

# 1 MeLSI: Metric Learning for Statistical Inference in 2 Microbiome Community Composition Analysis

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## 6 ABSTRACT

7 Microbiome beta diversity analysis relies on distance-based methods including  
8 PERMANOVA combined with fixed ecological distance metrics (Bray-Curtis, Euclidean,  
9 Jaccard, and UniFrac), which treat all microbial taxa uniformly regardless of their biological  
10 relevance to community differences. This “one-size-fits-all” approach may miss subtle but  
11 biologically meaningful patterns in complex microbiome data. We present MeLSI (Metric  
12 Learning for Statistical Inference), a novel machine learning framework that learns data-  
13 adaptive distance metrics optimized for detecting community composition differences in  
14 multivariate microbiome analyses. MeLSI employs an ensemble of weak learners using  
15 bootstrap sampling, feature subsampling, and gradient-based optimization to learn  
16 optimal feature weights, combined with rigorous permutation testing for statistical  
17 inference. The learned metrics can be used with PERMANOVA for hypothesis testing and  
18 with Principal Coordinates Analysis (PCoA) for ordination visualization. Comprehensive  
19 validation on synthetic benchmarks and real datasets shows that MeLSI maintains proper  
20 Type I error control while delivering competitive or superior F-statistics when signal  
21 structure aligns with CLR-based weighting and, crucially, supplies interpretable feature-  
22 weight profiles that clarify which taxa drive group separation. On the Atlas1006 dataset,  
23 MeLSI achieved stronger effect sizes than the best traditional methods, and even when  
24 performance was comparable, the learned feature weights provided biological insight that  
25 fixed metrics cannot supply. MeLSI therefore offers a statistically rigorous tool that  
26 augments beta diversity analysis with transparent, data-driven interpretability.

## 27 IMPORTANCE

28 Understanding which microbes differ between groups of interest could reveal therapeutic  
29 targets and diagnostic biomarkers. However, current analysis methods treat all microbes  
30 equally (similar to using the same ruler to measure everything, regardless of what matters  
31 most). This means subtle but clinically important differences may go undetected,  
32 especially when only a few key species drive disease while hundreds of “bystander”  
33 species add noise. MeLSI solves this by learning which microbes matter most for each  
34 specific comparison. In comparing male and female gut microbiomes, MeLSI identified  
35 specific bacterial families driving the differences, providing actionable biological insights  
36 that standard methods miss. This capability is particularly crucial for detecting early

37 disease biomarkers, where differences are subtle and masked by biological variability. By  
38 telling researchers not just whether groups differ, but which specific microbes drive those  
39 differences, MeLSI accelerates the path from microbiome data to testable biological  
40 hypotheses and clinical applications.

41 **Keywords:** microbiome analysis, metric learning, beta diversity, community composition,  
42 PERMANOVA, distance metrics, permutation testing

## 43 INTRODUCTION

### 44 The microbiome and human health

45 The human microbiome, the complex community of microorganisms inhabiting our bodies,  
46 plays fundamental roles in health and disease (1, 2). Recent advances in high-throughput  
47 sequencing technologies have enabled comprehensive profiling of microbial communities,  
48 revealing associations between microbiome composition and diverse conditions including  
49 inflammatory bowel disease, obesity, diabetes, and neurological disorders (3, 4). A central  
50 question in microbiome research is comparing overall microbial community composition  
51 between groups of interest, typically assessed through beta diversity analysis, which  
52 studies compositional differences between samples.

### 53 Current approaches and their limitations

54 Microbiome beta diversity analysis predominantly relies on distance-based multivariate  
55 methods including PERMANOVA (Permutational Multivariate Analysis of Variance)  
56 combined with fixed ecological distance metrics (5, 6). Commonly used metrics include  
57 Bray-Curtis dissimilarity, Euclidean distance, Jaccard index, and phylogenetically-  
58 informed metrics including UniFrac (7). These approaches have proven valuable for  
59 hypothesis testing about community differences and visualization through ordination  
60 methods such as Principal Coordinates Analysis (PCoA) (8).

61 However, fixed distance metrics suffer from a fundamental limitation. They apply the same  
62 mathematical formula to all datasets, treating all microbial taxa with equal importance  
63 regardless of their biological relevance to the specific research question (9). For instance,  
64 Bray-Curtis dissimilarity equally weights all taxa based on their relative abundances, while  
65 Euclidean distance treats all features identically. This “one-size-fits-all” approach may fail  
66 to capture subtle but biologically meaningful differences when only a subset of taxa drive  
67 group separation (10).

68 Furthermore, microbiome data presents unique analytical challenges including high  
69 dimensionality (often hundreds to thousands of taxa), compositionality (relative  
70 abundances sum to a constant), sparsity (many zero counts), and heterogeneous  
71 biological signal across features (11). Fixed metrics cannot adapt to these complexities in  
72 a data-driven manner.

73 **The need for statistical rigor**

74 A critical requirement for any beta diversity method is proper statistical inference with  
75 controlled Type I error rates (false positive rates). While machine learning approaches  
76 often prioritize predictive accuracy, hypothesis testing for community composition  
77 differences requires rigorous F-statistic and p-value calculation under the null hypothesis  
78 of no group differences (12). Permutation testing provides a non-parametric framework for  
79 valid inference that makes minimal distributional assumptions (13), making it particularly  
80 suitable for complex microbiome data and distance-based analyses such as PERMANOVA.

81 **Metric learning: an emerging paradigm**

82 Metric learning, a branch of machine learning, offers a principled approach to address  
83 these limitations (14, 15). Rather than using fixed distance formulas, metric learning  
84 algorithms learn optimal distance metrics from data by identifying which features  
85 contribute most to separating groups of interest. In the context of supervised learning,  
86 metric learning algorithms optimize distance functions to maximize between-group  
87 distances while minimizing within-group distances (16, 17).

88 We formalize metric learning as follows: Let  $\mathbf{X} \in \mathbb{R}^{n \times p}$  denote a feature abundance matrix  
89 with  $n$  samples and  $p$  taxa, and let  $\mathbf{y} = (y_1, \dots, y_n)$  denote group labels. A distance metric is  
90 parameterized by a positive semi-definite matrix  $\mathbf{M} \in \mathbb{R}^{p \times p}$ , where the Mahalanobis  
91 distance between samples  $i$  and  $j$  is  $d_M(\mathbf{x}_i, \mathbf{x}_j) = \sqrt{(\mathbf{x}_i - \mathbf{x}_j)^T \mathbf{M} (\mathbf{x}_i - \mathbf{x}_j)}$ . For diagonal  $\mathbf{M}$ ,  
92 this reduces to weighted Euclidean distance with feature-specific weights  $M_{jj}$  representing  
93 the importance of feature  $j$ .

94 Mahalanobis distance learning (18) learns a positive semi-definite matrix  $\mathbf{M}$  that defines  
95 distances as  $d(\mathbf{x}_i, \mathbf{x}_j) = \sqrt{(\mathbf{x}_i - \mathbf{x}_j)^T \mathbf{M} (\mathbf{x}_i - \mathbf{x}_j)}$ . When  $\mathbf{M}$  is diagonal, this reduces to  
96 learning feature-specific weights, providing interpretable importance scores (17).

