Marco T. Morazán

Ctata

Language with Explicit References

Language wit Implicit References

Mutable Pai

Parameter Passing Part IV: State

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Mutable Pair

Parameter Passing Variations

- 1 State
- 2 Language with Explicit References
- 3 Language with Implicit References
- 4 Mutable Pairs
- **5** Parameter Passing Variations

Language with Explicit References

Language wit Implicit References

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Paramete Passing Variations

- Computations may also have effects
 - print
 - change a memory location
 - change a file
- An effect is global: affects the entire computation
- We will now study assignment (aka mutation)

Language wit Explicit References

Language with Implicit References

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Parameter Passing Variations

- Assignment is about sharing values/information between unrelated parts of a computation
- CSAS 1115: telephone book, bank account
- Memory model
 - A finite map of locations to storable values (aka store or heap)
 - A place in memory where values can be stored
- Implementation
 - Typically, storable values are the same as the expressed values
 - A data structure that represents a location is called a reference (aka pointer)

Language with Explicit References

Language with Implicit References

Mutable Pair

Paramete Passing Variations

- Two ways to design a language with store
- Explicit references
- programmer allocates, dereferences, and mutates locations/memory
- Implicit references
- language packages common patterns of allocation, dereferencing, and mutation

Language with Explicit References

- expval = int + bool + proc + ref(expval)
- denval = expval
- 3 new ops needed:

newref allocates a new location and returns a reference to the new location deref returns the content of a reference

setref changes the content of a referenced location

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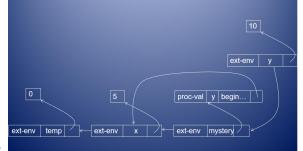
Language with Explicit References

Language with Explicit References

Value?

```
let temp = newref(0)
   let x = newref(5)
        let mystery = proc (y)
                        begin
                          setref(temp, deref(x)));
                          setref(x, deref(y));
                          setref(y, deref(temp));
                          deref(x)
        end
```

in (mystery newref(10))



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Language with Explicit References

Language wit Implicit

Mutable Pair

Parameter Passing

Language with Explicit References

```
let temp = newref(0)
   let x = newref(5)
        let mystery = proc (y)
                        begin
                           setref(temp, deref(x)));
                           setref(x, deref(y));
                           setref(y, deref(temp));
                           deref(x)
        end
    in (mystery newref(10))
```

Language with Explicit References

Language wit Implicit

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Parameter Passing

Language with Explicit References

```
let temp = newref(0)
      let x = newref(5)
           let mystery = proc (y)
                              begin
                                setref(temp, deref(x)));
                                setref(x, deref(y));
                                setref(y, deref(temp));
                                deref(x)
           end
       in (mystery newref(10))
                                                      ext-env
                                           proc-val y begin...
                 temp
                           ext-env
                                           ext-env
                                                  mystery
          ext-env
```

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Language with Explicit References

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Parameter Passing

Language with Explicit References

```
let temp = newref(0)
   let x = newref(5)
       let mystery = proc (y)
                         begin
                           setref(temp, deref(x)));
                           setref(x, deref(y));
                           setref(y, deref(temp));
                           deref(x)
        end
    in (mystery newref(10))
                                               ext-env
```



Returns: 10

proc-val

y begin...

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Parameter Passing

Language with Explicit References

```
let x = newref(newref(10))
in begin
setref(deref(x), 20));
+(20, deref(deref(x)))
   end
```

Mutable Pair

Paramete Passing

Language with Explicit References

```
• let x = newref(newref(10))
in begin
setref(deref(x), 20));
+(20, deref(deref(x)))
    end
```

Mutable Pair

Parameter Passing

Language with Explicit References

```
let x = newref(newref(10))
in begin
setref(deref(x), 20));
+(20, deref(deref(x)))
  end
```

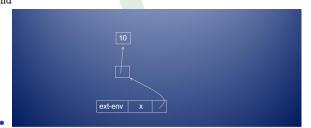


Mutable Pai

Parameter Passing

Language with Explicit References

```
let x = newref(newref(10))
in begin
setref(deref(x), 20));
+(20, deref(deref(x)))
end
```



