Concordia University

Department of Computer Science and Software

Engineering

SOEN 331:

Formal Methods for Software Engineering

Exercises in Z and Object-Z

Nathan Grenier, Nirav Patel

March 28, 2024

PROBLEM 1 (40 pts)

Consider a system that handles railway connections as it associates (source) cities to all their corresponding destinations. The requirements of the system are as follows:

- 1. A source city may have connections to possibly multiple destination cities.
- 2. Multiple source cities may share the same group of destination cities.

We introduce the type *CITY*. A possible state of the system is shown below as it is captured by variable *connections*:

```
connections = \\ \{ \\ Montreal \mapsto \{Ottawa, Kingston, Quebec, Halifax\}, \\ Ottawa \mapsto \{Montreal, Toronto\}, \\ Toronto \mapsto \{Montreal, Ottawa\}, \\ Halifax \mapsto \{Montreal, Quebec\}, \\ Quebec \mapsto \{Montreal, Halifax\}, \\ Kingston \mapsto \{Montreal\} \\ \}
```

1. (2 pts) Is connections a binary relation? Explain why, and if so express this formally.

Solution:

Yes, the variable *connections* represents a binary relation. A binary relation is a set of ordered pairs where each pair consists of two elements. In this case, the pairs in *connections* are formed by associating a source city with its corresponding set of destination citites.

Formally, a binary relation R from set A to set B is defined as a subset of the cartesian product $A \times B$. In this context, the set of connections can be expressed formally as:

$$connections \subseteq \{(source, destination) \mid source \in CITY, destination \in CITY\}$$

Therefore, the variable *connections* conforms to the definition of a binary relation as it relates source cities to their respective destination cities in pairs.

2. (2 pts) In the expression $connections \in (...)$, what would RHS be?

The right-hand side would be the set of all possible binary relations on the set of cities, denoted as 'CITY'.

Formally, the right-hand side can be represented as:

$$(CITY \times \mathcal{P}(CITY))$$

Where:

- 'CITY' is the set of all cities
- ' $\mathcal{P}(CITY)$ ' is the power set of 'CITY', which represents the set of all possible subsets of 'CITY'.
- 'CITY $\times \mathcal{P}(\text{CITY})$ ' is the Cartesian product of 'CITY' and ' $\mathcal{P}(\text{CITY})$ ', which represents the set of all ordered pairs '(source, destinations)' where 'source' is a city and 'destinations' is a set of cities.

Therefore, the expression 'connections $\in (CITY, \mathcal{P}(CITY))$ ' means that the connections variable is an element of the set of all binary relations on the set of cities.

3. (2 pts) Is *connections* a function? If so, define the function formally, and reason about the properties of injectivity, surjectivity, and bijectivity.

To determine if *connections* is a function, we need to ensure that each source city maps to exactly one set of destination cities.

We see that each source city (e.g., Montreal, Ottawa, Toronto, Halifax, Quebec, Kingston) maps to exactly one set of destination cities, satisfying the definition of a function.

Now, let's define the function formally:

Let f be the function representing the railway connections, where:

- Domain (Dom(f)): Set of source cities.
- Codomain (Cod(f)): Set of sets of destinations cities.
- f(x): Set of destination cities connected to the source city x.

Formally:

f(x) = Set of destination cities connected to source city x

We then analyze whether the function is injective, surjective, and bijective:

- (a) Injectivity: The function is injective if each source city maps to a unique set of destination cities. In this case, it's not injective because multiple source cities may share the same group of destination cities.
- (b) Surjectivity: The function is surjective if every set of destination cities is mapped to by some source city. Since there can be multiple source cities mapping to the same group of destination cities, it is surjective.
- (c) Bijectivity: The function is bijective if it is both injective and surjective. Since it's not injective but surjective, it's not bijective.

In conclusion, the *connections* variable represents a function, but it is not injective or bijective, only surjective.

4. (2 pts) Describe the meaning and evaluate the following expression:

 $\{Montreal, Halifax\} \triangleleft connections$

The symbol \triangleleft denotes the domain restriction operator. When applied to a function or a relation, it restricts the domain of a function to a specified subset.

In the expression $\{Montreal, Halifax\} \triangleleft connections$, we are restricting the domain of the function represented by connections to the set $\{Montreal, Halifax\}$.

We are essentially interested in the subset of the connections that involve either Montreal or Halifax as the source city.

We evaluate the expression:

$$Montreal \mapsto \{Ottawa, Kingston, Quebec, Halifax\},$$

 $Halifax \mapsto \{Montreal, Quebec\}$

So, after the domain restriction, we only have connections involving Montreal and Halifax as source cities.

In conclusion, the expression $\{Montreal, Halifax\} \triangleleft connections$ yields the connections from Montreal and Halifax to their respective destination cities.

5. (2 pts) Describe the meaning and evaluate the following expression:

$$connections \triangleright \{\{Montreal, Halifax\}\}$$

The symbol ▷ represents the range restriction operator. When applied to a function, it restricts the range of the function to a specified subset.

In the expression $connections \triangleright \{\{Montreal, Halifax\}\}$, we are restricting the range of the function represented by connections to the set containing the destinations Montreal and Halifax.

