



# TDDCI7

## Seminar II Search I Physical Symbol Systems Uninformed Search



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Department of Computer and Information Science  
Linköping University, Sweden



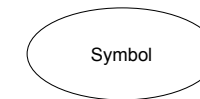
## Physical Symbol System Hypothesis

Computer Science as Empirical Enquiry: Symbols and Search  
Newell and Simon (1976)

Newell and Simon are trying to lay the foundational basis for the science of artificial intelligence.

What are the structural requirements for intelligence?

Can we define laws of qualitative structure for the systems being studied?



What is a symbol, that intelligence may use it, and intelligence, that it may use a symbol? (McCulloch)



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## Physical Symbol Systems

The adjective “physical” denotes two important aspects:

- Such systems clearly obey the laws of physics -- they are realizable by engineered systems made of engineered components.
- The use of the term “symbol” is not restricted to human symbol systems.

A physical symbol system consists of:

- a set of entities called symbols which are physical patterns that can occur as components of another type of entity called an expression (or symbol structure).
- At any instant of time the system will contain a collection of symbol structures.
- The system also contains a collection of processes that operate on expressions to produce other expressions: processes of creation, modification, reproduction, and destruction.

A physical-symbol system is a machine that produces through time an evolving collection of symbol structures and exists in a world of objects wider than just those symbol structures themselves.



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## Designation and Interpretation

There are two concepts central to these structures of expressions, symbols and objects:

Designation - An expression designates an object if, given the expression, the system can either effect the object itself or behave in ways depending on the object.

Interpretation - The system can interpret an expression if the expression designates a process and if, given the expression, the system can carry out the process.

Some additional requirements in the paper



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## Physical-Symbol System Hypothesis



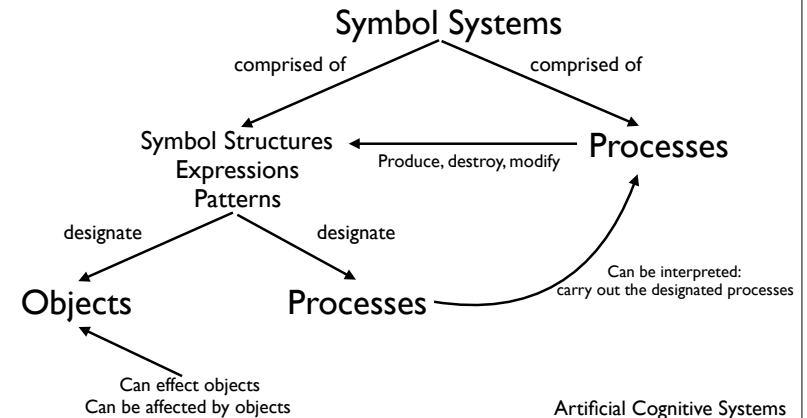
*The Physical-Symbol System Hypothesis* - A physical-symbol system has the necessary and sufficient means for general intelligent action.

*necessary* - any system exhibiting intelligence will prove upon analysis to be a physical symbol system.

*sufficient* - any physical-symbol system of sufficient size can be organized further to exhibit general intelligence.



## Graphical summary of PSS Hypothesis



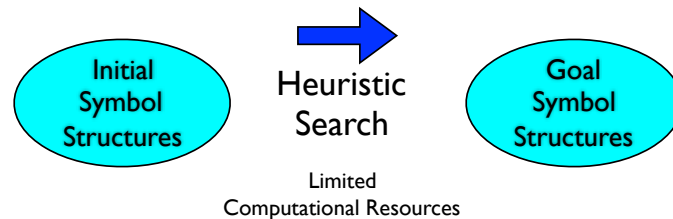
Artificial Cognitive Systems  
David Vernon, MIT Press



