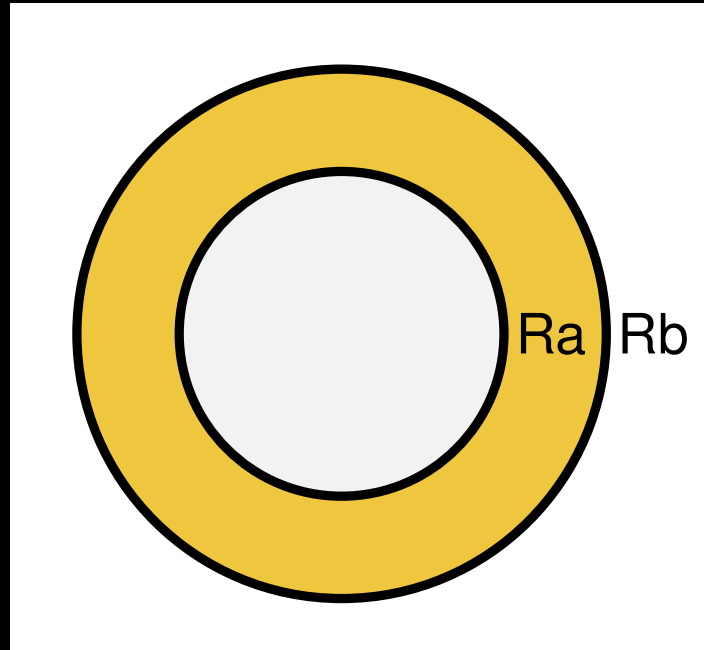


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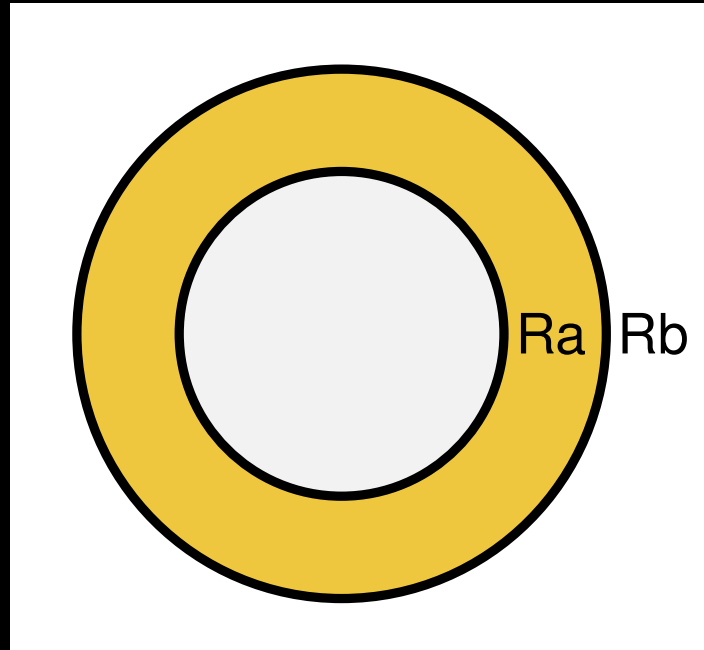
Sphère métallique de rayon  $R_a$ , charge totale  $Q_0$ ,  
couche diélectrique ( $\epsilon$ ,  $\epsilon_0$ ) d'épaisseur  $R_b - R_a$



Quelle densité de charges pour ce problème ?

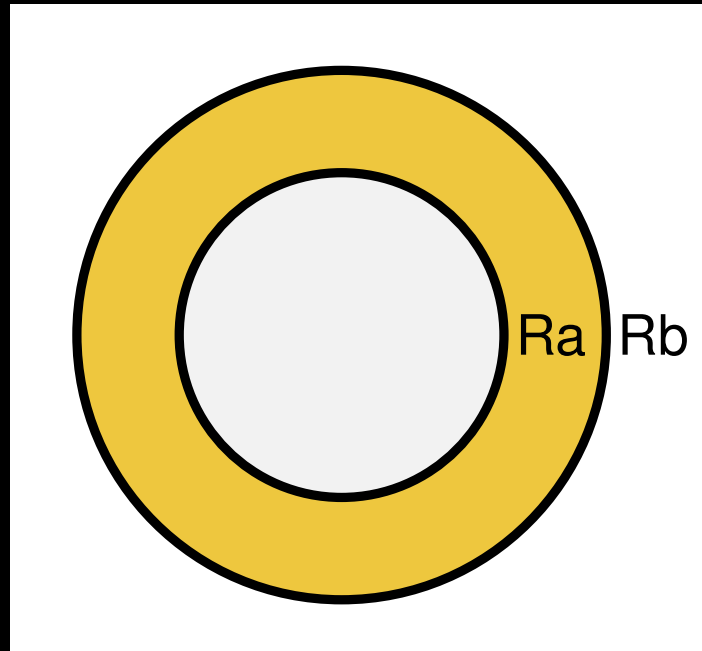
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Sphère métallique de rayon  $R_a$ , charge totale  $Q_0$ ,  
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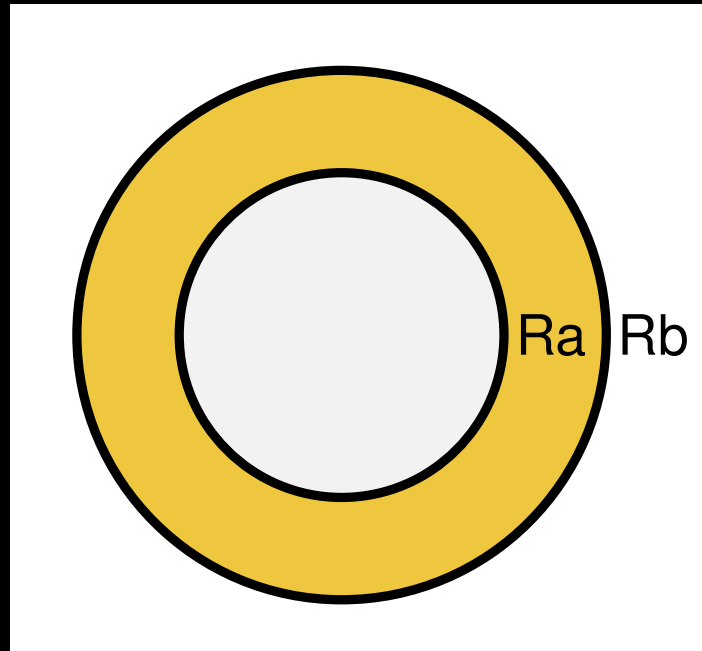


Quelle densité de charges pour ce problème ?

- A.  $\rho_s = Q_0 / (4\pi R_a^2)$
- B.  $\rho = Q_0 / (\frac{4}{3}\pi R_a^3)$
- C.  $\rho_s = Q_0 / (4\pi R_b^2)$
- D.  $\rho = Q_0 / (\frac{4}{3}\pi R_b^3)$
- E. Aucune bonne réponse.

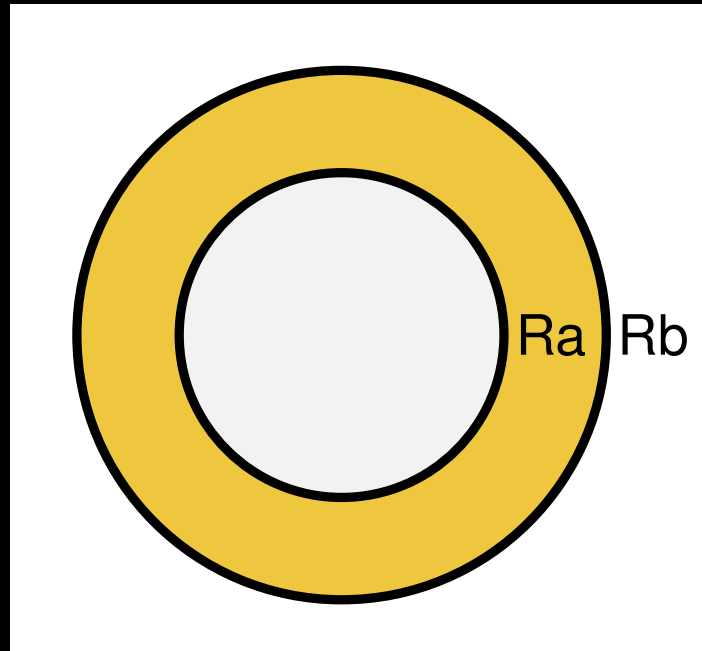


Comment démarrer pour arriver au champ  $\vec{E}$  ?

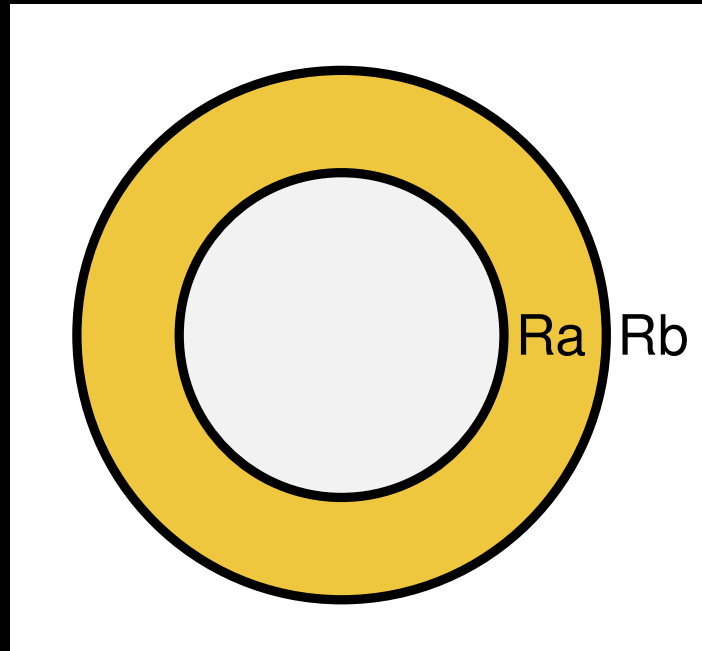


Comment démarrer pour arriver au champ  $\vec{E}$  ?

- A. Loi de Gauss intégrale sur  $\vec{E}$ .
- B. Loi de Gauss intégrale sur  $\vec{D}$ .
- C. Loi de Gauss locale sur  $\vec{E}$ .
- D. Loi de Gauss locale sur  $\vec{D}$ .
- E. Trouver les charges de polarisation à partir de  $\vec{P}$ .