We evaluate the expression:

$$Quebec \mapsto \{Montreal, Halifax\}$$

So, after the range restriction, we only have connections where the destination is either Montreal or Halifax.

In conclusion, the expression $connections \triangleright \{\{Montreal, Halifax\}\}\$ yields the connections from source cities that map to the destinations Montreal and Halifax.

6. (2 pts) Describe the meaning and evaluate the following expression:

$$\{Montreal, Quebec, Halifax\} \triangleleft connections$$

The symbol \triangleleft represents the domain subtraction or domain anti-restriction operator. When applied to a function or a relation, it removes a specified subset from the domain of the function/relation.

In the expression $\{Montreal, Quebec, Halifax\} \ \, \iff \ \, connections$, we are subtracting the set $\{Montreal, Quebec, Halifax\}$ from the domain of the function connections.

We evaluate the expression:

$$Ottawa \mapsto \{Montreal, Toronto\},$$

$$Toronto \mapsto \{Montreal, Ottawa\},$$

$$Kingston \mapsto \{Montreal\}$$

So, after the domain subtraction, we only have connections originating from Ottawa, Toronto, and Kingston.

In conclusion, the expression $\{Montreal, Quebec, Halifax\} \triangleleft connections$ yields the connections excluding those originating from Montreal, Quebec, and Halifax.

7. (2 pts) Describe the meaning and evaluate the following expression:

 $connections \triangleright \{\{Ottawa, Kingston, Quebec, Halifax\}, \{Montreal, Ottawa\}, \{Montreal\}\}$ The symbol \triangleright represents the range subtraction operator. When applied to a function, it removes a specified subset from the range of the function. In the expression $connections \triangleright \{\{Ottawa, Kingston, Quebec, Halifax\}, \{Montreal, Ottawa\}, \{Montreal, ott$

We evaluate the expression:

```
Ottawa \mapsto \{Montreal, Toronto\},
Halifax \mapsto \{Montreal, Quebec\},
Quebec \mapsto \{Montreal, Halifax\}
```

So, after the range subtraction, we only have connections starting from Ottawa, Halifax and Quebec.

In conclusion, the expression $connections \triangleright \{\{Ottawa, Kingston, Quebec, Halifax\}, \{Montreal, Ottawa\}\}$ yields the connections excluding those leading to the sets defined in the expression.

8. (2 pts) Describe the meaning and evaluate the following expression that forms a post-condition to some operation:

```
connections' = connections \oplus \{ Halifax \mapsto \{Montreal, Charlottetown, Quebec\}, Charlottetown \mapsto \{Halifax\} \}
```

The expression given represents a post-condition for an operation involving the variable connections. The operator being used here is the relational overriding operated denoted by \oplus . This operator combines two relations, where the right-hand side relation takes

precedence over the left-hand side in case of conflicting keys.

After evaluating this expression with the overriding operator:

- (a) The existing entry for Halifax in *connections* will be replaced with the new set of destinations: {Montreal, Charlottetown, Quebec}.
- (b) A new entry for Charlottetown with destinations {Halifax} will be added to connections.

The resulting updated *connections* will be:

```
connections = \{ \\ Montreal \mapsto \{Ottawa, Kingston, Quebec, Halifax\}, \\ Ottawa \mapsto \{Montreal, Toronto\}, \\ Toronto \mapsto \{Montreal, Ottawa\}, \\ Halifax \mapsto \{Montreal, Charlottetown, Quebec\}, \\ Quebec \mapsto \{Montreal, Halifax\}, \\ Kingston \mapsto \{Montreal\} \\ Charlottetown \mapsto \{Halifax\} \} \\ \}
```

- 9. (6 pts) Assume that we need to add a new entry into the database table represented by *connections*. We have decided <u>not</u> to deploy a precondition. What could be the consequences to the system if we deployed a) **set union** and b) **relational overriding**?
 - (a) Set Union: If set union is deployed without a pre-condition when adding a new entry to the *connections* database table, the consequences could include:

- Duplication of Data: Without a precondition, set union may lead to duplicate entries being added to the database. This can result in inefficiencies and potential data inconsistencies.
- **Increased Complexity**: The set union operation may add unnecessary complexity to the system, especially if it allows for redundant or conflicting data entries.
- Potential Data Integrity Issues: Inconsistent data entries may arise if set union is used without proper checks, leading to data integrity issues within the system.

(b) Relational Overriding:

- Loss of Existing Data: Relational overriding will replace existing data without considering any conditions. This can lead to the loss of valuable information if not handled carefullly.
- Potential Data Loss: If relational overriding is applied without caution, it
 can overwrite critical information unintentionally, resulting in data loss and
 inconsistencies.
- Inconsistencies in Data: Without a precondition, relational overriding may introduce inconsistencies in the database by replacing existing connections with new ones without proper validation.

In both cases, deploying these operations without preconditions can introduce risks to the system's data integrity, consistency, and overall functionality.

10. (2 pts) Consider operation AddOperation to add a new entry to the table, defined by the following pair of assertions.

```
city? \notin dom\ connections
connections' = connections \cup \{city? \mapsto destinations?\}
```

What would be the result of the call AddConnection(Montreal, (Boston, NYC)), and in the case of failure, whom should we blame and why?