97 Despite its promise, metric learning has seen limited application in microbiome beta  
98 diversity analysis. Previous work has explored metric learning for clinical prediction tasks  
99 (19), but not specifically for statistical inference in community composition analysis where  
100 rigorous Type I error control is essential.

101 **Study objectives**

102 We developed MeLSI (Metric Learning for Statistical Inference) to bridge the gap between  
103 adaptive machine learning approaches and rigorous statistical inference for microbiome  
104 beta diversity and community composition analysis. Our specific objectives were to (1)  
105 design an ensemble metric learning framework that learns data-adaptive distance metrics  
106 for PERMANOVA and ordination while preventing overfitting, (2) integrate metric learning  
107 with permutation testing to ensure valid statistical inference, (3) comprehensively validate  
108 Type I error control, statistical power, scalability, parameter sensitivity, and computational  
109 efficiency, (4) demonstrate practical utility on real microbiome datasets, and (5) provide

110 interpretable feature importance scores to identify biologically relevant taxa driving  
111 community separation.

112 This paper presents the MeLSI framework, comprehensive validation results, and  
113 discussion of its implications for microbiome beta diversity research.

## 114 MATERIALS AND METHODS

### 115 Overview of the MeLSI framework

116 MeLSI integrates metric learning with permutation-based statistical inference through two  
117 main phases:

#### 118 Phase 1: Metric Learning

119 1. Apply conservative pre-filtering to focus on high-variance features

120 2. For each of B weak learners:

- 121     ○ Bootstrap sample the data
- 122     ○ Subsample features

123     ○ Optimize metric matrix  $\mathbf{M}$  is a gradient descent

124 3. Combine weak learners via performance-weighted ensemble averaging

125 4. Compute robust distance matrix using eigenvalue decomposition

#### 126 Phase 2: Statistical Inference

127 5. Calculate observed F-statistic using the learned metric

128 6. Generate null distribution via permutation testing (relearn metric on each  
129     permutation)

130 7. Compute permutation-based p-value

131 Each component addresses specific challenges in microbiome data analysis while  
132 maintaining statistical validity. The following sections formalize the mathematical  
133 framework and detail each algorithmic component, organized by phase.

#### 134 Phase 1: Metric Learning

##### 135 Problem formulation

136 Let  $\mathbf{X} \in \mathbb{R}^{n \times p}$  denote a feature abundance matrix with  $n$  samples and  $p$  taxa (features), and  
137 let  $\mathbf{y} = (y_1, \dots, y_n)$  denote group labels. Our goal is to learn a distance metric optimized for  
138 separating groups defined by  $\mathbf{y}$  while ensuring valid statistical inference.

139 We parameterize the distance metric using a diagonal positive semi-definite matrix  $\mathbf{M} \in$   
140  $\mathbb{R}^{p \times p}$ , where  $M_{jj}$  represents the weight (importance) of feature  $j$ . The learned Mahalanobis  
141 distance between samples  $i$  and  $k$  is:

$$142 d_M(\mathbf{x}_i, \mathbf{x}_k) = \sqrt{(\mathbf{x}_i - \mathbf{x}_k)^T \mathbf{M} (\mathbf{x}_i - \mathbf{x}_k)}$$

143 For diagonal  $\mathbf{M}$ , this simplifies to a weighted Euclidean distance:

144

145 
$$d_M(\mathbf{x}_i, \mathbf{x}_k) = \sqrt{\sum_j M_{jj} (x_{ij} - x_{kj})^2}$$

146 *Conservative pre-filtering*

147 To improve computational efficiency and reduce noise, MeLSI applies conservative  
148 variance-based pre-filtering. For pairwise comparisons, we calculate a feature importance  
149 score combining mean differences and variance:

150

151 
$$I_j = \frac{|\mu_{1j} - \mu_{2j}|}{\sqrt{\sigma_{1j}^2 + \sigma_{2j}^2}}$$

152 where  $\mu_{1j}$  and  $\mu_{2j}$  are the mean abundances of feature  $j$  in groups 1 and 2, and  $\sigma_{1j}^2$  and  $\sigma_{2j}^2$   
153 are their variances. We retain the top 70% of features by this importance score,  
154 maintaining high statistical power while reducing dimensionality.

155 For multi-group comparisons (3 or more groups), we use ANOVA F-statistics to rank  
156 features and apply the same 70% retention threshold. Critically, this pre-filtering is applied  
157 consistently to both observed and permuted data during null distribution generation to  
158 avoid bias.

159 *Ensemble learning with weak learners*

160 MeLSI constructs an ensemble of  $B$  weak learners (default  $B = 30$ ) to improve robustness  
161 and prevent overfitting. For each weak learner  $b$ :

- 162 1. **Bootstrap sampling:** Draw  $n$  samples with replacement from the original data to  
163 create a bootstrap dataset  $(\mathbf{X}_b, \mathbf{y}_b)$
- 164 2. **Feature subsampling:** Randomly select  $m = \lfloor p \times m_{frac} \rfloor$  features (default  $m_{frac} =$   
165 0.8) without replacement
- 166 3. **Metric optimization:** Learn  $\mathbf{M}_b$  on the bootstrapped, subsampled data

167 The combination of bootstrap sampling (sample-level randomness) and feature  
168 subsampling (feature-level randomness) ensures diversity among weak learners, reducing  
169 overfitting risk (20).

170 *Optimization objective*

171 For each weak learner, we optimize  $\mathbf{M}$  to maximize between-group distances while  
172 minimizing within-group distances. For a two-group comparison (groups  $G_1$  and  $G_2$ ), we  
173 maximize the objective:

174      
$$F(\mathbf{M}) = \frac{1}{|G_1||G_2|} \sum_{i \in G_1} \sum_{k \in G_2} d_M(\mathbf{x}_i, \mathbf{x}_k)^2 - \frac{1}{2|G_1|^2} \sum_{i,j \in G_1} d_M(\mathbf{x}_i, \mathbf{x}_j)^2 - \frac{1}{2|G_2|^2} \sum_{i,j \in G_2} d_M(\mathbf{x}_i, \mathbf{x}_j)^2$$

175      This objective encourages large between-group distances and small within-group  
 176      distances, analogous to maximizing the F-ratio in ANOVA. This formulation is inspired by  
 177      standard metric learning objectives that maximize between-class to within-class distance  
 178      ratios (17, 16), adapted here for direct compatibility with PERMANOVA's F-statistic  
 179      framework.

180      *Gradient-based optimization*

181      Each weak learner optimizes its metric matrix  $\mathbf{M}$  using stochastic gradient descent,  
 182      sampling within-group and between-group pairs to compute gradients that maximize  
 183      between-group distances while minimizing within-group distances. We use an adaptive  
 184      learning rate  $\eta_t = \eta_0 / (1 + 0.1t)$  (default  $\eta_0 = 0.1$ ) and constrain  $M_{jj} \geq 0.01$  to ensure  
 185      positive definiteness. Early stopping monitors F-statistics every 20 iterations, terminating if  
 186      performance stagnates (no improvement for 5 consecutive checks) to prevent overfitting.