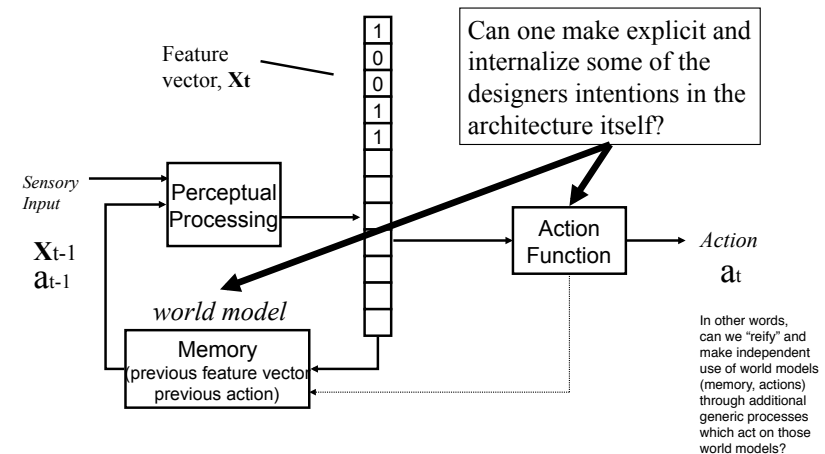
## Heuristic Search Hypothesis



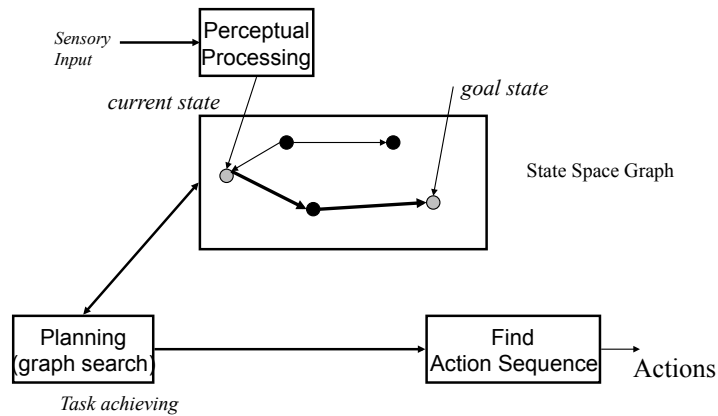
*Heuristic Search Hypothesis* - The solutions to problems are represented as symbol structures. A physical-symbol system exercises its intelligence in problem solving by search -- that is, by progressively modifying symbol structures until it produces a solution structure.



## Recall: State Machine Agent



## Problem-Solving Agent (Version I)



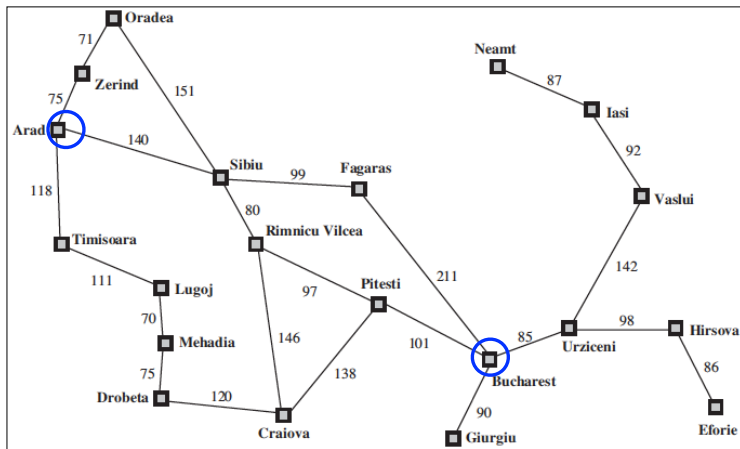
## Simple Problem-Solving Agent

```

function SIMPLE-PROBLEM-SOLVING-AGENT(percept) returns an action
  persistent: seq, an action sequence, initially empty
               state, some description of the current world state
               goal, a goal, initially null
               problem, a problem formulation

  state ← UPDATE-STATE(state, percept)
  if seq is empty then
    goal ← FORMULATE-GOAL(state)
    problem ← FORMULATE-PROBLEM(state, goal)
    seq ← SEARCH(problem)
    if seq = failure then return a null action
  action ← FIRST(seq)
  seq ← REST(seq)
  return action
    
```

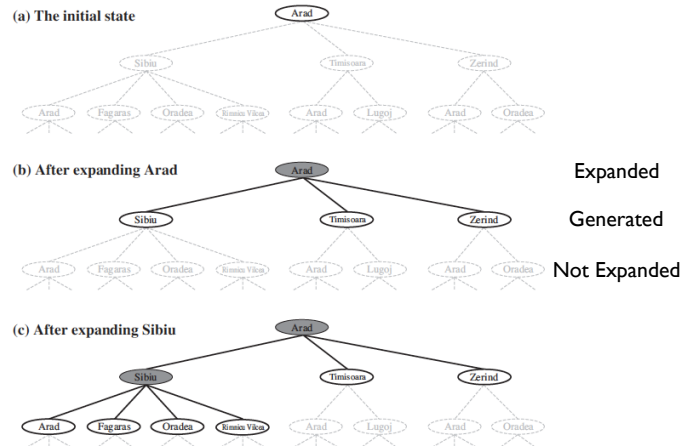
## Romania Route Finding Problem



## Problem Formulation

- **Initial State** - The state the agent starts in
    - $\text{In}(\text{Arad})$
  - **Actions(State)** - A description of what actions are available in each state.
    - $\text{Actions}(\text{In}(\text{Arad})) = \{\text{Go}(\text{Sibiu}), \text{Go}(\text{Timisoara}), \text{Go}(\text{Zerind})\}$
  - **Result(State, Action)** - A description of what each action does (Transition function)
    - $\text{Result}(\text{In}(\text{Arad}), \text{Go}(\text{Zerind})) = \text{In}(\text{Zerind})$
  - **Goal Test** - Tests whether a given state is a goal
    - Often a set of states:  $\{\text{In}(\text{Bucharest})\}$
  - **Path Cost** - A function that assigns a cost to each path
    - # of actions, sum of distances, etc.
  - **Solution** - A path from the start state to the goal state
- } State Space

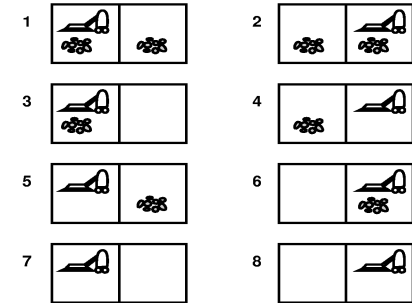
## Search Space: Route Finding



## Problem Formulation for the Vacuum Cleaner World

### - World states:

2 positions, dirt or no dirt  
→ 8 world states



### - Actions:

Left (L), Right (R), or Suck (S)

