathcal{S}, \mathcal{B}_T \rangle}$, we will use $com_T(\vec{x}_i) = \langle b_{Ti}, e_i \rangle$ and $com_S(\vec{x}_i) = \langle b_{1i}, \dots, b_{ni}, e_i \rangle$ to project the enacted target and the enacted system states encoded in \vec{x}_i , respectively, and $a(\vec{x}_i) = a_i$ to project the action request encoded in \vec{x}_i . A game state is of the form $\langle \vec{x}, y \rangle$.

Lemma 10. Let $G_{\langle \mathcal{S}, \mathcal{B}_T \rangle}$ be the safety-game structure derived for a behavior composition problem, as above. Then, for each game state $\langle \vec{x}, y \rangle$, there exists \vec{x}' such that $\rho_s(\vec{x}, y, \vec{x}')$, and for each such \vec{x}' there exists y' such that $\rho_c(\vec{x}, y, \vec{x}', y')$.

Proof. If cases 5(a) and 5(b) do not account for any system player’s move, then case 5(c) will apply and $\rho_s(\vec{x}, y, \vec{x}')$ will hold with \vec{x}' matching \vec{x} except, possibly, for $a(\vec{x}')$. Moreover, for every \vec{x}, y and \vec{x}' , $\rho_c(\vec{x}, y, \vec{x}', y')$ holds, for any $y' \in \{1, \dots, n\}$. \square

Once proven that $G_{\langle \mathcal{S}, \mathcal{B}_T \rangle}$ is a legal safety-game structure, we show a useful property of (certain) successor game states. In words, the following lemma says that a successor game state captures a legal evolution of the enacted target behavior \mathcal{T}_T and the enacted system \mathcal{T}_S . In addition, provided the successor game state encodes an actual action request, such request conforms with the enacted target behavior.

Lemma 11. Let $G_{\langle \mathcal{S}, \mathcal{B}_T \rangle}$ be the safety-game structure derived for a behavior composition problem, as above. Let $\langle \vec{x}, y \rangle$ be a (non-initial) game state of $G_{\langle \mathcal{S}, \mathcal{B}_T \rangle}$ such that there exist transitions $com_S(\vec{x}) \xrightarrow{a(\vec{x}), y} s_S$ in \mathcal{T}_S and $com_T(\vec{x}) \xrightarrow{a(\vec{x})} s_T$ in \mathcal{T}_T , for some $s_S \in S_S$ and $s_T \in S_T$. Then, $\langle \vec{x}', y' \rangle$ is a successor state of $\langle \vec{x}, y \rangle$ iff

- $y' \neq \sharp$;
- $com_T(\vec{x}) \xrightarrow{a(\vec{x})} com_T(\vec{x}')$ in \mathcal{T}_T (and, since \mathcal{B}_T is deterministic, $com_T(\vec{x}') = s_T$);
- $com_S(\vec{x}) \xrightarrow{a(\vec{x}), y} com_S(\vec{x}')$ in \mathcal{T}_S ; and

¹² We assume an empty set of conjuncts is equal to \perp .

- if $a(\vec{x}') \neq \sharp$, then there exists $s'_T \in S_T$ such that $\text{com}_T(\vec{x}') \xrightarrow{a(\vec{x}')} s'_T$ in \mathcal{T}_T .

Proof. All three claims follow directly from $G_{(\mathcal{S}, \mathcal{B}_T)}$'s ρ_s definition (see condition 5). Observe that since the system and target both have transitions, conditions 5(a) and 5(c) may not apply. The first claim follows from conditions 5(b)i and 5(b)iv. The second one is a consequence of conditions 5(b)ii, 5(b)iii and 5(b)iv. Finally, the third claim follows from the constraint imposed on $a(\vec{x}')$. \square

Finally, consider the goal formula φ . As for the first disjunct, it is trivially satisfied by the initial state only. Concerning the second one, it is better understood by looking at subformulae fail_i and final_i . The former holds if behavior \mathcal{B}_i is selected (i.e., $\text{ind} = i$), but cannot execute the requested action a , that is, each transition outgoing from its current state b_i for action a has its guard not satisfied by the current environment state e . The latter holds if the target behavior is in a final state, but not all available behaviors are. The target fails (fail_T) if it requests an action incompatible with its specification. Essentially, φ requires that the controller player makes an adequate decisions: it never selects a behavior that may not be able to execute the current requested action.

Once the game structure is built, the problem we deal with is that of synthesizing a (winning) strategy for the controller player that guarantees φ to hold along all possible plays starting from the initial state. We shall demonstrate next that this corresponds to synthesizing a composition. More specifically, in Theorem 14, we will show that by computing $G_{(\mathcal{S}, \mathcal{B}_T)}$'s winning set, one is able to construct the controller generator.

We start by exploring the relationship between $G_{(\mathcal{S}, \mathcal{B}_T)}$'s maximal winning set and the largest ND-simulation relation.

Theorem 12. Let $\mathcal{S} = \langle \mathcal{B}_1, \dots, \mathcal{B}_n, \mathcal{E} \rangle$ be a system and \mathcal{B}_T a target behavior over \mathcal{E} . Let $G_{(\mathcal{S}, \mathcal{B}_T)} = \langle \mathcal{V}, \mathcal{X}, \mathcal{Y}, \Theta, \rho_s, \rho_c, \Box \varphi \rangle$ be a \Box -GS derived as above from \mathcal{S} and \mathcal{B}_T , and let $W \subseteq V$ be the maximal set of controller winning states for $G_{(\mathcal{S}, \mathcal{B}_T)}$. Then, for all $b_i \in B_i$, with $i \in \{1, \dots, n\}$, $e \in E$ and $a \in \mathcal{A} \cup \{\sharp\}$:

$$\langle \langle b_1, \dots, b_n, e, b_T, a \rangle, \text{ind} \rangle \in W, \text{ for some } \text{ind} \in \{1, \dots, n\} \quad \text{if and only if} \quad \langle b_T, e \rangle \preceq \langle b_1, \dots, b_n, e \rangle.$$

Proof. (ONLY-IF PART) Assume that $\langle \vec{x}_0, y_0 \rangle = \langle \langle b_1, \dots, b_n, e, b_T, a \rangle, \text{ind} \rangle \in W$, for some $\text{ind} \in \{1, \dots, n\}$. Hence, there exists a winning strategy f from $\langle \vec{x}_0, y_0 \rangle$. Using such a strategy, we define a relation $R \subseteq S_T \times S_S$ as follows:

$\langle s_T, s_S \rangle \in R \quad \text{iff} \quad \text{there exists a game play } \eta = \langle \vec{x}_0, y_0 \rangle \langle \vec{x}_1, y_1 \rangle \dots \text{ compliant with } f \text{ such that}$

$$\text{com}_T(\vec{x}_\ell) = s_T \text{ and } \text{com}_S(\vec{x}_\ell) = s_S, \text{ for some } \ell \geq 1.$$

Clearly, $\eta = \langle \vec{x}_0, y_0 \rangle \langle \vec{x}, f(\langle \vec{x}_0, y_0 \rangle, \vec{x}) \rangle \langle \vec{x}, f(\langle \vec{x}_0, y_0 \rangle, \vec{x}\vec{x}) \rangle \dots$ where $\vec{x} = \langle b_1, \dots, b_n, e, b_T, \sharp \rangle$ is an f -compliant play. Since, $\text{com}_T(\vec{x}) = \text{com}_T(\vec{x}_0) = \langle b_T, e \rangle$ and $\text{com}_S(\vec{x}) = \text{com}_S(\vec{x}_0) = \langle b_1, \dots, b_n, e \rangle$, we get that $\langle \langle b_T, e \rangle, \langle b_1, \dots, b_n, e \rangle \rangle \in R$.

So, let us prove that R is indeed an ND-simulation of \mathcal{T}_T by \mathcal{T}_S , that is, we are to prove the three requirements of ND-simulations (see page 114). To that end, assume $\langle s_T, s_S \rangle \in R$. By definition of R , $\text{env}(s_T) = \text{env}(s_S)$ holds, so requirement 1 holds.

Since $\langle s_T, s_S \rangle \in R$, there exists a game play $\eta = \langle \vec{x}_0, y_0 \rangle \langle \vec{x}_1, y_1 \rangle \dots$ compliant with f such that $\text{com}_T(\vec{x}_k) = s_T$ and $\text{com}_S(\vec{x}_k) = s_S$, for some $k \geq 1$. Because f is a winning strategy, $\langle \vec{x}_k, y_k \rangle \models \varphi$. Hence, $\langle \vec{x}_k, y_k \rangle \models (\text{final}_T \rightarrow \bigwedge_{i=1}^n \text{final}_i)$, which yields requirement 2: if the target is in a final state in \vec{x}_k , so are all available behaviors.

Finally, for the third requirement of ND-simulations, consider a transitions $s_T \xrightarrow{a'} s'_T$ in \mathcal{T}_T . First, from condition 5(b) in $G_{(\mathcal{S}, \mathcal{B}_T)}$'s definition, it follows that there exists an f -compliant game play $\eta' = \langle \vec{x}'_0, y'_0 \rangle \langle \vec{x}'_1, y'_1 \rangle \dots$ such that $\vec{x}'_i = \vec{x}_i$ and $y'_i = y_i$, for all $i \in \{0, \dots, k-1\}$, and $\text{com}_T(\vec{x}_k) = \text{com}_T(\vec{x}'_k) = s_T$ and $\text{com}_S(\vec{x}_k) = \text{com}_S(\vec{x}'_k) = s_S$ —play η' is exactly like η up to game state $\langle \vec{x}_k, y_k \rangle$, except that \vec{x}'_k may (possibly) encode a different requested action. Due to the rules of ρ_s , either $a(\vec{x}'_k) = \sharp$ or $a(\vec{x}'_k)$ is a legal target transition in $\text{com}_T(\vec{x}'_k)$. In the former case, the third ND-simulation constraint follows trivially. So, suppose that $a(\vec{x}'_k) = a' \in \mathcal{A}$ and that $s_T \xrightarrow{a'} s'_T$ in \mathcal{T}_T .

Due to conditions 5(b)iv and 5(b)i in $G_{(\mathcal{S}, \mathcal{B}_T)}$'s definition, we can assume that η' is such that $\text{com}_T(\vec{x}_{k+1}) = s'_T$ —there is one such η' . Since $a(\vec{x}'_k)$ is a valid target request (and hence, $\langle \vec{x}'_k, y'_k \rangle \models \text{validReq}$), f is winning, and η' is compliant

with f , $\langle \vec{x}'_k, y'_k \rangle \models \neg \text{fail}_{y'_k}$. So, from conditions 7, 5(b)ii, 5(b)iii and 5(b)iv in $G_{(\mathcal{S}, \mathcal{B}_T)}$'s definition, $\text{com}_S(\vec{x}'_k) \xrightarrow{a(\vec{x}'_k), y'_k} \text{com}_S(\vec{x}'_{k+1})$ follows, and requirement 3(a) of ND-simulations applies (again, it is trivially true that $\text{env}(\text{com}_S(\vec{x}_{k+1})) = \text{env}(\text{com}_T(\vec{x}_{k+1}))$).

Finally, consider any $s_S \xrightarrow{a'} s'_S$ in \mathcal{T}_S with $\text{env}(s'_S) = \text{env}(s'_T)$. Again, since every possible evolution of the enacted system is accounted by some successor game states (Lemma 11), we can assume that η' is such that $\text{com}_S(\vec{x}'_{k+1}) = s'_S$. Thus, by R 's definition (see any such η' is still compliant with f), it follows that $R(s'_T, s'_S)$ and condition 3(b) of ND-simulation follows.