187      *Ensemble averaging with performance weighting*

188      After training all weak learners, we combine them into a final ensemble metric  $\mathbf{M}_{ensemble}$   
 189      using performance-weighted averaging:

190      
$$\mathbf{M}_{ensemble} = \sum_b w_b \mathbf{M}_b$$

191      where weights are normalized F-statistics:

192      
$$w_b = \frac{F_b}{\sum_{b'} F_{b'}}$$

193      and  $F_b$  is the PERMANOVA F-statistic achieved by weak learner  $b$  on its bootstrap sample.  
 194      This weighting scheme emphasizes better-performing learners while maintaining diversity.

195      *Robust distance calculation*

196      To ensure numerical stability, we compute the learned Mahalanobis distance using  
 197      eigenvalue decomposition:

- 198      1. Compute eigendecomposition:  $\mathbf{M}_{ensemble} = \mathbf{V}\Lambda\mathbf{V}^T$  where  $\mathbf{V}$  is the matrix of  
 199      eigenvectors and  $\Lambda$  is the diagonal matrix of eigenvalues
- 200      2. Enforce positive eigenvalues:  $\max(\Lambda_{ii}, 10^{-6}) \rightarrow \Lambda_{ii}$
- 201      3. Compute  $\mathbf{M}^{-1/2} = \mathbf{V}\Lambda^{-1/2}\mathbf{V}^T$
- 202      4. Transform data:  $\mathbf{Y} = \mathbf{X}\mathbf{M}^{-1/2}$
- 203      5. Calculate Euclidean distances in transformed space:  $d_M = \|\mathbf{y}_i - \mathbf{y}_k\|_2$

204 This approach is more numerically stable than direct matrix inversion, particularly for high-  
205 dimensional data.

## 206 Phase 2: Statistical Inference

207 Phase 2 focuses on statistical inference using the learned metric from Phase 1. We  
208 compute p-values through permutation testing to ensure valid statistical inference.

### 209 Statistical inference via permutation testing

#### 210 *Test statistic*

211 We use the PERMANOVA F-statistic as our test statistic (5):

$$212 \quad F_{obs} = \frac{SS_{between}/(k - 1)}{SS_{within}/(n - k)}$$

213 where  $SS_{between}$  is the between-group sum of squares,  $SS_{within}$  is the within-group sum of  
214 squares,  $k$  is the number of groups, and  $n$  is the total number of samples. This statistic  
215 measures how well the learned metric separates groups relative to within-group variation.

#### 216 *Null distribution generation*

217 To compute valid p-values, we generate a null distribution under the hypothesis of no  
218 group differences:

- 219 1. Permute group labels: random permutation of  $\mathbf{y} \rightarrow \mathbf{y}_{perm}$
- 220 2. Apply identical pre-filtering to permuted data
- 221 3. Learn metric  $\mathbf{M}_{perm}$  on  $(\mathbf{X}_{filtered}, \mathbf{y}_{perm})$  using the full MeLSI algorithm (repeating  
222 Phase 1: pre-filtering, ensemble construction, and metric optimization)
- 223 4. Calculate  $F_{perm}$  on  $(\mathbf{X}_{filtered}, \mathbf{y}_{perm})$  with  $\mathbf{M}_{perm}$
- 224 5. Repeat steps 1-4 for  $n_{perms}$  permutations (default  $n_{perms} = 200$ )

225 This approach ensures that the null distribution accurately reflects the variability  
226 introduced by the metric learning procedure itself, avoiding anticonservative (inflated Type  
227 I error) inference.

#### 228 *P-value calculation*

229 The permutation-based p-value is computed as:

$$230 \quad p = \frac{\sum \mathbb{I}(F_{perm} \geq F_{obs}) + 1}{n_{perms} + 1}$$

231 where  $\mathbb{I}$  is the indicator function. The “+1” terms provide a small-sample correction  
232 ensuring  $p \geq 1/(n_{perms} + 1)$  (21).

233 **Validation experiments**

234 We conducted comprehensive validation experiments to assess:

235 **Type I error control and statistical power:** Performance on null data (no true group  
236 differences) and ability to detect true effects of varying magnitude across synthetic  
237 datasets (Sections 3.1-3.2) 2. Scalability: Performance across varying sample sizes and  
238 dimensionalities (Section 3.3) 3. Parameter sensitivity: Robustness to hyperparameter  
239 choices (Section 3.4) 4. Feature correlation robustness: Performance under varying levels  
240 of feature correlation (Section 3.5) 5. Pre-filtering value: Benefit of conservative feature  
241 pre-filtering (Section 3.6) 6. Real data validation: Comparative performance against  
242 standard distance metrics on Atlas1006, DietSwap, and SKIOME datasets (Section 3.7) 7.  
243 Biological interpretability: Feature importance weights and visualization (Section 3.8) 8.  
244 Computational performance: Runtime characteristics on standard hardware (Section 3.9)

245 *Synthetic data generation*

246 Synthetic datasets were generated using negative binomial count distributions to mimic  
247 microbiome abundance profiles. For each experiment we drew counts as  $X_{ij} \sim NB(\mu =$   
248 30, size = 0.8) and set values smaller than three to zero to induce sparsity. Unless  
249 otherwise noted, we simulated  $n = 100$  samples and  $p = 200$  taxa split evenly across two  
250 groups. To introduce signal we multiplied a subset of taxa in the first group by fold changes  
251 of 1.5 (5 taxa, “small” effect), 2.0 (10 taxa, “medium” effect), or 3.0 (20 taxa, “large” effect).  
252 Sample size ( $n$ ) and dimensionality ( $p$ ) were varied in the scalability experiments (Section  
253 3.3), while null datasets were formed by random label permutations or by shuffling labels  
254 in real data without adding signal.

255 *Real data sources*

256 Real microbiome datasets included:

- 257 1. **Atlas1006** (22): 1,114 Western European adults with 123 genus-level taxa from  
258 HITChip microarray technology. Analysis compared males (n=560) versus females  
259 (n=554).
- 260 2. **DietSwap** (23): 74 stool samples from African American adults participating in a  
261 short-term dietary intervention. We analyzed the timepoint-within-group baseline  
262 samples (timepoint.within.group = 1) comparing the Western diet group (HE, n=37)  
263 to the traditional high-fiber diet group (DI, n=37).

264 Data were preprocessed using centered log-ratio (CLR) transformation for Euclidean  
265 distance analyses to address compositionality (24, 11). CLR transformation converts  
266 relative abundances to log-ratios, making the data suitable for Euclidean distance while  
267 preserving relative relationships between taxa. CLR treats abundance ratios more  
268 equitably than count-based metrics, which can be dominated by highly abundant taxa.  
269 However, CLR transformation may attenuate large fold-change signals compared to count-  
270 based metrics (Bray-Curtis, UniFrac), as evidenced by our results showing that traditional

271 count-based methods achieve higher F-statistics on synthetic data with large effects (3×  
272 fold change). CLR is particularly appropriate when signals are distributed across multiple  
273 taxa rather than concentrated in highly abundant taxa, and when interpretability through  
274 feature weights is prioritized. Bray-Curtis dissimilarity, Jaccard, and UniFrac distances  
275 were computed on raw count data, as these metrics are inherently designed to handle  
276 compositional data (25, 7).

277 MeLSI was run with 200 permutations to balance computational efficiency with statistical  
278 precision, while traditional PERMANOVA methods used 999 permutations (the field  
279 standard). This conservative comparison favors traditional methods with more precise p-  
280 value estimation, making our results a stringent test of MeLSI's performance.