### - Transition model: next slide

### - Initial State: Choose.

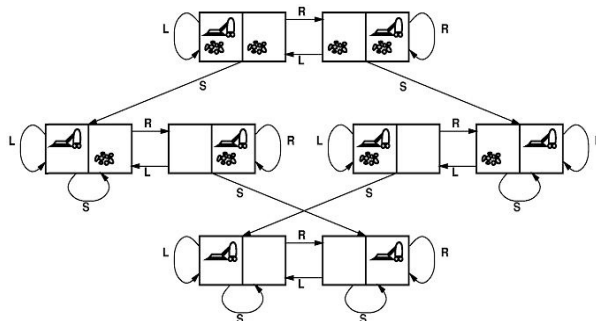
### - Goal Test:

no dirt in the rooms

### - Path costs:

one unit per action

## Vacuum World: State Space



If the environment is **completely accessible**, the vacuum cleaner always knows where it is and where the dirt is. The solution then can be found by **searching** for a path from the initial state to the goal state.

States for the search: The world states 1-8.

## Example: Missionaries and Cannibals

Informal problem description:

- Three missionaries and three cannibals are on **one side** of a river that they wish to cross.
- A boat is available that can hold **at most two people**.
- You must never leave a group of **missionaries outnumbered by cannibals** on the same bank.

- ➔ How should the **state space** be represented?
- ➔ What is the **initial state**?
- ➔ What is the **goal state**?
- ➔ What are the **actions**?

## Formalization of the M&C Problem



**States:** triple  $(x,y,z)$  with  $0 \leq x,y,z \leq 3$ , where  $x,y$ , and  $z$  represent the number of missionaries, cannibals and boats currently on the original bank.

**Initial State:**  $(3,3,1)$

**Successor function:** from each state, either bring one missionary, one cannibal, two missionaries, two cannibals, or one of each type to the other bank.

**Note:** not all states are attainable (e.g.,  $(0,0,1)$ ), and some are illegal.

**Goal State:**  $(0,0,0)$

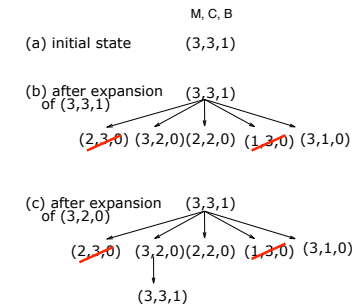
**Path Costs:** 1 unit per crossing



## General Search



From the initial state, produce all successive states step by step  $\rightarrow$  search tree.



## Examples of Real-World Problems



- **Route Planning, Shortest Path Problem**
  - Routing video streams in computer networks, airline travel planning, military operations planning...
- **Travelling Salesperson Problem (TSP)**
  - A common prototype for NP-complete problems
- **VLSI Layout**
  - Another NP-complete problem
- **Robot Navigation (with high degrees of freedom)**
  - Difficulty increases quickly with the number of degrees of freedom. Further possible complications: errors of perception, unknown environments
- **Assembly Sequencing**
  - Planning of the assembly of complex objects (by robots)



## Implementing the Search Tree



**Data structure for nodes in the search tree:**

**State:** state in the state space

**Parent-Node:** Predecessor nodes

**Action:** The operator that generated the node

**Depth:** number of steps along the path from the initial state

**Path Cost:** Cost of the path from the initial state to the node

**Operations on a queue:**

**Make-Queue(Elements):** Creates a queue

**Empty?(Queue):** Empty test

**First(Queue):** Returns the first element of the queue (Non-destructive)

**Remove-First(Queue):** Returns the first element

**Insert(Element, Queue):** Inserts new elements into the queue (various possibilities)

**Insert-All(Elements, Queue):** Inserts a set of elements into the queue



## States and Nodes

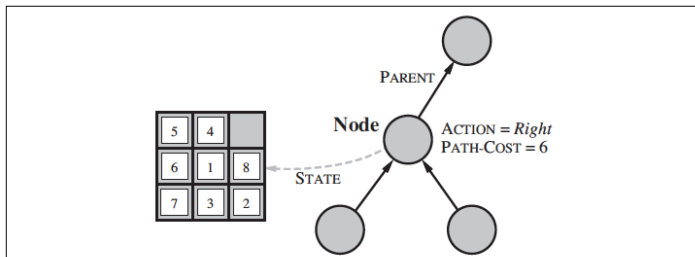


Figure 3.10 Nodes are the data structures from which the search tree is constructed. Each has a parent, a state, and various bookkeeping fields. Arrows point from child to parent.

Finite set of states but sometimes infinite nodes in a search tree

## Tree/Graph Search Algorithm

**function** TREE-SEARCH(*problem*) **returns** a solution, or failure  
 initialize the frontier using the initial state of *problem*  
**loop do**  
   if the frontier is empty **then return** failure  
   choose a leaf node and remove it from the frontier  
   if the node contains a goal state **then return** the corresponding solution  
   expand the chosen node, adding the resulting nodes to the frontier

**function** GRAPH-SEARCH(*problem*) **returns** a solution, or failure  
 initialize the frontier using the initial state of *problem*  
**initialize the explored set to be empty**  
**loop do**  
   if the frontier is empty **then return** failure  
   choose a leaf node and remove it from the frontier  
   if the node contains a goal state **then return** the corresponding solution  
   **add the node to the explored set**  
   expand the chosen node, adding the resulting nodes to the frontier  
   **only if not in the frontier or explored set**

Avoids redundant paths and loops

Figure 3.7 An informal description of the general tree-search and graph-search algorithms. The parts of GRAPH-SEARCH marked in bold italic are the additions needed to handle repeated states.

