Concordia University

Dept. of Computer Science and Software Engineering

COMP 335 – Introduction to Theoretical Computer Science

Fall 2024

Assignment 6

Submission through Moodle is due by Sunday, December 1st at 23:55

- 1. [30 Points] Classify the following languages into one of the three categories a) regular, b) context-free but not regular, and c) not context-free. Prove your answer.
 - (a) $L_1 = \{a^i b^j c^k \mid k = i \times j \text{ and } 0 < i < 10 < j\}$ (b) $L_2 = \{xyz \mid x, y, z \in \{a, b\}^* \text{ and } n_a(x) = n_b(z)\}$ (c) $L_3 = \{wuw^R \mid w, u \in \{a, b\}^* \text{ and } |w| = |u|\}$

Note that in order to show that a language is context-free but not regular, you need to prove both that it is context-free and also that it is not regular.

- 2. [10 Points] Give a Turing machine for $L = \{a\} \cdot \{a, b\}^+$ that does not halt on rejection.
- 3. [20 Points] Give a Turing machine for each of the following languages:

 - (a) $L_1 = \{a^n b^m c^k \mid m \ge n, k \ge 1\}.$ (b) $L_2 = \{xy \mid x \in \{a, b\}^+, y \in \{c\}^+ \text{ and } n_a(x) = n_c(y)\}.$
- 4. [20 Points] Draw transition diagrams for Turing machines that compute the following functions. In each case, give a brief description in English of your solution strategy.

 - (a) $f(1^n) = 1^{2n}$ (b) $f(1^n) = 1^{n^2}$