### 281 *Comparison methods*

282 MeLSI was compared against standard PERMANOVA analyses using five fixed distance  
283 metrics:

- 284 1. **Euclidean distance:** Standard Euclidean distance calculated on CLR-transformed  
285 data, treating all features equally
- 286 2. **Bray-Curtis dissimilarity:** Count-based dissimilarity metric that accounts for  
287 relative abundances
- 288 3. **Jaccard dissimilarity:** Binary (presence/absence) dissimilarity metric
- 289 4. **Weighted UniFrac:** Phylogenetically-informed distance metric using abundance-  
290 weighted branch lengths (requires phylogenetic tree)
- 291 5. **Unweighted UniFrac:** Phylogenetically-informed distance metric using  
292 presence/absence of taxa along phylogenetic branches (requires phylogenetic tree)

293 To ensure a robust comparison, traditional methods (Weighted/Unweighted UniFrac) were  
294 provided with appropriate phylogenetic structures: random trees for synthetic benchmarks  
295 and published phylogenies for real-world datasets.

### 296 *Multi-group extensions*

297 For studies with three or more groups, MeLSI provides an omnibus test that jointly  
298 evaluates differences across all groups, with post-hoc pairwise comparisons when  
299 significant. P-values are adjusted for multiple testing using the Benjamini-Hochberg false  
300 discovery rate (FDR) procedure (26). The statistical framework (permutation testing, Type I  
301 error control) is identical to two-group analyses, ensuring valid inference regardless of  
302 group number. Real-world validation on the SKIOME skin microbiome dataset (3 groups,  
303 511 samples) demonstrates utility beyond two-group comparisons (see Results section).

### 304 *Implementation and computational considerations*

305 MeLSI is implemented in R (version >= 4.0) as an open-source package. Key dependencies  
306 include vegan (27) for PERMANOVA calculations, ggplot2 (28) for visualization, and base R

307 for matrix operations. The algorithm is parallelizable across permutations and weak  
308 learners, though the current implementation is serial.  
309 Time complexity is  $O(n^2 p^2 B \cdot n_{\text{perms}})$  in the worst case, but conservative pre-filtering  
310 reduces effective dimensionality, and early stopping in gradient descent reduces iteration  
311 counts. For typical microbiome datasets ( $n < 500$ ,  $p < 1000$ ), analysis completes in minutes  
312 on standard hardware.

## 313 DATA AVAILABILITY

314 MeLSI source code and all validation scripts are permanently archived at Zenodo (DOI:  
315 10.5281/zenodo.1771484) and available at <https://github.com/NathanBresette/MeLSI>  
316 under the MIT license. All validation data and analysis scripts are included in the package  
317 repository for full reproducibility. The Atlas1006 and DietSwap datasets are available  
318 through the R microbiome package (<https://microbiome.github.io/>).

## 319 RESULTS

320 Our validation strategy follows a rigorous progression from statistical validity to biological  
321 utility. We first establish proper Type I error control on null data where no true differences  
322 exist, ensuring MeLSI does not produce false positives despite its adaptive nature. We then  
323 assess statistical power across synthetic datasets with varying effect sizes, comparing  
324 MeLSI's ability to detect true differences against traditional fixed metrics. Finally, we  
325 demonstrate practical utility on real microbiome datasets and evaluate computational  
326 performance, parameter sensitivity, and biological interpretability. This order ensures that  
327 before claiming any advantage, we verify that MeLSI maintains the statistical rigor required  
328 for valid scientific inference.

### 329 Type I error control

330 Proper Type I error control is essential for valid statistical inference. We evaluated MeLSI  
331 on two null datasets where no true group differences exist (Table 1). The first uses  
332 synthetic data with randomly assigned group labels, while the second uses real Atlas1006  
333 data with shuffled group labels (preserving the data structure while breaking group  
334 associations).

335 **Table 1. Type I Error Control on Null Data**

| Dataset Type   | n   | MeLSI Type I | Euclidean Type I | Bray-Curtis Type I | Jaccard Type I | Weighted UniFrac Type I | Unweighted UniFrac Type I |
|----------------|-----|--------------|------------------|--------------------|----------------|-------------------------|---------------------------|
| Null Synthetic | 50  | 5%           | 7%               | 7%                 | 6%             | 3%                      | 4%                        |
| Null Synthetic | 100 | 4%           | 3%               | 2%                 | 5%             | 2%                      | 4%                        |
| Null           | 200 | 3%           | 0%               | 5%                 | 2%             | 2%                      | 4%                        |

| Dataset Type       | n   | MeLSI Type I | Euclidean Type I | Bray-Curtis Type I | Jaccard Type I | Weighted UniFrac Type I | Unweighted UniFrac Type I |
|--------------------|-----|--------------|------------------|--------------------|----------------|-------------------------|---------------------------|
| Synthetic          |     |              |                  |                    |                |                         |                           |
| Null Real Shuffled | 50  | 3%           | 4%               | 4%                 | 6%             | 6%                      | 9%                        |
| Null Real Shuffled | 100 | 4%           | 4%               | 4%                 | 3%             | 4%                      | 4%                        |
| Null Real Shuffled | 200 | 6%           | 4%               | 4%                 | 2%             | 4%                      | 1%                        |

336 Abbreviations: n, sample size; Type I, empirical Type I error rate (percentage of simulations  
 337 with  $p < 0.05$ ). Results based on 100 simulations per condition.

338 Across all conditions, MeLSI maintained proper Type I error control, with empirical  
 339 rejection rates near the nominal 5% level (range: 3-6%). All traditional methods also  
 340 maintained appropriate error rates (range: 0-9%). The permutation testing framework  
 341 properly accounts for the flexibility of learned metrics, ensuring that MeLSI's adaptive  
 342 approach does not inflate false positive rates.

### 343 Performance across synthetic and real datasets

344 We evaluated MeLSI's ability to detect true group differences across synthetic datasets  
 345 with varying effect sizes and real microbiome datasets (Table 2).

346 **Table 2. Statistical Power Analysis Across Effect Sizes and Sample Sizes**

| Effect Size | n   | MeLSI Power | MeLSI Mean F | MeLSI Rank |
|-------------|-----|-------------|--------------|------------|
| Small       | 50  | 6%          | 1.230        | 1/6        |
| Small       | 100 | 10%         | 1.342        | 1/6        |
| Small       | 200 | 16%         | 1.432        | 1/6        |
| Medium      | 50  | 16%         | 1.307        | 3/6        |
| Medium      | 100 | 50%         | 1.504        | 3/6        |
| Medium      | 200 | 96%         | 1.780        | 3/6        |
| Large       | 50  | 84%         | 1.585        | 3/6        |
| Large       | 100 | 100%        | 2.129        | 3/6        |
| Large       | 200 | 100%        | 3.129        | 3/6        |

347 Abbreviations: n, sample size; Power, empirical statistical power (percentage of  
 348 simulations with  $p < 0.05$ ); F, PERMANOVA F-statistic (mean across 50 simulations per  
 349 condition); Rank, MeLSI's rank among 6 methods (1/6 = best, 6/6 = worst) based on F-  
 350 statistic. Results based on 50 simulations per condition. See Supplementary Tables S1-S2  
 351 for recovery metrics and individual method comparisons.