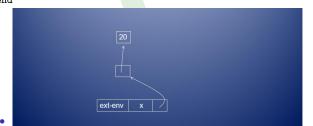
Language wit Implicit

Mutable Pair

Parameter Passing

Language with Explicit References

```
let x = newref(newref(10))
in begin
setref(deref(x), 20));
+(20, deref(deref(x)))
end
```



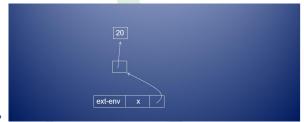
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Language with Explicit References

• Is this a valid program? If so, what does it evaluate to?

```
let x = newref(newref(10))
in begin
setref(deref(x), 20));
+(20, deref(deref(x)))
   end
```



Returns 40

Charles

Language with Explicit References

Language with Implicit

Mutable Pai

Paramete Passing

Language with Explicit References

Expressed Values

```
(define-datatype expval expval?
    (num-val
     (value number?))
    (bool-val
     (boolean boolean?))
    (proc-val
     (proc proc?))
    (ref-val
     (ref reference?)))
;; expval --> ref throws error
  ;; Purpose: Extract ref from given expval
  (define (expval2ref v)
    (cases expval v
      (ref-val (ref) ref)
      (else (expval-extractor-error 'reference v))))
```

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Parameter Passing

Language with Explicit References

- To have effects values must be stored somewhere
- σ ranges over the store (or heap)
- $[I=v]\sigma o$ the store σ extended with location I mapped to v
- We shall think of the store as an argument to value-of
- (value-of exp1 ρ σ_0) = (val1, σ_1)
- σ_0 may or may not be the same as σ_1

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Parameter Passing

Language with Explicit References Specification

- (value-of (const-exp n) ρ σ) = ((numval n), σ)
 - $\frac{(\textit{value-of exp1}\ \rho\ \sigma_0) = (\textit{val1},\ \sigma_1)\ \land\ (\textit{value-of exp2}\ \rho\ \sigma_1) = (\textit{val2},\ \sigma_2)}{(\textit{value-of (diff-exp exp1 exp2)}\ \rho\ \sigma_0) = ((\textit{num-val val1-val2})\ \sigma_2)}$

$$\frac{(\textit{value-ofe1}\ \rho\ \sigma_0) = (\textit{v1},\sigma_1)}{(\textit{value-of}\ (\textit{if-exp}\ e1\ e2\ e3)}\ \rho\ \sigma_0) = \begin{cases} ((\textit{value-of}\ e2\ \rho\ \sigma_1),\sigma_2) & \text{if } (\exp\rightarrow\textit{val}\ \textit{v1}) = \#t\\ ((\textit{value-of}\ e3\ \rho\ \sigma_1),\sigma_2) & \text{otherwise} \end{cases}$$

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Parameter Passing

Language with Explicit References Specification

```
 \frac{(\textit{value-of exp } \rho \ \sigma_0) = (\textit{val1}, \ \sigma_1) \ \textit{l} \not\in \textit{dom}(\sigma_0) }{(\textit{value-of (newref-exp exp)} \ \rho \ \sigma_0) = ((\textit{ref-val } l), \ [\textit{l} = \textit{val1}]\sigma_1) }
```

- I is a new store location
- $\frac{(\textit{value-ofexp } \rho \ \sigma_0) = (\textit{I}, \ \sigma_1)}{(\textit{value-of } (\textit{deref-exp exp}) \ \rho \ \sigma_0) = (\sigma_1(\textit{I}), \ \sigma_1)}$
- $\frac{(value\text{-}of\ exp1\ \rho\ \sigma_0)=(l,\ \sigma_1)\ \land\ (value\text{-}of\ exp2\ \rho\ \sigma_1)=(val,\ \sigma_2)}{(value\text{-}of\ (setref\text{-}exp\ exp1\ exp2)\ \rho\ \sigma_0)=(\varnothing,\ [l=val]\sigma_2)}$