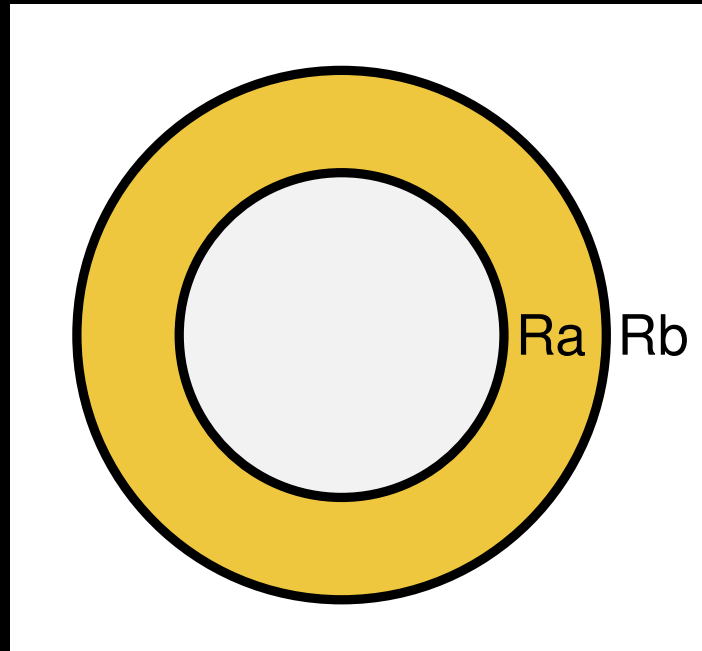


Que déduire des symmétries du problème ?

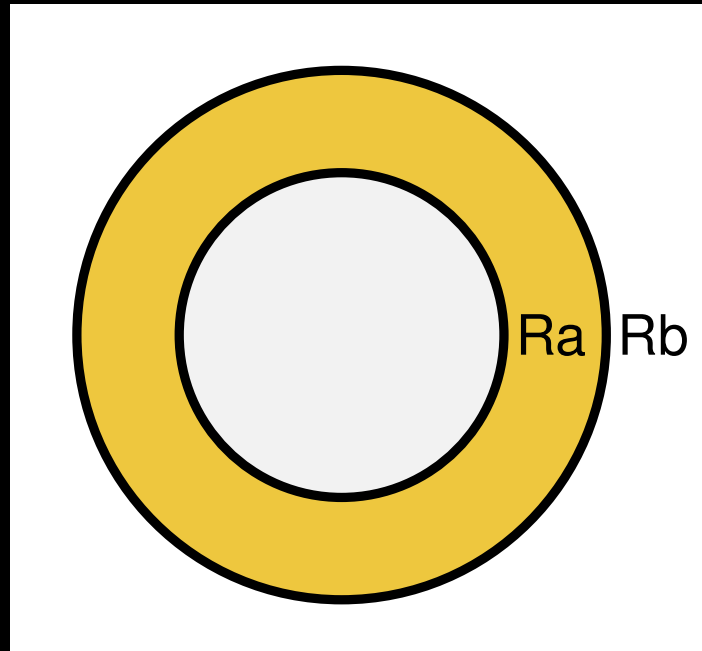


Que déduire des symmétries du problème ?

- A.  $\vec{D}(\vec{r}) = \vec{D}(r)\hat{e}_r$
- B.  $\vec{D}(\vec{r}) = D(\vec{r})\hat{e}_r$
- C.  $\vec{D}(\vec{r}) = D(\hat{r})\hat{e}_r$
- D.  $\vec{D}(\vec{r}) = D(r)\hat{e}_r$



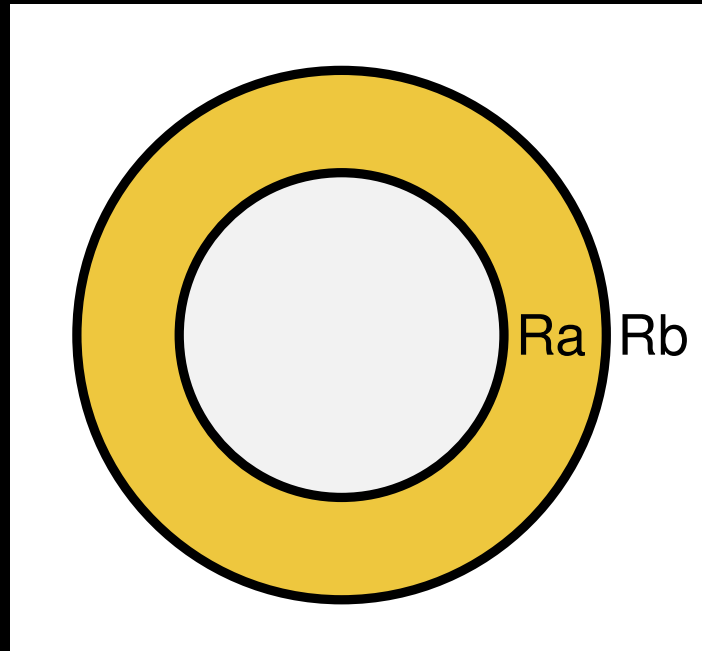
Quelle surface fictive  $S$  pour appliquer la loi de Gauss intégrale ?



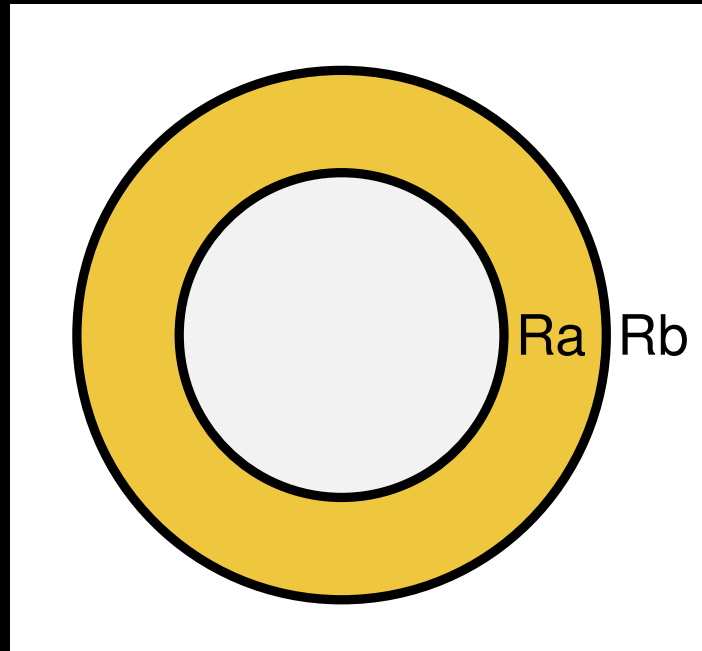
Quelle surface fictive  $S$  pour appliquer la loi de Gauss intégrale ?

- A. Un cube.
- B. Un cylindre.
- C. Une sphère.
- D. Peu importe, à condition d'avoir une surface fermée.



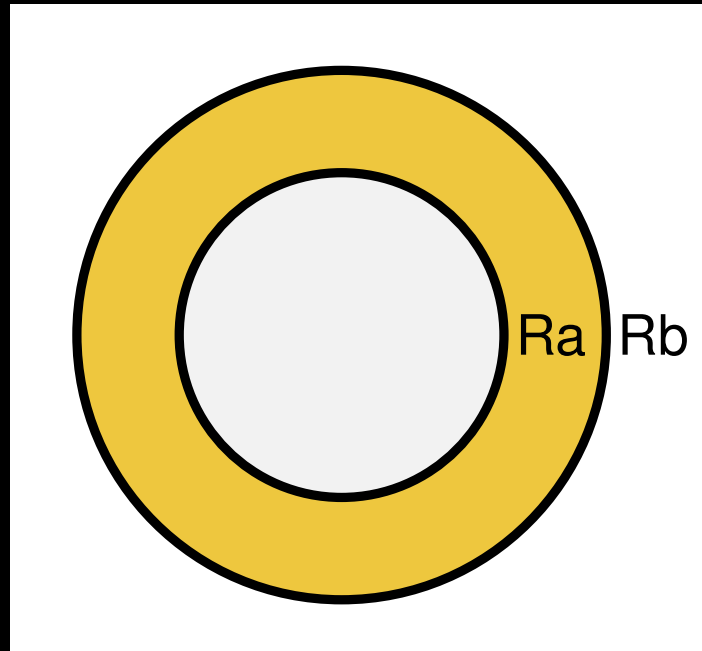


Quel rayon pour la sphère fictive  $S$  ?

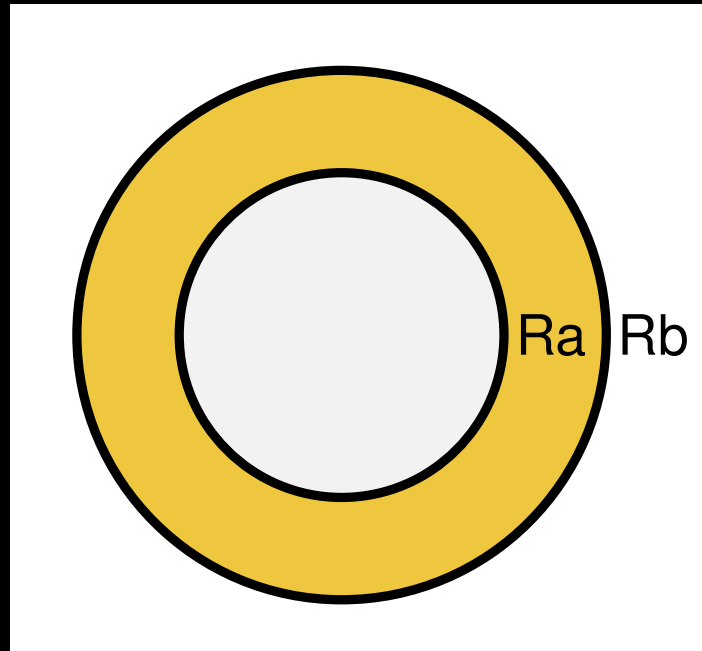


Quel rayon pour la sphère fictive  $S$  ?