352 MeLSI demonstrated superior sensitivity for subtle signals (small effects, 1.5 $\times$  fold change),  
353 ranking 1/6 and outperforming all traditional methods. For medium and large effects,  
354 MeLSI achieved competitive performance (3/6 rank) while providing interpretable feature  
355 importance weights. Power increased appropriately with sample size, and learned feature  
356 weights reliably identify true signal taxa (Supplementary Table S1). MeLSI's CLR-based  
357 approach excels at medium effect sizes where signals are distributed across multiple taxa;  
358 for large effects (3 $\times$  fold change), count-based methods (Bray-Curtis, UniFrac) may be  
359 preferable due to their sensitivity to abundance dominance. The CLR transformation is  
360 most appropriate when signals are distributed across multiple taxa and when  
361 interpretability through feature weights is prioritized.

## 362 Scalability analysis

363 We assessed MeLSI's performance across varying sample sizes (n) and dimensionalities (p)  
364 using synthetic datasets with medium effect sizes (Table 3). For sample size scaling, we  
365 fixed p=200 taxa and varied n from 20 to 500. For dimensionality scaling, we fixed n=100  
366 samples and varied p from 50 to 1000 taxa.

367 **Table 3. Scalability Across Sample Size and Dimensionality**

|                          | n   | p    | MeLSI F | MeLSI Time | MeLSI Rank |
|--------------------------|-----|------|---------|------------|------------|
| <b>Varying n (p=200)</b> |     |      |         |            |            |
| n=20                     | 20  | 200  | 1.132   | 486.9      | 2/6        |
| n=50                     | 50  | 200  | 1.277   | 457.9      | 2/6        |
| n=100                    | 100 | 200  | 1.497   | 513.3      | 3/6        |
| n=200                    | 200 | 200  | 1.836   | 739.5      | 3/6        |
| n=500                    | 500 | 200  | 2.511   | 2055.8     | 3/6        |
| <b>Varying p (n=100)</b> |     |      |         |            |            |
| p=50                     | 100 | 50   | 1.666   | 244.8      | 3/6        |
| p=100                    | 100 | 100  | 1.670   | 337.5      | 3/6        |
| p=200                    | 100 | 200  | 1.470   | 523.4      | 3/6        |
| p=500                    | 100 | 500  | 1.375   | 1829.0     | 1/6        |
| p=1000                   | 100 | 1000 | 1.331   | 8633.0     | 1/6        |

368 Abbreviations: n, sample size; p, number of taxa/features; F, PERMANOVA F-statistic; Time,  
369 computation time in seconds; Rank, MeLSI's rank among 6 methods (1/6 = best, 6/6 =  
370 worst) based on F-statistic. Values shown as mean across 10 simulations per condition.  
371 See Supplementary Table S3 for individual method comparisons.

372 MeLSI's F-statistics increased monotonically with sample size, demonstrating appropriate  
373 power gains with larger datasets. MeLSI ranked 2/6 at smaller sample sizes and 3/6 at  
374 larger sizes, with computation time scaling as O(n<sup>2</sup>). Across dimensionalities, MeLSI

375 ranked 3/6 at lower dimensionalities and 1/6 at higher dimensionalities ( $p \geq 500$ ).  
376 Computation time scales as  $O(p^2)$ , but pre-filtering substantially mitigates this scaling. For  
377 very high-dimensional datasets ( $p > 1000$ ), we recommend pre-filtering, feature aggregation,  
378 or traditional methods if interpretability is not prioritized.

### 379 Parameter sensitivity analysis

380 We evaluated robustness to two key hyperparameters: ensemble size (B) and feature  
381 subsampling fraction (m\_frac) using a synthetic dataset with 100 samples, 200 taxa, and  
382 medium effect size (2x fold change in 10 signal taxa) (Table 4).

383 **Table 4. Parameter Sensitivity Analysis**

| Parameter                        | Value | F-statistic | p-value | Time (s) |
|----------------------------------|-------|-------------|---------|----------|
| <b>Ensemble Size (B)</b>         |       |             |         |          |
|                                  | 1     | 1.365       | 0.421   | 32.9     |
|                                  | 10    | 1.543       | 0.094   | 233      |
|                                  | 20    | 1.538       | 0.089   | 419.8    |
|                                  | 30    | 1.530       | 0.091   | 576.8    |
|                                  | 50    | 1.529       | 0.093   | 760      |
|                                  | 100   | 1.528       | 0.102   | 1284.1   |
| <b>Feature Fraction (m_frac)</b> |       |             |         |          |
|                                  | 0.5   | 1.578       | 0.093   | 405.2    |
|                                  | 0.7   | 1.551       | 0.083   | 523.7    |
|                                  | 0.8   | 1.530       | 0.091   | 578.2    |
|                                  | 0.9   | 1.517       | 0.097   | 630.3    |
|                                  | 1.0   | 1.498       | 0.100   | 666.7    |

384 Abbreviations: B, ensemble size (number of weak learners); m\_frac, feature subsampling  
385 fraction; F, PERMANOVA F-statistic; Time, computation time in seconds. Values shown as  
386 mean across 25 replications per parameter value. See Supplementary Table S4 for  
387 standard deviations.

388 F-statistics remained stable across ensemble sizes (B=10-100), with the single-learner  
389 baseline (B=1) showing substantially higher variance, demonstrating that ensemble  
390 learning reduces variance and prevents overfitting. Performance varied modestly across  
391 feature fractions (m\_frac=0.5-1.0). The default settings (B=30, m\_frac=0.8) provide a good  
392 balance between performance and computational cost.

### 393 Feature correlation robustness

394 A critical concern for microbiome data analysis is that taxa are not independent but exhibit  
395 correlations due to ecological relationships (e.g., co-occurring taxa in microbial

396 communities). To validate MeLSI's robustness to feature correlation, we evaluated  
397 performance across four correlation levels: None ( $r=0$ ), Low ( $r=0.3$ ), Moderate ( $r=0.6$ ), and  
398 High ( $r=0.8$ ), using 50 simulations per condition (200 total simulations) with synthetic  
399 datasets containing 100 samples, 200 taxa, and medium effect size ( $2\times$  fold change in 10  
400 signal taxa) (Table 5).

401 **Table 5. Effect of Feature Correlation on MeLSI Performance**

| Correlation Level | Correlation Value | n  | MeLSI Power (%) | MeLSI F | Precision at 10 | Recall at 10 | AUC-ROC | MeLSI Rank |
|-------------------|-------------------|----|-----------------|---------|-----------------|--------------|---------|------------|
| None              | 0.0               | 50 | 50              | 1.512   | 0.392           | 0.392        | 0.817   | 3/6        |
| Low               | 0.3               | 50 | 42              | 1.481   | 0.348           | 0.348        | 0.788   | 3/6        |
| Moderate          | 0.6               | 50 | 46              | 1.498   | 0.356           | 0.356        | 0.783   | 2/6        |
| High              | 0.8               | 50 | 44              | 1.507   | 0.368           | 0.368        | 0.769   | 1/6        |

402 Abbreviations: n, number of simulations per correlation level (not sample size); F,  
403 PERMANOVA F-statistic (mean across 50 simulations); Precision at 10, proportion of top-  
404 10 features that are true signals; Recall at 10, proportion of true signals found in top-10  
405 features; AUC-ROC, area under receiver operating characteristic curve; Rank, MeLSI's rank  
406 among 6 methods (1/6 = best, 6/6 = worst) based on F-statistic. See Supplementary Table  
407 S5 for individual method comparisons.