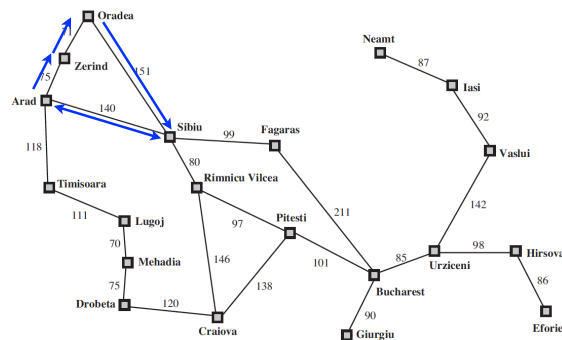
## Romanian Roadmap

Arad-Sibiu-Arad

*Loopy Path*- makes the complete search space infinite even though there are only 20 states

Arad-Sibiu  
Arad- Zerind-Oradea-Sibiu

*Redundant Path*- more than one way to get from one state to another



## Search Strategies

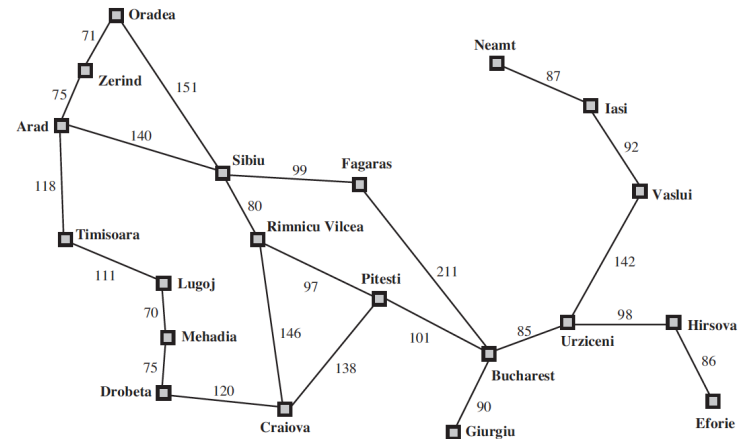
- A **Strategy** is defined by picking the *order of node expansion*
- Strategies are evaluated along the following dimensions:
  - Completeness** – does it always find a solution if one exists?
  - Time Complexity** – number of nodes generated/expanded
  - Space Complexity** – maximum number of nodes in memory
  - Optimality** – does it always find a least cost solution
- Time & space complexity are measured in terms of
  - $b$  – maximum branching factor of the search tree
  - $d$  – depth of the least cost solution
  - $m$  – maximum length of any path in the state space (possibly infinite)

## Some Search Classes

- Uninformed Search (Blind Search)
  - No additional information about states besides that in the problem definition.
  - Can only generate successors and compare against goal state.
  - Some examples
    - Breadth first search, Depth first search, iterative deepening DFS
- Informed Search (Heuristic Search)
  - Strategies have additional information whether non-goal states are more promising than others.
  - Some examples
    - Greedy Best-First search, A\* search,



## Romanian Roadmap



## Breadth-First Graph Search

```

function BREADTH-FIRST-SEARCH(problem) returns a solution, or failure
    node ← a node with STATE = problem.INITIAL-STATE, PATH-COST = 0
    if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
    frontier ← a FIFO queue with node as the only element
    explored ← an empty set
    loop do
        if EMPTY?(frontier) then return failure
        node ← POP(frontier) /* chooses the shallowest node in frontier */
        add node.STATE to explored
        for each action in problem.ACTIONS(node.STATE) do
            child ← CHILD-NODE(problem, node, action)
            if child.STATE is not in explored or frontier then
                if problem.GOAL-TEST(child.STATE) then return SOLUTION(child)
                frontier ← INSERT(child, frontier)
    
```



