AS91522 - Physics 3.2

Circular Motion of a Stunt Glider

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1 Vertical Circle: Loop the loop including Dip and Arch

1.1 Achieved

During motion, 3 forces are acting on the stunt glider:

- 1. Gravity $(\vec{F_q})$ (i.e. Weight) always vertically downwards (i.e. toward center of Earth).
- 2. Lift $(\vec{F_L})$ perpendicular to direction of velocity, toward the center of the circular path.
- 3. Air Resistance $(\vec{F_R})$ (i.e. Friction, Drag) opposite to direction of velocity.

The force of gravity is always constant in both magnitude and direction (vertically downwards) regardless of the glider's velocity or position in the loop (top, bottom, and anywhere else). This is because $|\vec{F}_g| = mg$ where mass (m) and the acceleration of gravity (g) are constants.

Conversely, the force of lift varies in both direction and magnitude as the glider performs the loop the loop. Lift's magnitude $(|\vec{F_L}|)$ is greatest at the bottom, $|\vec{F_L}| = \frac{1}{2}p|\vec{v}|^2AC_L$, $|\vec{F_L}| \propto v^2$. Because velocity is greatest at bottom, lift force is as well. To maintain circular motion the centripetal force $(|\vec{F_c}| = |\vec{F_L}| - |\vec{F_g}|)$ towards the center of the circular path must have a magnitude value great enough to provide necessary centripetal acceleration for the circular path radius, meaning the lift force upwards must at least be greater than the gravity force downwards $(|\vec{F_L}| > |\vec{F_g}|)$ in order for $|\vec{F_c}| > 0$.

Lift's magnitude $(|\vec{F_L}|)$ is least at the top, because the direction of gravity force is toward the center of the circular path. This means $(|\vec{F_c}| = |\vec{F_L}| + |\vec{F_g}|)$.

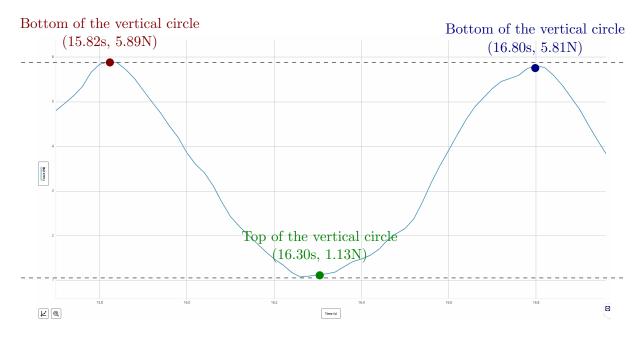


Figure 1: Graph of a complete vertical loop

At the bottom of the vertical circle, the tension force (emulating the lift force, $\vec{F_L}$) is greatest, which occurs at 15.82 seconds with 5.89N.

Once the force meter (emulating motion of glider) reaches the top of the vertical circle, the tension force is at its least, which - when smoothing the curve of data and reducing random variation/noise - occurs at Check if sine model or quadratic helps - then return to this section.

During the loop the loop, as the glider ascends, its kinetic energy (E_K) is converted into gravitational potential energy (E_p) . As the glider descends, its gravitational potential energy (E_p) is converted back into kinetic energy (E_K) .

1.2 Merit

$$E_K = \frac{1}{2}m|\vec{v}|^2\tag{1}$$

$$\therefore |\vec{v}|^2 \propto E_K \tag{2}$$

$$|\vec{v}| \propto \sqrt{E_K}$$
 (3)

During the loop the loop, as the glider ascends, its kinetic energy (E_K) is converted into gravitational potential energy (E_p) . This decreases its velocity as it is proportional to kinetic energy, which decreased when converted to gravitational potential energy.

As the glider descends, its gravitational potential energy (E_p) is converted back into kinetic energy (E_K) . This increases its velocity as it is proportional to kinetic energy, which increased when the gravitational potential energy was converted back into it.

A glider's ability to successfully perform a vertical loop relies on its ability to provide an adequate lift force, increasing both net and centripital force.

$$|\vec{F_L}| = \frac{1}{2}p|\vec{v}|^2 AC_L \tag{4}$$

$$\therefore |\vec{F_L}| \propto |\vec{v}|^2 \tag{5}$$

Equation (5) shows that velocity is a major factor in the magnitude of the lift force. Without adequate velocity, inadequate lift force is provided for the vertical loop to be successful. As kinetic energy is converted to gravitational potential energy during ascent, if the velocity drops below what is required for the circular path radius its motion will instead imitate that of a projectile.

