# Economics 631 IO - Fall 2019 Problem Set 3

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# 1 Production Function Estimation

### 1.1 Summary Statistics

## Summary Statistics - Mean and Variance

Variable	Full Mean	Bal. Mean	Tstat	Full VAR	Bal. VAR	Fstat
ldsal	5.67	6.91	-17.15	3.84	3.38	1.14
lemp	1.26	2.41	-17.94	3.15	2.63	1.20
ldnpt	4.47	5.92	-17.81	4.91	4.23	1.16
ldrst	3.40	4.89	-19.60	4.12	3.72	1.11
$\operatorname{ldrnd}$	1.79	3.22	-18.42	4.21	3.98	1.06
ldinv	2.67	4.07	-17.27	4.71	4.22	1.12

#### Summary Statistics - Min and Max

Variable	Full Min	Bal. Min	Full max	Bal. max
ldsal	-0.86	1.66	11.70	11.70
lemp	-3.77	-2.07	6.73	6.73
ldnpt	-1.39	0.81	11.11	11.11
ldrst	-4.29	0.06	9.97	9.97
$\operatorname{ldrnd}$	-5.31	-2.71	8.43	8.43
ldinv	-3.84	-2.08	8.99	8.89

There appear to be significant differences between the full sample and the balanced panel. In particular, the mean of each of the variables in the balanced panel is higher than that in the full sample, suggesting that firms which stay in the sample for the entire time period are generally larger and invest more. This makes sense, as we'd expect firms who eventually exit the market to be the least productive firms, and therefore produce and invest less. The full panel also has higher variance than the balanced panel, which would make sense as we are including firms with generally lower values relative to the balanced panel, which should increase the variance. The minimum values are similarly lower in the full sample relative to the balanced panel, and the maximum values all appear in the balanced panel. Broadly it seems clear that the balanced panel is a selected sample.

#### 1.2 Production Function Estimation

#### **Production Function Coefficients**

statistic	bias	std.error
0.97	0.05	0.05
0.48	0.05	0.04
0.43	-0.03	0.02
0.05	-0.01	0.01
1.00	0.00	0.00
	0.97 0.48 0.43 0.05	0.97 0.05 0.48 0.05 0.43 -0.03 0.05 -0.01

The production function estimates are reported above, with the bootstrapped standard errors reported on the right. A few things – we interpreted "ignoring the selection issue" to mean using the non-balanced panel and not worrying about the fact that exiting firms should have lower productivity. Estimates using the balanced panel were quite similar. In our reported results we stratified the bootstrap at the firm level, but have also experimented with iid bootstrapping at the observation level. Our concern with the latter was figuring out how to deal with the lagged variables. Realistically the answer is probably to block-bootstrap but we decided to stratify at the firm level as a middle ground.

In terms of the coefficients, a few things to note are that the production function is DRS, but only weakly so – in fact, the coefficients sum to .96, which is much closer to 1 than we expected. We weren't sure what to make of the  $\rho$  being so close to 1. This appears to be the case regardless of which sample we use. This means that any productivity shock is basically entirely persistent. If this were the case we could potentially treat the productivity shocks as a firm-specific fixed effect we could get rid of by differencing.

$$\mathbb{E}[w_{it} - w_{it-1}] = \mathbb{E}[w_{it-1} * \rho + \xi_{it} - w_{it-1}] \approx \mathbb{E}[\xi_{it}] = 0$$

Seems weird, although this potentially points to an error in our code.