(IF PART) Assume $\langle b_T, e \rangle \preceq \langle b_1, \dots, b_n, e \rangle$ and let $\omega(\cdot, \cdot)$ be the output function of the controller generator of \mathcal{S} for \mathcal{B}_T (see page 116).

Let $\vec{x}_0 = \langle b_1, \dots, b_n, e, b_T, a \rangle$. We define $y_0 = \omega(\langle \langle b_T, e \rangle, \langle b_1, \dots, b_n, e \rangle \rangle, a)$, if $a \in \mathcal{A}$ is a legal action for the target to request at state b_T when the environment is in state e ; otherwise y_0 can take any arbitrary value in $\{1, \dots, n\}$. It is important to note that, in the former case, $\omega(\langle \langle b_T, e \rangle, \langle b_1, \dots, b_n, e \rangle \rangle, a) \neq \emptyset$ and hence $y_0 \in \{1, \dots, n\}$. This is because since

$\text{com}_S(\vec{x}_0)$ can mimic any possible move of $\text{com}_T(\vec{x}_0)$, including the target compatible action a , there must exist $\sigma' \in \Sigma$ such that $\langle \text{com}_T(\vec{x}_0), \text{com}_S(\vec{x}_0) \rangle \xrightarrow{a(\vec{x}_0), i} \sigma'$ in CG, for some $i \in \{1, \dots, n\}$. Note that $\langle \text{com}_T(\vec{x}_0), \text{com}_S(\vec{x}_0) \rangle \in \Sigma$ is a state in CG, as $\text{com}_T(\vec{x}_0) \preceq \text{com}_S(\vec{x}_0)$.

To prove that $\langle \vec{x}_0, y_0 \rangle \in W$, we show that there is a strategy $f(\cdot, \cdot)$ that is winning from game state $\langle \vec{x}_0, y_0 \rangle$. Consider then any strategy $f(\cdot, \cdot)$ such that for all sequences $\vec{x}_1 \dots \vec{x}_k$, with $k \geq 1$, it is the case that $f(\langle \vec{x}_0, y_0 \rangle, \vec{x}_1 \dots \vec{x}_k) \in \{1, \dots, n\}$ and

$$f(\langle \vec{x}_0, y_0 \rangle, \vec{x}_1 \dots \vec{x}_k) \in \omega(\langle \text{com}_T(\vec{x}_k), \text{com}_S(\vec{x}_k) \rangle, a(\vec{x}_k)),$$

whenever $a(\vec{x}_k) \neq \sharp$, $\text{com}_T(\vec{x}_k) \preceq \text{com}_S(\vec{x}_k)$, and $\rho_S(\vec{x}_{k-1}, y_{k-1}, \vec{x}_k)$ hold true. Informally, we pick any strategy that always selects a behavior compatible with the controller generator output function whenever the enacted system state simulates the enacted target state in the last move \vec{x}_k of the system player and there is a proper action request. In all other cases, the strategy can pick any behavior arbitrarily (but never \sharp).

First, we argue that f is well-defined and indeed a valid strategy in $G_{(S, B_T)}$. It never selects \sharp and hence adheres to $G_{(S, B_T)}$'s condition 6. Moreover, whenever $a(\vec{x}_k) \neq \sharp$, $\text{com}_T(\vec{x}_k) \preceq \text{com}_S(\vec{x}_k)$, and $\rho_S(\vec{x}_{k-1}, y_{k-1}, \vec{x}_k)$ apply, we can follow the same reasoning we did above for y_0 to conclude that $\omega(\langle \text{com}_T(\vec{x}_k), \text{com}_S(\vec{x}_k) \rangle, a(\vec{x}_k)) \neq \emptyset$. We just need to note that because $a(\vec{x}_k) \neq \sharp$ and $\rho_S(\vec{x}_{k-1}, y_{k-1}, \vec{x}_k)$, then $a(\vec{x}_k)$ ought to stand for an action that is legal for the target at $\text{com}_T(\vec{x}_k)$ (condition 5(b) and third claim in Lemma 11).

So, let us next prove that for any f -compliant game play $\eta = \langle \vec{x}_0, y_0 \rangle \langle \vec{x}_1, y_1 \rangle \dots$, it is the case that $\text{com}_T(\vec{x}_i) \preceq \text{com}_S(\vec{x}_i)$ (i.e., $\langle b_{Ti}, e_i \rangle \preceq \langle b_{1i}, \dots, b_{ni}, e_i \rangle$), for all $i \geq 0$. The base case when $i = 0$ is trivial by definition of \vec{x}_0 and the assumption.

Consider now game state $\langle \vec{x}_{k+1}, y_{k+1} \rangle$, for some $k \geq 0$. By induction hypothesis, $\text{com}_T(\vec{x}_k) \preceq \text{com}_S(\vec{x}_k)$ applies. Because η is a game play, one of the three cases of condition 5 in $G_{(S, B_T)}$'s definition must apply for each transition. First of all, because $y_i \in \{1, \dots, n\}$ for every $i \geq 0$, condition 5(a) never applies. Now, if $a(\vec{x}_k)$ is not a legal target transition (including $a(\vec{x}_k) = \sharp$), then case 5(c) ought to apply, $\text{com}_T(\vec{x}_{k+1}) = \text{com}_T(\vec{x}_k)$ and $\text{com}_S(\vec{x}_{k+1}) = \text{com}_S(\vec{x}_k)$ hold, and $\text{com}_T(\vec{x}_{k+1}) \preceq \text{com}_S(\vec{x}_{k+1})$ follows directly.

Assume next that $a(\vec{x}_k)$ does stand for a legal action transition in the target at game state \vec{x}_k , that is, $\langle \vec{x}_k, y_k \rangle \models \text{validReq}$. If $k = 0$, then by definition of f for the first move, $y_0 \in \omega(\langle \text{com}_T(\vec{x}_0), \text{com}_S(\vec{x}_0) \rangle, a(\vec{x}_0))$. If $k \geq 1$, then because $\text{com}_T(\vec{x}_k) \preceq \text{com}_S(\vec{x}_k)$ (by induction hypothesis), $a(\vec{x}_k) \neq \sharp$ (by assumption), and $\rho_S(\vec{x}_{k-1}, y_{k-1}, \vec{x}_k)$ (η is a game play), we know by definition of f that $y_k \in \omega(\langle \text{com}_T(\vec{x}_k), \text{com}_S(\vec{x}_k) \rangle, a(\vec{x}_k))$. So, $y_k \in \omega(\langle \text{com}_T(\vec{x}_k), \text{com}_S(\vec{x}_k) \rangle, a(\vec{x}_k))$, for all $k \geq 0$, which implies that $y_k \in \{1, \dots, n\}$, as we proved above that f is indeed a well-defined strategy for $G_{(S, B_T)}$.

By definition of CG's output function, $\langle \text{com}_T(\vec{x}_k), \text{com}_S(\vec{x}_k) \rangle \xrightarrow{a(\vec{x}_k), y_k} \langle s'_T, s'_S \rangle$ in CG, for some $s'_T \in S_T$ and $s'_S \in S_S$. By CG's transition relation ϑ , this means that $\text{com}_T(\vec{x}_k) \xrightarrow{a(\vec{x}_k)} s'_T$ and $\text{com}_S(\vec{x}_k) \xrightarrow{a(\vec{x}_k), y_k} s'_S$. Due to Lemma 11, we conclude that:

$$\text{com}_S(\vec{x}_k) \xrightarrow{a(\vec{x}_k), y_k} \text{com}_S(\vec{x}_{k+1}); \tag{2}$$

$$\text{com}_T(\vec{x}) \xrightarrow{a(\vec{x})} \text{com}_T(\vec{x}_{k+1}). \tag{3}$$

From (2) and the third condition in CG's transition relation, it follows that $\langle s'_T, \text{com}_S(\vec{x}_{k+1}) \rangle \in \Sigma$ is a state in CG, and thus $s'_T \preceq \text{com}_S(\vec{x}_{k+1})$. Due to the first requirement of ND-simulations, $\text{env}(s'_T) = \text{env}(\text{com}_S(\vec{x}_{k+1}))$ applies. What is more, $\text{env}(s'_T) = \text{env}(\text{com}_T(\vec{x}_{k+1}))$, since $\text{env}(\text{com}_S(\vec{x}_{k+1})) = \text{env}(\text{com}_T(\vec{x}_{k+1}))$. This, together with (3) and the fact that the target behavior B_T is deterministic, implies that $s'_T = \text{com}_T(\vec{x}_{k+1})$, and as a result, $\text{com}_T(\vec{x}_{k+1}) \preceq \text{com}_S(\vec{x}_{k+1})$ follows.

So, we have proven that for any f -compliant game play $\eta = \langle \vec{x}_0, y_0 \rangle \langle \vec{x}_1, y_1 \rangle \dots$, it is the case that $\text{com}_T(\vec{x}_i) \preceq \text{com}_S(\vec{x}_i)$, for all $i \geq 1$. Consider next any game state $\langle \vec{x}_\ell, y_\ell \rangle$ in η , with $\ell \geq 0$, and let us prove that $\langle \vec{x}_\ell, y_\ell \rangle \models \varphi$. From $\text{com}_T(\vec{x}_\ell) \preceq \text{com}_S(\vec{x}_\ell)$ and requirement 2 of ND-simulations, we conclude that $\langle \vec{x}_\ell, y_\ell \rangle \models \text{final}_T \rightarrow \text{final}_i$, for each $i \in \{1, \dots, n\}$. Now, if $a(\vec{x}_\ell)$ is not a legal transition for the target at game state \vec{x}_ℓ (including \sharp), then $\langle \vec{x}_\ell, y_\ell \rangle \models \neg \text{validReq}$ follows. Otherwise, $a(\vec{x}_\ell) \in \mathcal{A}$ is a target compatible action, then, by the way we defined f above, we know that $y_\ell \in \omega(\langle \text{com}_T(\vec{x}_\ell), \text{com}_S(\vec{x}_\ell) \rangle, a(\vec{x}_\ell))$; observe $\text{com}_T(\vec{x}_\ell) \preceq \text{com}_S(\vec{x}_\ell)$ and $\langle \vec{x}_\ell, y_\ell \rangle$ is part of a legal play respecting ρ_S . This means that there exists a transition $\langle \text{com}_T(\vec{x}_\ell), \text{com}_S(\vec{x}_\ell) \rangle \xrightarrow{a(\vec{x}_\ell), y_\ell} \sigma'$ in controller generator CG, for some $\sigma' \in \Sigma$. By CG's transition relation definition, there exists a transition $\text{com}_S(\vec{x}_\ell) \xrightarrow{a(\vec{x}_\ell), y_\ell} s'_S$ in T_S , which—by the notion of enacted system—implies that behavior B_{y_ℓ} can make a transition on action $a(\vec{x}_\ell)$ and $\langle \vec{x}_\ell, y_\ell \rangle \models \neg \text{fail}_{y_\ell}$ follows. Finally, $\langle \vec{x}_\ell, y_\ell \rangle \models \neg \text{fail}_i$ trivially, for all $i \in \{1, \dots, n\} \setminus \{y_\ell\}$.

Putting it all together, the strategy f is a winning from game state $\langle \vec{x}_0, y_0 \rangle = \langle \langle b_1, \dots, b_n, e, b_T, a \rangle, \omega(\langle b_T, e \rangle, \langle b_1, \dots, b_n, e \rangle, a) \rangle$, and $\langle \vec{x}_0, y_0 \rangle \in W$. \square

While Theorem 12 only talks about non-initial states, it can be easily further extended to the unique initial state.