- A.  $R_a$
- B.  $R_b$
- C.  $R_g$
- D.  $\rho$
- E.  $r$

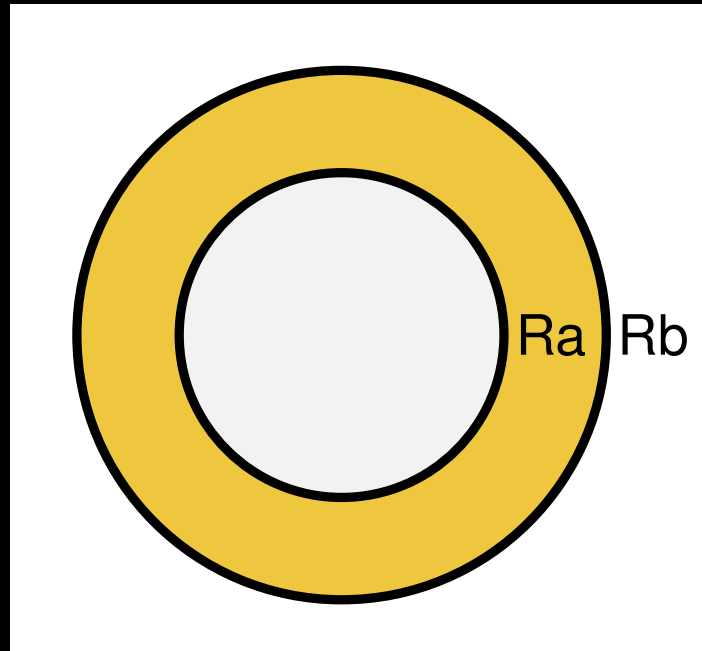


Quel est le flux de  $\vec{D}$  à travers  $S$  ?



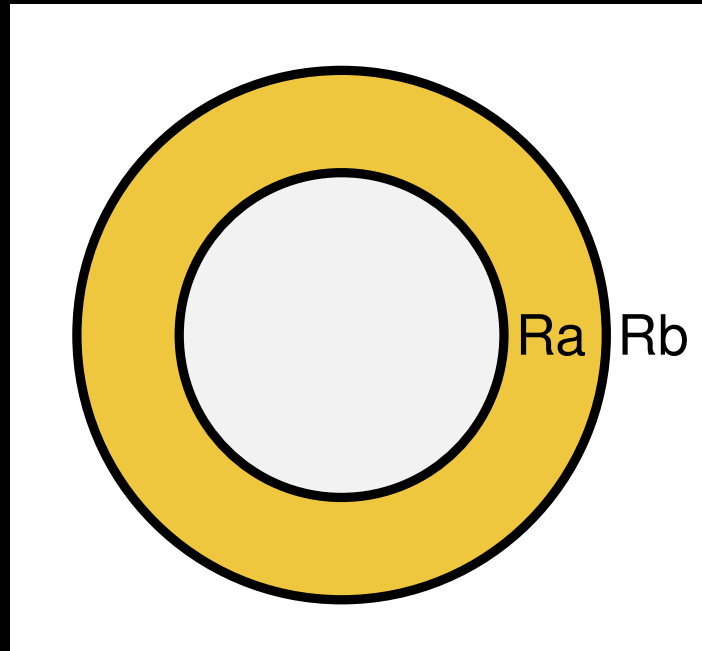
Quel est le flux de  $\vec{D}$  à travers  $S$  ?

$$\oint_S \vec{D}(\vec{r}) \cdot \hat{n} \, dS =$$



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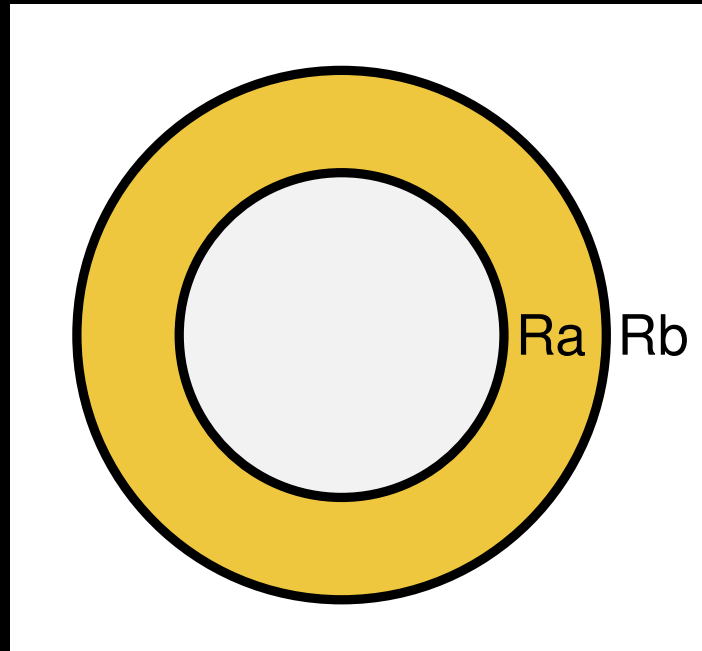
$$\oint_S \vec{D}(\vec{r}) \cdot \hat{n} \, dS = \oint_S D(r) \hat{e}_r \cdot \hat{e}_r \, dS =$$



Quel est le flux de  $\vec{D}$  à travers  $S$  ?

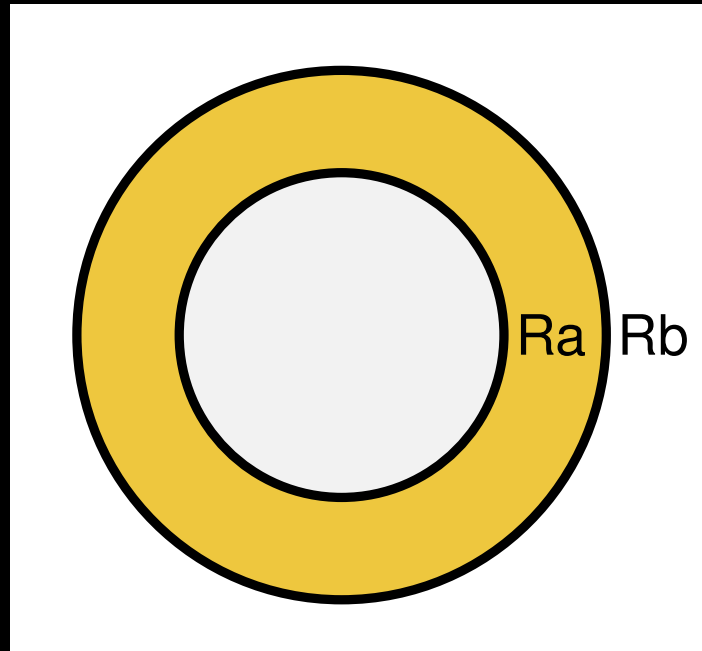
$$\oint_S \vec{D}(\vec{r}) \cdot \hat{n} \, dS = \oint_S D(r) \hat{e}_r \cdot \hat{e}_r \, dS =$$

- A.  $D(r) \oint_S dS = D(r) 4\pi r^2$
- B.  $D(r) \oint_S dS = D(r) 4\pi R_g^2$
- C.  $D(R_g) \oint_S dS = D(R_g) 4\pi R_g^2$
- D.  $D(R_g) \oint_S dS = D(R_g) \frac{4}{3}\pi R_g^3$
- E.  $D(R_g) \oint_S dS = D(R_g) 2\pi R_g$



Quelle charge  $Q_{\text{int}}^{\text{libres}}$  dans les trois cas

i.  $R_g < R_a$ , ii.  $R_a < R_g < R_b$  iii.  $R_b < R_g$  ?



Quelle charge  $Q_{\text{int}}$  libres dans les trois cas

i.  $R_g < R_a$ , ii.  $R_a < R_g < R_b$  iii.  $R_b < R_g$  ?