Given the call AddConnection(Montreal, (Boston, NYC)), let's evaluate it step by step:

- (a) Check if Montreal is not already in the domain of connections. Since Montreal is present in the domain, the first assertion fails.
- (b) Since the first assertion fails, the operation cannot proceed to update the connections. Therefore, the call to AddConnection(Montreal, (Boston, NYC)) fails.

If this operation fails, the blame would typically fall on the caller of the function, who invoked the AddConnection function with a city that already exists in the domain of connections. It suggests that the caller did not properly check whether the city being added already exists in the system, leading to a violation of the precondition specified by the first assertion. Therefore, the caller should be responsible for handling such cases or ensuring that only valid data is passed to the AddConnection function.

11. (2 pts) Consider the following modification to the postcondition of AddOperation:

$$connections' = connections \oplus \{city? \mapsto destinations?\}$$

What would be the result of the call AddConnection(Kingston, (Boston, NYC)? In the absence of a precondition, can relational overriding unintentionally capture the intent of the operation?

The modified postcondition for the AddOperation utilizes relational overriding (\oplus) to update the connections. It specifies that the new entry $city? \mapsto destinations?$) should be added to the existing connections, overriding any existing mapping for the same city if it exists.

Now, let's consider the call AddConnection(Kingston, (Boston, NYC)):

(a) Since Kingston is not in the domain of connections, the operation can proceed

without any conflict.

(b) The postcondition specifies that the connections should be updated using rela-

tional overriding, meaning that if Kingston already exists in the connections,

its destinations will be replaced with the new destinations (Boston, NYC). If

Kingston does not exist in the connections, a new entry will be added for it.

In this case, since Kingston is not already in the connections, the postcondition simply

adds a new entry for Kingston mapped to the destinations (Boston, NYC).

In the absence of a precondition, relational overriding can unintentionally capture the

intent of the operation if there are conflicting entries. For example, if Kingston already

existed in the connections with different destinations, the use of relational overriding

would replace those destinations with the new ones (Boston, NYC), potentially over-

riding the existing connections unintentionally.

Therefore, careful consideration should be given to the potential consequences of using

relational overriding without a precondition to ensure that it aligns with the intended

behavior of the operation.

12. (3 pts) Consider the following state schema in the Z Specification Language:

 $_Railway Management _$

cities : PCITY

connections : $CITY \rightarrow \mathcal{P}CITY$

 $cities = dom \ connections$

Define the schema for operation GetDestinations which returns all destinations for one

given city.

To define the schema for the operation GetDestinationsGetDestinations, which returns

all destinations for one given city, we can use the Z notation. The schema will take

a city as input and return its corresponding set of destinations. Here's how we can

define it:

11

```
\_GetDestinations \_
\_\Delta Railway Management
city?: CITY
destinations!: \mathcal{P}CITY
city? \in cities
destinations! = connections(city?)
```

In this schema:

- GetDestinations GetDestinations represents the operation schema.
- \triangle RailwayManagement denotes that this operation may update the state of the system represented RailwayManagement.
- city? is an input variable representing the city for which destinations are requested
- destinations! is an output variable representing the set of destinations corresponding to the input city.
- The where clause ensures that the input city (city?) is a valid city in the system (i.e., it exists in the set cities).
- The assignment destinations! = connections(city?) retrieves the set of destinations for the given city from the connections mapping.

This schema ensures that the operation *GetDestinations* operates correctly within the context of the *RailwayManagement* state schema, returning the set of destinations for a given city.

13. (1 pt) (**PROGRAMMING**) Define global variables *connections* in Common LISP and populate it with some sample data. Demonstrate that the variable indeed contains the ordered pairs as shown above.

```
1 (defvar *connections* '())
2
3 (defun add-connection (source destinations)
4  (push (cons source destinations) *connections*))
5
```

```
6 (defun initialize-connections ()
    (setq *connections*
          '((Montreal . (Ottawa Kingston Quebec Halifax))
            (Ottawa . (Montreal Toronto))
            (Toronto . (Montreal Ottawa))
            (Halifax . (Montreal Quebec))
            (Quebec . (Montreal Halifax))
            (Kingston . (Montreal)))))
15 ;; Initialize connections
  (initialize-connections)
  ;; Function to display connections with arrows
  (defun display-connections-with-arrows ()
    (format t "Connections: ~%")
20
    (dolist (connection *connections*)
21
      (let ((source (car connection))
            (destinations (cdr connection)))
        (format t "~a -> " source)
2.4
        (dolist (destination destinations)
25
          (format t "~a, " destination))
        (terpri))))
  ;; Display the contents of connections with arrows
30 (display-connections-with-arrows)
```

We explain a basic rundown of the code:

- (a) The code begins by initializing the global variable *connections* to an empty list using defvar. This variable will store the railway connections data.
- (b) The add-connection function is defined to add a new connection to the *connections* variable. It takes two arguments: source, representing the source city, and destinations, representing a list of destination cities. It uses push to add a new cons cell representing the connection to the *connections* list.
- (c) The initialize-connections function is defined to populate the *connections* vari-