Mutable Pair

Parameter Passing

Language with Explicit References

Grammar

Mutable Pair

Parameter Passing Variations

Language with Explicit References

Implementation

 Design choice: the store is a global variable Design choice: Represent the store as a (listof expval) :: reference? : RacketVal --> Bool (define (reference? v) (and (integer? v) (>= v 0))) • :: the-store: the current state of the store (define the-store 'uninitialized) • ;; empty-store : --> store (define (empty-store) '()) • :: initialize-store! : --> store (define (initialize-store!) (set! the-store (empty-store))) • ;; newref : expval --> ref (define (newref val) (let ((next-ref (length the-store))) (set! the-store (append the-store (list val))) next-ref)) • ;; deref : ref --> expval (define (deref ref) (list-ref the-store ref)) ;; setref : ref expval --> expval (define (setref! ref new-expval) (set! the-store (append (take the-store ref) (list new-expval) (drop the-store (add1 ref)))))

Mutable Pair

Parameter Passing

Language with Explicit References

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Language with Explicit References

Language wit Implicit

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Parameter Passing

Language with Explicit References

Implementation

```
(define (value-of exp env)
  (cases expression exp
    (const-exp (num) (num-val num))
    (true-exp () (bool-val #t))
    (false-exp () (bool-val #f))
    (var-exp (var) (apply-env env var))
    (diff-exp (exp1 exp2)
              (let ((num1 (expval2num (value-of exp1 env)))
                    (num2 (expval2num (value-of exp2 env))))
                (num-val (- num1 num2))))
    (zero?-exp (exp1)
               (let ((val1 (expval2num (value-of exp1 env))))
                 (if (zero? val1)
                     (bool-val #t)
                     (bool-val #f))))
    (if-exp (exp1 exp2 exp3)
            (let ((val1 (value-of exp1 env)))
              (if (expval2bool val1)
                  (value-of exp2 env)
                  (value-of exp3 env))))
    (let-exp (vars exps body)
             (let [(vals (map (lambda (e) (value-of e env)) exps))]
               (value-of body
                          (foldr (lambda (var val acc)
                                   (extend-env var val acc))
                                 env
                                 vars
                                 vals))))
```

Language wit

Mutable Pair

Parameter Passing

Language with Explicit References

```
    (define (value-of exp env)

     (cases expression exp
       (proc-exp (params body)
                 (proc-val (procedure params body (vector env))))
       (call-exp (rator rands)
                 (let [(proc (expval2proc (value-of rator env)))
                       (args (map (lambda (rand) (value-of rand env)) rands))]
                   (apply-procedure proc args)))
       (letrec-exp (names params bodies letrec-body)
                   (value-of letrec-body (mk-letrec-env names params bodies env)))
       (begin-exp (exp exps)
                  (foldl (lambda (e v) (value-of e env)) (value-of exp env) exps))
       (newref-exp (exp1)
                   (let ((v1 (value-of exp1 env)))
                     (ref-val (newref v1))))
       (deref-exp (exp1)
                  (let ((v1 (value-of exp1 env)))
                    (let ((ref1 (expval2ref v1)))
                      (deref ref1))))
       (setref-exp (exp1 exp2)
                   (let ((ref (expval2ref (value-of exp1 env))))
                     (let ((v2 (value-of exp2 env)))
                       (begin
                         (setref! ref v2)
                         (num-val -1)))))))
```

Mutable Pain

Parameter Passing

Language with Explicit References

• 4.1, 4.2, 4.4, 4.8, 4.9

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Parameter Passing Variations

Language with Implicit References

- Most modern PLs package common patterns of allocation, dereferencing, and mutation
- Programmers do not need to worry about these operations
- Every variable denotes a reference
- References are no longer expressed values and exist only as bindings of vars expval = int + bool + proc denval = ref(expval)
- Locations are created with each binding operation: procedure call, let, and letrec
- What happens when the interpreter encounters a var-exp?
 - env look-up to find the location to which it's bound
 - look-up in the store to find the value at that location
 - two-level system for var-exps

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Parameter Passing Variations

- The content of a location can be changed (or mutated)
- expression \rightarrow set identifier = expression
- the identifier is not an expression; not evaluated
- vars are mutable
- Extend LETREC language and implement call-by-value semantics
- Values are passed to every function
- Formal parameters bound to locations of operand values
- It is the most common form of parameter passing
- Why are chains of references not possible?
- Refs are not expressed values

