

UNITED STATES DEPARTMENT OF COMMERCE, Charles Sawyer, Secretary
NATIONAL BUREAU OF STANDARDS, E. U. Condon, Director

ATOMIC ENERGY LEVELS

As Derived From the Analyses of Optical Spectra

Volume I

The Spectra of Hydrogen, Deuterium, Tritium, Helium,
Lithium, Beryllium, Boron, Carbon, Nitrogen, Oxygen,
Fluorine, Neon, Sodium, Magnesium, Aluminum, Silicon,
Phosphorus, Sulfur, Chlorine, Argon, Potassium, Calcium,
Scandium, Titanium, and Vanadium

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HELIUM

He I

2 electrons

 $Z=2$ Ground state $1s^2\ ^1S_0$ $1s^2\ ^1S_0\ 198305 \pm 15\text{ cm}^{-1}$

I. P. 24.580 volts

Most of the terms are taken from Paschen-Götze with the term values subtracted from Paschen's limit as quoted by Robinson in 1937. Higher members of the $^1F^\circ$ and $^3F^\circ$ series are taken from Meggers and Dieke. The term $2p\ ^3P^\circ$ has been calculated from its combination with $2s\ ^3S_1$, using the resolved triplet as observed by Meggers, the intervals being -0.078 cm^{-1} and -0.996 cm^{-1} . The components of $3p\ ^3P^\circ$ are based on Paschen's value of $3p\ ^3P_2$ and the intervals observed by Gibbs and Kruger; -0.165 cm^{-1} and -0.192 cm^{-1} .

Some doubt exists regarding the correct classifications of lines attributed to doubly excited helium, such as those observed at 309.04 Å and 320.38 Å by Compton and Boyce, and at 320.392 Å and 357.507 Å by Kruger. Approximate theoretical computations of the energies of doubly excited levels have been made by a number of authors and are summarized by Wu. His classification of the line observed at 320.4 Å as $2p\ ^3P^\circ - 2p^2\ ^3P$ has been adopted and used for the calculation of $2p^2\ ^3P$.

Several references deal with intercombinations in He I, namely, those by Lyman, Hopfield, Paschen, Suga, and others. The term values based on the excellent long series have been adopted in the table, since it is believed that they are the most accurate.