- able with sample data. It sets *connections* to a list of cons cells, each representing a connection from a source city to its corresponding destinations.
- (d) The display-connections-with-arrows function is defined to visually display the connections stored in the *connections* variable. It iterates over each connection in *connections*, extracting the source city and its destinations, and prints them with arrows separating the source city from its destinations.
- (e) Finally, the code calls the initialize-connections function to populate the *connections* variable with sample data and then calls the display-connections-with-arrows function to display the contents of *connections* in a visually formatted way with arrows.

```
Absolute running time: 0.16 sec, cpu time: 0.02 sec, memory peak: 9 Mb, absolute service time: 0,28 sec

Connections:

MONTREAL -> OTTAWA, KINGSTON, QUEBEC, HALIFAX,

OTTAWA -> MONTREAL, TORONTO,

TORONTO -> MONTREAL, OTTAWA,

HALIFAX -> MONTREAL, QUEBEC,

QUEBEC -> MONTREAL, HALIFAX,

KINGSTON -> MONTREAL,
```

Figure 1: Environment Interaction for Question 1 - Part 13

14. (3 pts) Describe how you would validate variable *connections*, i.e. how to show that it holds a function.

To validate that the variable *connections* holds a function, we need to verify that it satisfies the properties of a mathematical function. In mathematical terms, a function is a relation between a set of inputs (the domain) and a set of possible outputs (the codomain), such that each input is related to exactly one output.

Here's how we can validate variable *connections* to ensure it holds a function:

(a) **Domain Check**: Ensure that each source city in the domain of connections is associated with at least one destination city. This ensures that every input (source

- city) has a corresponding output (destination city).
- (b) **Unique Outputs**: Ensure that each source city is associated with a unique set of destination cities. In other words, there are no duplicate entries for the same source city. This ensures that each input is related to exactly one output.
- (c) **Consistency**: Ensure that the relation is consistent, meaning that if a source city s is associated with a destination city dd, then dd must be present in the domain of *connections* with s as one of its destinations. This ensures that the relation does not contain contradictory information.
- (d) **No Extra Entries**: Ensure that there are no extra entries in *connections* that do not conform to the function's definition. This means ensuring that every key-value pair in *connections* adheres to the function's mapping rules.
- 15. (3 pts) (**PROGRAMMING**) Define a predicate function, isfunction, in Common Lisp that reads a variable like *connections* and indicates if the variable corresponds to a function or not.

```
(defun isfunctionp (variable)
    "Check if the given variable corresponds to a function."
    (and (listp variable)
                                          ; Check if variable is a list
         (every #'consp variable)
                                          ; Check if all elements are
     cons cells
         (every (lambda (pair)
                                          ; Check if each cons cell is a
      valid key-value pair
                  (and (consp pair)
                        (symbolp (car pair))
                        (listp (cdr pair))))
                variable)))
9
  ;; Example 1: Variable corresponds to a function
  (setq *connections-function*
        '((Montreal . (Ottawa Kingston Quebec Halifax))
13
          (Ottawa . (Montreal Toronto))
14
          (Toronto . (Montreal Ottawa))
          (Halifax . (Montreal Quebec))
```

```
(Quebec . (Montreal Halifax))
          (Kingston . (Montreal))))
19
  ;; Test the function for *connections-function*
  (if (isfunctionp *connections-function*)
      (format t "The variable *connections-function* corresponds to a
     function. ~%")
      (format t "The variable *connections-function* does not
     correspond to a function. "%"))
24
 ;; Example 2: Variable does not correspond to a function
  (setq *connections-nonfunction* '(Montreal Ottawa Toronto))
27
  ;; Test the function for *connections-nonfunction*
  (if (isfunctionp *connections-nonfunction*)
      (format t "The variable *connections-nonfunction* corresponds to
     a function. ~%")
      (format t "The variable *connections-nonfunction* does not
     correspond to a function. "%"))
```

We describe a basic run-down of the code:

- (a) The isFunction function checks whether a given variable corresponds to a function.
- (b) It checks if the variable is a list (listp), ensuring it has the structure of a function.
- (c) It verifies if every element of the list is a cons cell (consp), ensuring each element is a key-value pair.
- (d) It checks if each cons cell consists of a symbol as the key and a list as the value, as expected for a function.
- (e) Example 1 demonstrates a variable (*connections function*) that corresponds to a function, with a list of key-value pairs.
- (f) Example 2 demonstrates a variable (*connections nonfunction*) that does not correspond to a function, being just a list of symbols without the key-value pair structure.

```
Absolute running time: 0.16 sec, cpu time: 0.02 sec, memory peak: 9 Mb, absolute service time: 0,25 sec

The variable *connections-function* corresponds to a function.

The variable *connections-nonfunction* does not correspond to a function.
```