# 2 Appendix

## 2.1 R Code

# pset 3 631

```
#======#
# ==== IO Pset 3 ====
#======#
#----#
# ==== load packages/data ====
#======#
 rm(list = ls(pos = ".GlobalEnv"), pos = ".GlobalEnv")
 options(scipen = 999)
 cat("\f")
 library(package)
 library(data.table)
 library(xtable)
 # set option for who is running this
 opt_nate <- TRUE
 # load data and set directories
 if(opt_nate){
   # load data
   gmdt <- fread("c:/Users/Nmath_000/Documents/MI_school/Third Year/Econ 631/ps3/GMdata.csv")</pre>
   f_out <- "c:/Users/Nmath_000/Documents/Code/Econ_631/ps3/"</pre>
   # if running on tyler's computer
   }else{
     # load data from tylers locaiton
    gmdt <- fread("C:/Users/tyler/Box/coursework/Econ_631/ps3/GMdata.csv")</pre>
    f_out <- "C:/Users/tyler/Box/coursework/Econ_631/ps3"</pre>
 }
#======#
# ==== summary stats ====
#======#
 #----#
 # ==== Make balanced panel ====
 #=======#
```

```
# make the balanced panel version of data
 # first get number of years by firm
 gmdt[, num_years := .N, index]
 # check how many are in each group
 gmdt[, .N, num_years]
 # make balanced panel
 gmdt_b <- gmdt[num_years == max(gmdt$num_years)]</pre>
 # drop variable
 gmdt[, num_years := NULL]
 gmdt_b[, num_years := NULL]
# ==== do comparison ====
#======#
 # make list of variables
 vars <- grep("1", colnames(gmdt_b), value = TRUE)</pre>
 # get each column of summart stats
 sum_stats_li <- list()</pre>
 sum_stats_li[[1]] <- data.table(Variable = vars)</pre>
 # means
 sum_stats_li[[2]] <- gmdt[, list("Full Mean" = lapply(.SD, mean)), .SDcols = vars]</pre>
 sum_stats_li[[3]] <- gmdt_b[, list("Bal. Mean" = lapply(.SD, mean)), .SDcols = vars]</pre>
 # t.test for mean equlity
 # function to do it
 tstat_fun <- function(var_i){</pre>
 res <- t.test(gmdt[, get(var_i)], gmdt_b[, get(var_i)])</pre>
 return(res$statistic)
 }
 # apply over variales
 sum_stats_li[[4]] <- data.table( "Tstat" = unlist(lapply(vars, tstat_fun)))</pre>
 # varianvce
 sum_stats_li[[5]] <- gmdt[, list("Full VAR" = lapply(.SD, var)), .SDcols = vars]</pre>
 sum_stats_li[[6]] <- gmdt_b[, list("Bal. VAR" = lapply(.SD, var)), .SDcols = vars]</pre>
 # fstat for equalit of variance
 ftest_fun <- function(var_i){</pre>
   res <- var.test(gmdt[, get(var_i)], gmdt_b[, get(var_i)])</pre>
   return(res$statistic)
 }
  #apply over variables
```

```
sum_stats_li[[7]] <- data.table( "Fstat" = unlist(lapply(vars, ftest_fun)))</pre>
   #min
   sum_stats_li[[8]] <- gmdt[, list("Full Min" = lapply(.SD, min)), .SDcols = vars]</pre>
   sum_stats_li[[9]] <- gmdt_b[, list("Bal. Min" = lapply(.SD, min)), .SDcols = vars]</pre>
   sum_stats_li[[10]] <- gmdt[, list("Full max" = lapply(.SD, max)), .SDcols = vars]</pre>
   sum_stats_li[[11]] <- gmdt_b[, list("Bal. max" = lapply(.SD, max)), .SDcols = vars]</pre>
   # get variance
   sum_stats <- do.call(cbind, sum_stats_li)</pre>
   #check it out!
   sum_stats
 #=======#
 # ==== save table to tex ====
 #=======#
   # split this into two tables
   sum_stat_1 <- sum_stats[, 1:7, with=FALSE]</pre>
   sum_stat_2 <- sum_stats[, c(1, 8:11), with = FALSE]</pre>
   # save summary stats
   print(xtable(sum_stat_1, type = "latex"),
         file = pasteO(f_out, "sum_stats_1.tex"),
         include.rownames = FALSE,
         floating = FALSE)
   print(xtable(sum_stat_2, type = "latex"),
         file = pasteO(f_out, "sum_stats_2.tex"),
         include.rownames = FALSE,
         floating = FALSE)
#----#
# ==== Estimate Production Function ==== #
#=======#
   # Step 1: Get measurement error from second-order polynomial
   # (including interactions) of emp, dnpt, drst and investment
   setnames(gmdt, c("ldsal", "ldnpt", "ldrst"), c("lsales","lcap", "lrdcap"))
   gmdt[,dummy:=1]
   # do it for balanced too just for fun
   setnames(gmdt_b, c("ldsal", "ldnpt", "ldrst"), c("lsales","lcap", "lrdcap"))
```

```