Theorem 13. Let $W \subseteq V$ be the maximal set of winning states for \square -GS $G_{(S, B_T)}$, as above, and let $\langle \vec{x}_0, y_0 \rangle$ be the initial state of the game, that is, $\langle \vec{x}_0, y_0 \rangle \models \Theta$. Then, $\langle \vec{x}_0, y_0 \rangle \in W$ iff $\langle b_{T0}, e_0 \rangle \preceq \langle b_{10}, \dots, b_{n0}, e_0 \rangle$.

Proof. This follows from the fact that, due to case 5(a) in $G_{(\mathcal{S}, \mathcal{B}_T)}$ definition, each successor of the initial game state represents the initial state of the composition problem. That is, $\langle \vec{x}, y \rangle$ is a game successor of $\langle \vec{x}_0, y_0 \rangle$ iff $com_{\mathcal{S}}(\vec{x}) = \langle b_{10}, \dots, b_{n0}, e_0 \rangle$ and $com_T(\vec{x}) = \langle b_{T0}, e_0 \rangle$. So, if $\langle b_{T0}, e_0 \rangle \preceq \langle b_{10}, \dots, b_{n0}, e_0 \rangle$, then by Theorem 12, for each such (initial) system move \vec{x} , there exists a controller move ind such that $\langle \vec{x}, ind \rangle \in W$ is a winning state, and as a result, $\langle \vec{x}_0, y_0 \rangle \in W$, too. Conversely, $\langle \vec{x}_0, y_0 \rangle$ can only be winning if for every system move \vec{x} from $\langle \vec{x}_0, y_0 \rangle$, there exists a controller move ind such that the successor state $\langle \vec{x}, ind \rangle$ of the initial state is winning, which by Theorem 12, implies that $\langle b_{T0}, e_0 \rangle \preceq \langle b_{10}, \dots, b_{n0}, e_0 \rangle$. \square

As a straightforward consequence of this result and Theorem 1, we have that \square -GS $G_{(\mathcal{S}, \mathcal{B}_T)}$ is winning if and only if there exists a composition of the target in the system.

In addition to this, the following result holds, which gives us an actual procedure to build a controller generator and, hence, all possible compositions.

Theorem 14. Let $\mathcal{S} = \langle \mathcal{B}_1, \dots, \mathcal{B}_n, \mathcal{E} \rangle$ be a system and \mathcal{B}_T a target behavior over \mathcal{E} . Let $G_{(\mathcal{S}, \mathcal{B}_T)} = \langle \mathcal{V}, \mathcal{X}, \mathcal{Y}, \Theta, \rho_s, \rho_c, \square \varphi \rangle$ be the \square -GS derived as above, and assume that $\langle \langle b_{10}, \dots, b_{n0}, e_0, b_{T0}, \sharp \rangle, \sharp \rangle \in W$, where W is the maximal set of winning states. Let $\widehat{CG} = \langle \widehat{\Sigma}, \mathcal{A}, \{1, \dots, n\}, \widehat{\partial}, \widehat{\omega} \rangle$, where:

- $\widehat{\Sigma} = \{ \langle \langle b_T, e \rangle, \langle b_1, \dots, b_n, e \rangle \rangle \mid \langle \langle b_1, \dots, b_n, e, b_T, a \rangle, ind \rangle \in W \}$.
- $\widehat{\partial} \subseteq \widehat{\Sigma} \times \mathcal{A} \times \{1, \dots, n\} \times \widehat{\Sigma}$ is such that $\langle \sigma, a, k, \sigma' \rangle \in \widehat{\partial}$, where $\sigma = \langle \langle b_T, e \rangle, \langle b_1, \dots, b_n, e \rangle \rangle$ and $\sigma' = \langle \langle b'_T, e' \rangle, \langle b'_1, \dots, b'_n, e' \rangle, e' \rangle$, if and only if
 - $\langle \langle b_1, \dots, b_n, e, b_T, a \rangle, k \rangle \in W$;
 - $\langle \langle b_1, \dots, b_n, e, b_T, a \rangle, k \rangle \models validReq$; and
 - $\rho_s(\langle b_1, \dots, b_n, e, b_T, a \rangle, k, \langle b'_1, \dots, b'_n, e', b'_T, a' \rangle)$, for some $a' \in \mathcal{A} \cup \{\sharp\}$.
- $\widehat{\omega}(\sigma, a) = \{k \mid \exists \sigma' \in \widehat{\Sigma} \text{ s.t. } \sigma \xrightarrow{a, k} \sigma' \text{ is in } \widehat{CG}\}$.

Then, $\widehat{CG} = CG$, that is, \widehat{CG} is the controller generator of \mathcal{S} for \mathcal{B}_T .

Proof. Consider the definition of controller generator CG in Section 3; page 116. We need to show that $\Sigma = \widehat{\Sigma}$, $\widehat{\partial} = \partial$, and $\widehat{\omega} = \omega$.

By definition of $\widehat{\Sigma}$, $\langle \langle b_T, e \rangle, \langle b_1, \dots, b_n, e \rangle \rangle \in \widehat{\Sigma}$ iff $\langle \langle b_1, \dots, b_n, e, b_T, a \rangle, ind \rangle \in W$, for some a and ind . Thus, by Theorem 12, $\langle \langle b_T, e \rangle, \langle b_1, \dots, b_n, e \rangle \rangle \in \widehat{\Sigma}$ iff $\langle b_T, e \rangle \preceq \langle b_1, \dots, b_n, e \rangle$. This, together with the definition of Σ in CG and the fact that if $s_T \preceq s_S$ then $env(s_T) = env(s_S)$, implies that $\langle \langle b_T, e \rangle, \langle b_1, \dots, b_n, e \rangle \rangle \in \widehat{\Sigma}$ iff $\langle \langle b_T, e \rangle, \langle b_1, \dots, b_n, e \rangle \rangle \in \Sigma$. Hence, $\Sigma = \widehat{\Sigma}$.

Let us prove next that $\widehat{\partial} = \partial$. Suppose that $\langle \sigma, a, k, \sigma' \rangle \in \widehat{\partial}$. Then, $\langle \langle b_1, \dots, b_n, e, b_T, a \rangle, k, \langle b'_1, \dots, b'_n, e', b'_T, a' \rangle \rangle \in \rho_s$. Because $a, k \neq \sharp$ due to the definition of $\widehat{\partial}$, case 5(a) (page 126) of $G_{(\mathcal{S}, \mathcal{B}_T)}$ does not apply. Moreover, a is a target and environment compatible action, due to $\langle \langle b_1, \dots, b_n, e, b_T, a \rangle, k \rangle \models validReq$, that can be legally performed by behavior \mathcal{B}_k , due to $\langle \langle b_1, \dots, b_n, e, b_T, a \rangle, k \rangle \models \neg fail_k$ (as $\langle \langle b_1, \dots, b_n, e, b_T, a \rangle, k \rangle \in W$). Thus, case 5(c) of $G_{(\mathcal{S}, \mathcal{B}_T)}$ cannot apply either.

So, case 5(b) of $G_{(\mathcal{S}, \mathcal{B}_T)}$ must apply. Then, $com_T(\sigma) \xrightarrow{a} com_T(\sigma')$ in \mathcal{T}_T and $com_S(\sigma) \xrightarrow{a, k} com_S(\sigma')$ in \mathcal{T}_S . Let us next prove the third requirement for ∂ in CG . To that end, consider any transition $com_S(\sigma) \xrightarrow{a, k} s''_S = \langle b''_1, \dots, b''_n, e' \rangle$ in \mathcal{T}_S . Due to Lemma 11, game state $\langle \langle b_1, \dots, b_n, e, b_T, a \rangle, k \rangle$ ought to have a successor state of the form $\langle \langle b''_1, \dots, b''_n, e', b'_T, \sharp, k'' \rangle, k'' \rangle$ where $k'' \neq \sharp$. Moreover, since $\langle \langle b_1, \dots, b_n, e, b_T, a \rangle, k \rangle \in W$, there is at least one such k'' such that $\langle \langle b''_1, \dots, b''_n, e', b'_T, a'' \rangle, k'' \rangle \in W$. Then, by Theorem 12, $\langle b'_T, e' \rangle \preceq \langle b''_1, \dots, b''_n, e' \rangle$ applies and therefore, by definition of Σ in CG , $\langle \langle b'_T, e' \rangle, \langle b''_1, \dots, b''_n, e' \rangle \rangle \in \Sigma$ follows. Then, $\langle \sigma, a, k, \sigma' \rangle \in \partial$ follows and $\widehat{\partial} \subseteq \partial$.

Now, let us prove that $\partial \subseteq \widehat{\partial}$. Assume $\langle \sigma, a, k, \sigma' \rangle \in \partial$. We want to prove $\langle \sigma, a, k, \sigma' \rangle \in \widehat{\partial}$. To that end, we show that:

1. $\langle \vec{x}, k \rangle = \langle \langle b_1, \dots, b_n, e, b_T, a \rangle, k \rangle \in W$; and
2. $\rho_s(\langle b_1, \dots, b_n, e, b_T, a \rangle, k, \langle b'_1, \dots, b'_n, e', b'_T, \sharp \rangle)$.

To prove the first claim, take a successor $\langle \vec{x}^*, k^* \rangle = \langle \langle b_1^*, \dots, b_n^*, e^*, b_T^*, a^* \rangle, k^* \rangle$ of $\langle \vec{x}, k \rangle$ in $G_{(\mathcal{S}, \mathcal{B}_T)}$. Because $\langle \sigma, a, k, \sigma' \rangle \in \partial$, $com_T(\sigma) \xrightarrow{a} com_T(\sigma')$ in \mathcal{T}_T and $com_S(\sigma) \xrightarrow{a, k} com_S(\sigma')$ in \mathcal{T}_S . Thus, Lemma 11 applies and we conclude that $com_S(\sigma) \xrightarrow{a, k} com_S(\vec{x}^*)$ in \mathcal{T}_S and $com_T(\sigma) \xrightarrow{a} com_T(\vec{x}^*)$ in \mathcal{T}_T . (Note that because the target behavior is deterministic $b_T^* = b'_T$.) Again, since $\langle \sigma, a, k, \sigma' \rangle \in \partial$, the third requirement in the definition of ∂ implies that $\langle com_T(\vec{x}^*), com_S(\vec{x}^*) \rangle \in \Sigma$ and therefore $com_T(\vec{x}^*) \preceq com_S(\vec{x}^*)$. By applying Theorem 12, there exists one such $k^* \in \{1, \dots, n\}$ such that $\langle \vec{x}^*, k^* \rangle \in W$. Note that for such particular k^* , $\langle \vec{x}^*, k^* \rangle$ is still a successor game state of $\langle \vec{x}, k \rangle$ by requirement 6 (page 126) of $G_{(\mathcal{S}, \mathcal{B}_T)}$ definition. Informally, at game state $\langle \vec{x}, k \rangle$, the controller can force the game to a winning state no matter the system plays its next move \vec{x}^* . So, to prove that $\langle \vec{x}, k \rangle \in W$, it remains to be shown that $\langle \vec{x}, k \rangle \models \varphi$, that is, game state $\langle \vec{x}, k \rangle$ itself satisfies the winning condition. Since $com_S(\sigma) \xrightarrow{a, k} com_S(\sigma')$ in \mathcal{T}_S , then $b_k \xrightarrow{g, a} b'_k$ in \mathcal{B}_k such that $g(e) = \top$, and therefore

$\langle \vec{x}, k \rangle \models \neg \text{fail}_k$. (Note that $\langle \vec{x}, k \rangle \models \neg \text{fail}_i$ trivially for all $i \neq k$.) Next, because $\sigma \in \Sigma$, $\text{com}_T(\sigma) \preceq \text{com}_{\mathcal{S}}(\sigma)$. Then, if b_T is final in \mathcal{B}_T , so are all b_i in \mathcal{B}_i . Hence, $\langle \vec{x}, k \rangle \models \neg \text{final}_T \rightarrow \bigwedge_{i=1}^n \text{final}_i$.