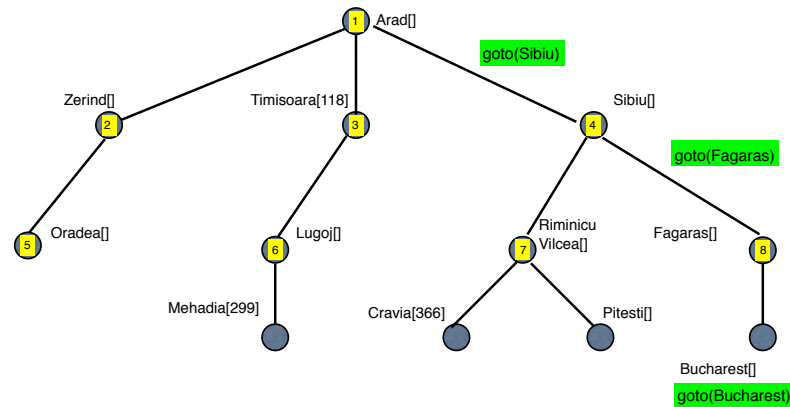
## Breadth-First Search: Romania

	Frontier (FIFO queue)	Explored
INIT	['arad']	
POP	arad	['arad']
Add Children	['zerind', 'timisoara', 'sibiu']	
POP	zerind	['arad', 'zerind']
Add Children	['timisoara', 'sibiu', 'oradea']	
POP	timisoara	['arad', 'zerind', 'timisoara']
Add Children	['sibiu', 'oradea', 'lugoj']	
POP	sibiu	['arad', 'zerind', 'timisoara', 'sibiu']
Add Children	['oradea', 'lugoj', 'rimnicu vilcea', 'fagaras']	
POP	oradea	['arad', 'zerind', 'timisoara', 'sibiu', 'oradea']
Add Children	['lugoj', 'rimnicu vilcea', 'fagaras']	
POP	lugoj	['arad', 'zerind', 'timisoara', 'sibiu', 'oradea', 'lugoj']
Add Children	['rimnicu vilcea', 'fagaras', 'mehadia']	
POP	rimnicu vilcea	['arad', 'zerind', 'timisoara', 'sibiu', 'oradea', 'lugoj', 'r_v']
Add Children	['fagaras', 'mehadia', 'craiva', 'pitesti']	
POP	fagaras	['arad', 'zerind', 'timisoara', 'sibiu', 'oradea', 'lugoj', 'r_v', 'fagaras']
Add Children	['bucharest', 'mehadia', 'craiva', 'pitesti']	
Goal Node	bucharest	

Solution:: ['goto(sibiu)', 'goto(fagaras)', 'goto(bucharest)']



## Breadth-first Search Romania



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## Computational Complexity Theory

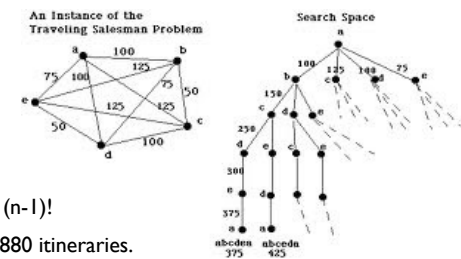


## Traveling Salesman Problem



- The Traveling Salesman Problem is one of the most intensively studied problems in computational mathematics.
- A traveling salesman has  $n$  number of cities to visit. He wants to know the shortest route which will allow him to visit all cities one time and return to his starting point.
- Solving this problem becomes MUCH harder as the number of cities increases; the figure in the middle shows the solution for the 13,509 cities and towns in the US that have more than 500 residents.

## Traveling Salesman Problem



- Suppose there are  $n$  cities to visit.
- The number of possible itineraries is  $(n-1)!$ 
  - For  $n=10$  cities, there are  $9!=362,880$  itineraries.
- What if  $n=40$ ?
  - There are now  $39!$  itineraries to check which is greater than  $10^{45}$
  - Examining  $10^{15}$  tours per second, the required time would be several billion lifetimes of the universe
  - In fact, no supercomputer, existing or projected can run this fast.
- $(n-1)!$  grows faster than  $2^n$ . So the time it takes to solve the problem grows **exponentially** with the size of the input.



# Sequential Search: Telephone Book



- Suppose a telephone book has  $N=1000000$  entries.
- Given the name  $Y$ , search the telephone book sequentially for  $Y$ 's telephone number
  - Entries  $\langle X_1, T_1 \rangle, \langle X_2, T_2 \rangle, \dots, \langle X_{1000000}, T_{1000000} \rangle$
  - At each iteration  $Y$  is compared with  $X_i$
  - Assume time increases relative to the number of comparisons, so we are counting comparison instructions. (there may be other instructions...)
- In the worst case, 1000000 comparisons may have to be made.
- Call the algorithm  $A$ . We say it has a worst case running time which is **on the order of  $N$** .
- $A$  runs in time  $O(N)$  in the worst case, where  $N$  is the number of entries in the telephone book.
  - In other words, the time complexity of  $A$  is dependent on the size of the input.
  - $A$  has worst case behavior which is linear in the size of the input to  $A$ .

# Big-O Notation



- We do not care whether the algorithm takes time  $N, 3N, 100N$ , or even a fraction of  $N$ :  $N/6$ 
  - The only thing that matters is that the running time of the algorithm grows **linearly** with  $N$ .
  - In other words, there is some constant  $k$  such that the algorithm runs in time that is no more than  $k \times N$  in the worst case
- Let  $T(n)$  be a function on  $n$  (the size of the input to an algorithm) then  $T(n)$  is **on the order of  $f(n)$**  if:

$T(n)$  characterizes the running time of the algorithm, i.e., lines of code, # of additions, etc. as a function of input  $n$ .

$T(n)$  usually characterizes worst case running time.