A. 0, 0, 0

B. 0, 0,  $Q_0$

C. 0,  $Q_0$ , 0

D.  $Q_0$ , 0, 0

E. 0,  $Q_0$ ,  $Q_0$

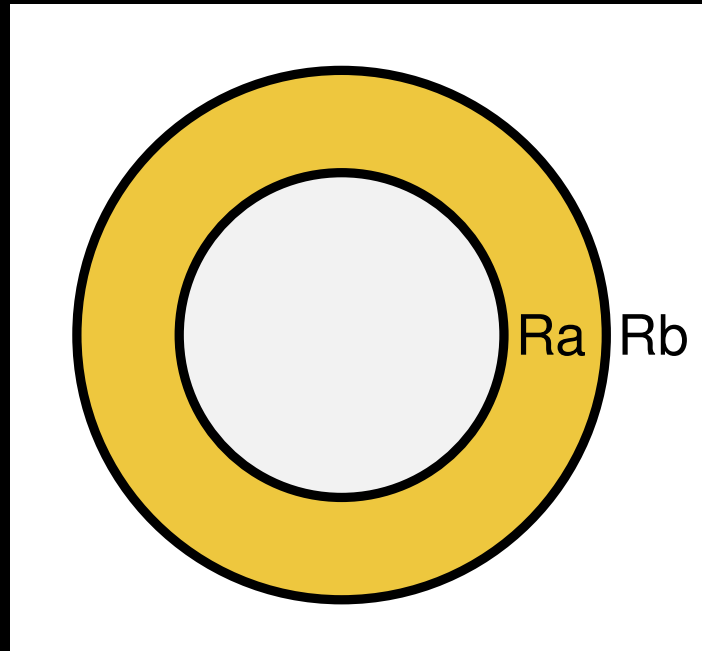
F.  $Q_0$ , 0,  $Q_0$

G.  $Q_0$ ,  $Q_0$ , 0

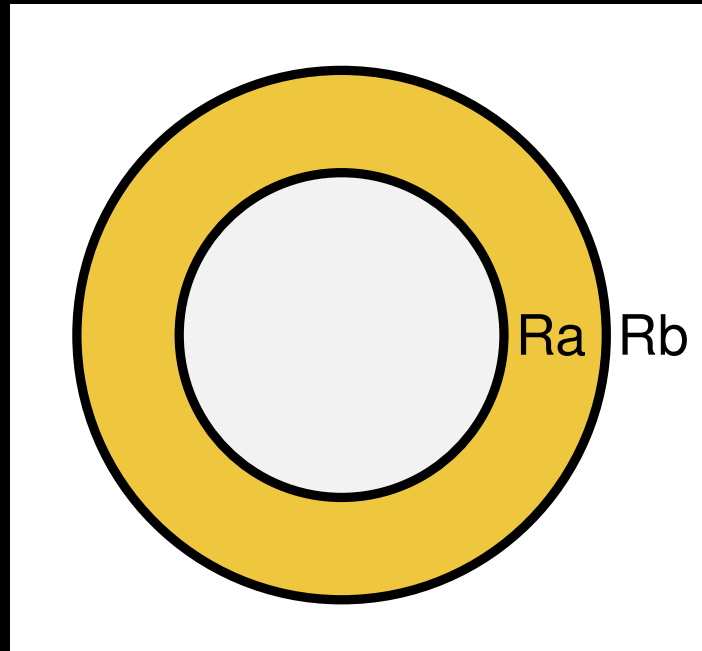
H.  $Q_0$ ,  $Q_0$ ,  $Q_0$

I. Aucune bonne réponse.



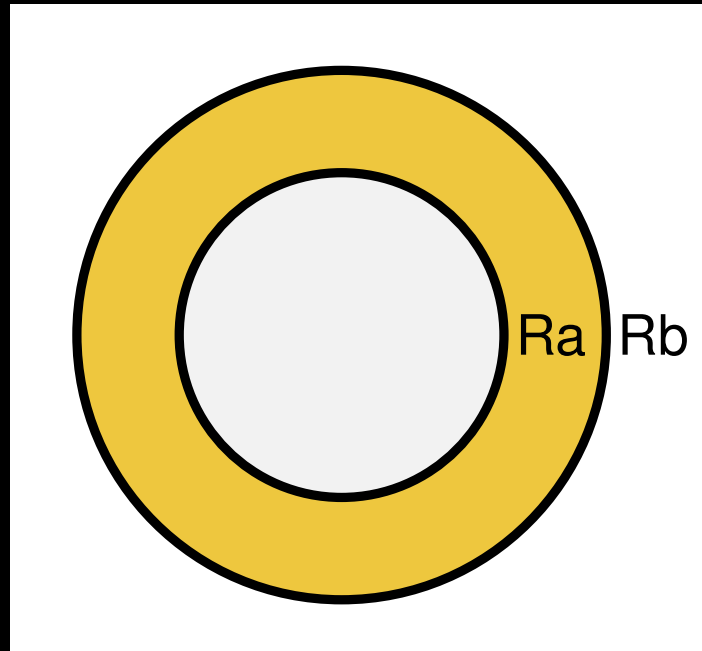


$$\vec{D} = \epsilon \vec{E} = \epsilon_0 \epsilon_r \vec{E}$$



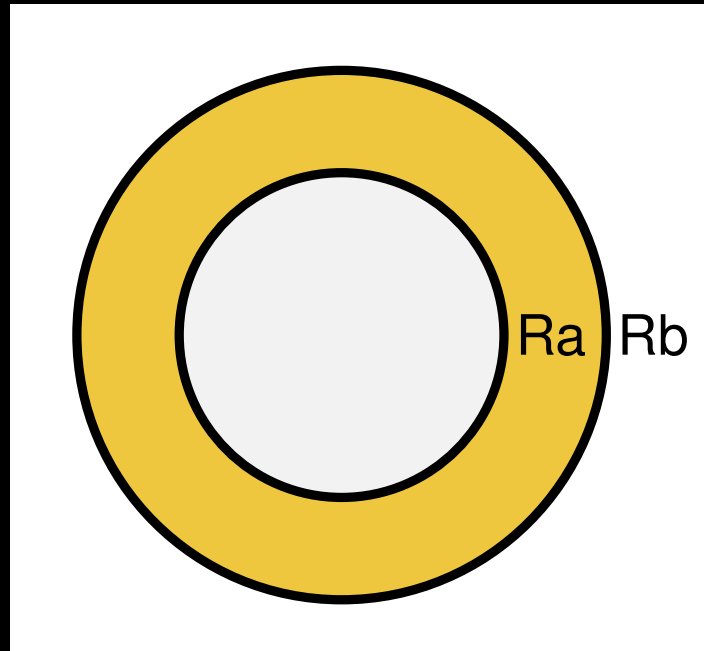
$$\vec{D} = \epsilon \vec{E} = \epsilon_0 \epsilon_r \vec{E}$$

$$\vec{D}(\vec{r}) = \begin{cases} \vec{0} & r < R_a \\ \frac{Q_0}{4\pi r^2} \hat{e}_r & R_a < r < R_b \\ \frac{Q_0}{4\pi r^2} \hat{e}_r & R_b < r \end{cases}$$

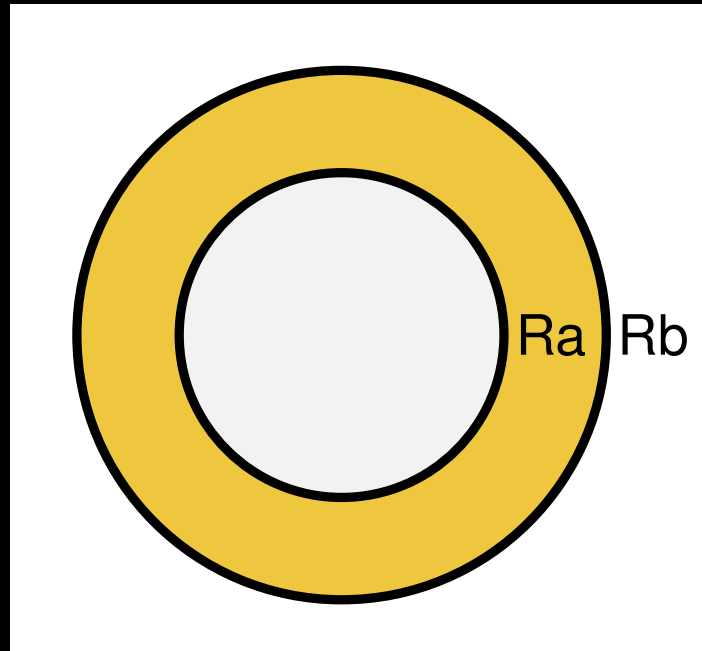


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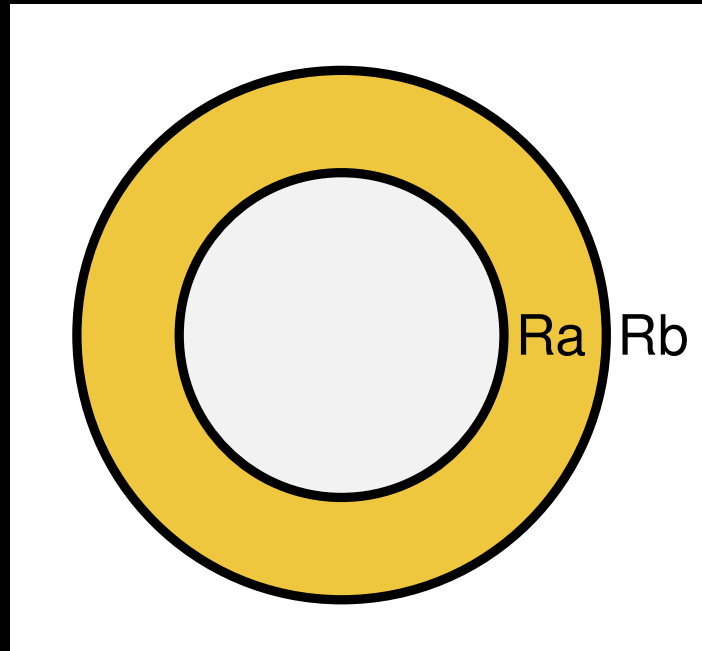


$$\vec{P} = \epsilon_0 \chi_e \vec{E}$$



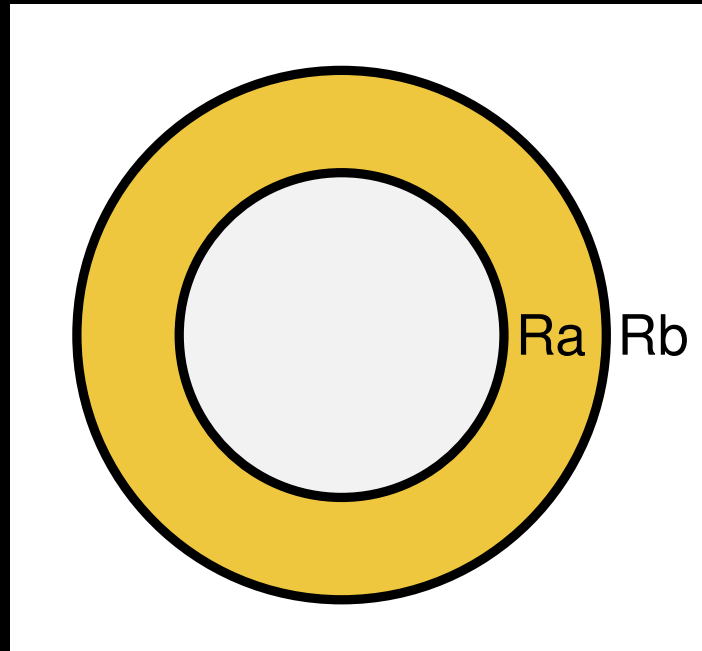
$$\vec{P} = \epsilon_0 \chi_e \vec{E}$$

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$$\vec{P} = \epsilon_0 \chi_e \vec{E}$$

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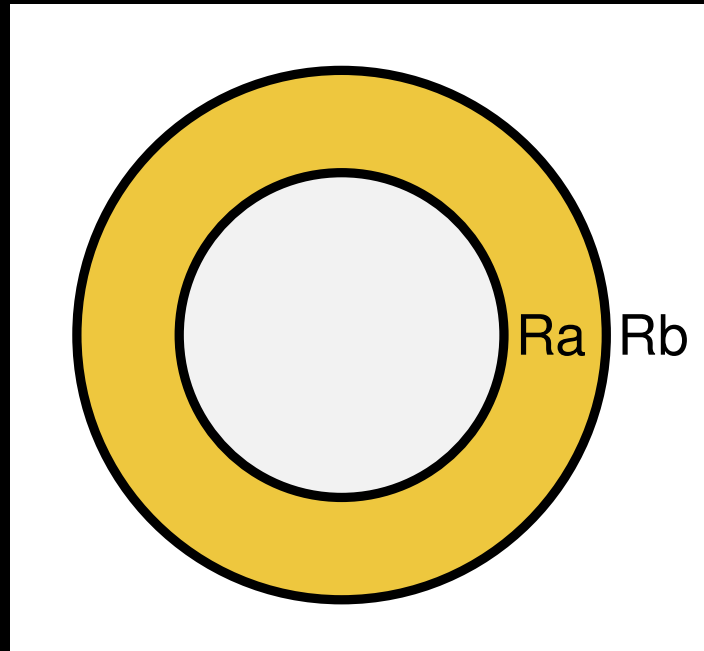
$$\vec{P}(\vec{r}) = \begin{cases} \vec{0} & r < R_a \\ \frac{\epsilon_0 \chi_e Q_0}{4\pi\epsilon_0\epsilon_r r^2} \hat{e}_r & R_a < r < R_b \\ ??? & R_b < r \end{cases}$$