408 MeLSI demonstrated robust performance across correlation levels, maintaining stable F-  
409 statistics ( $\pm 1.7\%$  variation:  $F=1.512$  at  $r=0$ ,  $F=1.481$  at  $r=0.3$ ,  $F=1.498$  at  $r=0.6$ ,  $F=1.507$  at  
410  $r=0.8$ ) and consistent statistical power (50%, 42%, 46%, 44% respectively). The stability of  
411 F-statistics demonstrates that MeLSI effectively handles correlated features without  
412 performance degradation. Feature recovery metrics also remained stable: Precision at 10  
413 (0.392, 0.348, 0.356, 0.368) and AUC-ROC (0.817, 0.788, 0.783, 0.769) showed minimal  
414 variation across correlation levels, confirming that MeLSI's ability to identify true signal  
415 taxa is maintained even when taxa exhibit high correlation. MeLSI's competitive ranking  
416 (1/6 to 3/6) across all correlation levels demonstrates that the method maintains  
417 statistical power comparable to traditional methods while providing interpretability, even  
418 when features are correlated. Notably, MeLSI achieved its best ranking (1/6) at high  
419 correlation ( $r=0.8$ ), suggesting the method may be particularly effective when taxa exhibit  
420 strong ecological relationships.

## 421 Pre-filtering analysis

422 We evaluated the benefit of conservative pre-filtering by comparing MeLSI with and without  
423 this step using synthetic datasets with varying effect sizes (small:  $1.5\times$  fold change in 5  
424 taxa, medium:  $2.0\times$  in 10 taxa, large:  $3.0\times$  in 20 taxa) and high sparsity (70% zero-inflated  
425 features) (Table 6).

426 **Table 6. Benefit of Conservative Pre-filtering**

| Effect | Features | Filter F | Filter Power | No Filter F | No Filter Power | Delta F | Delta Time |
|--------|----------|----------|--------------|-------------|-----------------|---------|------------|
| Small  | 500      | 1.756    | 100%         | 1.281       | 4%              | +37.1 % | +39.8%     |
| Medium | 200      | 1.831    | 94%          | 1.337       | 14%             | +36.9 % | +18.0%     |
| Large  | 100      | 1.928    | 84%          | 1.416       | 14%             | +36.1 % | +16.5%     |

427 Abbreviations: Effect, effect size category (Small: 1.5× fold change in 5 taxa; Medium: 2.0×  
 428 in 10 taxa; Large: 3.0× in 20 taxa); Features, number of taxa; F, PERMANOVA F-statistic  
 429 (mean across 50 simulations); Power, empirical statistical power (percentage of  
 430 simulations with  $p < 0.05$ ); Filter, with pre-filtering (top 70% by importance score); No Filter,  
 431 without pre-filtering; Delta F, percent change in F-statistic; Delta Time, percent change in  
 432 computation time (positive = time savings). Results based on 50 simulations per condition.

433 Variance-based pre-filtering (retaining the top 70% of features by importance score)  
 434 demonstrated substantial benefits across all effect sizes. Pre-filtering improved F-  
 435 statistics by 36-37% across all effect sizes, increasing power from 4-14% to 84-100% for  
 436 small effects. Time savings ranged from 16.5% to 39.8%, increasing with dimensionality.

437 The variance-based importance score ( $I_j = |\mu_{1j} - \mu_{2j}| / \sqrt{\sigma_{1j}^2 + \sigma_{2j}^2}$ ) efficiently identifies  
 438 features with large between-group differences relative to within-group variation. Pre-  
 439 filtering is particularly valuable when signal is concentrated in a subset of features,  
 440 focusing metric learning on the most informative taxa while reducing computational  
 441 burden.

## 442 Real data validation

443 To evaluate MeLSI's utility in real-world applications, we analyzed three published  
 444 microbiome datasets: Atlas1006 (sex-associated differences), DietSwap (dietary  
 445 intervention), and SKIOME (multi-group skin microbiome validation).

### 446 *Atlas1006 dataset*

447 On the Atlas1006 dataset (1,114 Western European adults, male vs. female), MeLSI  
 448 achieved  $F = 5.141$  ( $p = 0.005$ ) versus  $F = 4.711$  ( $p = 0.001$ ) for Euclidean distance (the best  
 449 traditional method), representing a 9.1% improvement. MeLSI's improvement over the best  
 450 fixed metric suggests that learned metrics can capture biologically relevant patterns in  
 451 subtle, high-dimensional comparisons, consistent with previously documented sex-  
 452 associated microbiome differences (29, 30).

### 453 *DietSwap dataset*

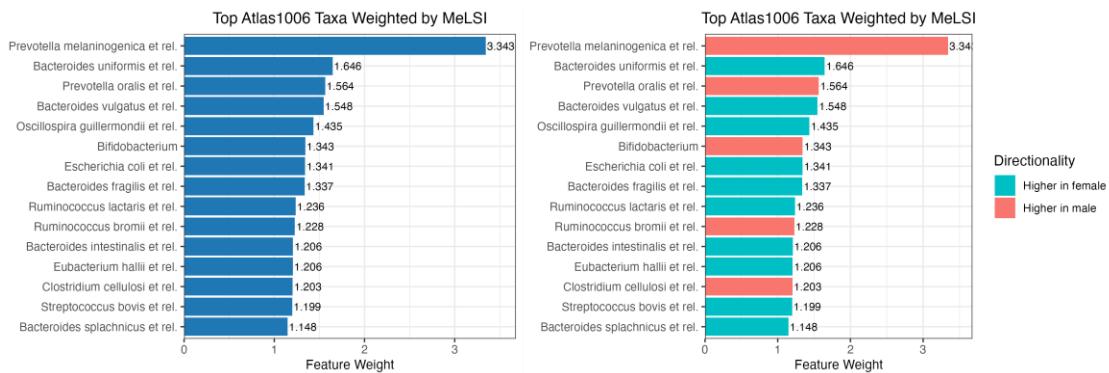
454 On the DietSwap dataset (Western vs. high-fiber diets), MeLSI detected a significant  
 455 community difference with  $F = 2.856$  ( $p = 0.015$ ), outperforming all traditional metrics. The

456 strongest fixed metric was Bray-Curtis ( $F = 2.153$ ,  $p = 0.058$ ). These results suggest that  
457 MeLSI's adaptive weighting captures diet-induced compositional shifts that fixed metrics  
458 only weakly detect.

## 459 Feature importance and biological interpretability

460 MeLSI provides interpretable feature importance weights. For the Atlas1006 dataset, the  
461 learned metric assigned highest weights to genera in the families Bacteroidaceae,  
462 Lachnospiraceae, and Ruminococcaceae, taxonomic groups previously associated with  
463 sex differences in gut microbiome composition (30, 31). Figure 1 displays the top 15 taxa  
464 by learned feature weight.

