• 
$$e^x = \sum_{n=0}^{+\infty} \frac{1}{n!} x^n$$
  $= 1 + x + \frac{x^2}{2!} + \frac{x^3}{3!} + \dots$   $R = +\infty$ 

• 
$$e^{-x} = \sum_{n=0}^{+\infty} \frac{(-1)^n}{n!} x^n$$
  $= 1 - x + \frac{x^2}{2!} - \frac{x^3}{3!} + \dots$   $R = +\infty$ 

• 
$$\operatorname{ch} x = \sum_{n=0}^{+\infty} \frac{1}{(2n)!} x^{2n} = 1 + \frac{x^2}{2!} + \frac{x^4}{4!} + \dots$$
  $R = +\infty$ 

• 
$$\operatorname{sh} x = \sum_{n=0}^{+\infty} \frac{1}{(2n+1)!} x^{2n+1} = x + \frac{x^3}{3!} + \frac{x^5}{5!} + \dots$$
  $R = +\infty$ 

• 
$$\cos x = \sum_{n=0}^{+\infty} \frac{(-1)^n}{(2n)!} x^{2n} = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \dots$$
  $R = +\infty$ 

• 
$$\sin x = \sum_{n=0}^{+\infty} \frac{(-1)^n}{(2n+1)!} x^{2n+1} = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \dots$$
  $R = +\infty$ 

• 
$$\frac{1}{1-x} = \sum_{n=0}^{+\infty} x^n = 1 + x + x^2 + x^3 + \dots \quad R = 1$$

• 
$$\frac{1}{1+x} = \sum_{n=0}^{+\infty} (-1)^n x^n = 1 - x + x^2 - x^3 + \dots$$
  $R = 1$ 

$$\bullet \quad \frac{1}{x-a} = \qquad \dots \qquad = \dots$$

$$\bullet \quad \frac{1}{(x-a)^p} = \quad \dots \qquad \qquad = \dots$$

• 
$$\ln(1+x) = \sum_{n=1}^{+\infty} \frac{(-1)^{n-1}}{n} x^n = \frac{x}{1} - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots$$
  $R = 1$ 

• 
$$\ln(1-x) = \sum_{n=1}^{+\infty} \frac{-1}{n} x^n$$
  $= -\frac{x}{1} - \frac{x^2}{2} - \frac{x^3}{3} - \frac{x^4}{4} - \dots$   $R = 1$ 

• 
$$\ln\left(\frac{1+x}{1-x}\right) = \sum_{n=0}^{+\infty} \frac{2}{2n+1} x^{2n+1} = 2x + \frac{2x^3}{3} + \frac{2x^5}{5} + \frac{2x^7}{7} + \dots$$
  $R = 1$ 

• Arctan 
$$x = \sum_{n=0}^{+\infty} \frac{(-1)^n}{2n+1} x^{2n+1} = x - \frac{x^3}{3} + \frac{x^5}{5} - \frac{x^7}{7} + \dots$$
  $R = 1$ 

• 
$$(1+x)^{\alpha} = 1 + \sum_{n=1}^{+\infty} \frac{\alpha(\alpha-1)\dots(\alpha-n+1)}{n!} x^n$$
 
$$R = \begin{cases} 1 & \text{si } \alpha \notin \mathbb{N} \\ +\infty & \text{si } \alpha \in \mathbb{N} \end{cases}$$

• 
$$\sqrt{1-x} = 1 - \frac{x}{2} - \frac{x^2}{8} - \frac{5x^4}{128} - \dots - \frac{1 \times 3 \times \dots (2n-3)}{2 \times 4 \times \dots \times 2n} x^n - \dots R = 1$$

• 
$$\frac{1}{\sqrt{1-x}} = 1 + \frac{x}{2} + \frac{x^2}{8} + \frac{5x^4}{128} + \dots + \frac{1 \times 3 \times \dots (2n-3)}{2 \times 4 \times \dots \times 2n} x^n + \dots R = 1$$