A.  $\frac{\epsilon_0 \chi_e Q_0}{4\pi\epsilon_0 r^2} \hat{e}_r$

B.  $\frac{\epsilon_r \chi_e Q_0}{4\pi\epsilon_0 r^2} \hat{e}_r$

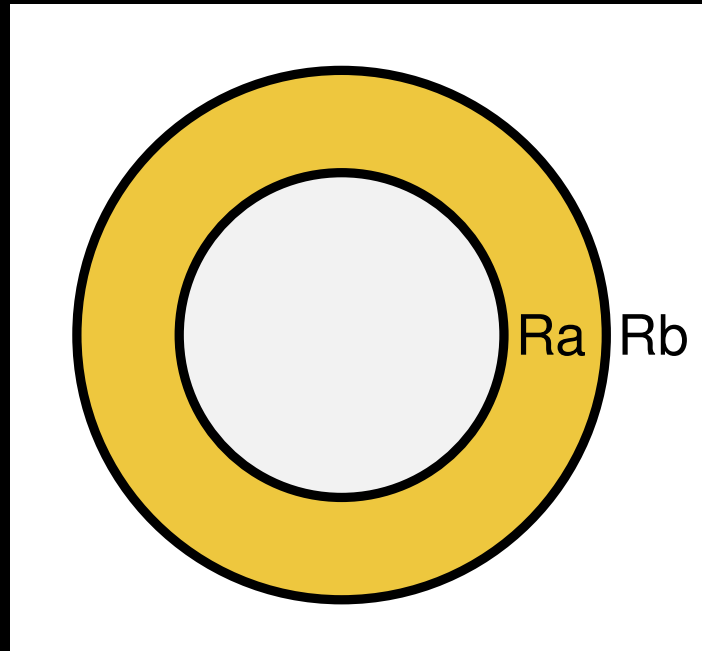
C.  $\vec{0}$

D. Aucune bonne réponse.

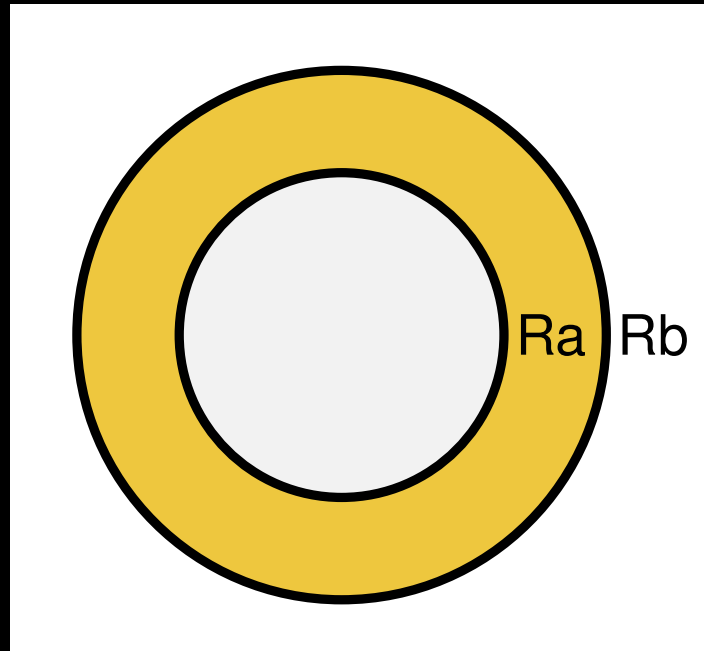


$$\vec{P}(\vec{r}) = \frac{\epsilon_0 \chi_e Q_0}{4\pi \epsilon_0 \epsilon_r r^2} \hat{e}_r$$

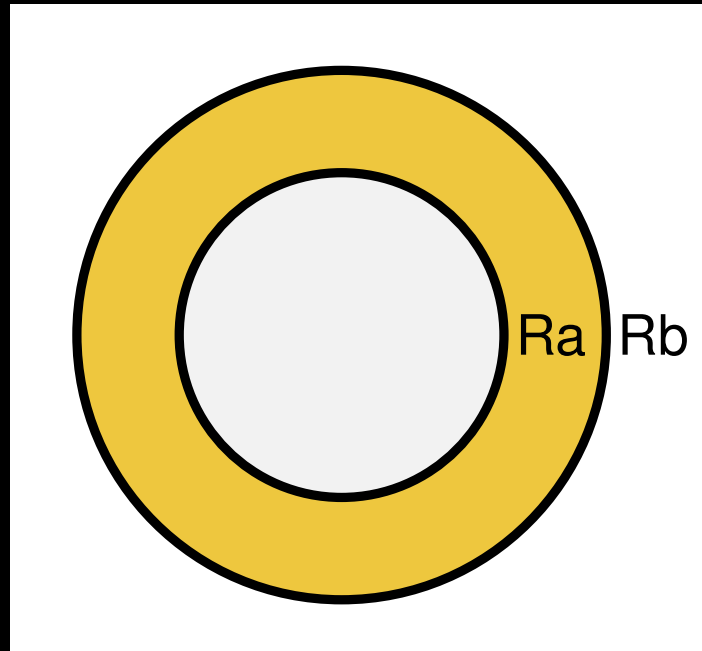




$$\vec{P}(\vec{r}) = \frac{\epsilon_0 \chi_e Q_0}{4\pi \epsilon_0 \epsilon_r r^2} \hat{e}_r = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r$$

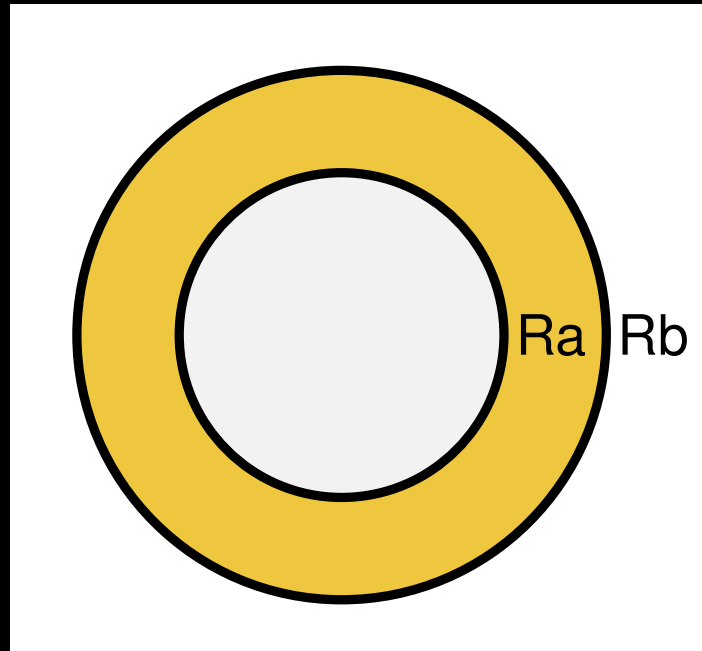


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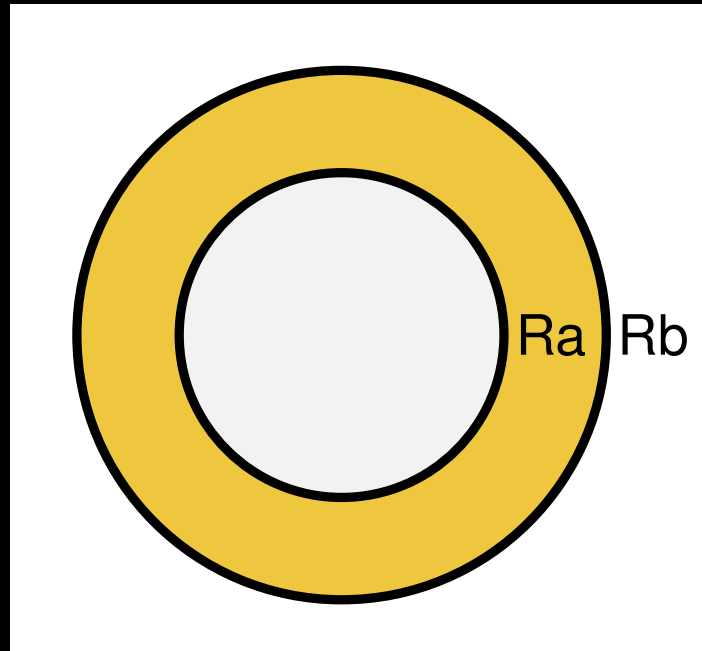
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$$\rho_{\text{pol}} =$$