Finally, $\rho_{\mathcal{S}}(\langle b_1, \dots, b_n, e, b_T, a \rangle, k, \langle b'_1, \dots, b'_n, e', b'_T, \sharp \rangle)$ follows due to Lemma 11 and the fact that \sharp is always a legal action in the game.

Putting it all together, we have just shown that $\widehat{\partial} = \partial$, that is, the transition relation for \widehat{CG} is exactly that of the controller generator. As an immediate consequence of this, we obtain $\omega = \widehat{\omega}$, as their definitions coincide. Hence, $CG = \widehat{CG}$. \square

The above theorems show how one can exploit tools from reactive system synthesis for computing all compositions of a given target behavior. In details, starting from $\mathcal{S} = \langle \mathcal{B}_1, \dots, \mathcal{B}_n, \mathcal{E} \rangle$ and \mathcal{B}_T , one can build the corresponding game structure $G_{\langle \mathcal{S}, \mathcal{B}_T \rangle}$, then compute the winning set W , and, if it contains $G_{\langle \mathcal{S}, \mathcal{B}_T \rangle}$'s initial state, use W to generate the controller generator. In fact, this last step is not really needed. It is not hard to see that given a system state $\langle b_1, \dots, b_n, e, b_T, a \rangle$ (including action $a \in \mathcal{A}$ to be executed next), a behavior selection ind is “good” (i.e., the selected behavior can actually execute the action and the whole system can still ND-simulate the target behavior) if and only if W contains a tuple $\langle \langle b_1, \dots, b_n, e, b_T, a \rangle, \text{ind} \rangle$. Consequently, at each step, based on (current) target behavior state b_T , available behaviors' states b_1, \dots, b_n , environment state e , and requested action a , one can select a tuple from W , extract its ind component, and use it to select the next behavior.

Finally, note that the time complexity of Algorithm 3 is polynomial in $|V|$, the size of the input \square -GS state space. Since, in our encoding, $|V|$ is polynomial in $|\mathcal{B}_1|, \dots, |\mathcal{B}_n|, |\mathcal{B}_T|, |\mathcal{E}|$, and $|\mathcal{A}|$, and exponential in n , we get the following result:

Theorem 15. *Let $\mathcal{S} = \langle \mathcal{B}_1, \dots, \mathcal{B}_n, \mathcal{E} \rangle$ be a system and \mathcal{B}_T a target behavior over \mathcal{E} . Checking the existence of compositions by reduction to safety games can be done in polynomial time w.r.t. $|\mathcal{B}_1|, \dots, |\mathcal{B}_n|, |\mathcal{B}_T|, |\mathcal{E}|$, and $|\mathcal{A}|$, and exponential time in n .*

Such a result says that computing a composition using safety games has the same computational complexity as computing the ND-simulation relation for solving behavior composition problems (cf. Theorem 2). Since the composition problem is EXPTIME-hard [61], the technique based on safety games is actually optimal with respect to worst-case time complexity.

6. Implementing behavior composition in tlv

With the behavior composition problem formally reduced to that of synthesizing a winning strategy in a special safety-game, one can appeal to existing implemented systems that are capable of searching for winning strategies in game structures, such as tlv [71], ANZU [45], LILY [44], and MOCHA [4]. We note that, even though not all of these tools offer efficient, or more appropriately optimized, solution techniques, there are currently promising efforts in this direction (cf., e.g., [44]), so we may likely expect formal synthesis technology to become available as an effective alternative in the future—similarly to model checking [23]. In that sense, in this section we explain in detail how a proof-of-concept implementation of what was presented in the previous section can be readily obtained. Although we shall focus on tlv, all basic concepts discussed here remain valid for all other tools.

tlv (Temporal Logic Verifier) is a (generic) software for verification and synthesis of LTL specifications, which exploits Binary Decision Diagrams (BDDs) for symbolic state manipulation, in order to contain state explosion. Generally speaking, tlv takes two inputs: (i) a synthesis procedure; and (ii) an LTL specification, encoded in smv language [59], to be processed by the input procedure. In particular, for (i), we consider a specific procedure for dealing with safety games and refer to the so-obtained system as tlv \square .¹³ Essentially, tlv \square takes as input an LTL specification encoding a \square -GS and derives from the game's maximal winning set, if non-empty, a structure representing the controller generator, as shown in Theorem 14. We refer to [71] for further details on tlv and the input language smv, here introducing some essentials only.

Our approach consists in: (i) building, as described in Section 5.2, the \square -GS corresponding to a given behavior composition problem; (ii) deriving the smv encoding for the obtained \square -GS; and (iii) executing the encoding in tlv \square , to both check whether the composition problem is solvable and, if so, compute the controller generator. Next, we detail (ii).

In the smv encoding, every aspect of a \square -GS, e.g., the available behaviors or the controller, is modeled as a so-called “module”. Fig. 6 shows the basic blocks of the encoding for our painting world running example (see Fig. 1; page 109). Modules, e.g., ArmSys, can be built from submodules, by declaring these in the VAR section, which is what we actually do in our construction. When doing so, according to the smv semantics, the execution of the composite module corresponds to the synchronous execution of its submodules. Asynchronicity can be emulated by allowing a module to loop at each state via a no-op transition. This is indeed what we do so as to accommodate the asynchronous execution of the available behaviors (see definition of enacted system in Section 2): each submodule that represents an available behavior is forced to loop at each step when not “selected”, by means of auxiliary no-op action none.

Module Main, consisting of submodules sys and contr, wraps all the other modules, and represents the whole game structure. In particular, module sys captures the system player, by encoding the enacted system behavior (asys) together with the enacted target behavior (client), i.e., informally, the external uncontrollable system. Module contr, on the other

¹³ This specific procedure for safety games was originally coded by Amir Pnueli.

```

MODULE System(alop, a2op, a3op)
VAR
  asys : ArmSys(client.req,alop,a2op,a3op);
  client : Client(asys.envstate);
DEFINE
  initial:= asys.initial & client.initial;
  failfinal := client.final & !asys.final;
  failure := asys.fail | failfinal;
  req := client.req;

MODULE ArmSys(req, alop, a2op, a3op)
VAR
  env : Environment(req);
  a1 : ArmA(alop, env.state);
  a2 : ArmB(a2op, env.state);
  a3 : ArmC(a3op, env.state);
DEFINE
  initial := env.initial &
    a1.initial & a2.initial & a3.initial;
  fail := a1.fail | a2.fail | a3.fail;
  final := s1.final & s2.final & s3.final;
  envstate := env.state;

MODULE Client(env)
VAR
  target : Target(env, req);
  req: {start,none,prepare,clean,...};
INIT
  req = start
TRANS
  case
    next(target.state) = t2 :
      next(req) in {paint,clean};
    ...
    TRUE : next(req) = none;
  esac
DEFINE
  ...
  ...

MODULE main
VAR
  sys: system System(contr.alop,contr.a2op,contr.a3op);
  contr: system Controller(sys.req);
DEFINE
  good := (contr.initial & sys.initial) | !(sys.failure);

```

Fig. 6. A tlv sample fragment encoding.

hand, encodes the constraints on the controller player in the game structure, that is, the module to be synthesized. Finally, variable `good` encodes the goal invariant property to be respected, which states that a game state (including both player states) is “good” if and only if either both players are at their dummy initial states or the external system—the system player—has not been brought into a failure state. The external system may reach a failure state, for instance, if an available behavior is requested an action it cannot perform in its current state, or if the target behavior is in a final state but some available behavior is not.

Modules `sys` and `contr` are meant to evolve *synchronously*, the former choosing the next requested action to be performed and the latter selecting the available behavior for its execution. Consequently, the requested action (`sys.req`) is passed as an input argument to the `contr` module, and the chosen available behavior is passed as an input to the `sys` module. Notice that instead of merely returning just the index of the available behavior meant to execute the currently requested action (as in the game structure previously defined), the `contr` module outputs one action per available behavior—e.g., `a2op` denotes the action assigned to behavior arm `a2`, using the distinguished action constant `none` to state that no action is requested. This approach enables the encoding of settings where more than one behavior may execute at the same time, like in [79]. We refer to this encoding as it introduces no additional difficulty while being clearly more general.

Next, we detail the submodules representing the two players of the game structure. As for `contr`, which is an instance of `Controller`, the transition relation defined by the constraints in the `INIT` and `TRANS` sections encodes an *unconstrained controller*, which assigns, at each step, one action to each available behavior, by assigning values to the state variables `alop`, `a2op`, and `a3op`. The synthesis goal is to restrict such a relation so as to obtain a winning strategy. In particular, the constraints enforced on the controller player’s state are as follows. According to the `INIT` section, in its initial state (where variable `initial` holds true) the controller must instruct every behavior to initialize itself by performing the dummy action `start` (all behaviors initialize simultaneously). As for non-initial states, the `TRANS` section defines the following constraints: (i) no initialization action can be assigned to any behavior; (ii) the current action request must match at least one of the behavior

actions; (iii) a behavior can be instructed to execute an action only if that action is the one currently requested; and (iv) at most one behavior can be instructed to act at a time.

Concerning module `sys`, which is an instance of `System`, it essentially captures, as said above, all the aspects of the system player. Precisely, `sys` is the synchronous product of the enacted available system (submodule `asys`) and the client issuing the action requests (submodule `client`). On the one hand, submodule `asys` accounts for the available behaviors running in the environment, according to both the currently requested action (variable `req`) and the controller assignment to variables `a1op`, `a2op`, and `a3op`; on the other hand, submodule `client` provides, at every game state, the requested action (variable `req`), which is, of course, required to be compliant with the target behavior. Observe that `client` requests action `none` (last rule) only when no other legal action can be requested anymore. Since the execution of `none` yields no change in the current game state, it turns out that once executed, `none` remains the only action available to the target, from that point on.

Distinguished abbreviations are used to define, in the `DEFINE` section, initial, final, and failure states. In particular, the enacted system behavior (`ArmSys`) fails (`failure`) when any of the available behaviors does, an available behavior failing when instructed to perform an action it cannot execute, depending on its and the environment's current state. Avoiding such situations, by properly constraining `sys`'s transition relation, is exactly the synthesis procedure's aim. Clearly, the only way to achieve this is by suitably assigning `sys`'s *controllable* input variables `a1op`, `a2op`, and `a3op`, that is, ultimately, by suitably "crafting" the `contr` module (while respecting its constraints). Finally, the whole enacted system does not respect the final-state condition (`failfinal`) when the client is in a state where it may legally terminate its execution but the available system does not.

