Assignment: Terminal Velocity and Round-Off Error **Due: 9:05 am, Wed Sep. 28**

Write a Python program to calculate the terminal velocity of a drop with radius from 1 to $10 \, \mu m$. Use the equation from the notes and numerical constants given on page 2 of this assignment. Calculate the terminal velocity at 1000 points evenly spaced between a drop radius of 1 and 10 μm . Output the drop radius and terminal velocity to a file. Use Python to create a plot of drop radius versus terminal velocity.

Modify the Python program you wrote from above to calculate the relative error for the following two cases.

Case 1: If you only used one significant figure for all numerical constants.

Case 2: If you use 32-bit floating-point constants and variables for your calculations.

For the "true" values, use the value obtained when using all 64-bit constants and variables (the original code above).

Output your answers to a file with three columns:

Radius Case 1 relative error Case 2 relative error

Also plot the two cases on a single plot (use a legend). Make sure the y-axis is logarithmic.

Concept Question:

Iterative Solutions

Numerical solutions are often iterative, meaning that each step forward in the solution depends on the previous step.

- a) Explain why this current solution is not iterative.
- b) How might the problem be changed to become iterative?

Round-off Errors

- a) Describe at least one <u>specific</u> example of numerical round-off error due to floating point representation in this program. Explain why this error occurs.
- b) Does this error have a significant impact on the numerical analysis? Why or why not?

Write a concise summary of the program.

See the class website for the rubric used for grading the report.

Absolute Error - The magnitude of the difference between the approximation $(\widehat{\chi})$ and the true value $(\widehat{\chi})$.

$$\varepsilon_{abs} = |\tilde{\chi} - \chi|$$

Relative Error – The absolute error relative to the true value.

$$\varepsilon_{rel} = \frac{|\tilde{\chi} - \chi|}{|\chi|}$$

Constants:

Using a temperature of 15 C.

$$\begin{array}{ll} \rho_w &= 999.102 \; kg \; m^{\text{-}3} \\ \rho_a &= 1.229 \; kg \; m^{\text{-}3} \\ \eta &= 1.812 \; x \; 10^{\text{-}5} \; kg \; m^{\text{-}1} \; s^{\text{-}1} \\ g &= 9.810 \; m \; s^{\text{-}2} \end{array}$$

Math check:

For
$$r = 2.5 \text{ x } 10^{-6} \text{ m}$$
, $v_t = 7.5 \text{ x } 10^{-4} \text{ m s}^{-1}$

Some Programming Tips

Python:

- The default variables in Python are 64-bit. To make something 32-bit, use the numpy float32 function.
- To output very small or very large numbers, use exponential format (%e) instead of regular float format (%f).
- To plot with a logarithmic y-axis, use the matplotlib semilogy function.