Language with Explicit References

Language with Implicit References

Mutable Pair

Parameter Passing

Consider

let a = 3
in let p = proc (x) set x = 4
 in begin (p a); a end

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Language with Explicit References

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Mutable Pair

Parameter Passing Consider

let a = 3
in let p = proc (x) set x = 4
in begin (p a); a end



Explicit
References

Language with Implicit References

Mutable Pai

Parameter Passing

```
Consider
let a = 3
in let p = proc (x) set x = 4
in begin (p a); a end
```

Explicit
References

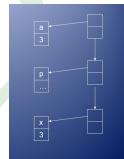
Language with Implicit References

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Parameter Passing

```
• Consider
let a = 3
```

let a = 3
in let p = proc (x) set x = 4
in begin (p a); a end

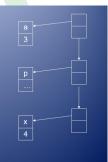


Language with Implicit References

Mutable Pair

Parameter Passing Consider

let a = 3
in let p = proc (x) set x = 4
in begin (p a); a end



• Returns 3

Mutable Pair

Parameter Passing Variations

State Specification

- (value-of (var-expv) ρ σ) = ($\sigma(\rho(v))$, σ)
- Get v's binding (a reference) and access store for v's expval
- The store is unchanged

$$\frac{(\textit{value-of exp1 } \rho \ \sigma_0) = (\textit{val1}, \ \sigma_1)}{(\textit{value-of}(\textit{set-exp } v \ \textit{exp1}) \ \rho \ \sigma_0) = (\varnothing, \ [\sigma(\textit{v}) = \textit{val1}]\sigma_1)}$$

- The location of v is changed to store val1
- The original value stored in $\sigma(v)$ is lost forever
- (apply-procedure (procedure v b ρ) val σ) = (value-of b [v = l] ρ [l = val] σ)
- The body is evaluated in a store where I contains the value of the parameter and an environment that binds the parameter to I
- $\frac{(\textit{value-of exp1 } \rho \ \sigma) = (\textit{val}, \ \sigma_1)}{(\textit{value-of (let-exp var exp1 exp2)} \ \rho \ \sigma) = (\textit{value-of exp2 [var=l]} \rho \ [l = \textit{val}] \sigma_1)}$
- Evaluate the body of the let-exp in a store where I contains the value of the local variable and the local variable is bound to I

Mutable Pair

Parameter Passing

State

- $\frac{(\textit{value-of e0 } \rho \ \sigma_0) = (p, \ \sigma_1) \ \land \ (\textit{value-of e1 } \rho \ \sigma_1) = (v1, \sigma_2) \ \land \ (\textit{value-of e2 } \rho \ \sigma_2) = (v2, \ \sigma_3) \land \ \dots}{(\textit{value-of (call-exp e0 e1...en) } \rho \ \sigma_0) = (\textit{apply-procedure } p \ v1...vn \ \sigma_{n+1})}$
- Evaluate all expressions using the given environment
- Evaluate ei using σ_i
- Apply the proc to the args using the store state after evaluating all expressions
- $\bullet \quad \frac{\rho_n = [n_1 = l_1 \dots n_n = l_n] \rho \ \land \ p1 = (proc val \ n_1 \ p_1 \ e_1 \ \rho_n) \ \land \dots \land \ pn = (proc val \ n_n \ p_n \ e_n \ \rho_n)}{(v o \ (letrec exp \ n_1 \dots n_n \ p_1 \dots p_n \ e_1 \dots e_n \ e_{n+1}) \ \rho \ \sigma) = (v o \ e_{n+1} \ \rho_n \ [l_1 = p1 \dots l_n = pn] \sigma)}$
- v-o = value-of
- All procs are allocated in the store

```
Part IV: State
```

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State

Language wit Explicit References

Language with Implicit References

Mutable Pair

Paramete Passing Variations

State

Implementation

```
(expression
        ("begin" expression (arbno ";" expression) "end")
       begin-exp)
  (expression ("set" identifier "=" expression) set-exp)

    The store is the same as with Explicit Refs

  (define-datatype expval expval?
    (num-val
     (value number?))
    (bool-val
     (boolean boolean?))
    (proc-val
     (proc proc?)))

    Unlike Explicit Refs, no ref-val

    Same as Explicit Refs

  (define (value-of-program pgm)
    (begin
      (initialize-store!)
      (cases program pgm
         (a-program (exp1)
                     (value-of exp1 (empty-env))))))
```