We encoded our running example for `TLV`, and run it to compute the corresponding winning set, along with the controller generator. The result obtained was an automaton with 16 states and 21 transitions, from where controllers can be easily extracted. We report three sample states of the automaton:

```

State 3
sys.asys.env.state = e2,           sys.asys.a1.state = a1,
sys.asys.a2.state = b2,           sys.asys.a3.state = c1,
sys.client.target.state = t2,     sys.client.req = paint,
contr.a1op = none, contr.a2op = paint, contr.a3op = none,
```



```

State 15
sys.asys.env.state = e2,           sys.asys.a1.state = a1,
sys.asys.a2.state = b3,           sys.asys.a3.state = c1,
sys.client.target.state = t4,     sys.client.req = dispose,
contr.a1op = dispose, contr.a2op = none, contr.a3op = none,
```



```

State 16
sys.asys.env.state = e2,           sys.asys.a1.state = a1,
sys.asys.a2.state = b1,           sys.asys.a3.state = c1,
sys.client.target.state = t4,     sys.client.req = dispose,
contr.a1op = dispose, contr.a2op = none, contr.a3op = none,
```

In state 3, for instance, the environment is in state e_2 , the available arms are in states a_1 , b_2 , and c_1 , the target behavior is in state t_2 , the action requested next is *paint*, and the controller has selected arm B_2 for carrying out the action. States 15 and 16 are the possible successor states that the game can be in, depending on how the non-deterministic transition in behavior B_2 turns out.

The complete `TLV` specification for our example can be found in [Appendix A](#).

We close by noting that the implementation discussed in this section is only concerned with the synthesis of the controller generator (see Section 3), and as a result is not meant to deal with the run-time adaptation techniques developed in Section 4 for dealing with failures. Indeed such techniques are expected to be part of a "smart" composition executor which will execute and adapt controller generators at run-time.

7. Related work

The framework developed in this paper can be seen as a core account for behavior composition, and can be extended in a number of directions. In [79], a distributed version of the problem is presented, where instead of a central entity that embodies the controller, a set of local controllers, one per available behavior, are meant to jointly realize the target behavior, by exploiting an underlying, shared communication channel. Another extension involves realizing not one but several target behaviors concurrently, using the same available system [77]. Composition under partial observability was also explored by De Giacomo [24], whereas composition with data exchange was investigated by Berardi et al. [12] in the context of web-services. Finally, [78,28] propose two frameworks (and corresponding techniques) for composing agent high-level programs. The techniques for all these extensions vary, from PDL satisfiability [79,12] to LTL/ATL synthesis [24, 77,28], to computation of specific fix-points [78]. Also, a direct search-based technique for the core composition account

was recently proposed by Stroeder and Pagnucco [85], which could turn out to be promising when it comes to applying heuristics.

The composition technique we proposed here is related to synthesis of reactive systems from LTL temporal specifications [70,69,47], which is proven 2EXPTIME-complete, in general [70]. In our particular case, however, we can restrict to a class of specifications, namely GR(1), for which the problem is EXPTIME-complete [69]. Though a subclass of full LTL, GR(1) type formulas are expressive enough to deal with many, if not most, realistic applications. They, for instance, have been used to support advanced forms of path planning in robots [49,48,11,33]. Notably, a work that is inspired by our behavior composition is that of Lustig and Vardi [54], where the problem of synthesizing LTL specifications by coordinating given modules from an existing library is studied (and proven 2EXPTIME-complete). In turn, De Giacomo and Felli [25] showed how to solve the behavior composition problem by ATL model checking. ATL (Alternating-time Temporal Logic) [3] is a logic especially aimed for reasoning about multi-player games, where players can form coalitions to satisfy certain formulae. The result is important in that it gives access to some of the state-of-the-art model checking techniques and tools, such as MC-MAS,¹⁴ that have been recently developed within the agent community. Since the behavior composition task can be seen as winning a special kind of game (see Section 5), it would be interesting to explore whether the heuristic-based techniques developed in the context of General-Game Playing [35] can be applied for “playing” composition games that are either too difficult to solve at the outset or directly unsolvable.

Our work directly relates to several others (e.g., [38,19,13,31,12,15,37,73]) on Service Oriented Computing (SOC) [2]. Indeed, available behaviors, ultimately transition systems, can be seen as the conceptual model for *conversational*, or stateful, (web) services. By taking this perspective, many results presented here become applicable, almost *off-the-shelf*, in the SOC area. One line of research that is quite related to ours is that reported in [65,66,68,16] which exploits techniques for conditional planning for temporally extended goals. Starting from a set of conversational available services, specified in BPEL4WS (Business Process Execution Language for Web Services), and a goal specified as a branching temporal formulae (in the language EAGLE, a suitable extension of CTL [22]), conditional planning techniques are exploited to find an interleaved execution of available services, so as to satisfy the desired goal. Roughly speaking, a goal represents a main, finite, desired path of states, plus some secondary paths to be followed when “exceptions” (i.e., deviation from the main path) arise. This technique, actually implemented in the system ASTRO¹⁵ based on the Model Based Planner (MBP3) [21], exploits Model Checking technology (ultimately, BDDs) to control the state space explosion. Two main features differentiate such work from ours. Firstly, our goals are actually new services (behaviors), rather than desired executions, which, once realized, can be executed as any other one. What is more, the behaviors we synthesize are really intended to interact with some executor, instead of executing on their own, like plans do. So, from a high-level perspective, we aim at extending the set of services offered by a given system, whereas the work above focuses more on serving particular requests by taking advantage of the existing system. A research line on services that adopts the same approach as ours is that in [8–10]. Like ours, these works rely on techniques borrowed from controller synthesis, though the approach therein is more theoretical. In contrast, we fully take advantage of such results for practical reasons, by (i) exploiting controller synthesis techniques to build *flexible* solutions, and (ii) by showing how to use the actual existing technology, based on a symbolic approach, for effective solution construction.

In the series of works [57,58,83], the Situation Calculus logical framework is adopted as a theoretical framework for composing *semantic* Web services (specified in the OWL-S process ontology [56]). Available and goal services are modeled as (complex) Golog programs, and the objective is to find a terminating execution of the available services that corresponds to an execution of the goal service. Based on the same Situation Calculus semantics, Sirin et al. [82] exploits Hierarchical Task Networks (HTN) to model available (OWL-S) services, and then uses an HTN planner [62] to build a plan representing an actual, finite, execution of a desired target service. All such works share the idea of *achieving* a desired goal—being it a state or a situation—by executing a *terminating* plan or program. Our approach is different, and, in a sense, more general, essentially due to two major differences: first, we consider realization of *infinite* target behavior executions; second, a solution to our composition problem is required to realize *all* possible behavior service executions, rather than just one.

Behavior composition is also related to several forms of automated planning in AI, in particular, to planning for temporally extended goals (as mentioned above in the context of services), which investigates techniques for building finite or infinite plans that satisfy linear- or branching-time specifications [7,67,46]. Indeed, our problem requires an advanced conditional plan (with loops) that always guarantees all possible target requests to be served, which is, ultimately, a (temporal) invariant property. More specifically, the solutions obtained via the simulation technique developed in this work are akin to the so-called *universal plans* [81], i.e., plans representing every possible solution. A further recent work about planning, where temporal fairness constraints are explicitly stated so as to capture long-term effects of action executions is [29]. We conjecture that some of the concepts there can be exploited in our context to make the notion of behaviors to be composed more sophisticated.

Composing behaviors can also be linked to (multi-)agent systems in natural ways. For instance, a Belief-Desire-Intention agent operates on the coordinated execution of pre-defined non-deterministic plans—the available behaviors—in order to achieve its goals [75,36]. One could then imagine composing such available plans so as to bring about another non-available

¹⁴ <http://www-lai.doc.ic.ac.uk/mcmas/>.

¹⁵ <http://astropproject.org>.

plan—the target behavior—that represents all the goals of the agent. Similarly, composing behaviors can be seen as realizing a “team-oriented” behavior (e.g., a RoboCup sophisticated abstract “team” player), represented by the target behavior, from the behavior of single agents (e.g., a set of actual RoboCup robotic players with different capabilities), represented by the various available behaviors. Of course, the core composition framework as presented here lacks, so far, convenient features for programming team agent systems [72,43], such as roles, holons, communication channels, etc.

Finally, behavior composition, as studied in this paper, is tightly related to the problem of integrating simple functionalities to implement advanced (intelligent) behaviors in the context of robot ecologies [76,18,17]. The idea of leveraging on the capabilities of many simple robotic devices (e.g., vacuum cleaners, blinds, cameras, robot arms, etc.) in order to achieve complex tasks has attracted much attention lately given the marked tendency toward the embedding of intelligent, networked robotic devices in our homes and offices. While very close in “spirit”, the work done in robot ecologies so far focuses on differs aspects. Most of the work in “composing” functionalities within an ecology of robots is devoted to the generation of adequate ways of *connecting* existing functionalities via so-called *configurations* in order to be able to carry a particular task, such as making the output of a video camera the input of a moving robot lacking visual capabilities. Instead of dealing explicitly with such connectivity issues (except for the interaction with the environment), our work focuses on how each component needs to be actually operated in order to achieve the target process. Also, the integration of functionalities is either done fully by hand (e.g., [76,18]) or semi-automatically through hand-tailored planning techniques (e.g., [52,53]) in the style of HTN planning. In the latter case, one is meant to define standard “recipes” to describe ways to combine functionalities for specific purposes. Our approach is more of a first-principles one, no domain information is available on how available behaviors can or should be combined. More importantly, while we took a high-level perspective on agents and shared devices, and focused on the synthesis problem only, the aforementioned work on robot ecologies deals better with many other practical aspects of concern when it comes to implementing the solution. For instance, how to design such devices so that they can easily interoperate among themselves, as we assume here, and how such interoperability is actually realized, via an appropriate middleware [17]. In fact, we expect a fruitful cross-fertilization between the theoretical studies on automated synthesis of agents, as the one in the present paper, and practical work on experimenting device integration in robot ecologies and ambient intelligence.

8. Conclusions

In this paper, we have carried out a deep investigation on the behavior composition problem, that is, the problem of realizing a desired, but non-available, target behavior by reusing and re-purposing accessible modules (devices, agents, plans, etc.), which are the only behaviors actually available. In particular, we have proposed a technique, based on the notion of *simulation*, for building a controller that coordinates the concurrent executions of the available behaviors so as to “mimic” the target behavior. What is more, we showed that such technique can be directly related to building a winning strategy for a *safety game*, which opens the door for relying on symbolic model checking technology. Because of this, the results from Sections 3 and 5 can be easily linked. While Theorem 1 connects the existence of a composition controller with that of certain simulation relation, Theorem 12 connects the latter with the existence of a winning strategy, thus closing the loop from compositions to winning strategies in a safety game. Similarly, Theorem 14 (which is a surplus of Theorem 12) can be seen as the counterpart of simulation-based Theorem 3 (which is a surplus of Theorem 1) for safety games. Finally, Theorems 2 and 15 describe the complexity of the problem in terms of finding an adequate simulation relation or a winning set for a safety game, respectively, without overhead for the latter.

This work lays the basis for several further developments, some of which have already been mentioned in the related work section. We would like to close the paper by briefly discussing two of them that still require further study. The first one concerns the possibility of interchanging actions. More precisely, in this work we have implicitly assumed that two actions are equivalent if and only if they are named the same way, and hence, they are exactly the same action. Clearly, there are situations requiring a more flexible model, for instance when the domain includes actions with different names that execute, in fact, the same task; or where some actions specialize some other, more abstract, ones. For example, actions *paint-red* and *paint-blue* may stand for specializations (or implementations) of the more abstract, and maybe not even directly available, action *paint*. Both concrete actions, when abstracting from other details, may be considered equivalent in terms of the effect of having an object painted. One natural way to generalize the composition framework developed in this paper is to assume the existence of an underlying *compatibility relation* $\ll \subseteq \mathcal{A} \times \mathcal{A}$ among actions: if $a \ll \hat{a}$ (i.e., action \hat{a} is compatible with action a), then an execution of action a can be satisfied by the actual execution of action \hat{a} . With a domain compatibility relation at hand, one can then generalize the notion of ND-simulation from Section 3 to account for the fact that whenever an action a is requested by the target (e.g., *paint*), a compatible action \hat{a} , i.e., $a \ll \hat{a}$, can be carried out by some available behavior (e.g., *paint-red*). We expect all results presented here to still hold in such a generalized case, though further work is needed in order to formalize this intuition. While above we do not make any assumption on relation \ll , in practice it may be natural to assume that it satisfies certain properties. For instance, a reflexive compatibility relation captures the fact that every action can be always replaced by itself; a partial order captures a *hierarchy* of actions, where a general action a can be replaced by a more specific one, but not vice versa; and finally an equivalence relation can be used to assert that some actions carry out the very same task (relative

to some features of interest). A further study of which properties of relation \ll in specific applications is certainly of interest.