gmdt_b[,dummy:=1]
#=======#
# ==== internal functions ====
#======#
 in_data <- gmdt
 get_resid_fun <- function(in_data){</pre>
   dt_copy <- copy(in_data)</pre>
   X <- as.matrix(dt_copy[,.(dummy, lemp,lcap,lrdcap,ldinv, lemp*lemp,lemp*lcap, lemp*lrdcap,</pre>
                            lemp*ldinv,lcap*lcap,lcap*lrdcap,lcap*ldinv,lrdcap*lrdcap,lrdcap*ldinv,ld
   Y <- as.matrix(dt_copy[,.(lsales)])
   # Get the coefficients of all these interactions
   beta1 <- solve(t(X)%*%X)%*%t(X)%*%Y
   # Get the fitted values
   theta <- X%*%beta1
   # Add the fitted values to the datatable
   dt_copy[,theta:= theta]
   # get lags of emp, cap, rdcap and theta, remove observations without lag values
   cols = c("lemp","lcap","lrdcap", "theta")
   anscols = paste("lag", cols, sep="_")
   dt_copy[, (anscols) := shift(.SD, 1, NA, "lag"), .SDcols=cols]
   dt_copy <- dt_copy[!is.na(lag_lemp),]</pre>
   return(dt_copy)
 }
 # ttest the funciton
 gmdt2 <- get_resid_fun(gmdt)</pre>
 # function to run GMM
  # a lot of inputs here but this is how you get around using global objects
 # THis is supposed to be better practice but it doe sget a bit wild with all these
 gmm_obj_f <- function(parm_vector.in,</pre>
                        Y.in = Y,
                        X.in = X,
                        1X.in = 1X,
                        ltheta.in = ltheta,
                        Z.in = Z,
                        W.in = W){
   beta <- as.matrix(parm_vector.in[1:4])</pre>
```

```
rho <- parm_vector.in[5]</pre>
  current.resid <- Y.in - X.in%*%beta
  lag.w <- as.matrix(ltheta.in) - lX.in%*%beta</pre>
  m <- current.resid - rho*lag.w</pre>
  m <- as.matrix(m)</pre>
  distance <- t(Z.in) %*%m
  result <- t(distance/length(m)) %*% W.in %*% (distance/length(m))
  # get function value
 return(result)
parm_vector \leftarrow c(1, .6, .2, .2, .8)
# Get X's and lag X's and Zs for GMM estimation
X <- as.matrix(gmdt2[,.(dummy, lemp, lcap, lrdcap)])</pre>
1X <- as.matrix(gmdt2[,.(dummy, lag_lemp, lag_lcap, lag_lrdcap)])</pre>
Z <- as.matrix(gmdt2[,.(dummy, lag_lemp, lcap, lrdcap)])</pre>
Y <- as.matrix(gmdt2[,.(lsales)])</pre>
ltheta <- as.matrix(gmdt2[,.(lag_theta)])</pre>
W \leftarrow diag(1, 4, 4)
# test it out
f <- gmm_obj_f(parm_vector.in = parm_vector,</pre>
                       = Y,
               Y.in
               X.in
                              = X,
               lX.in
                              = 1X,
               ltheta.in = ltheta,
               Z.in
                              = Z,
                              = W)
               W.in
# Run the initial GMM using the identity matrix as the weighting matrix
Results.step1 <- optim(par = parm_vector,</pre>
                                    = gmm_obj_f,
                         fn
                         Y.in
                                     = Y
                         X.in
                                     = X,
                                     = 1X,
                         ltheta.in = ltheta,
                         Z.in
                                     = Z.
                         W.in
                                     = W)
# Function to calculate optimal weighting matrix
find.optimal.W <- function(results.in,</pre>
                            Y.in = Y,
                            X.in = X,
                            1X.in = 1X,
                            ltheta.in = ltheta,
                            Z.in = Z){
```

```
beta <- as.matrix(results.in$par[1:4])</pre>
      rho <- results.in$par[5]</pre>
     current.resid <- Y.in - X.in\*\beta
     lag.w <- as.matrix(ltheta.in) - lX.in%*%beta</pre>
     m <- current.resid - rho*lag.w</pre>
     m <- as.matrix(m)</pre>
     distance \leftarrow t(Z.in*cbind(m, m, m, m))%*%(Z.in*cbind(m, m, m, m))
     W <- distance/length(m)
     W.inv <- solve(W)
 return(W.inv)