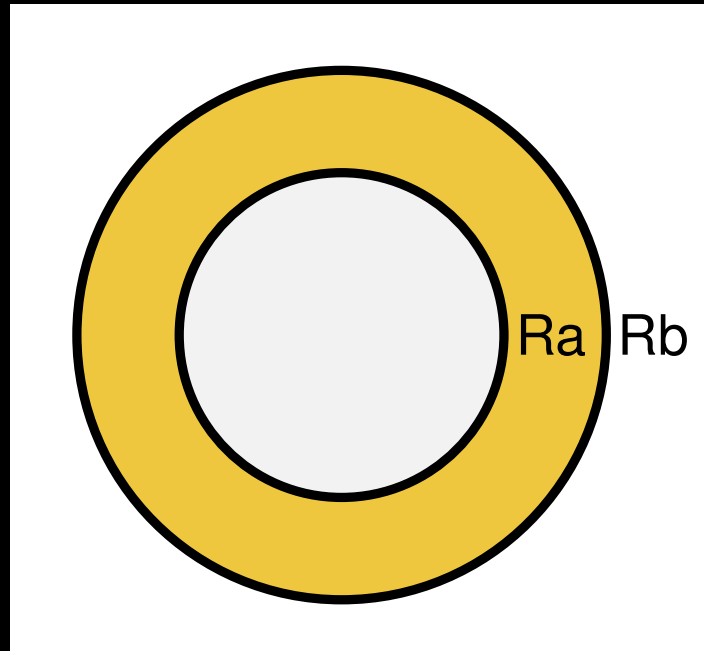
$$\vec{P}(\vec{r}) = \frac{\epsilon_0 \chi_e Q_0}{4\pi \epsilon_0 \epsilon_r r^2} \hat{e}_r = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$

$$\rho_{\text{pol}} = -\text{div} \vec{P}$$

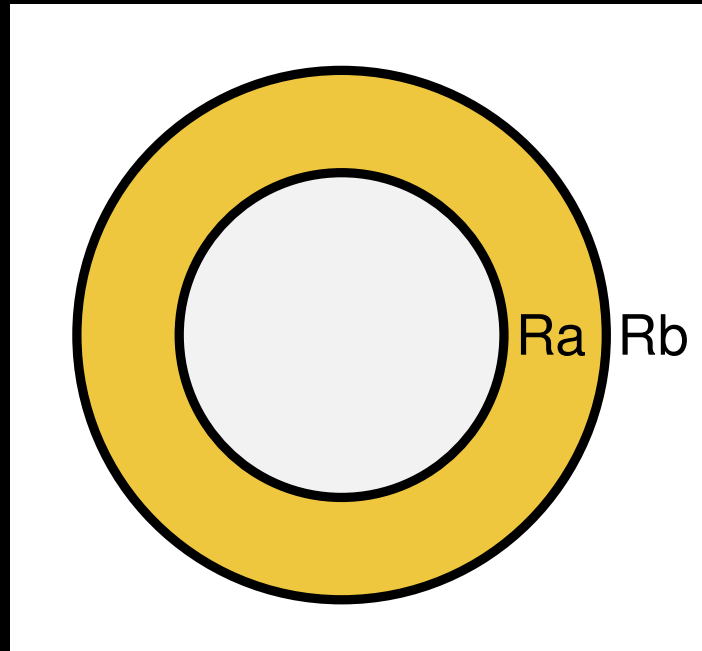


$$\vec{P}(\vec{r}) = \frac{\epsilon_0 \chi_e Q_0}{4\pi \epsilon_0 \epsilon_r r^2} \hat{e}_r = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$

$$\rho_{\text{pol}} = -\text{div} \vec{P} = 0$$



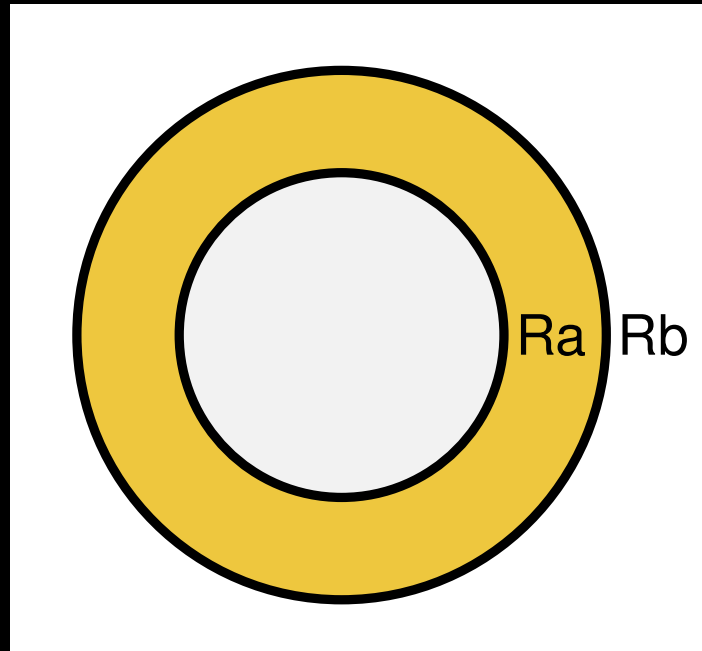
$$\vec{P}(\vec{r}) = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$



$$\vec{P}(\vec{r}) = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$

Quelle densité de charge surfacique de polarisation à  $R_b$  ?

$\rho_{s \text{ pol}} =$

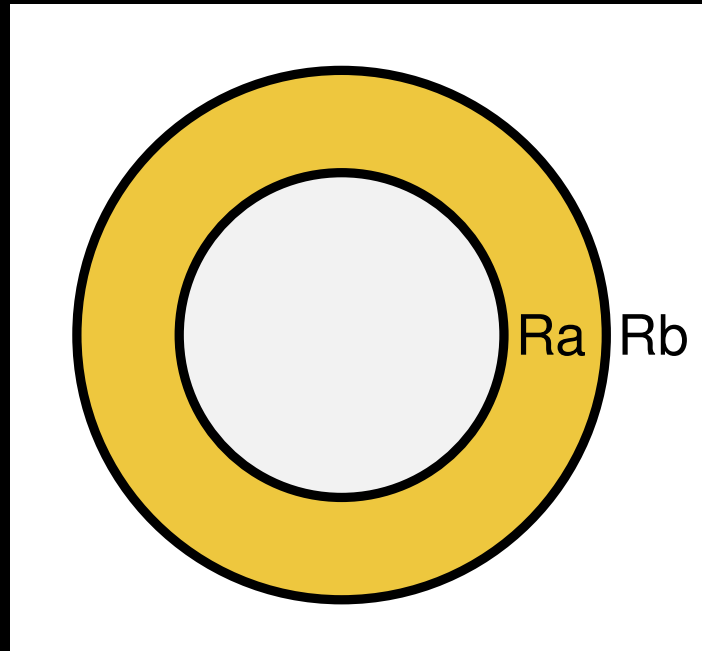


$$\vec{P}(\vec{r}) = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$

Quelle densité de charge surfacique de polarisation à  $R_b$  ?

$$\rho_{s \text{ pol}} = \vec{P} \cdot \hat{n} =$$





$$\vec{P}(\vec{r}) = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$

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$$\rho_{s \text{ pol}} = \vec{P} \cdot \hat{n} =$$

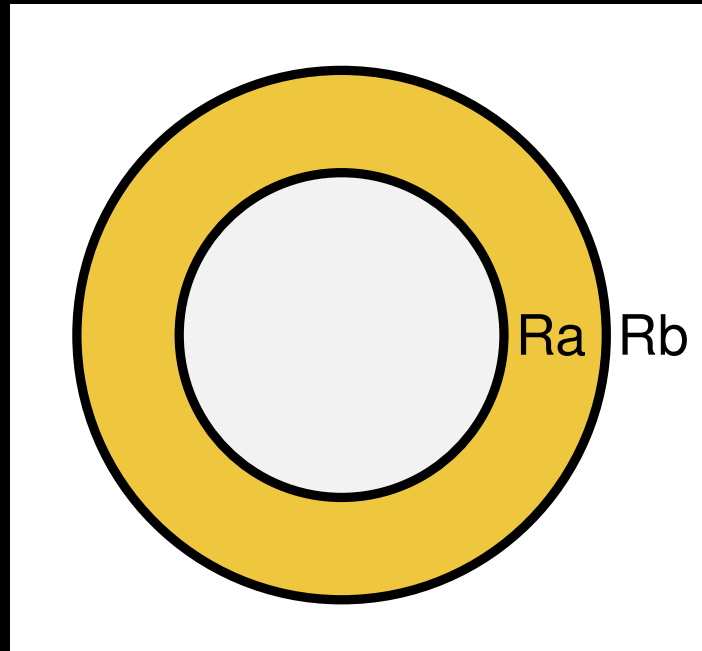
A.  $\frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2}$

B.  $-\frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2}$

C.  $\frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi R_a^2}$

D.  $-\frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi R_a^2}$

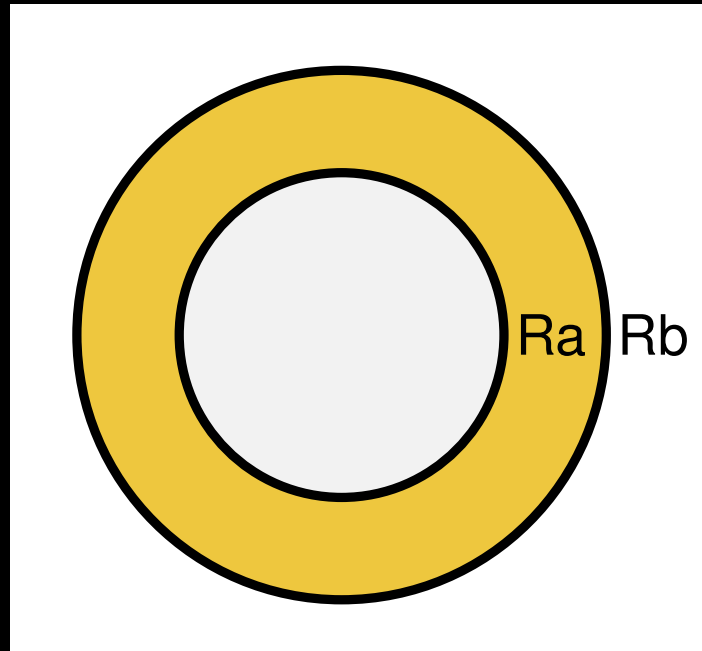
E. Aucune bonne réponse.



$$\vec{P}(\vec{r}) = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$

Quelle densité de charge surfacique de polarisation à  $R_a$  ?

$$\rho_{s \text{ pol}} = \vec{P} \cdot \hat{n} =$$



$$\vec{P}(\vec{r}) = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$

Quelle densité de charge surfacique de polarisation à  $R_a$  ?

$$\rho_{s \text{ pol}} = \vec{P} \cdot \hat{n} =$$

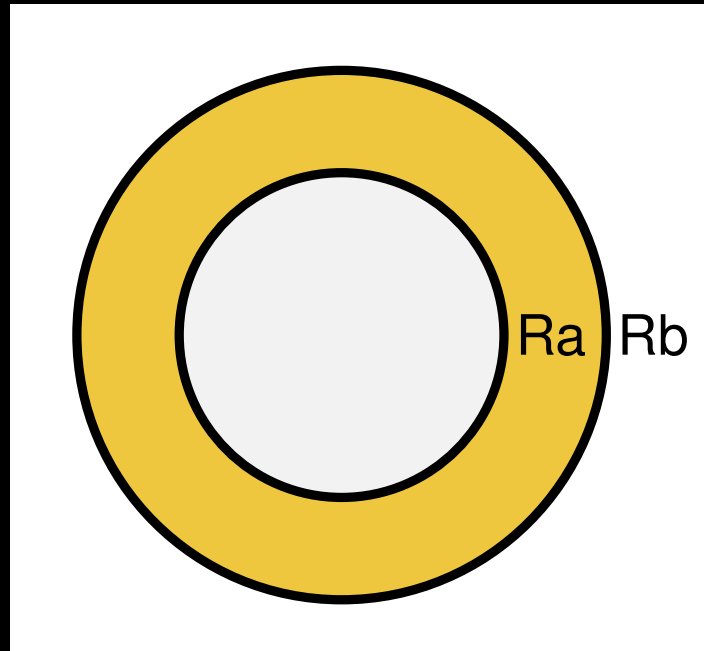
A.  $\frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2}$