State

Implementation

```
Language w
Explicit
```

Explicit References

Language with Implicit References

Mutable Pair

Parameter Passing Variations

```
(check-equal? (eval "if zero?(1) then 1 else 2")
                (num-val 2))
  (check-equal? (eval "-(15, 10)")
                (num-val 5))
  (check-equal?
    (eval "let x = 10 in if zero?(-(x, x)) then x else 2")
    (num-val 10))
  (check-equal? (eval "let decr = proc (a) -(a, 1) in (decr 30)")
                 (num-val 29))
  (check-equal? (eval "( proc (g) (g 30) proc (y) -(y, 1))")
                (num-val 29))
  (check-equal? (eval "let x = 200
                        in let f = proc(z) - (z, x)
                           in let x = 100
                              in let g = proc(z) - (z, x)
                                 in - ((f 1), (g 1))")
                 (n_{11}m-val -100))
```

Language with Implicit References

Mutable Pain

Parameter Passing

State

```
(check-equal?
    (eval "let sum = proc (x) proc (y) -(x, -(0, y)) in ((sum 3) 4)"
    (num-val 7))
  (check-equal?
    (eval "let sum = proc (x) proc (y) -(x, -(0, y))
           in letrec sigma (n) = if zero?(n)
                                  then 0
                                  else ((sum n) (sigma -(n, 1)))
              in (sigma 5)")
    (num-val 15))
  (check-equal? (eval "letrec even(n) = if zero?(n)
                                         then zero?(n)
                                         else if zero?(-(n, 1))
                                              then zero?(n)
                                              else (even -(n, 2))
                       in (even 501)")
                (bool-val #f))
```

Mutable Pai

Parameter Passing

State

```
• (check-equal? (eval "let a = 3
                        in let p = proc(x) set x = 4
                           in begin
                                (p a);
                              end")
                 (num-val 3))
  (check-equal? (eval "let x = 0
                        in letrec f(x) = set x = +(x, 1)
                                  g(a) = set x = +(x, 2)
                           in begin
                                (f x);
                                (g x);
                                x
                              end")
                 (num-val 2))
```

State

Language wir Explicit References

Language with Implicit References

Mutable Pair

Paramete Passing Variations

State

```
• (define (value-of exp env)
    (cases expression exp
      (const-exp (num) (num-val num))
      (true-exp () (bool-val #t))
      (false-exp () (bool-val #f))
      (var-exp (var) (deref (apply-env env var)))
      (diff-exp (exp1 exp2)
                (let ((num1 (expval2num (value-of exp1 env)))
                       (num2 (expval2num (value-of exp2 env))))
                   (num-val (- num1 num2))))
      (zero?-exp (exp1)
                  (let ((val1 (expval2num (value-of exp1 env))))
                    (if (zero? val1)
                        (bool-val #t)
                        (bool-val #f))))
```

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Language wi Explicit References

Language with Implicit References

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Parameter Passing Variations

State

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```
(if-exp (exp1 exp2 exp3)
    (let ((val1 (value-of exp1 env)))
      (if (expval2bool val1)
          (value-of exp2 env)
          (value-of exp3 env))))
(let-exp (vars exps body)
         (let [(vals (map (lambda (e) (value-of e env)) exps))]
          (value-of body
                    (foldr (lambda (var val acc)
                             (extend-env var (newref val) acc))
                           env
                           vars
                           vals))))
(proc-exp (params body)
          (proc-val (procedure params body (vector env))))
(call-exp (rator rands)
          (let [(proc (expval2proc (value-of rator env)))
                (args (map (lambda (rand) (value-of rand env))
            (apply-procedure proc args)))
```

State

Language with Explicit References

Language with Implicit References

Mutable Pain

Parameter Passing

State

State

Explicit
References

Language with Implicit References

Mutable Pairs

Parameter Passing

State

```
    (define (mk-letrec-env names params bodies env)