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He I

He I

Config.	Desig.	J	Level	Config.	Desig.	J	Level
$1s^2$	$1s^2\ ^1S$	0	0 ± 15	$1s\ 7s$	$7s\ ^1S$	0	195973. 19
$1s\ 2s$	$2s\ ^3S$	1	159850. 318	$1s\ 7p$	$7p\ ^3P^\circ$	2, 1, 0	196021. 72
$1s\ 2s$	$2s\ ^1S$	0	166271. 70	$1s\ 7d$	$7d\ ^3D$	3, 2, 1	196064. 00
$1s\ 2p$	$2p\ ^3P^\circ$	2 1 0	169081. 111 169081. 189 169082. 185	$1s\ 7d$	$7d\ ^1D$	2	196064. 31
$1s\ 2p$	$2p\ ^1P^\circ$	1	171129. 148	$1s\ 7f$	$7f\ ^1F^\circ$	3	196065. 4
$1s\ 3s$	$3s\ ^3S$	1	183231. 08	$1s\ 7f$	$7f\ ^3F^\circ$	4, 3, 2	196065. 51
$1s\ 3s$	$3s\ ^1S$	0	184859. 06	$1s\ 7p$	$7p\ ^1P^\circ$	1	196073. 41
$1s\ 3p$	$3p\ ^3P^\circ$	2 1 0	185558. 92 185559. 085 185559. 277	$1s\ 8s$	$8s\ ^3S$	1	196455. 79
$1s\ 3d$	$3d\ ^3D$	3, 2, 1	186095. 90	$1s\ 8s$	$8s\ ^1S$	0	196529. 03
$1s\ 3d$	$3d\ ^1D$	2	186099. 22	$1s\ 8p$	$8p\ ^3P^\circ$	2, 1, 0	196561. 08
$1s\ 3p$	$3p\ ^1P^\circ$	1	186203. 62	$1s\ 8d$	$8d\ ^3D$	3, 2, 1	196589. 42
$1s\ 4s$	$4s\ ^3S$	1	190292. 46	$1s\ 8d$	$8d\ ^1D$	2	196589. 73
$1s\ 4s$	$4s\ ^1S$	0	190934. 50	$1s\ 8f$	$8f\ ^1F^\circ$	3	196590. 3
$1s\ 4p$	$4p\ ^3P^\circ$	2, 1, 0	191211. 42	$1s\ 8f$	$8f\ ^3F^\circ$	4, 3, 2	196590. 42
$1s\ 4d$	$4d\ ^3D$	3, 2, 1	191438. 83	$1s\ 8p$	$8p\ ^1P^\circ$	1	196595. 56
$1s\ 4d$	$4d\ ^1D$	2	191440. 71	$1s\ 9s$	$9s\ ^3S$	1	196856. 37
$1s\ 4f$	$4f\ ^3F^\circ$	4, 3, 2	191446. 61	$1s\ 9s$	$9s\ ^1S$	0	196907. 13
$1s\ 4f$	$4f\ ^1F^\circ$	3	191447. 24	$1s\ 9p$	$9p\ ^3P^\circ$	2, 1, 0	196929. 68
$1s\ 4p$	$4p\ ^1P^\circ$	1	191486. 95	$1s\ 9d$	$9d\ ^1D$	2	196949. 49
$1s\ 5s$	$5s\ ^3S$	1	193341. 33	$1s\ 9d$	$9d\ ^3D$	3, 2, 1	196949. 63
$1s\ 5s$	$5s\ ^1S$	0	193657. 78	$1s\ 9f$	$9f\ ^1F^\circ$	3	196950. 3
$1s\ 5p$	$5p\ ^3P^\circ$	2, 1, 0	193795. 07	$1s\ 9f$	$9f\ ^3F^\circ$	4, 3, 2	196950. 36
$1s\ 5d$	$5d\ ^3D$	3, 2, 1	193911. 48	$1s\ 9p$	$9p\ ^1P^\circ$	1	196953. 95
$1s\ 5d$	$5d\ ^1D$	2	193912. 54	$1s\ 10s$	$10s\ ^3S$	1	197139. 76
$1s\ 5f$	$5f\ ^1F^\circ$	3	193914. 31	$1s\ 10s$	$10s\ ^1S$	0	197176. 36
$1s\ 5f$	$5f\ ^3F^\circ$	4, 3, 2	193915. 79	$1s\ 10p$	$10p\ ^3P^\circ$	2, 1, 0	197192. 63
$1s\ 5p$	$5p\ ^1P^\circ$	1	193936. 75	$1s\ 10d$	$10d\ ^1D$	2	197207. 08
$1s\ 6s$	$6s\ ^3S$	1	194930. 46	$1s\ 10d$	$10d\ ^3D$	3, 2, 1	197207. 30
$1s\ 6s$	$6s\ ^1S$	0	195109. 17	$1s\ 10f$	$10f\ ^1F^\circ$	4, 3, 2	197208. 0
$1s\ 6p$	$6p\ ^3P^\circ$	2, 1, 0	195187. 21	$1s\ 10p$	$10p\ ^1P^\circ$	1	197210. 41
$1s\ 6d$	$6d\ ^3D$	3, 2, 1	195254. 37	$1s\ 11s$	$11s\ ^3S$	1	197347. 05
$1s\ 6d$	$6d\ ^1D$	2	195255. 02	$1s\ 11p$	$11p\ ^3P^\circ$	2, 1, 0	197386. 98
$1s\ 6f$	$6f\ ^1F^\circ$	3	195256. 7	$1s\ 11d$	$11d\ ^1D$	2	197397. 62
$1s\ 6f$	$6f\ ^3F^\circ$	4, 3, 2	195256. 82	$1s\ 11d$	$11d\ ^3D$	3, 2, 1	197397. 75
$1s\ 6p$	$6p\ ^1P^\circ$	1	195269. 17	$1s\ 11f$	$11f\ ^1F^\circ$	4, 3, 2	197398. 6
$1s\ 7s$	$7s\ ^3S$	1	195862. 63	$1s\ 11p$	$11p\ ^1P^\circ$	1	197400. 18
				$1s\ 12s$	$12s\ ^3S$	1	197503. 69
				$1s\ 12s$	$12s\ ^1S$	0	197524. 26

He I—Continued

Config.	Desig.	<i>J</i>	Level	Config.	Desig.	<i>J</i>	Level
1s 12p	12p ³ P°	2, 1, 0	197534. 44	1s 16d	16d ³ D	3, 2, 1	197876. 41
1s 12d	12d ¹ D	2	197542. 54	1s 16p	16p ¹ P°	1	197877. 04
1s 12d	12d ³ D	3, 2, 1	197542. 67	1s 17p	17p ³ P°	2, 1, 0	197922. 51
1s 12p	12p ¹ P°	1	197544. 56	1s 17d	17d ³ D	3, 2, 1	197925. 33
1s 13s	13s ³ S	1	197624. 98	1s 17p	17p ¹ P°	1	197925. 87
1s 13p	13p ³ P°	2, 1, 0	197649. 07	1s 18p	18p ³ P°	2, 1, 0	197964. 02
1s 13s	13s ¹ S	0	197649. 78	1s 18d	18d ³ D	3, 2, 1	197966. 75
1s 13d	13d ¹ D	2	197655. 19	1s 18p	18p ¹ P°	1	197966. 80
1s 13d	13d ³ D	3, 2, 1	197655. 47	1s 19p	19p ³ P°	2, 1, 0	197999. 12
1s 13p	13p ¹ P°	1	197656. 95	1s 19d	19d ³ D	3, 2, 1	198001. 43
1s 14s	14s ³ S	1	197721. 13	1s 19p	19p ¹ P°	1	198001. 44
1s 14p	14p ³ P°	2, 1, 0	197739. 90	1s 20p	20p ³ P°	2, 1, 0	198029. 07
1s 14d	14d ¹ D	2	197744. 918	1s 20p	20p ¹ P°	1	198031. 02
1s 14d	14d ³ D	3, 2, 1	197744. 94	1s 20d	20d ³ D	3, 2, 1	198031. 41
1s 14p	14p ¹ P°	1	197746. 15	1s 21p	21p ³ P°	2, 1, 0	198054. 83
1s 15s	15s ³ S	1	197796. 63	1s 21d	21d ³ D	3, 2, 1	198056. 50
1s 15p	15p ³ P°	2, 1, 0	197813. 11	1s 22p	22p ³ P°	2, 1, 0	198077. 15
1s 15d	15d ³ D	3, 2, 1	197817. 05				
1s 15p	15p ¹ P°	1	197818. 12	He II (² S _{1/2})	Limit		198305
1s 16p	16p ³ P°	2, 1, 0	197872. 95	2p ²	2p ² ³ P	2, 1, 0	481198

