

```
1
2
3 Recursive 'Algorithms' {
4
5     [LAPC CS 131]
6
7
8
9     return Presentation
10
11
12 }
13
14
```

What is Recursion {

In computer science,
<An algorithm is called *recursive* if it solves a problem by
reducing it to an instance of the same problem with smaller input.
>

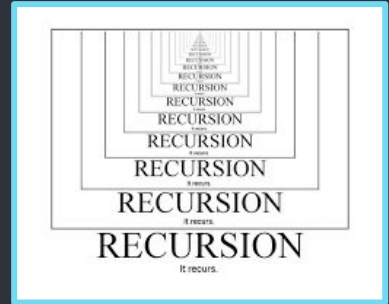
< /1 >

- *Direct*
- a call to a function appears in that function's body

< /2 >

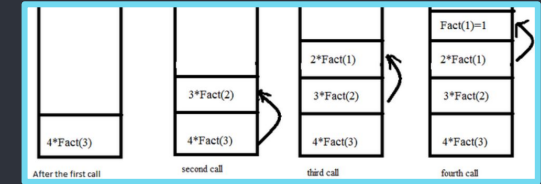
- *Indirect*
- the pattern is some function calls some other function

}



Iteration vs Recursion {

RECURSION	Iteration
Uses more storage space requirement	Less storage space requirement
Overhead during runtime	Less Overhead during runtime
Runs slower	Runs faster
a better choice, a more elegant solution for recursive problems	Less elegant solution for recursive problems



Call stack

Real World Problem {

Problem: collect \$1,000.00 from a 1000 people in the room by asking them for **1 dollar**.

Iterative solution: visit the 1,000 people, and ask each for a \$1

Recursive solution: give a \$1 to person otherwise visit 10 people and ask them each to collect 1/10 the amount that you are asked to raise; collect the money they give you into one bag; give this bag to the person who asked you for the money

}

Form: Directly Recursive Function {

```
def Solve(Problem):
```

```
    if Base case then Solve Problem directly and return solution
```

```
    else:
```

```
        (1) Decompose Problem
```

```
        (2) Recursively call Solve (this function) on each smaller subproblem
```

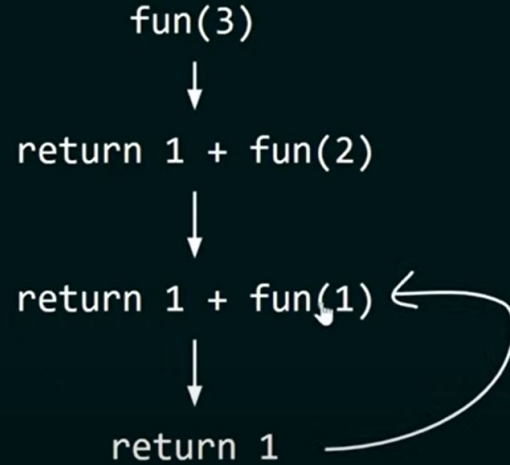
```
        (3) Combine the returned solutions to smaller subproblems
```

```
        (4) Return the solution to the Solve Function
```

```
}
```

Ex: Factorial {

```
1  int fun(int n)
2  {
3      if(n == 1)
4          return 1;
5      else
6          return 1 + fun(n-1)
7  }
8
9  int main() {
10     int n = 3;
11     printf("%d", fun(n));
12     return 0;
13 }
```



Proving Recursive Functions {

```
1  
2  procedure square(n: nonnegative integer)  
3  if n = 0 then return 0  
4  else return square (n - 1) + 2(n - 1) + 1  
5  
6
```

Using Mathematical Induction:

Base Case n=0:

$0^2 = 0$, then that's satisfied

Inductive Case:

Assume k is an int

Then for k + 1:

$$\text{square}(k) + 2(k+1) - 1 = k^2 + 2k + 1 = (k + 1)^2$$

13
14 }

Cited Works {

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