465



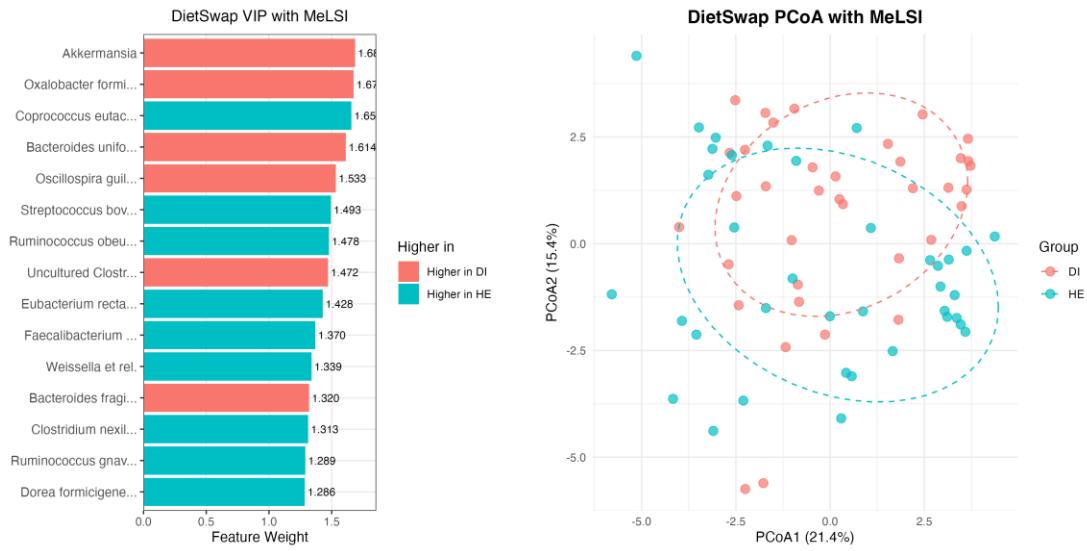
466

467 **Figure 1.** Top 15 taxa ranked by MeLSI feature weights for Atlas1006 dataset, colored by  
468 directionality. Taxa from Bacteroidaceae, Lachnospiraceae, and Ruminococcaceae  
469 families show strongest contributions.

470 The diagonal elements of the learned metric matrix  $\mathbf{M}$  directly represent feature  
471 importance: higher values indicate taxa that contribute more to group separation. MeLSI  
472 automatically calculates directionality and effect sizes on CLR-transformed data.  
473 Directionality is determined by identifying which group has the higher mean abundance on  
474 CLR-transformed data, ensuring consistency with the metric learning process. Effect size  
475 is reported as the difference in CLR-transformed means between groups ( $\mu_{CLR,1} - \mu_{CLR,2}$ ).  
476 Because CLR data is already in log-ratio space, this difference is the standard way to  
477 represent log-fold change for compositional data, ensuring that reported effect sizes are  
478 directly derived from the same feature space used to calculate distances in MeLSI. The  
479 learned distance matrices can also be used for Principal Coordinates Analysis (PCoA)  
480 ordination to visualize group separation, just as traditional distance metrics (Bray-Curtis,  
481 Euclidean, etc.) are used with PCoA throughout the microbiome field. For datasets where  
482 group separation is visually apparent, PCoA ordination provides complementary  
483 visualization alongside feature importance weights (see Figures 2-3 for DietSwap and  
484 SKIOME examples).

485 *DietSwap dataset*

486 For the DietSwap dataset, MeLSI's learned feature weights identified taxa including  
487 Akkermansia and Oxalobacter as key drivers of diet-induced community differences.  
488 Figure 2 displays the top 15 taxa by learned feature weight alongside the PCoA ordination.

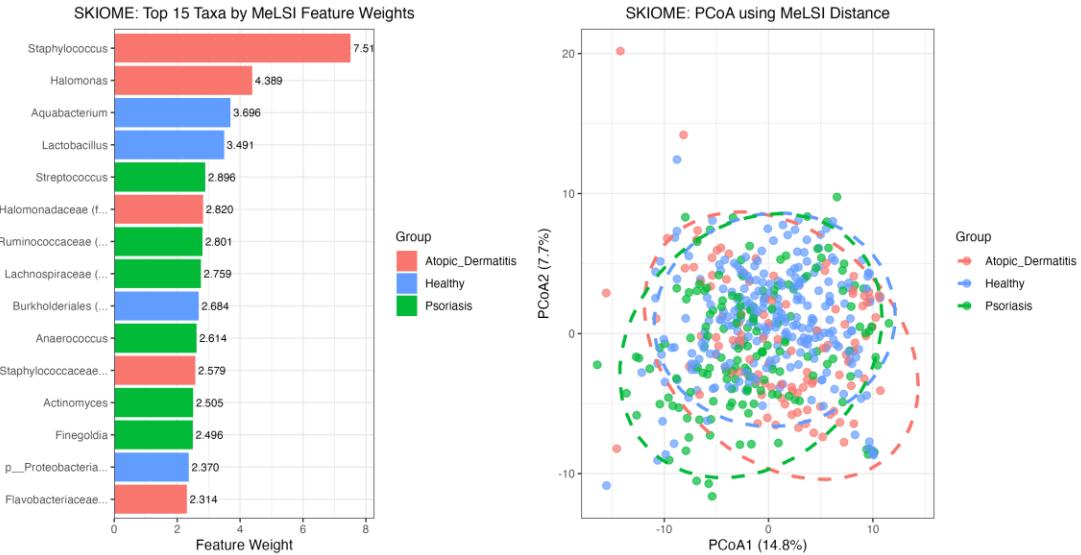


489

490 **Figure 2.** DietSwap dataset: Top 15 taxa by feature weights (left) and PCoA ordination  
491 (right). Taxa including Akkermansia and Oxalobacter show strong contributions. Dashed  
492 ellipses show 95% confidence intervals.

493 *SKIOME dataset: Multi-group validation*

494 To validate multi-group capability, we analyzed the SKIOME skin microbiome dataset  
495 (PRJNA554499, 511 samples, 3 groups: Atopic\_Dermatitis, Healthy, Psoriasis). MeLSI's  
496 omnibus test detected significant differences ( $F = 4.895$ ,  $p = 0.005$ ), comparable to  
497 Euclidean distance ( $F = 4.897$ ,  $p = 0.001$ ) but lower than count-based methods (Bray-Curtis:  
498  $F = 16.275$ , Jaccard:  $F = 11.058$ , both  $p = 0.001$ ). All pairwise comparisons remained  
499 significant after FDR correction ( $p = 0.005$  for all pairs). Figure 3 displays feature  
500 importance weights and PCoA ordination, demonstrating MeLSI's interpretability for multi-  
501 group analyses. This validates MeLSI's utility beyond two-group comparisons and across  
502 different body sites (skin vs. gut microbiome).



503

504 **Figure 3.** SKIOME multi-group validation: Feature importance weights (left) and PCoA  
 505 ordination (right) for three-group comparison (Atopic\_Dermatitis, Healthy, Psoriasis). Top  
 506 15 taxa are colored by the group with highest mean abundance. Dashed ellipses show 95%  
 507 confidence intervals. Consistent with significant omnibus PERMANOVA result ( $F=4.895$ ,  
 508  $p=0.005$ ).