The second direction for further study stems from the observation that, when no compositions exist, it may be of interest to approximate “solutions”. That is, if a composition does not exist, one may be interested in understanding which part of the target cannot be realized and which can. Some compelling contribution in this direction can be found in the area of supervisory control of deterministic discrete event systems [74]. In particular, there is a foundational result of great interest: given a specification of the allowed behavior in terms of a language, i.e., a possibly infinite set of runs that are deemed as “allowed”, it is always possible to find a single maximal subset of such runs that can be obtained by controlling a given system, the so called “supremal controllable sublanguage” [90]. It would be quite interesting to understand if, at least in certain cases, an analogous property holds for behavior composition as well. The question then is what an “optimal” controller amounts to. Besides some domain-independent criteria (e.g., number of transitions realized), allowing the specification of additional domain information could help define what such best controllers are, such as quantifying all or some non-deterministic transitions and specifying preferences over target actions or available behaviors. Initial steps toward “optimization” versions of the composition problem studied in this article have been recently proposed by Yadav and Sardina [91,92], who developed a (quantitative) decision-theoretic composition framework as well as a qualitative account for “approximate” composition.

Acknowledgements

The authors would like to thank the anonymous reviewers for their suggestions and comments that helped improve the paper. This research was partially supported by the Australian Research Council (grants DP1094627 and DP120100332), the EU FP7-ICT Project ACSI (grant no. 257593), as well as two mobility awards (Australian Academy of Science “Scientific Visit to Europe” and RMIT Visiting Researcher’s awards).

Appendix A. tlv implementation for the painting block example

We list here the smv code that completes the one presented in Fig. 6. As for module `main`, we refer the reader to Fig. 6, where the full encoding is reported. Concerning the code for module `Environment`, it is as follows:

```
MODULE Environment(act) -- Environment
VAR
  st: {ini,e1,e2,e3,e4};
INIT
  st = ini
TRANS
  case
    st = ini & act = start : next(st) = e1;
    act = none : next(st) = st;
    st = e1 & act = recharge : next(st) = e1;
    st = e1 & act = prepare : next(st) = e2;
    st = e2 & act in {paint,recharge} : next(st) = e2;
    st = e2 & act = dispose : next(st) = e1;
    st = e2 & act = clean : next(st) in {e2,e3}; -- nondet!
    st = e3 & act in {paint,clean}: next(st) = e3;
    st = e3 & act = dispose : next(st) = e4;
    st = e3 & act = recharge : next(st) = e2;
    st = e4 & act = prepare : next(st) = e3;
    st = e4 & act = recharge : next(st) = e1;
    TRUE : FALSE; -- no other transitions possible!
  esac
DEFINE
  initial := st = ini;
```

Observe that the environment has one dummy state `ini` and one dummy action `start`, which, when executed in the initial state, makes the environment move to state `e1`. Every line in the `TRANS` section encodes a transition, that is, it defines the next state of the module (`next(st)`) given the environment's current state (`st`) and the action being performed, which is an *input* parameter (variable `act`).

We next list the code corresponding to the three available arms B_1 , B_2 , and B_3 . Their encoding is similar to that of the environment, though with some differences. Firstly, as the dynamics of each behavior—captured in the module's `TRANS` section—depends on both the action being performed by the behavior itself and the current environment state, both the action and the environment state appear as inputs (variables `act` and `env`) in each behavior module. As for the `TRANS` section, similarly to the environment's, each of its entries within the `case` body captures a behavior transition. In particular, observe that every behavior may be instructed to execute the dummy action `none` (second entry in `TRANS`), i.e., a no-op action that yields no state change in the module. Through this mechanism we implement the asynchronous execution of available behavior modules, as explained in Section 6. Secondly, to account for guards, the transitions occurring in a behavior module may contain (boolean) formulae involving the current state of the environment. For example, the fourth transition in the `ArmA` module states that the next state of the behavior is `a2`, provided: the current state is `a1`, the behavior is

executing action `clean`, and the environment is in either state `e1` or `e2`. Finally, each behavior defines its initial, final, and failure conditions. In particular, behavior failure is accounted for by introducing the distinguished absorbing state `failed`, that the module reaches whenever no transition rule applies for the current action and environment state input, i.e., when the behavior cannot legally execute the requested action.

```

MODULE ArmA(act, env)
VAR
  st: {ini,failed,a1,a2};
INIT
  st = ini
TRANS
  case
    st = ini & act = start :
      next(st) = a1;
    act = none : next(st) = st;
    st = a1 & act in {dispose,recharge} :
      next(st) = a1;
    st = a1 & act=clean & env in {e1,e2}:
      next(st) = a2;
    st = a2 & act = recharge :
      next(st) = a2;
    st = a2 & act = dispose :
      next(st) = a1;
    TRUE : next(st) = failed;
  esac
DEFINE
  initial := st = ini;
  final:= st = a1;
  fail := state = failed;
  
```

```

MODULE ArmB(act, env)
VAR
  st: {ini,failed,b1,b2,b3,b4};
INIT
  st = ini
TRANS
  case
    st = ini & act = start :
      next(st) = b1;
    act = none : next(st) = st;
    st = b1 & act = prepare :
      next(st) = b2;
    st = b2 & act = clean :
      next(st) = b1;
    st = b2 & act = paint :
      next(st) in {b1,b3};
    st = b3 & act = recharge :
      next(st) = b1;
    st = b3 & act = prepare :
      next(st) = b4;
    st = b4 & act = clean :
      next(st) = b3;
    TRUE : next(st) = failed;
  esac
DEFINE
  initial := st = ini;
  final:= st = b1;
  fail := state = failed;
  
```

```

MODULE ArmC(act, env)
VAR
  st: {ini,failed,c1,c2};
INIT
  st = ini
TRANS
  case
    st = ini & act = start : next(st) = c1;
    act = none : next(st) = st;
    st = c1 & act = recharge : next(st) = c2;
    st = c2 & act = prepare : next(st) = c2;
    st = c2 & act = paint : next(st) = c1;
    TRUE : next(st) = failed; -- failed!
  esac
DEFINE
  initial := st = ini;
  final:= st = c1;
  fail := state = failed;
  
```

The target specification is even simpler, as the target may not include any non-deterministic transition:

```

MODULE Target(env, req)
VAR
  state: {ini,t1,t2,t3,t4,t5};
INIT
  state = ini & req = start
TRANS
  case
    state = ini & req = start      : next(state) = t1;
    req = none                  : next(state) = state;
    state = t1 & req = prepare   : next(state) = t2;
    state = t2 & req = paint    : next(state) = t4;
    state = t2 & req = clean    : next(state) = t3;
    state = t3 & req = paint    : next(state) = t4;
    state = t4 & req = dispose   : next(state) = t5;
    state = t5 & req = recharge  : next(state) = t1;
  esac
DEFINE
  initial:= state = ini;
  final:= state = t1;
  
```

Using the target, we can then specify the client, which is meant to issue the request actions according, of course, to the target behavior:

```
MODULE Client(env)
VAR
  target : Target(env, req);
  req: {start,none,prepare,clean,paint,dispose,recharge};
INIT
  req = start
TRANS
  case
    next(tst) = t1 : next(req) = prepare;
    next(tst) = t2 : next(req) in {paint,clean} ;
    next(tst) = t3 : next(req) = paint;
    next(tst) = t4 : next(req) = dispose;
    next(tst) = t5 : next(req) = recharge;
    TRUE : next(req) = none;
  esac
DEFINE
  initial:= target.initial;
  tst := target.state;
  final:= target.final;
```

When the full specification is run against the TLV \square system, the following output is obtained:

```
TLV version 4.18.4
...
Resources used: user time: 0.11 s
BDD nodes allocated: 125962
max amount of BDD nodes allocated: 125962
Bytes allocated: 2228288
...

Automaton States

State 1
sys.availsys.env.state = start_st,           sys.availsys.a1.state = start_st,
sys.availsys.a2.state = start_st,           sys.availsys.a3.state = start_st,
sys.client.target.state = start_st,          sys.client.req = start_op,
contr.alop = start_op, contr.a2op = start_op, contr.a3op = start_op,

State 2
sys.availsys.env.state = e1,                 sys.availsys.a1.state = a1,
sys.availsys.a2.state = b1,                 sys.availsys.a3.state = c1,
sys.client.target.state = t1,                sys.client.req = prepare,
contr.alop = none, contr.a2op = prepare,     contr.a3op = none,

State 3
sys.availsys.env.state = e2,                 sys.availsys.a1.state = a1,
sys.availsys.a2.state = b2,                 sys.availsys.a3.state = c1,
sys.client.target.state = t2,                sys.client.req = paint,
contr.alop = none, contr.a2op = paint,       contr.a3op = none,

State 4
sys.availsys.env.state = e2,                 sys.availsys.a1.state = a1,
sys.availsys.a2.state = b2,                 sys.availsys.a3.state = c1,
sys.client.target.state = t2,                sys.client.req = clean,
contr.alop = clean, contr.a2op = none,       contr.a3op = none,

State 5
sys.availsys.env.state = e2,                 sys.availsys.a1.state = a2,
sys.availsys.a2.state = b2,                 sys.availsys.a3.state = c1,
sys.client.target.state = t3,                sys.client.req = paint,
contr.alop = none, contr.a2op = paint,       contr.a3op = none,

State 6
sys.availsys.env.state = e3,                 sys.availsys.a1.state = a2,
sys.availsys.a2.state = b2,                 sys.availsys.a3.state = c1,
sys.client.target.state = t3,                sys.client.req = paint,
contr.alop = none, contr.a2op = paint,       contr.a3op = none,

State 7
sys.availsys.env.state = e3,                 sys.availsys.a1.state = a2,
sys.availsys.a2.state = b3,                 sys.availsys.a3.state = c1,
sys.client.target.state = t4,                sys.client.req = dispose,
contr.alop = dispose, contr.a2op = none,     contr.a3op = none,
```

```

State 8
sys.availsys.env.state = e3,           sys.availsys.a1.state = a2,
sys.availsys.a2.state = b1,           sys.availsys.a3.state = c1,
sys.client.target.state = t4,           sys.client.req = dispose,
contr.alop = dispose, contr.a2op = none, contr.a3op = none,

State 9
sys.availsys.env.state = e4,           sys.availsys.a1.state = a1,
sys.availsys.a2.state = b1,           sys.availsys.a3.state = c1,
sys.client.target.state = t5,           sys.client.req = recharge,
contr.alop = recharge, contr.a2op = none, contr.a3op = none,

State 10
sys.availsys.env.state = e4,           sys.availsys.a1.state = a1,
sys.availsys.a2.state = b3,           sys.availsys.a3.state = c1,
sys.client.target.state = t5,           sys.client.req = recharge,
contr.alop = none, contr.a2op = recharge, contr.a3op = none,

State 11
sys.availsys.env.state = e2,           sys.availsys.a1.state = a2,
sys.availsys.a2.state = b3,           sys.availsys.a3.state = c1,
sys.client.target.state = t4,           sys.client.req = dispose,
contr.alop = dispose, contr.a2op = none, contr.a3op = none,

State 12
sys.availsys.env.state = e2,           sys.availsys.a1.state = a2,
sys.availsys.a2.state = b1,           sys.availsys.a3.state = c1,
sys.client.target.state = t4,           sys.client.req = dispose,
contr.alop = dispose, contr.a2op = none, contr.a3op = none,

State 13
sys.availsys.env.state = e1,           sys.availsys.a1.state = a1,
sys.availsys.a2.state = b1,           sys.availsys.a3.state = c1,
sys.client.target.state = t5,           sys.client.req = recharge,
contr.alop = recharge, contr.a2op = none, contr.a3op = none,

State 14
sys.availsys.env.state = e1,           sys.availsys.a1.state = a1,
sys.availsys.a2.state = b3,           sys.availsys.a3.state = c1,
sys.client.target.state = t5,           sys.client.req = recharge,
contr.alop = none, contr.a2op = recharge, contr.a3op = none,

State 15
sys.availsys.env.state = e2,           sys.availsys.a1.state = a1,
sys.availsys.a2.state = b3,           sys.availsys.a3.state = c1,
sys.client.target.state = t4,           sys.client.req = dispose,
contr.alop = dispose, contr.a2op = none, contr.a3op = none,

State 16
sys.availsys.env.state = e2,           sys.availsys.a1.state = a1,
sys.availsys.a2.state = b1,           sys.availsys.a3.state = c1,
sys.client.target.state = t4,           sys.client.req = dispose,
contr.alop = dispose, contr.a2op = none, contr.a3op = none,