    (let* [(temp-proc-vals
              (map (lambda (p b)
                     (proc-val (procedure p b (vector (empty-env)))))
                   params
                   bodies))
           (new-env (foldl (lambda (name proc env)
                              (extend-env name
                                           (newref proc)
                                           env))
                            env
                            names
                            temp-proc-vals))]
      (begin
        (for-each (lambda (p)
                     (cases proc p
                       (procedure (p b ve)
                                   (vector-set! ve 0 new-env))))
                   (map (lambda (p) (expval2proc p))
                        temp-proc-vals))
        new-env)))
```

State

Language with Explicit References

Language with Implicit References

Mutable Pair

Parameter Passing

State Implementation

params
vals)))))))

(map (lambda (p v) (list p v))

State

Language wit Explicit References

Language wit Implicit References

Mutable Pairs

Paramete Passing Variations

- We will add mutable pairs to IMPLICIT-REFS
- expval = int + bool + proc + mutpair
- mutpair = ref(expval) x ref(expval)
- DenVal = ref(expval)
- Specification
 - ightarrow newpair: expval expval ightarrow mutpair
 - ightarrow left: mutpair ightarrow expval
 - ightarrow right: mutpair ightarrow expval
 - \rightarrow setleft: mutpair expval $\rightarrow \varnothing$
 - \rightarrow setright: mutpair expval $\rightarrow \varnothing$
- (define-datatype expval expval?

```
(num-val
  (value number?))
(bool-val
  (boolean boolean?))
(proc-val
  (proc proc?))
(mutpair-val ;; new for mutable pairs
  (p mutpair?)))
```

State

Explicit
References

Language wit Implicit References

Mutable Pairs

Parameter Passing

Grammar

- \rightarrow (expression ("newpair" "(" expression "," expression ")") newpair-exp)
- → (expression ("left" "(" expression ")") left-exp)
- \rightarrow (expression ("setleft" expression "=" expression) setleft-exp)
- → (expression ("right" "(" expression ")") right-exp)
- → (expression ("setright" expression "=" expression) setright-exp)

State

Language w Explicit References

Language wit Implicit References

Mutable Pairs

Parameter Passing · Let's trace

```
(eval "let p = newpair(4, 5)
    in begin
        setleft p = 15;
        setright p = 15;
        -(left(p), right(p))
        end")
```

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Explicit
References

Language wit

Mutable Pairs

Parameter Passing Let's trace

```
(eval "let p = newpair(4, 5)
    in begin
        setleft p = 15;
        setright p = 15;
        -(left(p), right(p))
        end")
```



Part IV: State

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State

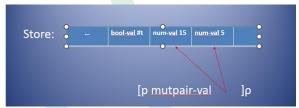
Explicit
References

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Mutable Pairs

Parameter Passing • Let's trace

```
(eval "let p = newpair(4, 5)
    in begin
        setleft p = 15;
        setright p = 15;
        -(left(p), right(p))
        end")
```



State

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Language wit Implicit References

Mutable Pairs

Parameter Passing Variations Let's trace

```
(eval "let p = newpair(4, 5)
    in begin
        setleft p = 15;
        setright p = 15;
        -(left(p), right(p))
        end")
```



• Returns (num-val 0)

Part IV: State

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Language with Implicit References

Mutable Pairs

Parameter Passing Variations • How can we represent a mutable pair?

```
• (define-datatype mutpair mutpair?
(a-pair (left-loc reference?)
(right-loc reference?)))
```

- Is this a good implementation choice?
- Does not take into account everything we know about mutable pairs
 - ightarrow The two locations are independently assignable
 - → Not independently allocated
 - Consider newpair(4, 5) and σ

$$\sigma = (...)
\sigma = (... 4)
\sigma = (... 4 5)$$

- If the left is in position p in σ , where is the right?
- What does this tell you?
- We can implement mutable pairs using a single reference

State

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Mutable Pairs

Parameter Passing Variations

```
• ;; expval --> reference throws error
  (define (expval->mutpair v)
    (cases expval v
      (mutpair-val (ref) ref)
      (else (expval-extractor-error 'mutable-pair v))))
• ;; mutpair? : X -> Boolean
  (define (mutpair? v) (reference? v))
;; make-pair : expval expval -> mutpair
  (define (make-pair val1 val2)
    (let ((ref1 (newref val1)))
      (let ((ref2 (newref val2)))
        ref1)))
;; left : mutpair -> expval
  (define (left p) (deref p))
  ;; right : mutpair -> expval
  (define (right p) (deref (+ 1 p)))
• ;; setleft : mutpair expval -> Unspecified
  (define (setleft p val) (setref! p val))
  ;; setright : mutpair expval -> Unspecified
  (define (setright p val) (setref! (+ 1 p) val))
```

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Mutable Pairs

Parameter Passing Variations