Figure 2: Environment Interaction for Question 1 - Part 15

16. (2 pts) (**PROGRAMMING**) Define function getDestinations in Common LISP.

```
1 (defun getDestinations (city connections)
    "Retrieve the destinations for a given city from the connections."
    (cdr (assoc city connections)))
5; Example usage:
6 (defvar *connections*
    '((Montreal . (Ottawa Kingston Quebec Halifax))
      (Ottawa . (Montreal Toronto))
      (Toronto . (Montreal Ottawa))
      (Halifax . (Montreal Quebec))
      (Quebec . (Montreal Halifax))
      (Kingston . (Montreal))))
14 ;; Get destinations for Montreal
15 (format t "Destinations for Montreal: ~a~%" (getDestinations '
     Montreal *connections*))
;; Get destinations for Ottawa
18 (format t "Destinations for Ottawa: ~a~%" (getDestinations 'Ottawa *
     connections*))
```

We explain a basic rundown of the code:

- (a) The *getDestinations* function takes two arguments: *city*, the city for which destinations are to be retrieved, and *connections*, the list of connections.
- (b) Inside the function, it uses the *assoc* function to search for the *city* in the *connections* list and retrieve the corresponding cons cell.

- (c) Then, it uses cdr to extract the destinations from the cons cell.
- (d) Finally, it returns the list of destinations for the given city.
- (e) Example usage demonstrates how to use the *getDestinations* function with the *connections* variable to retrieve destinations for Montreal and Ottawa.

```
Absolute running time: 0.16 sec, cpu time: 0.02 sec, memory peak: 9 Mb, absolute service time: 0,32 sec

Destinations for Montreal: (OTTAWA KINGSTON QUEBEC HALIFAX)

Destinations for Ottawa: (MONTREAL TORONTO)
```

Figure 3: Environment Interaction for Question 1 - Part 16

PROBLEM 2 (50 pts)

Consider an airport management system. Each airport has a unique id (e.g. Montreal:YUL). Let us introduce the types AIRPORT and CITY. We also introduce variable airports that contains associations between airport id's and their corresponding host cities. A possible state of the system is shown below:

```
airports = \{YUL \mapsto Montreal, \\ LCY \mapsto London\ UK, \\ LHR \mapsto London\ UK, \\ MIL \mapsto Milan, \\ SFO \mapsto San\ Francisco, \\ SDQ \mapsto Santo\ Domingo \\ \}
```

1. (1 pt) (PROGRAMMING) Define global variable airports in Common LISP and populate it with the above data. Demonstrate that the variable indeed contains the ordered pairs as shown above.



Figure 4: Output of Question 2 - Part 1

2. (2 pts) Provide a declaration of variable monitored that holds all airport id's.

Solution:

monitored: AIRPORT

3. (3 pts) What kind of variable is airports? Provide a formal definition together with

any and all applicable properties.

Solution:

airports is a partial many-to-one function that relates ordered pairs. The domain of

these ordered pairs are the set of airport ids included in the type AIRPORT. The range

of the ordered sets is the set of cities included in the type CITY. It is defined as follows:

 $airports: AIRPORT \rightarrow CITY$

4. (3 pts) Describe what data structure you would deploy to model variable airports.

Note that you may not use a Dictionary. Should this be an ordered or an unordered

structure? Discuss

Solution: I would use the linked list ADT to model the airport variable's relation in

the case where we can't use a dictionary. This would work because each node of the

list would contain a key and a value. When adding a new element, we would iterate

over all nodes and check if the new key to be added already exists. This check would

ensure that our list doesn't contain any duplicate keys. The linked list is an example

of an unordered ADT (the order of insertion doesn't matter).

5. (4 pts) Provide a formal specification of the state of the system in terms of a Z speci-

fication schema

Solution:

AirportManagement

 $monitored: \mathcal{P}(AIRPORT)$

 $airports: AIRPORT \rightarrow CITY$

monitored = dom(airports)

20

6. (6 pts) Provide a schema for operation AddAirportOK that adds a new airport to the system. With the aid of success and error schema(s), provide a definition for operation AddAirport that the system will place in its exposed interface.

 $MESSAGE ::= ok \mid error.$

```
Success \Xi AirportManagement response!: MESSAGE response! = 'ok'
```

```
AirportAlreadyExists
\Xi AirportManagement
airport?: AIRPORT
response!: MESSAGE
airport? \in monitored
response! = 'error'
```