B.  $-\frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2}$

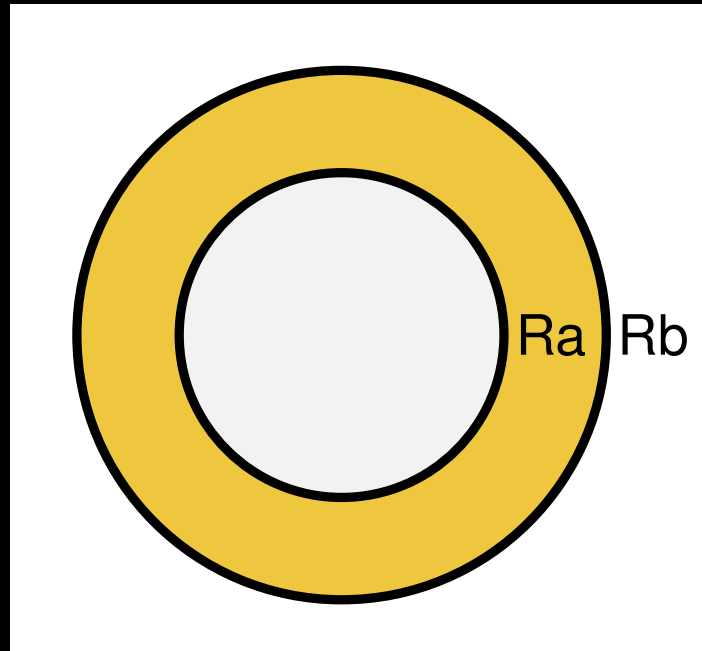
C.  $\frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi R_a^2}$

D.  $-\frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi R_a^2}$

E. Aucune bonne réponse.

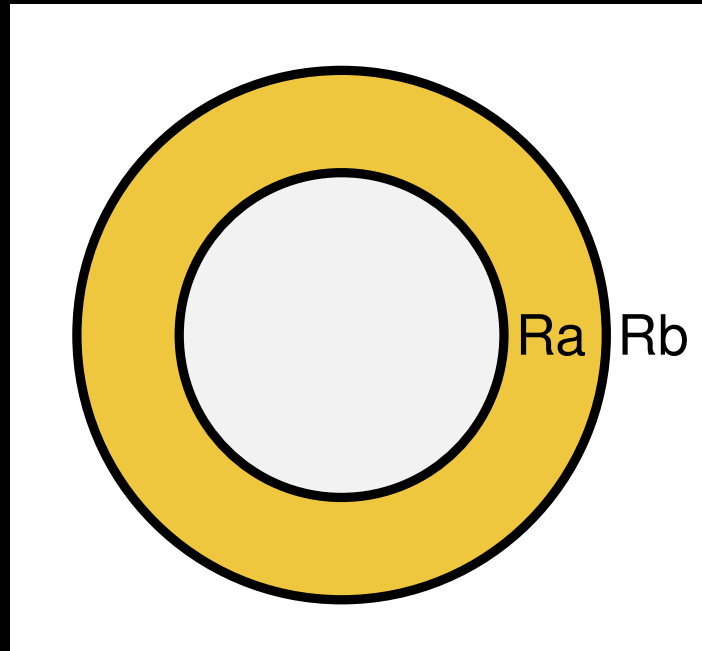


$$\vec{P}(\vec{r}) = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$



$$\vec{P}(\vec{r}) = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$

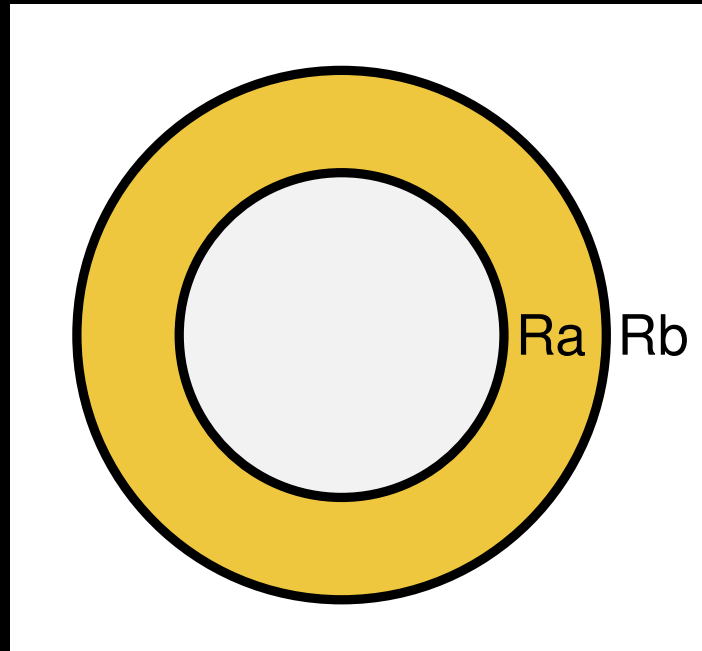
Quelles densités de charge pour ce problème ? Quelles charges ?



$$\vec{P}(\vec{r}) = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$

Quelles densités de charge pour ce problème ? Quelles charges ?

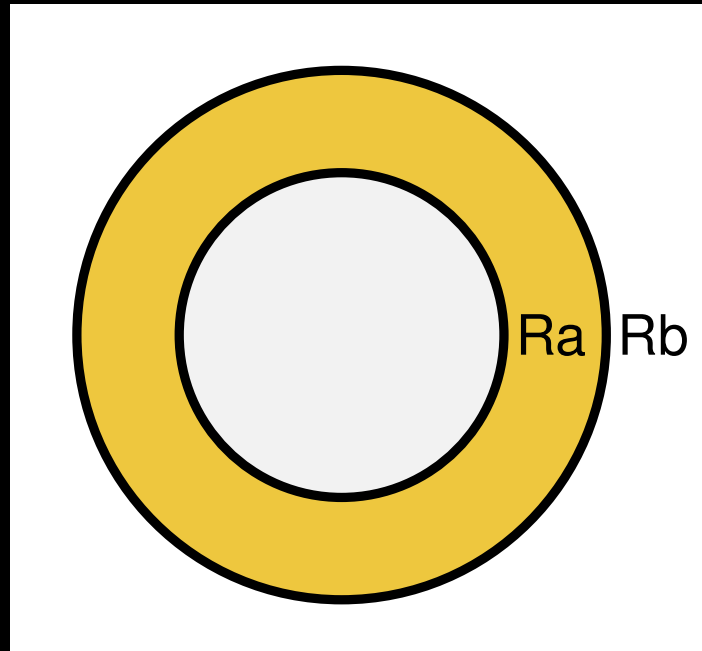
$$\blacktriangledown \text{ à } R_a : \rho_s = \frac{Q_0}{4\pi R_a^2} + \left( -\frac{\chi_e}{1+\chi_e} \frac{Q_0}{4\pi R_a^2} \right)$$



$$\vec{P}(\vec{r}) = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$

Quelles densités de charge pour ce problème ? Quelles charges ?

$$\blacktriangledown \text{ à } R_a : \rho_s = \frac{Q_0}{4\pi R_a^2} + \left( -\frac{\chi_e}{1+\chi_e} \frac{Q_0}{4\pi R_a^2} \right) = \frac{1}{1+\chi_e} \frac{Q_0}{4\pi R_a^2}$$

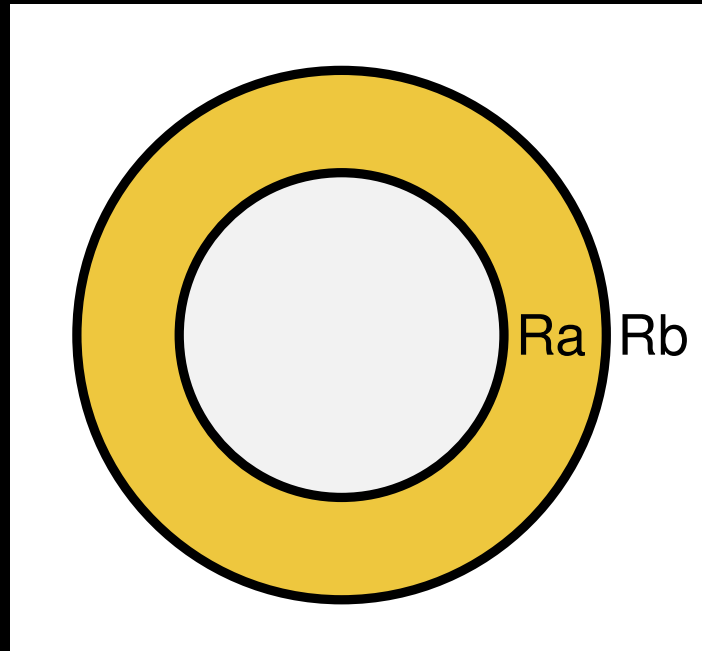


$$\vec{P}(\vec{r}) = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$

Quelles densités de charge pour ce problème ? Quelles charges ?

$$\begin{aligned} \blacktriangledown \text{ à } R_a : \rho_s &= \frac{Q_0}{4\pi R_a^2} + \left( -\frac{\chi_e}{1+\chi_e} \frac{Q_0}{4\pi R_a^2} \right) = \frac{1}{1+\chi_e} \frac{Q_0}{4\pi R_a^2} \\ \Rightarrow Q_a &= \int_S \rho_s dS = \end{aligned}$$