 # Get optimal weighting matrix
 W.opt <- find.optimal.W(results.in = Results.step1,</pre>
                           Y.in = Y,
                          X.in = X,
                          1X.in = 1X,
                          ltheta.in = ltheta,
                          Z.in = Z)
 # Run again with optimal weighting matrix
 Results.final <- optim(par
                                = parm_vector,
                    fn
                               = gmm_obj_f,
                    Y.in = Y,
                    X.in = X,
                    1X.in = 1X,
                    ltheta.in = ltheta,
                    Z.in = Z,
                    W.in = W.opt)
#======#
# ==== boot function ====
#======#
 in_data <- gmdt
 sample <- 1:nrow(in_data)</pre>
 to_boot_fun <- function(in_data, sample){</pre>
   boot_dt <- in_data[sample]</pre>
    # get resids
   boot_dt <- get_resid_fun(boot_dt)</pre>
   parm_vector \leftarrow c(1, .6, .2, .2, .8)
    \# Get X's and lag X's and Zs for GMM estimation
```

```
X <- as.matrix(boot_dt[,.(dummy, lemp, lcap, lrdcap)])</pre>
 1X <- as.matrix(boot_dt[,.(dummy, lag_lemp, lag_lcap, lag_lrdcap)])</pre>
 Z <- as.matrix(boot_dt[,.(dummy, lag_lemp, lcap, lrdcap)])</pre>
 Y <- as.matrix(boot dt[,.(lsales)])
 ltheta <- as.matrix(boot_dt[,.(lag_theta)])</pre>
 W \leftarrow diag(1, 4, 4)
  # test it out
 f <- gmm_obj_f(parm_vector.in = parm_vector,</pre>
                Y.in = Y,
                Z.in
                              = Z
                W.in
                              = W)
  # Run the initial GMM using the identity matrix as the weighting matrix
  Results.step1 <- optim(par = parm_vector,</pre>
                         fn
                                   = gmm_obj_f,
                                  = Y,
                         Y.in
                         X.in
                                   = X,
                         1X.in = 1X,
                         ltheta.in = ltheta,
                                   = Z,
                         Z.in
                                    = W)
                         W.in
  # Get optimal weighting matrix
 W.opt <- find.optimal.W(results.in = Results.step1,</pre>
                         Y.in = Y,
                         X.in = X,
                         1X.in = 1X,
                         ltheta.in = ltheta,
                         Z.in = Z
  # Run again with optimal weighting matrix
 Results.final <- optim(par = parm_vector,
                                    = gmm_obj_f,
                         fn
                         Y.in = Y,
                         X.in = X,
                         1X.in = 1X,
                         ltheta.in = ltheta,
                         Z.in = Z,
                         W.in = W.opt)
 return(Results.final$par)
}
to_boot_fun(gmdt, 1:(nrow(gmdt)))
# set seed and run boot
set.seed(1234)
```

```
boot_res <- boot(data = gmdt, statistic = to_boot_fun, R = 1000, strata = gmdt$index)</pre>
 # boot_res <- boot(data = qmdt_b, statistic = to_boot_fun, R = 1000, strata = qmdt_b$index)
 # boot_res2 <- boot(data = gmdt_b, statistic = to_boot_fun, R = 1000)</pre>
 # boot_res3 <- boot(data = gmdt, statistic = to_boot_fun, R = 1000)
# put it in a table
boot_dt <- data.table(broom::tidy(boot_res))</pre>
# add parameter names
parms <- c("B_0", "L", "K", "RD", "P")</pre>
boot_dt[, parm := parms]
setcolorder(boot_dt, "parm")
# save table
print(xtable(boot_dt, type = "latex"),
      file = pasteO(f_out, "boot_res.tex"),
      include.rownames = FALSE,
      floating = FALSE)
 #=======#
# ==== run r markdown for tex file ====
#======#
rmarkdown::render(input = "C:/Users/Nmath_000/Documents/Code/Econ_631/ps3/ps3_r_markdown.Rmd",
                  output_format = "pdf_document",
                  output_file = paste0(f_out, "assignment_3_r_code_pdf.pdf"))
```