Math 114 Assignment 4

Due: Friday Nov 18 by Noon, 12:00pm.

Section 2.8 10, 30

10. Suppose $4x^2 + 9y^2 = 36$, where x and y are functions of t.

(a) If $dy/dt = \frac{1}{3}$, find dx/dt when x = 2 and $y = \frac{2}{3}\sqrt{5}$.

(b) If dx/dt = 3, find dy/dt when x = -2 and $y = \frac{2}{3}\sqrt{5}$.

30. A kite 100 ft above the ground moves horizontally at a speed of 8 ft/s. At what rate is the angle between the string and the horizontal decreasing when 200 ft of string has been let out?

Section 2.9 2, 12, 26

1–4 Find the linearization L(x) of the function at a.

2. $f(x) = \sin x$, $a = \pi/6$

11–14 Find the differential dy of each function.

12. (a) $y = \frac{1+2u}{1+3u}$

(b) $y = \theta^2 \sin 2\theta$

23–28 Use a linear approximation (or differentials) to estimate the given number.

26. $\sqrt{100.5}$

Section 3.1 22, 40, 42, 52

15–28 Sketch the graph of f by hand and use your sketch to find the absolute and local maximum and minimum values of f. (Use the graphs and transformations of Sections 1.2 and 1.3.)

22. $f(t) = \cos t$, $-3\pi/2 \le t \le 3\pi/2$

29–42 Find the critical numbers of the function.

40. $g(\theta) = 4\theta - \tan \theta$

42. $g(x) = \sqrt{1 - x^2}$

45–56 Find the absolute maximum and absolute minimum values of f on the given interval.

52. $f(x) = \frac{x}{x^2 - x + 1}$, [0, 3]

Section 3.2 18

18. Let f(x) = 2 - |2x - 1|. Show that there is no value of c such that f(3) - f(0) = f'(c)(3 - 0). Why does this not contradict the Mean Value Theorem?