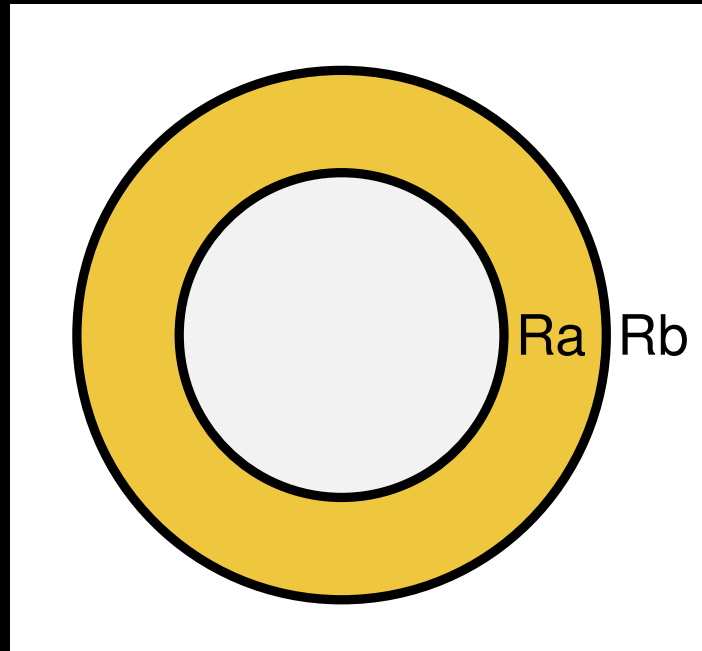




$$\vec{P}(\vec{r}) = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$

Quelles densités de charge pour ce problème ? Quelles charges ?

$$\begin{aligned} \blacktriangledown \text{ à } R_a : \rho_s &= \frac{Q_0}{4\pi R_a^2} + \left( -\frac{\chi_e}{1+\chi_e} \frac{Q_0}{4\pi R_a^2} \right) = \frac{1}{1+\chi_e} \frac{Q_0}{4\pi R_a^2} \\ \Rightarrow Q_a &= \int_S \rho_s dS = \frac{1}{1+\chi_e} Q_0 \end{aligned}$$



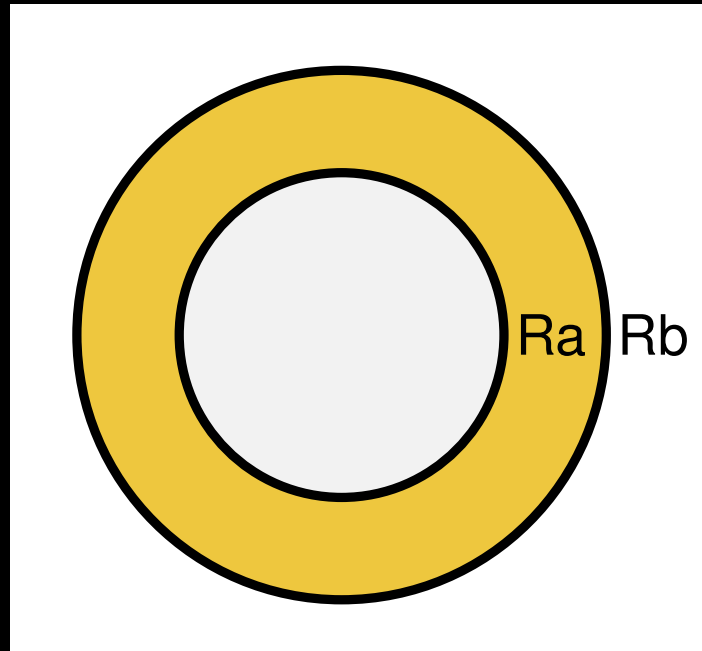
$$\vec{P}(\vec{r}) = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$

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$$\Rightarrow Q_a = \int_S \rho_s dS = \frac{1}{1+\chi_e} Q_0$$

$$\blacktriangledown \text{ à } R_b : \rho_s = \frac{\chi_e}{1+\chi_e} \frac{Q_0}{4\pi R_b^2}$$



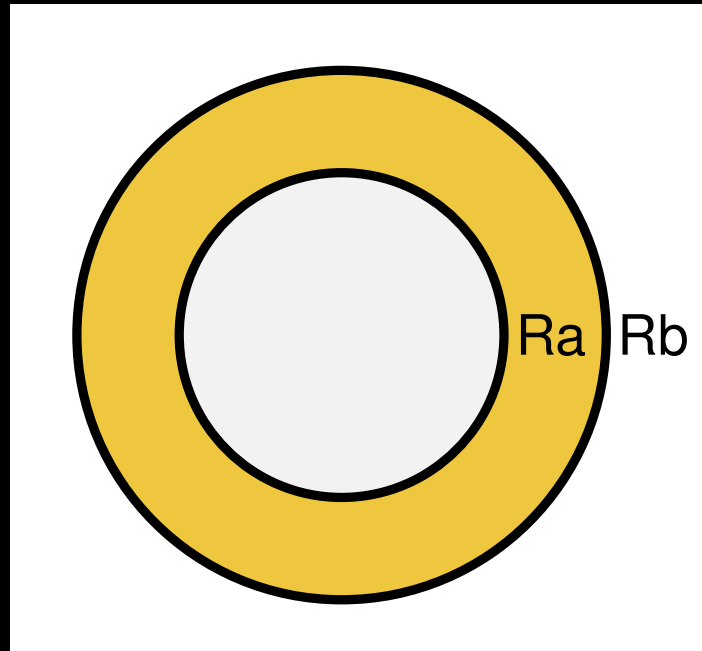
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Quelles densités de charge pour ce problème ? Quelles charges ?

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$$\Rightarrow Q_a = \int_S \rho_s dS = \frac{1}{1+\chi_e} Q_0$$

$$\blacktriangledown \text{ à } R_b : \rho_s = \frac{\chi_e}{1+\chi_e} \frac{Q_0}{4\pi R_b^2} \Rightarrow Q_b = \int_S \rho_s dS =$$



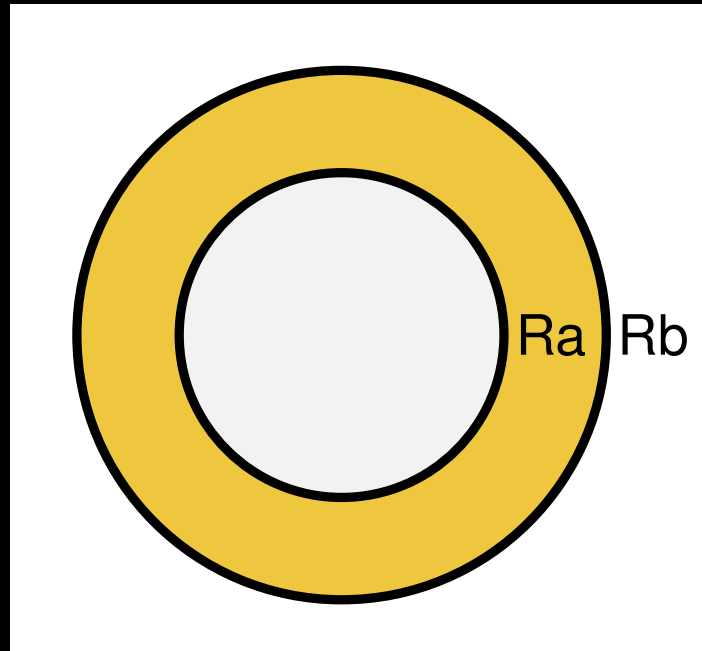
$$\vec{P}(\vec{r}) = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$

Quelles densités de charge pour ce problème ? Quelles charges ?

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$$\Rightarrow Q_a = \int_S \rho_s dS = \frac{1}{1+\chi_e} Q_0$$

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$$\vec{P}(\vec{r}) = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$

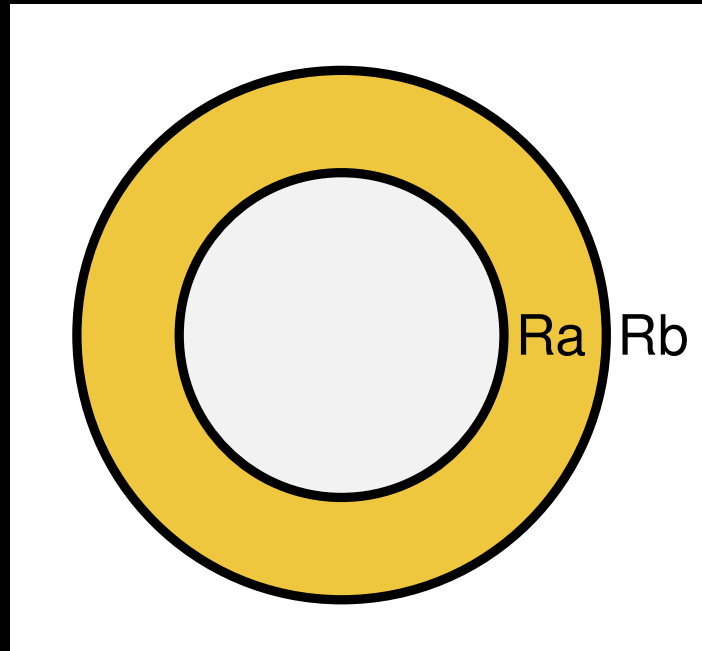
Quelles densités de charge pour ce problème ? Quelles charges ?

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$$\Rightarrow Q_a = \int_S \rho_s dS = \frac{1}{1+\chi_e} Q_0$$

$$\blacktriangledown \text{ à } R_b : \rho_s = \frac{\chi_e}{1+\chi_e} \frac{Q_0}{4\pi R_b^2} \Rightarrow Q_b = \int_S \rho_s dS = \frac{\chi_e}{1+\chi_e} Q_0$$

$$Q_a + Q_b =$$



$$\vec{P}(\vec{r}) = \frac{\chi_e}{1 + \chi_e} \frac{Q_0}{4\pi r^2} \hat{e}_r \quad (R_a < r < R_b)$$

Quelles densités de charge pour ce problème ? Quelles charges ?

$$\blacktriangledown \text{ à } R_a : \rho_s = \frac{Q_0}{4\pi R_a^2} + \left( -\frac{\chi_e}{1+\chi_e} \frac{Q_0}{4\pi R_a^2} \right) = \frac{1}{1+\chi_e} \frac{Q_0}{4\pi R_a^2}$$

$$\Rightarrow Q_a = \int_S \rho_s dS = \frac{1}{1+\chi_e} Q_0$$

$$\blacktriangledown \text{ à } R_b : \rho_s = \frac{\chi_e}{1+\chi_e} \frac{Q_0}{4\pi R_b^2} \Rightarrow Q_b = \int_S \rho_s dS = \frac{\chi_e}{1+\chi_e} Q_0$$

$$Q_a + Q_b = Q_0$$