 $AddAirport = (AddAirportOk \land Success) \oplus AirportAlreadyExists$

7. (3 pts) (PROGRAMMING) Define function AddAirport in Common LISP.

```
;; Initialize the hash table
2 (defvar *airports* (make-hash-table :test 'equal))
4 ;; Add some data to the hash table
5 (when (zerop (hash-table-count *airports*));; This line makes sure
     that the hash table is empty before adding data
      (setf (gethash 'YUL *airports*) 'Montreal)
      (setf (gethash 'LCY *airports*) 'London)
      (setf (gethash 'LHR *airports*) 'London)
      (setf (gethash 'MIL *airports*) 'Milan)
      (setf (gethash 'SFO *airports*) 'San_Francisco)
      (setf (gethash 'SDQ *airports*) 'Santo_Domingo))
13 ;; Initialize the monitored airports
14 (defvar *monitored* (list 'YUL 'LCY 'LHR 'MIL 'SFO 'SDQ))
  (defun AddAirport (airport city)
      (cond ((includes-airport airport *monitored*)
17
                (format t "Airport ~a already exists.~%" airport))
18
          (t (progn (setf (gethash airport *airports*) city)
19
                       (push airport *monitored*)
                       (format t "Added Airport: ~a -> ~a.~%" airport
21
     city)
                      ))))
22
  (defun includes-airport (airport monitored)
      (member airport monitored))
25
26
  (defun display-contents (list title)
      (format t "~a:~%" title)
      (case (type-of list)
          (hash-table (maphash (lambda (key value) (format t "~a ~a~%"
30
     key value)) list))
```

```
(cons (mapcar (lambda (value) (format t "~a~%" value)) list))
))

(cons (mapcar (lambda (value) (format t "~a~%" value)) list))
))

(cons (mapcar (lambda (value) (format t "~a~%" value)) list))

(cons (mapcar (lambda (value) (format t "~a~%" value)) list))

(display-contents *airports* "Initial Values of *airports*")

(AddAirport 'YUL 'Montreal)

(AddAirport 'UYL 'Toronto)

(display-contents *airports* "Values of *airports* After AddAirport(s )")

(display-contents *monitored* "Values of *monitored* After AddAirport (s)")
```

```
PROBLEMS
          OUTPUT
                   DEBUG CONSOLE
                                 PORTS 40
                                             REPL
                                                   TERMINAL
                                                                      COMMENTS
; compiling file "/code/concordia/SOEN-331/Assignment2/code/airports-2-7.lisp"
; wrote /code/concordia/SOEN-331/Assignment2/code/airports-2-7.fasl
; compilation finished in 0:00:00.000
Initial Values of *airports*:
YUL MONTREAL
LCY LONDON
LHR LONDON
MIL MILAN
SFO SAN FRANCISCO
SDQ SANTO DOMINGO
Airport YUL already exists.
Added Airport: LUY -> MONTREAL.
Added Airport: UYL -> TORONTO.
Values of *airports* After AddAirport(s):
YUL MONTREAL
LCY LONDON
LHR LONDON
MIL MILAN
SFO SAN FRANCISCO
SDQ SANTO DOMINGO
LUY MONTREAL
UYL TORONTO
Values of *monitored* After AddAirport(s):
LUY
YUL
LCY
LHR
MIL
SF0
SDQ
cl-user >
```

Figure 5: Output of Question 2 - Part 7

8. (6 pts) Provide a schema for operation UpdateAirportOK that updates the host city of a given airport. With the aid of success and error schema(s), provide a definition for operation UpdateAirport that the system will place in its exposed interface.

```
Success \Xi AirportManagement response!: MESSAGE response! = 'ok'
```

```
egin{align*} AirportDoesNotExist & & & \\ & \Xi AirportManagement & & \\ & airport?: AIRPORT & & \\ & response!: MESSAGE & & \\ & airport? 
otin monitored & \\ & response! = 'error' & & \\ \hline \end{align*}
```

```
\_AirportCityPairAlreadyExists \_
\Xi AirportManagement
airport?: AIRPORT
city?: CITY
response!: MESSAGE
airport? \mapsto city? \in airports
response! = 'error'
```

```
\label{eq:potential} \begin{split} UpdateAirport & \triangleq (UpdateAirportOK \land Success) \\ & \oplus (AirportDoesNotExist \lor AirportCityPairAlreadyExists) \end{split}
```

9. (1 pt) What would be the value of variable airports upon calling UpdateAirport(YUL, Dorval)?

Solution:

```
airports = \{YUL \mapsto Dorval, \\ LCY \mapsto London \ UK, \\ LHR \mapsto London \ UK, \\ MIL \mapsto Milan, \\ SFO \mapsto San \ Francisco, \\ SDQ \mapsto Santo \ Domingo \\ \}
```

10. (3 pts) (PROGRAMMING) Define function UpdateAirport in Common LISP.

```
14 (defvar *monitored* (list 'YUL 'LCY 'LHR 'MIL 'SFO 'SDQ))
(defun UpdateAirport (airport city)
      (cond ((not (includes-airport airport *monitored*)) (format t "
     Airport ~a does not exist in hash-table ~a.~%" airport (
     symbol-name '*airports*)))
            ((equal city (gethash airport *airports*)) (format t "
18
     Record (~a -> ~a) already exists.~%" airport city))
            (t (format t "Updated (~a -> ~a) to: ~a -> ~a.~%" airport (
19
     gethash airport *airports*) airport city) (setf (gethash airport *
     airports*) city))
          ))
20
21
  (defun includes-airport (airport monitored)
      (member airport monitored))
23
  (defun display-contents (list title)
      (format t "~a:~%" title)
      (case (type-of list)
27
          (hash-table (maphash (lambda (key value) (format t "~a ~a~%"
2.8
     key value)) list))
          (cons (mapcar (lambda (value) (format t "~a~%" value)) list))
     ))
31 (display-contents *airports* "Values of *airports* Before the Update"
     )
33 ;; Test the function
34 (UpdateAirport 'YUL 'Montreal)
35 (UpdateAirport 'ZZZ 'Toronto)
36 (UpdateAirport 'LCY 'Glasgow)
38 (display-contents *airports* "Values of *airports* After the Update")
```

```
PROBLEMS 3
             OUTPUT
                      DEBUG CONSOLE
                                    PORTS 43
                                                REPL
                                                      TERMINAL
                                                                         COMMENTS
; compiling file "/code/concordia/SOEN-331/Assignment2/code/airports-2-10.lisp"
; wrote /code/concordia/SOEN-331/Assignment2/code/airports-2-10.fasl
; compilation finished in 0:00:00.010
Values of *airports* Before the Update:
YUL MONTREAL
LCY LONDON
LHR LONDON
MIL MILAN
SFO SAN FRANCISCO
SDQ SANTO DOMINGO
LUY MONTREAL
UYL TORONTO
Record (YUL -> MONTREAL) already exists.
Airport ZZZ does not exist in hash-table *AIRPORTS*.
Updated (LCY -> LONDON) to: LCY -> GLASGOW.
Values of *airports* After the Update:
YUL MONTREAL
LCY GLASGOW
LHR LONDON
MIL MILAN
SFO SAN FRANCISCO
SDQ SANTO DOMINGO
LUY MONTREAL
UYL TORONTO
cl-user >
```