## 509 Computational performance

510 Across all experiments, MeLSI demonstrated practical computational performance on  
 511 standard hardware. Small datasets ( $n<100$ ,  $p<200$ ) completed in under 2 minutes, medium  
 512 datasets ( $n=100-500$ ,  $p=200-500$ ) required 2-15 minutes, and large datasets ( $n=1000+$ ,  
 513  $p=100-500$ ) took 15-60 minutes. For comparison, traditional PERMANOVA with fixed  
 514 metrics typically completes in under 1 second for similar datasets. However, MeLSI's  
 515 additional computation time is justified by improved statistical power and interpretability,  
 516 particularly for challenging datasets where fixed metrics perform poorly. Pre-filtering  
 517 increases statistical power by 36-37% while reducing computation time by 16-40% (Table  
 518 6). For typical microbiome studies ( $n=50-200$ ,  $p=100-500$ ), MeLSI completes in 2-30  
 519 minutes (Table 3), representing a modest time investment that yields both improved power  
 520 and interpretability through feature weights. For very large studies ( $n>500$ ) or when only  
 521 rapid screening is needed, traditional methods may be preferable.

## 522 CONCLUSIONS

### 523 Summary

524 MeLSI bridges adaptive machine learning and rigorous statistical inference for microbiome  
 525 beta diversity analysis by integrating metric learning with permutation testing.  
 526 Comprehensive validation demonstrates proper Type I error control across 100  
 527 simulations per condition, with empirical rejection rates near the nominal 5% level (3-6%  
 528 across all conditions and sample sizes) while delivering improvements on real data: 9.1%

529 higher F-statistics on Atlas1006 and significant detection on DietSwap where traditional  
530 metrics remained marginal ( $p = 0.015$  vs.  $p \geq 0.058$ ). However, on synthetic datasets with  
531 large effect sizes, count-based (Bray-Curtis) and phylogenetic (UniFrac) methods  
532 demonstrated superior sensitivity, suggesting MeLSI's CLR-transformed approach may not  
533 capture large fold-change signals as effectively as raw count-based metrics.

534 MeLSI's key innovation is interpretability: learned feature weights identify biologically  
535 relevant taxa (e.g., Bacteroidaceae, Lachnospiraceae, Ruminococcaceae in sex-  
536 associated differences), turning omnibus PERMANOVA results into actionable biological  
537 insights. MeLSI is recommended when: (1) effect sizes are moderate (2 $\times$  fold change)  
538 rather than very large, (2) interpretability through feature weights is needed to identify  
539 biologically relevant taxa, (3) traditional methods yield marginal results (p-values near  
540 0.05), and (4) signals are distributed across multiple taxa rather than concentrated in  
541 highly abundant taxa. Traditional methods (Bray-Curtis, UniFrac) are preferable for: (1)  
542 large, obvious effects (3 $\times$  fold change) where any method succeeds, (2) large-scale  
543 screening studies where speed is critical, and (3) when only omnibus significance testing is  
544 needed without feature-level interpretation. Critically, unlike prediction-focused machine  
545 learning (e.g., Random Forest, neural networks), MeLSI is an inference-focused approach:  
546 every learned metric undergoes rigorous permutation testing to ensure that p-values  
547 remain valid despite the adaptive nature of the method. This distinction is fundamental:  
548 MeLSI prioritizes statistical rigor over predictive accuracy, maintaining Type I error control  
549 while adapting to dataset-specific signal structure.

## 550 Limitations and future work

551 MeLSI requires more computation time than fixed metrics (minutes vs. seconds), reflecting  
552 the cost of learning optimal metrics through ensemble training and permutation testing.  
553 However, MeLSI's computational time (2-30 minutes for typical datasets) is justified by  
554 substantial interpretability gains through learned feature weights, combined with a  
555 favorable power-time trade-off through pre-filtering (Table 6). For large-scale screening  
556 studies with thousands of samples, traditional methods may be more appropriate.

557 Synthetic validation focused on two-group comparisons, which represent the primary use  
558 case; multi-group synthetic validation would require duplicating all validation tables and is  
559 addressed through real-world multi-group validation on the SKIOME skin microbiome  
560 dataset (3 groups, 511 samples). The statistical framework (permutation testing, Type I  
561 error control) is identical for two-group and multi-group analyses, ensuring valid inference  
562 regardless of group number.

563 The most immediate extensions are (1) regression and covariate adjustment to handle  
564 continuous outcomes and confounders (age, BMI, medication use), enabling integration  
565 with epidemiological frameworks, and (2) improved compositionality handling by learning  
566 metrics directly in compositional space using Aitchison geometry (24), potentially offering  
567 advantages for zero-inflated microbiome data.

568 MeLSI's learned distance metrics are compatible with other distance-based ordination  
569 and hypothesis testing methods. The learned distances can be used with Non-metric  
570 Multidimensional Scaling (NMDS) (32) and Analysis of Similarities (ANOSIM) (33), both of  
571 which operate on distance matrices and would benefit from MeLSI's data-adaptive metrics.  
572 However, Principal Component Analysis (PCA) is not compatible with MeLSI's learned  
573 distances, as PCA relies on Euclidean distances computed in the original feature space  
574 and cannot accommodate the learned Mahalanobis distance structure.

## 575 Software availability

576 MeLSI is freely available as an open-source R package under the MIT license at  
577 <https://github.com/NathanBresette/MeLSI> (DOI: 10.5281/zenodo.1771484). The package  
578 is currently under review for inclusion in Bioconductor. The package includes  
579 comprehensive documentation, tutorial vignettes, and example datasets. All validation  
580 experiments are fully reproducible using provided code and data. Recommended usage:  
581 aim for  $n \geq 50$  per group, apply CLR transformation, use default settings ( $B=30$ ,  
582  $m_{frac}=0.8$ ,  $n_{perms}=200$ ), and validate top-weighted features with univariate differential  
583 abundance methods.

## 584 SUPPLEMENTARY MATERIAL

585 Supplementary tables providing detailed results are available:

- 586 • **Supplementary Table S1:** Recovery of true signal taxa metrics (Precision at k,  
587 Recall at k, Mean Rank, AUC-ROC) across all effect sizes and sample sizes
- 588 • **Supplementary Table S2:** Individual method comparisons for power analysis  
(MeLSI vs. each traditional method) supporting rank calculations in Table 2
- 589 • **Supplementary Table S3:** Individual method comparisons for scalability analysis  
supporting rank calculations in Table 3
- 590 • **Supplementary Table S4:** Parameter sensitivity analysis with standard deviations  
(mean and SD for F-statistics, p-values, and computation times across 25  
593 replications per parameter value)
- 594 • **Supplementary Table S5:** Individual method comparisons for feature correlation  
analysis

597 These supplementary tables provide complete transparency for rank calculations (e.g., 1/6,  
598 3/6) shown in the main tables, allowing readers to see how MeLSI compares to each  
599 traditional method individually.

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607 **AUTHOR CONTRIBUTIONS**

608 Nathan Bresette conceived the study, developed the methodology, implemented the  
609 software, performed all analyses, generated all figures and tables, and wrote the  
610 manuscript. Aaron C. Ericsson provided substantial guidance on methodological  
611 development and improvements to the method and interpretability. Carter Woods  
612 contributed ideas and assisted with manuscript editing. Ai-Ling Lin provided project  
613 leadership and oversight as principal investigator.

614 **COMPETING INTERESTS**

615 The authors declare no competing interests.

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