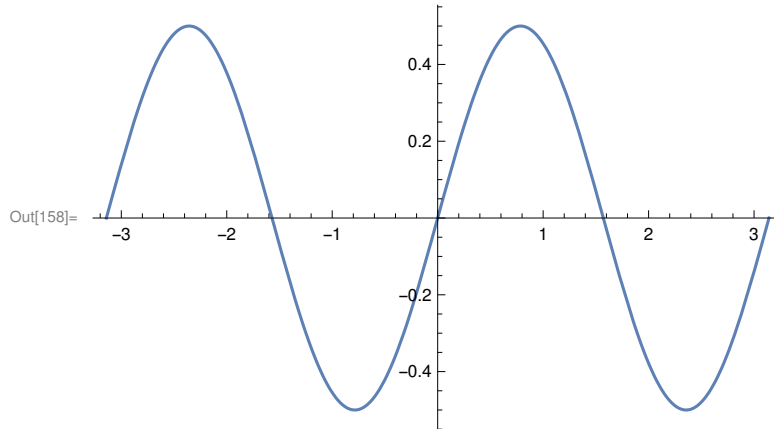


# Mathematica hw3 complex variables

## 37 iii

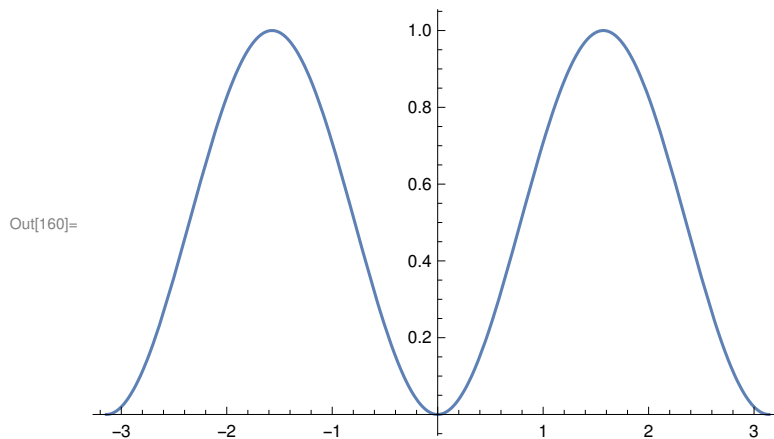
Using integrations to confirm symmetries

```
In[158]:= Plot[Sin[θ] Cos[θ], {θ, -Pi, Pi}]  
Integrate[Sin[θ] Cos[θ], {θ, -Pi, Pi}]
```



Out[159]= 0

```
In[160]:= Plot[Sin[θ] Sin[θ], {θ, -Pi, Pi}]  
Integrate[Sin[θ] Sin[θ], {θ, -Pi, Pi}]
```



Out[161]=  $\pi$

## Trying to integrate the infinite series

In[164]:= **bn37 = Sum** $\left[\frac{-1^{n+1} \text{Sin}[n * \theta]}{n}, \{n, 1, \text{Infinity}\}\right]$

Out[164]=  $-\frac{1}{2} i \left( \text{Log}\left[1 - e^{i \theta}\right] - \text{Log}\left[e^{-i \theta} (-1 + e^{i \theta})\right] \right)$

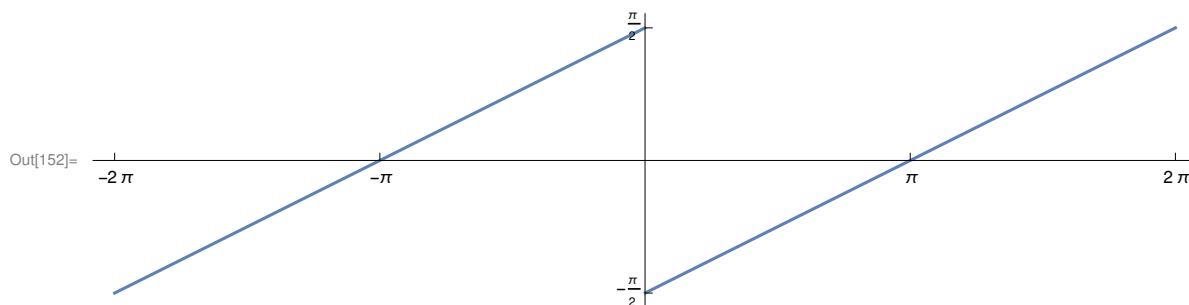
In[168]:=  $\frac{1}{\text{Pi}}$  \* **Integrate** $[\text{Sin}[n * \theta] \text{bn37}, \{\theta, -\text{Pi}, \text{Pi}\}]$

Out[168]=  $\frac{-n \pi + \text{Sin}[n \pi]}{n^2 \pi}$

## 37 iv

I get a slightly different plot than the book. Their line passes through 0 while mine jumps at 0. Given that  $\text{Sin}[0] = 0$ , it should definitely pass through the origin.

In[152]:= **Plot** $\left[\text{Sum}\left[-1^{n+1} \frac{\text{Sin}[n * \theta]}{n}, \{n, 1, \text{Infinity}\}\right], \{\theta, -2 \text{Pi}, 2 \text{Pi}\}, \right.$   
**Ticks**  $\rightarrow \left\{\{-2 \text{Pi}, -\text{Pi}, \text{Pi}, 2 \text{Pi}\}, \left\{\frac{-\text{Pi}}{2}, \frac{\text{Pi}}{2}\right\}\right\}, \text{AspectRatio} \rightarrow \text{Automatic}, \text{ImageSize} \rightarrow \text{Large}]$



## 38 iv

Identical plot to the one in the book.

```
In[156]:= Plot[Sum[ $\frac{\text{Sin}[(2 * n - 1) * \theta]}{(2 * n - 1)}$ , {n, 1, Infinity}], { $\theta$ , -2 Pi, 2 Pi},  
  Ticks → {{-2 Pi, -Pi, Pi, 2 Pi}, {- $\frac{\text{Pi}}{4}$ ,  $\frac{\text{Pi}}{4}$ }}, AspectRatio → Automatic, ImageSize → Large]
```