Figure 6: Output of Question 2 - Part 10

11. (6 pts) Provide a schema for operation DeleteAirportOK that removes an airport from the system. With the aid of success and error schema(s), provide a definition for operation DeleteAirport that the system will place in its exposed interface.

```
Delete Airport Ok \\ \Delta Airport Management \\ airport?: AIRPORT \\ airport? \in monitored \\ monitored' = monitored \setminus \{airport?\} \\ airports' = \{airport?\} \not = airports
```

```
Success \subseteq \Xi AirportManagement response!: MESSAGE response! = 'ok'
```

```
\_AirportDoesNotExist \_
\Xi AirportManagement
airport?: AIRPORT
response!: MESSAGE
airport? \not\in monitored
response! = 'error'
```

```
DeleteAirport = (DeleteAirportOk \land Success)
\oplus (AirportDoesNotExist)
```

12. (3 pts) (PROGRAMMING) Define function DeleteAirport in Common LISP.

```
;; Initialize the hash table
2 (defvar *airports* (make-hash-table :test 'equal))
4 ;; Add some data to the hash table
5 (when (zerop (hash-table-count *airports*));; This line makes sure
     that the hash table is empty before adding data
      (setf (gethash 'YUL *airports*) 'Montreal)
      (setf (gethash 'LCY *airports*) 'London)
      (setf (gethash 'LHR *airports*) 'London)
      (setf (gethash 'MIL *airports*) 'Milan)
      (setf (gethash 'SFO *airports*) 'San_Francisco)
      (setf (gethash 'SDQ *airports*) 'Santo_Domingo))
13 ;; Initialize the monitored airports
14 (defvar *monitored* (list 'YUL 'LCY 'LHR 'MIL 'SFO 'SDQ))
16 (defun DeleteAirport (airport)
      (cond ((not (includes-airport airport *monitored*)) (format t "
     Airport ~a does not exist in list ~a.~%" airport (symbol-name '*
     monitored*)))
            (t (progn (format t "Deleted element ~a -> ~a.~%" airport (
     gethash airport *airports*))
                      (remhash airport *airports*)
19
                      (setf *monitored* (remove airport *monitored*))
20
                      ))))
  (defun includes-airport (airport monitored)
      (member airport monitored))
24
25
  (defun display-contents (list title)
      (format t "~a:~%" title)
      (case (type-of list)
28
          (hash-table (maphash (lambda (key value) (format t "~a ~a~%"
```

```
key value)) list))

(cons (mapcar (lambda (value) (format t "~a~%" value)) list))

(display-contents *airports* "Value of *airports* Before Delete")

(DeleteAirport 'ZZZ)

(DeleteAirport 'YUL)

(display-contents *airports* "Values of *airports* After Delete")

(display-contents *monitored* "Values of *monitored* After Delete")
```

```
PROBLEMS 3
             OUTPUT
                      DEBUG CONSOLE
                                    PORTS 41
                                                REPL
                                                       TERMINAL
                                                                         COMMENTS
; compiling file "/code/concordia/SOEN-331/Assignment2/code/airports-2-12.lisp"
; wrote /code/concordia/SOEN-331/Assignment2/code/airports-2-12.fasl
; compilation finished in 0:00:00.010
Value of *airports* Before Delete:
YUL MONTREAL
LCY LONDON
LHR LONDON
MIL MILAN
SFO SAN FRANCISCO
SDQ SANTO DOMINGO
Airport ZZZ does not exist in list *MONITORED*.
Deleted element YUL -> MONTREAL.
Values of *airports* After Delete:
LCY LONDON
LHR LONDON
MIL MILAN
SFO SAN FRANCISCO
SDQ SANTO DOMINGO
Values of *monitored* After Delete:
LCY
LHR
MIL
SFO
SDQ
cl-user >
```