August 1946.

He II

(H sequence; 1 electron)

Z=2Ground state 1s ²S_{1/2}1s ²S_{1/2} He³ 438889.040 cm⁻¹I. P. He³ 54.400 volts1s ²S_{1/2} He⁴ 438908.670 cm⁻¹I. P. He⁴ 54.403 volts

The levels have been calculated by J. E. Mack, "using $R_{\text{He}^4}=109722.264$ and taking into account the fine structure as in hydrogen, but with $\Lambda=0.0402\pm0.009$, from the work of Skinner and Lamb on the 2s-level. The tentative experimental indication that Λ decreases with increasing n has been neglected. Assuming $R_{\text{He}^3}=109717.344$, the levels of He³ may be calculated to a close approximation from those of He⁴ by the equation

$$\text{Level}_{\text{He}^3, \text{II}} - \text{Level}_{\text{He}^4, \text{II}} = -(1-n^{-2})19.630 \text{ cm}^{-1}."$$

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He³ IIHe⁴ II

Config.	Desig.	<i>J</i>	Level	Level	Interval
1s	1s ² S	½	0.000	0.000	
2p	2p ² P°	½	329164.390	329179.102] 0.470 5.8434
2s	2s ² S	½	329164.860	329179.572	
2p	2p ² P°	1½	329170.135	329184.945	
3p	3p ² P°	½	390123.179	390140.622] 0.14 1.7314 0.5771
3s	3s ² S	½	390123.318	390140.761	
3p, 3d	3d ² D, 3p ² P°	1½	390124.910	390142.353	
3d	3d ² D	2½	390125.487	390142.930	
4p	4p ² P°	½	411458.517	411476.917] 0.06 0.7304 0.2435 0.1217
4s	4s ² S	½	411458.576	411476.976	
4p, 4d	4d ² D, 4p ² P°	1½	411459.248	411477.648	
4d, 4f	4d ² D, 4f ² F°	2½	411459.491	411477.891	
4f	4f ² F°	3½	411459.613	411478.013	
5p	5p ² P°	½	421333.629	421352.472] 0.03 0.3740 0.1247 0.0624 0.0374
5s	5s ² S	½	421333.659	421352.502	
5p, 5d	5d ² D, 5p ² P°	1½	421334.003	421352.846	
5d, 5f	5d ² D, 5f ² F°	2½	421334.128	421352.971	
5f, 5g	5g ² G, 5f ² F°	3½	421334.190	421353.033	
5g	5g ² G	4½	421334.228	421353.071	
6p	6p ² P°	½	426697.845	426716.928] 0.02 0.2164 0.0721 0.0361 0.0216 0.0144
6s	6s ² S	½	426697.862	426716.945	
6p, 6d	6d ² D, 6p ² P°	1½	426698.062	426717.145	
6d, 6f	6d ² D, 6f ² F°	2½	426698.134	426717.217	
6f, 6g	6g ² G, 6f ² F°	3½	426698.170	426717.253	
6g, 6h	6g ² G, 6h ² H°	4½	426698.192	426717.275	
6h	6h ² H°	5½	426698.206	426717.289	
7s, etc.	7s ² S, etc.	½, etc.	-----	429951.508 to .741	
8s, etc.	8s ² S, etc.	½, etc.	-----	432050.863 to 1.023	
9s, etc.	9s ² S, etc.	½, etc.	-----	433490.169 to .283	
10s, etc.	10s ² S, etc.	½, etc.	-----	434519.693 to .777	
11s, etc.	11s ² S, etc.	½, etc.	-----	435281.423 to .486	
12s, etc.	12s ² S, etc.	½, etc.	-----	435860.778 to .828	
13s, etc.	13s ² S, etc.	½, etc.	-----	436311.653 to .692	
14s, etc.	14s ² S, etc.	½, etc.	-----	436669.407 to .439	
15s, etc.	15s ² S, etc.	½, etc.	-----	436957.026 to 8.052	
	∞=Limit	-----	-----	438908. 670	

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