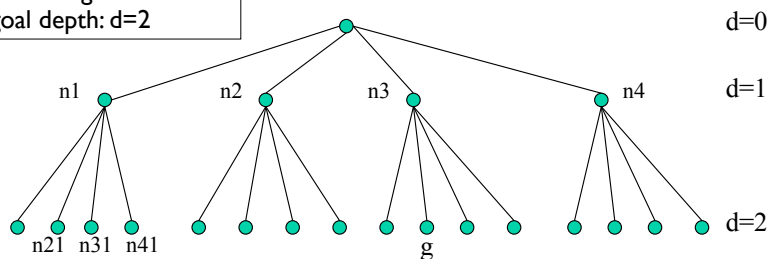
*Asymptotic Analysis*

**$T(n)$  is  $O(f(n))$  if  $T(n) < k \times f(n)$  for some  $k$ , for all  $n > n_0$**

# Analyzing Breadth-First Search



Branching Factor:  $b=4$   
goal depth:  $d=2$



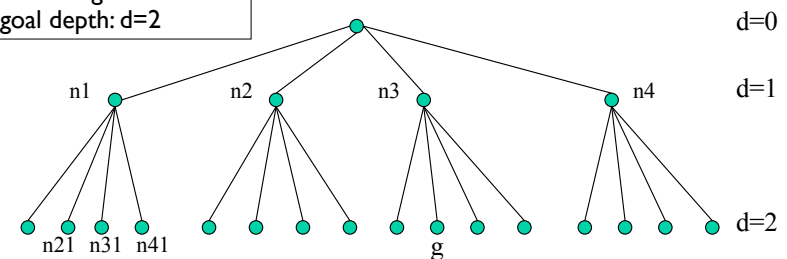
Time Complexity:  $O(b^d)$

- When checking for a goal node at level  $d$ , at least  $1 + b + b^2 + \dots + b^{d-1}$  nodes must be generated.
- Total nodes generated and checked may be as much as  $1 + b + b^2 + \dots + b^{d-1} + b^d$

# Analyzing Breadth-First Search



Branching Factor:  $b=4$   
goal depth:  $d=2$



Space Complexity:  $O(b^d)$

- For any graph search, every expanded node is stored in the explored set.
- There will be  $O(b^{d-1})$  nodes in the explored set and  $O(b^d)$  nodes in the frontier set.
- The space complexity is dominated by the nodes in the frontier.

## Analyzing Breadth-First Search



### Is it complete?

If the shallowest goal node is at some finite depth  $d$ , BFS will eventually find it after searching all shallower nodes  
(Provided the branching factor is finite)

### Is it optimal?

The shallowest goal node is not necessarily optimal, but it is optimal if the path cost is a non-decreasing function of the depth of the node. Example: each action has the same cost.



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## Exponential Complexity Bounds are Highly Problematic



Time/memory requirements for breadth-first search with branching factor  $b=10$   
1 million nodes/second; 1000bytes a node

Depth	Nodes	Time	Memory
2	110	.11 ms	107 kilobytes
4	11,110	11 ms	10.6 megabytes
6	$10^6$	1.1 s	1 gigabyte
8	$10^8$	2 min	103 gigabytes
10	$10^{10}$	3 hours	10 terabytes ( $10^{12}$ )
12	$10^{12}$	13 days	1 petabyte
14	$10^{14}$	3.5 years	99 petabytes
16	$10^{16}$	350 years	10 exabytes

$1000^4$



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## Uniform-Cost Search



We know that breadth-first search is optimal when all step-costs are equal.

This can be generalized to any step-cost function

Instead of expanding the shallowest node (FIFO queue), uniform-cost search expands the node  $n$  with the lowest path cost  $g(n)$  from the root. A priority queue on path costs of nodes is used instead of a FIFO queue.



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## Uniform-Cost Search



**function** UNIFORM-COST-SEARCH(*problem*) **returns** a solution, or failure

*node*  $\leftarrow$  a node with STATE = *problem*.INITIAL-STATE, PATH-COST = 0

*frontier*  $\leftarrow$  a priority queue ordered by PATH-COST, with *node* as the only element

*explored*  $\leftarrow$  an empty set

**loop do**

**if** EMPTY?(*frontier*) **then return** failure

*node*  $\leftarrow$  POP(*frontier*) /\* chooses the lowest-cost node in *frontier* \*/

**if** *problem*.GOAL-TEST(*node*.STATE) **then return** SOLUTION(*node*)

add *node*.STATE to *explored*

**for each** *action* in *problem*.ACTIONS(*node*.STATE) **do**

*child*  $\leftarrow$  CHILD-NODE(*problem*, *node*, *action*)

**if** *child*.STATE is not in *explored* or *frontier* **then**

*frontier*  $\leftarrow$  INSERT(*child*, *frontier*)

**else if** *child*.STATE is in *frontier* with higher PATH-COST **then**

replace that *frontier* node with *child*

1st goal node generated may be on a sub-optimal path

goal test during selection for expansion rather than generation as in BFS

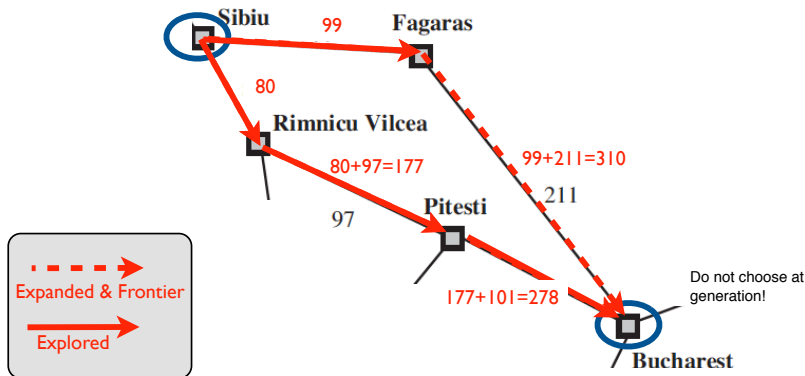
Replace, if better path to a node on the frontier is found