```

Automaton Transitions

```

From 1 to 2
From 2 to 3 4
From 3 to 15 16
From 4 to 5 6
From 5 to 11 12
From 6 to 7 8
From 7 to 10
From 8 to 9
From 9 to 2
From 10 to 2
From 11 to 14
From 12 to 13
From 13 to 2
From 14 to 2
From 15 to 14
From 16 to 13

```

Automaton has 16 states, and 21 transitions

The output states that an automaton with 16 states and 21 transition was successfully synthesized. Observe that the automaton encodes and accounts for the constraints of both the whole system and the client running the target,

as well as the controller performing the composition. In fact, the obtained result can be regarded as a representation of the controller generator for the painting blocks example. States can be read as follows: an assignment to variables `sys.availsys.env.state`, `sys.availsys.a1.state`, `sys.availsys.a2.state`, `sys.availsys.a3.state`, and `sys.client.target.state`, forms the current state of the enacted system; an assignment to `sys.client.req` represents the action currently requested; and an assignment to `contr.a1op`, `contr.a2op`, and `contr.a3op`, represents a possible action delegations to available behaviors for fulfilling the current request.

We close by mentioning that, by running the example on a 2011 mid-priced laptop, we get a solution in less than half a second.

References

- [1] M. Abadi, L. Lamport, P. Wolper, Realizable and unrealizable specifications of reactive systems, in: Proceedings of the International Colloquium on Automata, Languages and Programming (ICALP), 1989, pp. 1–17.
- [2] G. Alonso, F. Casati, H. Kuno, V. Machiraju, Web Services. Concepts, Architectures and Applications, Springer, 2004.
- [3] R. Alur, T.A. Henzinger, O. Kupferman, Alternating-time temporal logic, *Journal of the ACM* 49 (5) (2002) 672–713.
- [4] R. Alur, T.A. Henzinger, F.Y.C. Mang, S. Qadeer, S.K. Rajamani, S. Tasiran, MOCHA: Modularity in model checking, in: Proceedings of the International Conference Computer Aided Verification (CAV), 1998, pp. 521–525.
- [5] E. Asarin, O. Maler, A. Pnueli, Symbolic controller synthesis for discrete and timed systems, in: P. Antsaklis, W. Kohn, A. Nerode, S. Sastry (Eds.), Hybrid Systems II, in: LNCS, vol. 999, Springer, 1995, pp. 1–20.
- [6] E. Asarin, O. Maler, A. Pnueli, J. Sifakis, Controller synthesis for timed automata, in: IFAC Symposium on System Structure and Control, Elsevier Science Publishers Ltd., 1998, pp. 469–474.
- [7] F. Bacchus, F. Kabanza, Planning for temporally extended goals, *Annals of Mathematics and Artificial Intelligence* 22 (1–2) (1998) 5–27.
- [8] P. Balbiani, F. Cheikh, G. Feuillade, Composition of interactive web services based on controller synthesis, in: Proceedings of the IEEE Congress on Services (SERVICES), 2008, pp. 521–528.
- [9] P. Balbiani, F. Cheikh, G. Feuillade, Algorithms and complexity of automata synthesis by asynchronous orchestration with applications to web services composition, *Electronic Notes in Theoretical Computer Science (ENTCS)* 229 (3) (2009) 3–18.
- [10] P. Balbiani, F. Cheikh, G. Feuillade, Controller/orchestrator synthesis via filtration, *Electronic Notes in Theoretical Computer Science (ENTCS)* 262 (2010) 33–48.
- [11] C. Belta, A. Bicchi, M. Egerstedt, E. Frazzoli, E. Klavins, G.J. Pappas, Symbolic planning and control of robot motion: State of the art and grand challenges, *IEEE Robotics and Automation Magazine* 14 (1) (March 2007) 61–70.
- [12] D. Berardi, D. Calvanese, G. De Giacomo, R. Hull, M. Mecella, Automatic composition of transition-based semantic web services with messaging, in: Proceedings of the International Conference on Very Large Databases (VLDB), 2005, pp. 613–624.
- [13] D. Berardi, D. Calvanese, G. De Giacomo, M. Lenzerini, M. Mecella, Automatic composition of e-services that export their behavior, in: Proceedings of the International Joint Conference on Service Oriented Computing (ICSOC), 2003, pp. 43–58.
- [14] D. Berardi, D. Calvanese, G. De Giacomo, M. Lenzerini, M. Mecella, Automatic service composition based on behavioural descriptions, *International Journal of Cooperative Information Systems* 14 (4) (2005) 333–376.
- [15] D. Berardi, F. Cheikh, G. De Giacomo, F. Patrizi, Automatic service composition via simulation, *International Journal of Foundations of Computer Science* 19 (2) (2008) 429–451.
- [16] P. Bertoli, M. Pistore, P. Traverso, Automated composition of web services via planning in asynchronous domains, *Artificial Intelligence Journal* 174 (3–4) (2010) 316–361.
- [17] M. Bordignon, J. Rashid, M. Broxvall, A. Saffiotti, Seamless integration of robots and tiny embedded devices in a PEIS-ecology, in: Proceedings of the IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), 2007, pp. 3101–3106.
- [18] M. Broxvall, M. Gritt, A. Saffiotti, B.-S. Seo, Y.-J. Cho, PEIS ecology: Integrating robots into smart environments, in: Proceedings of the IEEE International Conference on Robotics and Automation (ICRA), 2006, pp. 212–218.
- [19] T. Bultan, X. Fu, R. Hull, J. Su, Conversation specification: a new approach to design and analysis of e-service composition, in: Proceedings of the International Conference on World Wide Web (WWW), 2003, pp. 403–410.
- [20] D. Calvanese, G. De Giacomo, M. Lenzerini, M. Mecella, F. Patrizi, Automatic service composition and synthesis: The roman model, *IEEE Data Engineering Bulletin* 31 (3) (2008) 18–22.
- [21] A. Cimatti, M. Pistore, M. Roveri, P. Traverso, Weak, strong, and strong cyclic planning via symbolic model checking, *Artificial Intelligence Journal* 147 (1–2) (2003) 35–84.
- [22] E. Clarke, E. Emerson, Design and synthesis of synchronization skeletons using branching time temporal logic, in: D. Kozen (Ed.), Logics of Programs, in: LNCS, vol. 131, Springer, Berlin/Heidelberg, 1982, pp. 52–71 (Chapter 5).
- [23] E.M. Clarke, O. Grumberg, D. Peled, Model Checking, The MIT Press, 1999.
- [24] G. De Giacomo, R. De Masellis, F. Patrizi, Composition of partially observable services exporting their behaviour, in: Proceedings of the International Conference on Automated Planning and Scheduling (ICAPS), 2009, pp. 90–97.
- [25] G. De Giacomo, P. Felli, Agent composition synthesis based on ATL, in: Proceedings of Autonomous Agents and Multi-Agent Systems (AAMAS), 2010, pp. 499–506.
- [26] G. De Giacomo, F. Patrizi, Automated composition of nondeterministic stateful services, in: Web Services and Formal Methods, 6th International Workshop, Revised Selected Papers, WS-FM 2009, Bologna, Italy, September 4–5, 2009, in: LNCS, vol. 6194, Springer, 2010, pp. 147–160.
- [27] G. De Giacomo, F. Patrizi, P. Felli, S. Sardina, Two-player game structures for generalized planning and agent composition, in: Proceedings of the National Conference on Artificial Intelligence (AAAI), 2010, pp. 297–302.
- [28] G. De Giacomo, F. Patrizi, S. Sardina, Agent programming via planning programs, in: Proceedings of Autonomous Agents and Multi-Agent Systems (AAMAS), May 2010, pp. 491–498.
- [29] G. De Giacomo, F. Patrizi, S. Sardina, Generalized planning with loops under strong fairness constraints, in: Proceedings of Principles of Knowledge Representation and Reasoning (KR), 2010, pp. 351–361.
- [30] G. De Giacomo, S. Sardina, Automatic synthesis of new behaviors from a library of available behaviors, in: Proceedings of the International Joint Conference on Artificial Intelligence (IJCAI), 2007, pp. 1866–1871.
- [31] A. Deutsch, L. Sui, V. Vianu, Specification and verification of data-driven web applications, *Journal of Computer and System Sciences* 73 (3) (2007) 442–474.
- [32] R. Fagin, J.Y. Halpern, Y. Moses, M.Y. Vardi, Reasoning About Knowledge, The MIT Press, Cambridge, Massachusetts, 1995.
- [33] G.E. Fainekos, A. Girard, H. Kress-Gazit, G.J. Pappas, Temporal logic motion planning for dynamic robots, *Automatica* 45 (2) (2009) 343–352.
- [34] M. Gelfond, V. Lifschitz, Action languages, *Electronic Transactions of AI (ETAI)* 2 (1998) 193–210.