Other factors proportional to velocity include surface area contacting air (A), and the coefficient of lift (C_L) , determined by shape and angle of attack).

Fluid density (p) is constant.

During motion, 3 forces are acting on the stunt glider:

- 1. Gravity $(\vec{F_g})$ (i.e. Weight) always vertically downwards (i.e. toward center of Earth).
- 2. Lift $(\vec{F_L})$ perpendicular to direction of velocity, toward the center of the circular path.
- 3. Air Resistance $(\vec{F_R})$ (i.e. Friction, Drag) opposite to direction of velocity.

Please note that vector arrow lengths are not perfectly proportionally accurate.

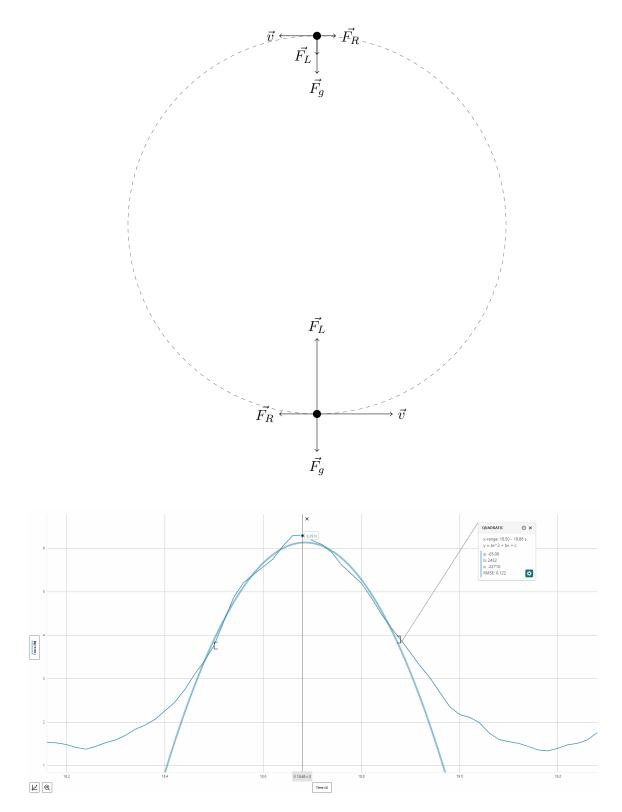
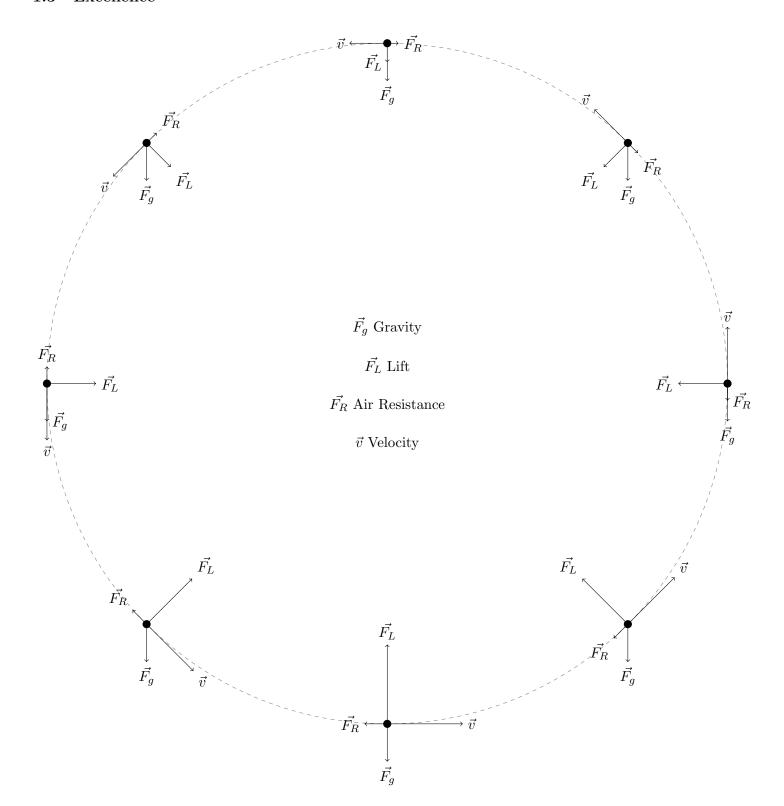