```
(check-equal? (eval "let p = newpair(4, 5)
                     in left(p)")
              (num-val 4))
(check-equal? (eval "let p = newpair(4, 5)
                     in right(p)")
              (num-val 5))
(check-equal? (eval "let p = newpair(4, 5)
                     in begin
                          setleft p = 15;
                          setright p = 15;
                          -(left(p), right(p))
                        end")
              (num-val 0))
```

```
    (define (value-of exp env)

Part IV: State
                     (cases expression exp
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                       (newpair-exp (exp1 exp2)
                         (let ((v1 (value-of exp1 env))
                                (v2 (value-of exp2 env)))
                            (mutpair-val (make-pair v1 v2))))
                       (left-exp (exp1)
                         (let ((v1 (value-of exp1 env)))
                            (let ((p1 (expval->mutpair v1)))
                              (left p1))))
Mutable Pairs
                       (right-exp (exp1)
                         (let ((v1 (value-of exp1 env)))
                            (let ((p1 (expval->mutpair v1)))
                              (right p1))))
                       (setleft-exp (exp1 exp2)
                         (let ((v1 (value-of exp1 env))
                                (v2 (value-of exp2 env)))
                            (let ((p (expval->mutpair v1)))
                              (begin (setleft p v2)
                                     (num-val 82))))); this is a don't care value.
                       (setright-exp (exp1 exp2)
                         (let ((v1 (value-of exp1 env))
                                (v2 (value-of exp2 env)))
                            (let ((p (expval->mutpair v1)))
                              (begin (setright p v2)
                                     (num-val 83))))) ;; this is a don't care value.
```

Part IV: State

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State

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Language wit Implicit References

Mutable Pairs

Parameter Passing • Homework: 4.28–4.30

Language wit Implicit References

Mutable Pain

Parameter Passing Variations

Parameter Passing Variations

- In call-by-value semantics the callee is isolated from the caller
- Assignments by the callee to its parameters can not be seen by the caller
- Sometimes it is desirable to pass in variables expecting the callee to make assignments to them
- This can be done by passing references to the callee instead of actual values
- This is known as call-by-reference
- If an operand is a variable, then a reference to the variable's location is passed
- The formal parameter is bound to this location
- If the operand is some other type of expression, then the formal parameter is bound to a new location containing the value of the operand
- Just like in call-by-value

c. .

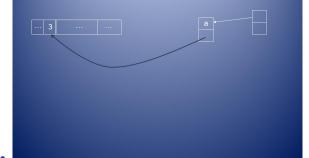
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Language with Implicit

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

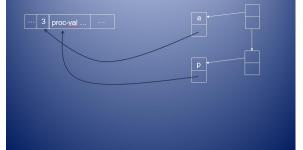


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Parameter Passing Variations

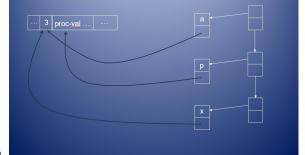


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Parameter Passing Variations

Parameter Passing Variations



Language wit Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

Call by Reference

```
let a = 3
p = proc(x) set x = 4
in begin
    (p a);
    a
   end
               proc-val ... ···
```

Returns 4

Language with Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations Call by Reference

- Why use call-by-reference?
 - → Return multiple values (by making assignments to parameters)
 - → Implementation of common operations

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Mutable Pair

Parameter Passing Variations

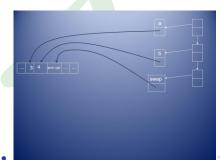
Parameter Passing Variations

Call by Reference

Call-by-Value

end

```
let a = 3
b = 4
    swap = proc (x, y)
    let temp = x
    in begin
        set x = y
        set y = temp
    end
in begin
    swap(a b)
    -(a, b)
```



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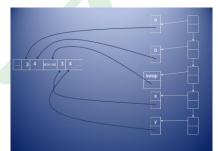
Parameter Passing Variations

Parameter Passing Variations

Call by Reference

Call-by-Value