## Generic Graph Search with modifications

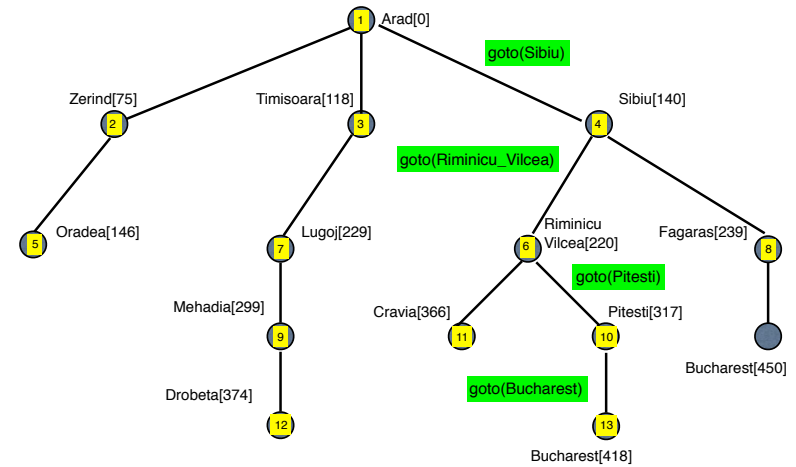


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## Uniform-Cost Search



## Uniform-Search Romania



## Depth-First Graph Search



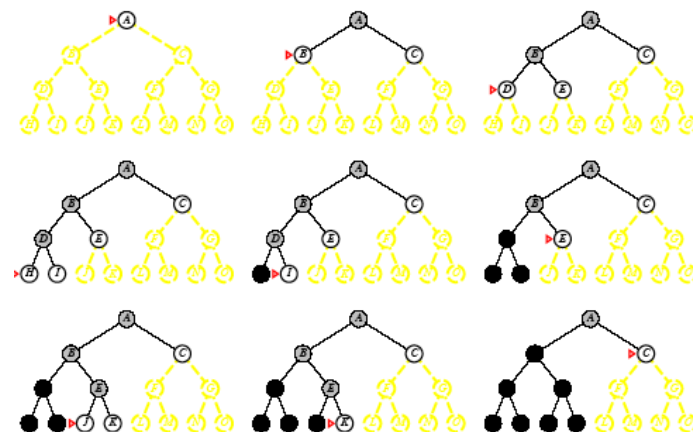
```

function Depth-FIRST-SEARCH(problem) returns a solution, or failure
  node ← a node with STATE = problem.INITIAL-STATE, PATH-COST = 0
  if problem.GOAL-TEST(node.STATE) then return SOLUTION(node)
  frontier ← a LIFO queue with node as the only element
  explored ← an empty set
  loop do
    if EMPTY?(frontier) then return failure
    node ← POP(frontier) /* chooses the shallowest node in frontier */
    add node.STATE to explored
    for each action in problem.ACTIONS(node.STATE) do
      child ← CHILD-NODE(problem, node, action)
      if child.STATE is not in explored or frontier then
        if problem.GOAL-TEST(child.STATE) then return SOLUTION(child)
        frontier ← INSERT(child, frontier)
    
```

Place new nodes on front of queue



## Depth-First Search on a Binary Tree



## Depth-First Search: Romania



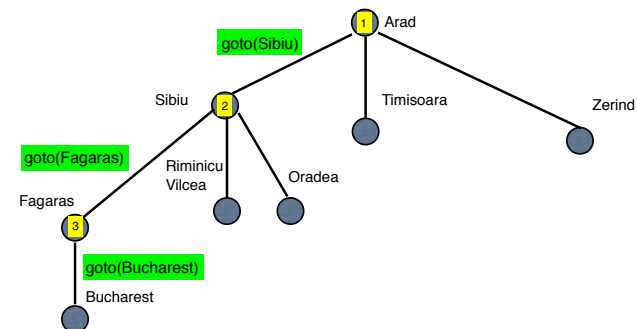
	Frontier (FIFO queue)	Explored
INIT	['arad']	
POP	arad	['arad']
Add Children	[sibiu,timisoara,'zerind']	
POP	sibiu	['arad','sibiu']
Add Children	['fagaras','r_v','oradea','timisoara','zerind']	
POP	fagaras'	['arad','sibiu','fagaras']
Add Children	['bucherast','r_v','oradea','timisoara','zerind']	
Terminal	Bucharest	['arad','sibiu','fagaras']

Solution:: ['goto(sibiu)', 'goto(fagaras)', 'goto(bucharest)']



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## Depth-First Search Romania



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## Analyzing Depth-First Search



### Time Complexity

Depth-First Graph search is bounded by the size of the state-space (which may be infinite).

