$$L = \int \sqrt{1 + (\frac{1}{X} - \frac{1}{4}X)^{2}} dX = \int \sqrt{\frac{1}{2} + \frac{1}{X^{2}} + \frac{1}{16}X^{2}} dX$$

$$= \int \sqrt{(\frac{1}{X} + \frac{1}{4}X)^{2}} dX = \int (\frac{1}{X} + \frac{1}{4}X) dX$$

$$= \ln(X) + \frac{X^{2}}{8} \Big|_{1}^{6} = \ln(6) + \frac{6^{2}}{8} - \ln(1) - \frac{1}{8}$$

$$= \ln(6) + \frac{35}{8}$$