- [35] M. Genesereth, N. Love, General game playing: Overview of the AAAI competition, *AI Magazine* 26 (2005) 62–72.
- [36] M.P. Georgeff, A.L. Lansky, Reactive reasoning and planning, in: Proceedings of the National Conference on Artificial Intelligence (AAAI), 1987, pp. 677–682.
- [37] C.E. Gerede, R. Hull, O.H. Ibarra, J. Su, Automated composition of e-services: Lookaheads, in: Proceedings of the International Joint Conference on Service Oriented Computing (ICSOC), 2004, pp. 252–262.
- [38] C.E. Gerede, O.H. Ibarra, B. Ravikumar, J. Su, Online and minimum-cost ad hoc delegation in e-service composition, in: Proceedings of the IEEE International Conference on Services Computing (SCC), 2005, pp. 103–112.
- [39] M. Ghallab, D. Nau, P. Traverso, *Automated Planning: Theory and Practice*, Morgan Kauffman, 2004.
- [40] A. Harding, M. Ryan, P.-Y. Schobbens, A new algorithm for strategy synthesis in LTL games, in: Proceedings of Tools and Algorithms for the Construction and Analysis of Systems (TACAS), 2005, pp. 477–492.
- [41] M.R. Henzinger, T.A. Henzinger, P.W. Kopke, Computing simulations on finite and infinite graphs, in: Proceedings of the Annual Symposium on Foundations of Computer Science (FOCS), 1995, pp. 453–462.
- [42] R. Hull, Web services composition: A story of models, automata, and logics, in: Proceedings of the IEEE International Conference on Services Computing (SCC), 2005, pp. 18–19.
- [43] B. Jarvis, D. Jarvis, L. Jain, Teams in multi-agent systems, in: Z. Shi, K. Shimohara, D. Feng (Eds.), *Intelligent Information Processing III*, in: IFIP International Federation for Information Processing, vol. 228, Springer, 2007, pp. 1–10 (Chapter 1).
- [44] B. Jobstmann, R. Bloem, Optimizations for LTL synthesis, in: Proceedings of the Formal Methods in Computer Aided Design (FMCAD), IEEE Computer Society Press, 2006, pp. 117–124.
- [45] B. Jobstmann, S. Galler, M. Weiglhofer, R. Bloem, Anzu: A tool for property synthesis, in: Proceedings of the International Conference Computer Aided Verification (CAV), 2007, pp. 258–262.
- [46] F. Kabanza, S. Thiébaux, Search control in planning for temporally extended goals, in: Proceedings of the International Conference on Automated Planning and Scheduling (ICAPS), 2005, pp. 130–139.
- [47] Y. Kesten, N. Piterman, A. Pnueli, Bridging the gap between fair simulation and trace inclusion, *Information and Computation* 200 (July 2005) 35–61.
- [48] H. Kress-Gazit, G.E. Fainekos, G.J. Pappas, Where's Waldo? Sensor-based temporal logic motion planning, in: Proceedings of the IEEE International Conference on Robotics and Automation (ICRA), 2007, pp. 3116–3121.
- [49] H. Kress-Gazit, G.E. Fainekos, G.J. Pappas, Temporal-logic-based reactive mission and motion planning, *IEEE Transactions on Robotics* 25 (6) (2009) 1370–1381.
- [50] O. Kupferman, M.Y. Vardi, Module checking, in: Proceedings of the International Conference Computer Aided Verification (CAV), 1996, pp. 75–86.
- [51] O. Kupferman, M.Y. Vardi, Church's problem revisited, *The Bulletin of Symbolic Logic* 5 (2) (1999) 245–263.
- [52] R. Lundy, L. Karlsson, A. Saffiotti, Plan-based configuration of an ecology of robots, in: Proceedings of the IEEE International Conference on Robotics and Automation (ICRA), 2007, pp. 64–70.
- [53] R. Lundy, L. Karlsson, A. Saffiotti, Automatic configuration of multi-robot systems: Planning for multiple steps, in: Proceedings of the European Conference in Artificial Intelligence (ECAI), 2008, pp. 616–620.
- [54] Y. Lustig, M.Y. Vardi, Synthesis from component libraries, in: Proceedings of the International Conference on Foundations of Software Science and Computational Structures (FOSSACS), in: LNCS, vol. 5504, Springer, 2009, pp. 395–409.
- [55] O. Marin, M. Bertier, P. Sens, DARX – a framework for the fault tolerant support of agent software, in: Proceedings of the IEEE International Symposium on Software Reliability Engineering (ISSRE), 2003, pp. 406–418.
- [56] D.L. Martin, M.H. Burstein, D.V. McDermott, S.A. McIlraith, M. Paolucci, K.P. Sycara, D.L. McGuinness, E. Sirin, N. Srinivasan, Bringing semantics to web services with OWL-S, in: Proceedings of the International Conference on World Wide Web (WWW), 2007, pp. 243–277.
- [57] S.A. McIlraith, T.C. Son, Adapting golog for composition of semantic web services, in: Proceedings of Principles of Knowledge Representation and Reasoning (KR), 2002, pp. 482–496.
- [58] S.A. McIlraith, T.C. Son, H. Zeng, Semantic web services, *IEEE Intelligent Systems* 16 (2) (2001) 46–53.
- [59] K.L. McMillan, *Symbolic Model Checking*, Kluwer Academic Publishers, Norwell, MA, USA, 1993.
- [60] R. Milner, An algebraic definition of simulation between programs, in: Proceedings of the International Joint Conference on Artificial Intelligence (IJCAI), 1971, pp. 481–489.
- [61] A. Muscholl, I. Walukiewicz, A lower bound on web services composition, *Logical Methods in Computer Science* 4 (2) (2008).
- [62] D.S. Nau, T.-C. Au, O. Ilghami, U. Kuter, J.W. Murdock, D. Wu, F. Yaman, SHOP2: An HTN planning system, *Journal of Artificial Intelligence Research* 20 (2003) 379–404.
- [63] M.P. Papazoglou, P. Traverso, S. Dustdar, F. Leymann, Service-oriented computing: State of the art and research challenges, *IEEE Computer* 40 (11) (2007) 38–45.
- [64] O. Pettersson, Execution monitoring in robotics: A survey, *Robotics and Autonomous Systems* 53 (2) (2005) 73–88.
- [65] M. Pistore, F. Barbon, P. Bertoli, D. Shaparau, P. Traverso, Planning and monitoring web service composition, in: Proceedings of the Artificial Intelligence: Methodology, Systems, and Applications (AIMSA), in: LNCS, vol. 3192, Springer, 2004, pp. 106–115.
- [66] M. Pistore, A. Marconi, P. Bertoli, P. Traverso, Automated composition of web services by planning at the knowledge level, in: Proceedings of the International Joint Conference on Artificial Intelligence (IJCAI), 2005, pp. 1252–1259.
- [67] M. Pistore, P. Traverso, Planning as model checking for extended goals in non-deterministic domains, in: Proceedings of the International Joint Conference on Artificial Intelligence (IJCAI), 2001, pp. 479–486.
- [68] M. Pistore, P. Traverso, P. Bertoli, A. Marconi, Automated synthesis of composite BPEL4WS web services, in: Proceedings of the IEEE International Conference on Web Services (ICWS), 2005, pp. 293–301.
- [69] N. Piterman, A. Pnueli, Y. Sa'ar, Synthesis of Reactive (1) Designs, in: Proceedings of the International Conference on Verification, Model Checking, and Abstract Interpretation (VMCAI), 2006, pp. 364–380.
- [70] A. Pnueli, R. Rosner, On the synthesis of a reactive module, in: Proceedings of the ACM SIGPLAN-SIGACT Symposium on Principles of Programming Languages (POPL), 1989, pp. 179–190.
- [71] A. Pnueli, E. Shahar, A platform for combining deductive with algorithmic verification, in: Proceedings of the International Conference Computer Aided Verification (CAV), 1996, pp. 184–195.
- [72] D.V. Pynadath, M. Tambe, N. Chauvat, L. Cavedon, Toward team-oriented programming, in: Proceedings of the International Workshop on Agent Theories, Architectures, and Languages (ATAL), Springer, 2000, pp. 233–247.
- [73] R. Ragab Hassen, L. Nourine, F. Toumani, Protocol-based web service composition, in: Proceedings of the International Joint Conference on Service Oriented Computing (ICSOC), in: LNCS, vol. 5364, Springer, 2008, pp. 38–53 (Chapter 7).
- [74] P.J. Ramadge, W.M. Wonham, Supervisory control of a class of discrete event processes, *SIAM Journal on Control and Optimization* 25 (1987) 206–230.
- [75] A.S. Rao, AgentSpeak(L): BDI agents speak out in a logical computable language, in: Proceedings of the Seventh European Workshop on Modelling Autonomous Agents in a Multi-Agent World (Agents Breaking Away), in: LNCS, vol. 1038, Springer, 1996, pp. 42–55.
- [76] A. Saffiotti, M. Broxvall, PEIS ecologies: Ambient intelligence meets autonomous robotics, in: Proceedings of the International Conference on Smart Objects and Ambient Intelligence, 2005, pp. 275–280.

- [77] S. Sardina, G. De Giacomo, Realizing multiple autonomous agents through scheduling of shared devices, in: Proceedings of the International Conference on Automated Planning and Scheduling (ICAPS), 2008, pp. 304–312.
- [78] S. Sardina, G. De Giacomo, Composition of ConGolog programs, in: Proceedings of the International Joint Conference on Artificial Intelligence (IJCAI), 2009, pp. 904–910.
- [79] S. Sardina, F. Patrizi, G. De Giacomo, Automatic synthesis of a global behavior from multiple distributed behaviors, in: Proceedings of the National Conference on Artificial Intelligence (AAAI), 2007, pp. 1063–1069.
- [80] S. Sardina, F. Patrizi, G. De Giacomo, Behavior composition in the presence of failure, in: Proceedings of Principles of Knowledge Representation and Reasoning (KR), 2008, pp. 640–650.
- [81] M.J. Schoppers, Universal plans for reactive robots in unpredictable environments, in: Proceedings of the International Joint Conference on Artificial Intelligence (IJCAI), 1987, pp. 1039–1046.
- [82] E. Sirin, B. Parsia, D. Wu, J. Hendler, D. Nau, HTN planning for web service composition using SHOP2, Journal of Web Semantics: Science, Services and Agents on the World Wide Web 1 (4) (October 2004) 377–396.
- [83] S. Sohrabi, N. Prokoshyna, S.A. McIlraith, Web service composition via generic procedures and customizing user preferences, in: Proceedings of the International Semantic Web Conference (ISWC), 2006, pp. 597–611.
- [84] S. Sohrabi, N. Prokoshyna, S.A. McIlraith, Web service composition via the customization of golog programs with user preferences, in: A.T. Borgida, V.K. Chaudhri, P. Giorgini, E.S. Yu (Eds.), Conceptual Modeling: Foundations and Applications, Springer, 2009, pp. 319–334 (Chapter Web and Services).
- [85] T. Stroeder, M. Pagnucco, Realising deterministic behaviour from multiple non-deterministic behaviours, in: Proceedings of the International Joint Conference on Artificial Intelligence (IJCAI), 2009, pp. 936–941.
- [86] J. Su (Ed.), IEEE Data Engineering Bulletin 31 (September 2008).
- [87] L. Tan, R. Cleaveland, Simulation revisited, in: Proceedings of Tools and Algorithms for the Construction and Analysis of Systems (TACAS), 2001, pp. 480–495.
- [88] A. Tripathi, R. Miller, Exception handling in agent-oriented systems, in: A. Romanovsky, C. Dony, J. Knudsen, A. Tripathi (Eds.), Advances in Exception Handling Techniques, in: LNCS, vol. 2022, Springer, 2001, pp. 128–146.
- [89] M.Y. Vardi, An automata-theoretic approach to fair realizability and synthesis, in: Proceedings of the International Conference Computer Aided Verification (CAV), 1995, pp. 267–278.
- [90] W. Wonham, P. Ramadge, On the supremal controllable sub-language of a given language, SIAM Journal on Control and Optimization 25 (3) (1987) 637–659.
- [91] N. Yadav, S. Sardina, Decision theoretic behavior composition, in: Yolum Turner, Stone Sonenberg (Eds.), Proceedings of Autonomous Agents and Multi-Agent Systems (AAMAS), 2011, pp. 575–582.
- [92] N. Yadav, S. Sardina, Qualitative approximate behavior composition, in: Proceedings of the European Conference on Logics in Artificial Intelligence (JELIA), in: LNCS, vol. 7519, Springer, 2012, pp. 450–462.