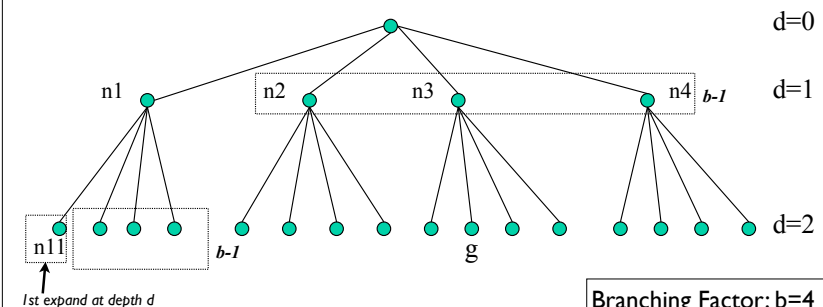
Depth-First Tree search may generate all of the  $O(b^m)$  nodes in the search tree where  $m$  is the maximum length of any path in the state space.

$m$  can be much greater than the size of the state space and can be much larger than  $d$ , the depth of the shallowest goal node, and is infinite if the tree is unbounded.



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## Analyzing Depth-First Tree Search



Space Complexity:  $O(d(b-1))$

Branching Factor:  $b=4$   
Goal Depth:  $d=2$

•For any tree search, when checking for a goal node at level  $d$ , at most  $d(b-1)$  nodes must be stored in the frontier.



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# Analyzing Depth-First Search



## Is it complete?

Yes, for the Graph Search version in finite state spaces. It avoids repeated states and redundant paths and will eventually expand every node.

No, for the Tree Search version. It may loop infinitely on one branch.

## Is it optimal?

Both versions are non-optimal



# Recursive Implementation of Depth-Limited Search



- Deals with failure of depth-first search in infinite state spaces
- Introduce a pre-determined cut-off depth limit  $l$

**function** DEPTH-LIMITED-SEARCH(*problem*, *limit*) **returns** a solution, or failure/cutoff  
**return** RECURSIVE-DLS(MAKE-NODE(*problem*.INITIAL-STATE), *problem*, *limit*)

**function** RECURSIVE-DLS(*node*, *problem*, *limit*) **returns** a solution, or failure/cutoff  
**if** *problem*.GOAL-TEST(*node*.STATE) **then** **return** SOLUTION(*node*)  
**else if** *limit* = 0 **then** **return** cutoff

**else**  
    *cutoff\_occurred?* ← false  
    **for each** *action* **in** *problem*.ACTIONS(*node*.STATE) **do**  
        *child* ← CHILD-NODE(*problem*, *node*, *action*)  
        *result* ← RECURSIVE-DLS(*child*, *problem*, *limit* - 1)  
        **if** *result* = cutoff **then** *cutoff\_occurred?* ← true  
        **else if** *result* ≠ failure **then** **return** *result*  
    **if** *cutoff\_occurred?* **then** **return** cutoff **else** **return** failure

If  $l < d$  then we may not find the goal and DLS is incomplete

If  $l > d$  then DLS is not optimal

DLS with  $l = \text{infinity}$  is in fact depth-first search

Time Complexity:  $O(b^l)$   
Space Complexity:  $O(bl)$



# Iterative-Deepening Depth-First Search



**function** ITERATIVE-DEEPENING-SEARCH(*problem*) **returns** a solution, or failure  
**for** *depth* = 0 **to**  $\infty$  **do**  
    *result* ← DEPTH-LIMITED-SEARCH(*problem*, *depth*)  
    **if** *result* ≠ cutoff **then** **return** *result*

- Combines the best of depth-first search and breadth-first search

Gradually increases the depth-limit of depth-first search by increments (0, 1, 2...).

Each increment basically does a breadth-first search to that limit

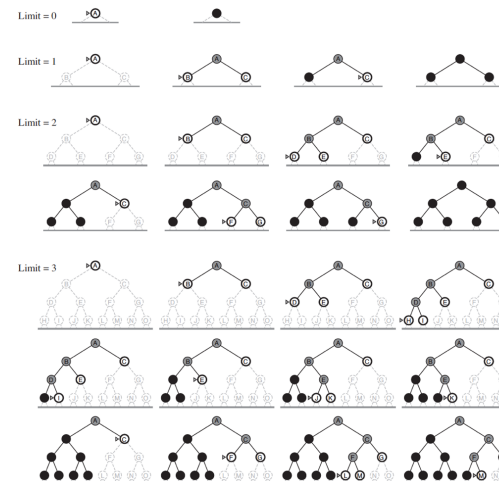
Complete when  
the branching  
factor is finite

Optimal when the path  
cost is a non-decreasing  
function of the depth of  
the node

Space Complexity:  $O(bd)$   
Time Complexity:  $O(b^d)$



# Iterative-Deepening (4 iterations)



# Summary of Analyses



## For Tree-Search Versions

Criterion	Breadth-First	Depth-First	Depth-Limited	Iterative-Deepening
Complete?	Yes <sup>a</sup>	No	No	Yes <sup>a</sup>
Time	$O(b^d)$	$O(b^m)$	$O(b^l)$	$O(b^d)$
Space	$O(b^d)$	$O(bm)$	$O(b)$	$O(bd)$
Optimal	Yes <sup>c</sup>	No	No	Yes <sup>c</sup>

a - complete if b is finite

c - optimal if step costs are all identical

Graph-Search Versions:  
 • DFS Complete for finite spaces  
 • Time/space complexities bounded by size of the state space