Figure 7: Output of Question 2 - Part 12

13. (6 pts) Provide a schema for operation GetAllAirportsOK that returns all airports hosted by a given city. With the aid of success and error schema(s), provide a definition for operation GetAllAirports that the system will place in its exposed interface.

```
Success \subseteq \Xi AirportManagement response!: MESSAGE response! = 'ok'
```

```
CityDoesNotExist \Xi AirportManagement city?: CITY response!: MESSAGE city? \not\in ran(airports) response! = 'error'
```

```
GetAllAirports = (GetAllAirportsOK \land Success)
\oplus (CityDoesNotExist)
```

14. (3 pts) (PROGRAMMING) Define function GetAllAirports in Common LISP.

```
;; Initialize the hash table
2 (defvar *airports* (make-hash-table :test 'equal))
4 ;; Add some data to the hash table
5 (when (zerop (hash-table-count *airports*));; This line makes sure
     that the hash table is empty before adding data
      (setf (gethash 'YUL *airports*) 'Montreal)
      (setf (gethash 'LCY *airports*) 'London)
      (setf (gethash 'LHR *airports*) 'London)
      (setf (gethash 'MIL *airports*) 'Milan)
      (setf (gethash 'SFO *airports*) 'San_Francisco)
      (setf (gethash 'SDQ *airports*) 'Santo_Domingo))
  (defun GetAllAirports (city)
      (format t "Getting all airports for city ~a:~%" city)
14
      (cond ((not (member city (get-values *airports*))) (format t "
     City ~a does not exist in hash-table ~a.~%" city (symbol-name '*
     airports*)))
            (t (mapcar (lambda (airport) (format t "~a -> ~a.~%"
16
     airport city)) (get-keys-from-value city *airports*)))))
18 ;; Get a list of all values in the hash table
  (defun get-values (hash-table)
      (let ((values '()))
20
          (maphash (lambda (key value)
                       (declare (ignore key)) ;; Ignore the key (
22
     removes warning)
                       (push value values))
                   hash-table)
24
          values))
27 ;; Get a list of all keys in the hash table that have a specific
     value
```

```
(defun get-keys-from-value (value hash-table)
      (let ((keys '()))
          (maphash (lambda (key val) (if (equal val value) (push key
30
     keys))) hash-table)
          keys))
31
32
  (defun display-contents (list title)
      (format t "~a:~%" title)
34
      (case (type-of list)
35
          (hash-table (maphash (lambda (key value) (format t "~a ~a~%"
36
     key value)) list))
          (cons (mapcar (lambda (value) (format t "~a~%" value)) list))
     ))
  (display-contents *airports* "Initial Elements in *airports*")
41 ;; Test the function
42 (GetAllAirports 'Montreal)
43 (GetAllAirports 'London)
```

```
PROBLEMS
          OUTPUT
                  DEBUG CONSOLE
                                 PORTS 44
                                             REPL
                                                   TERMINAL
                                                                      COMMENTS
; compiling file "/code/concordia/SOEN-331/Assignment2/code/airports-2-14.lisp"
; wrote /code/concordia/SOEN-331/Assignment2/code/airports-2-14.fasl
; compilation finished in 0:00:00.010
Initial Elements in *airports*:
YUL MONTREAL
LCY LONDON
LHR LONDON
MIL MILAN
SFO SAN FRANCISCO
SDQ SANTO DOMINGO
Getting all airports for city MONTREAL:
YUL -> MONTREAL.
Getting all airports for city LONDON:
LHR -> LONDON.
LCY -> LONDON.
cl-user >
```

Figure 8: Output of Question 2 - Part 14

PROBLEM 3 (10 pts)

Consider the temperature monitoring system from our lecture notes. In this part, we will extract the specification with a new requirement.

Operation ReplaceSensor Sensors are physical devices, subjected to deterioration, or other type of damage. We need to provide the ability of the system to replace a sensor with another. For simplicity, let us not plan ("fix", and) reuse them, but permanently remove them from the system."

```
Replaceable Sensor \_
(DeploySensor, ReadTemperature, ReplaceSensor)
TempMonitor
 \_ReplaceSensorOK\_
 \Delta Replaceable Sensor
 oldSensor?, newSensor?: SENSOR\_TYPE
 oldSensor? \in deployed
 newSensor? \not\in deployed
 deployed' = (deployed \setminus \{oldSensor?\}) \cup \{newSensor?\}
 map' = \{oldSensor?\} \triangleleft (map \cup \{newSensor? \mapsto map(oldSensor?)\})
 read' = \{oldSensor?\} \triangleleft (read \cup \{newSensor? \mapsto read(oldSensor?)\})
 SensorNotFound\_
 \Xi Replaceable Sensor
 oldSensor?: SENSOR\_TYPE
 response!: MESSAGE
 oldSensor? \not\in deployed
 response! = 'Sensor not found'
 . SensorAlreadyDeployed _____
 \Xi Replaceable Sensor
 newSensor?: SENSOR\_TYPE
 response!: MESSAGE
 newSensor? \in deployed
 response! = 'Sensor already deployed'
ReplaceSensor \cong (ReplaceSensorOK \land Success)
   \oplus (SensorNotFound \vee SensorAlreadyDeployed)
```