Figure 2: The dip section of vertical circular motion with a quadratic curve fit

Quadratic curve fit is applied to closely fit the lift force data in the section of the dip motion from 18.50s to 18.88s. It helps exclude random variation / noise in the data and provide consistent smoothness and symmetry. The line displayed in the center marks 18.68s, which is when the emulated glider reaches its lowest vertical height (i.e. lowest point in the dip), also aligning with the local peak in the emulated lift force at 6.29N. The reason for the greatest lift force being required at the bottom of the loop the loop is due to its direction oppositely opposing gravity, requiring the greatest magnitude to provide sufficient centripetal force for the vertical loop's radius. The velocity is also greatest here as it has the greatest $E_K: E_P$ ratio (i.e. $\frac{E_K}{E_P}$ is at its greatest in the time series) (as previously explained) which is a major factor in causing that required greatest lift force (as previously explained in Eq2,3,5 :: $E_K \propto |\vec{v}|^2 \propto |\vec{F_L}|$).

1.3 Excellence



	ш
Bottom of loop (\vec{v} direction is horizontally right)	Top of loop (\vec{v} direction is horizontally left)
$ec{F_L}$ $ec{F_c}$ $ec{F_g}$	$ec{v} \longleftrightarrow ec{F_L} \longleftrightarrow ec{F_g}$ $ec{F_c}$
$ec{F_c} = ec{F_L} + ec{F_g} \ ec{F_c} = ec{F_L} - ec{F_g} $	$ec{F_c} = ec{F_L} + ec{F_g} \ ec{F_c} = ec{F_L} + ec{F_g} $
$ ec{F_c} = ec{F_L} - ec{F_g} $	$ \vec{F_c} = \vec{F_L} + \vec{F_g} $
Lift and gravity force vectors add. Gravity reduces magnitude of centripetal force as it opposes in direction.	Lift and gravity force vectors add. Gravity increases magnitude of centripetal force as it aligns in direction.
On the graph from our force meter model, this position has the greatest tension force, which is used to emulate the lift force of the glider. As previously explained, this is what we should expect as kinetic energy, velocity, and consequently the lift force of glider should be greatest, which is crucial for it to counter gravity and provide sufficient magnitude. Although the tension force doesn't perfectly act as a lift force in that its force isnt proportional to velocity in the same way it instead almost instantaneously provides adequate force to decelerate outwards velocity to zero and if it remains on the circumference of the path with force applied against it, tension provides greater than or equal to to	new cell

counter it.

Right of loop (\vec{v} direction is vertically upwards)	Bottom Right of loop (\vec{v} direction is right at 45° above horizontal)
$ec{F_c} \overset{ec{v}}{\longleftrightarrow} ec{F_R} \ ec{F_g}$	$ec{F_L}$ $ec{V}$ $ec{F_C}$ $ec{F_R}$ $ec{F_{g_{C1}}}$ $ec{F_{g_{C2}}}$ $ec{F_{g_{C2}}}$
$ec{F_c} = ec{F_L}$	$\vec{F_c} = \vec{F_L} + \vec{F_{g_{C2}}}$
$ ec{F_c} = ec{F_L} $	$ec{F_c} = ec{F_L} + ec{F_{g_{C2}}}$ $ec{F_c} = ec{F_L} - ec{F_{g_{C2}}}ert$
Centripetal force can only be provided by lift force. All other forces are vertical (have no horizontal component that can contribute to centripetal force).	Lift and only a component of gravity $(\vec{F_{gC2}})$ add to provide the centripetal force. That component of gravity contributes in decreasing the magnitude of centripetal force as it opposes in direction.

2 Banked Corner

- 2.1 Achieved
- 2.2 Merit
- 2.3 Excellence

3 Additional Info

3.1 Comprehensive Version History

Access to all prior versions of this document during process of creation is publicly available at: https://github.com/NathanTaskerPersonal/AS91522

3.2 Graphical Analysis Files

Access to all graphical analysis files are publicly available at: middletonschoolnz-my.sharepoint.com/...

3.3 LATEX

This document has been entirely written in LATEX; a markup language for mathematical equations and diagrams. I'm more than happy to provide plain text for the entire document for convenience in AI detection.

3.4 Bibliography