```
let a = 3
    b = 4
    swap = proc (x, y)
        let temp = x
        in begin
            set x = y
            set y = temp
    end
in begin
    swap(a b)
    -(a, b)
    end
```



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Mutable Pairs

Parameter Passing Variations

Parameter Passing Variations

Call by Reference

Call-by-Value

end

```
let a = 3
    b = 4
    swap = proc (x, y)
    let temp = x
    in begin
        set x = y
        set y = temp
    end
in begin
    swap(a b)
    -(a, b)
```



Explicit References

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Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

Call by Reference

Call-by-Value

```
let a = 3
    b = 4
    swap = proc (x, y)
    let temp = x
    in begin
        set x = y
        set y = temp
    end
in begin
    swap(a b)
    -(a, b)
end
```



Language with Implicit References

Mutable Pairs

Parameter Passing Variations

Parameter Passing Variations

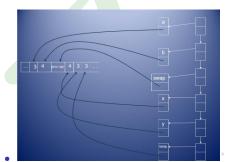
Call by Reference

Call-by-Value

end

```
let a = 3
    b = 4
    swap = proc (x, y)
        let temp = x
        in begin
        set x = y
        set y = temp
    end
in begin
    swap(a b)
    -(a, b)
```

Returns -1



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Mutable Pairs

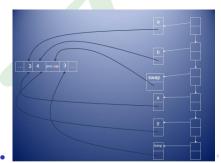
Parameter Passing Variations

Parameter Passing Variations

Call by Reference

Call-by-Reference

```
let a = 3
    b = 4
    swap = proc (x, y)
        let temp = x
        in begin
        set x = y
        set y = temp
    end
in begin
    swap(a b)
    -(a, b)
end
```



State

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Language with Implicit References

Mutable Pairs

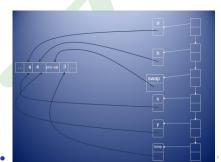
Parameter Passing Variations

Parameter Passing Variations

Call by Reference

Call-by-Reference

```
let a = 3
    b = 4
    swap = proc (x, y)
    let temp = x
    in begin
    set x = y
    set y = temp
end
in begin
    swap(a b)
    -(a, b)
end
```



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Parameter Passing Variations

Parameter Passing Variations

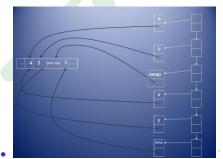
Call by Reference

Call-by-Reference

end

```
let a = 3
    b = 4
    swap = proc (x, y)
        let temp = x
        in begin
        set x = y
        set y = temp
    end
in begin
    swap(a b)
    -(a, b)
```

Returns 1



Language with Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- Only change is for when new references are created:
 - ightarrow call-by-value: a new reference is created for every operand evaluated
 - $\rightarrow\,$ call-by-reference: a new reference is created for evaluation of an operand other than a variable
- Under call-by-reference we need a new location for some operands and not for others

```
Part IV: State
```

CLARA

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Parameter Passing Variations

Parameter Passing Variations

Call by Reference

```
• ;; apply-procedure : proc (listof expval) -> expval
  (define (apply-procedure f vals)
    (cases proc f
      (procedure (params body envv)
        (let [(saved-env (vector-ref envv 0))]
          (value-of body
            (foldr (lambda (binding acc)
                      (extend-env (car binding)
                                  (newref (cadr binding))
                                  acc))
                   saved-env
                   (map (lambda (p v) (list p v)) params vals))))))
  Can't always allocate an argument in the store
• ;; apply-procedure : proc (listof ref) -> expval
  (define (apply-procedure f vals)
   (cases proc f
    (procedure (params body envv)
     (let [(saved-env (vector-ref envv 0))]
      (value-of body
               (foldr (lambda (binding acc)
                        (extend-env (car binding) (cadr binding) acc)
                       saved-env
                        (map (lambda (p v) (list p v)) params vals)));
```

Decision made in the evaluation of a call-exp

In value-of

Language with Implicit References

Mutable Pairs

Parameter Passing Variations

Parameter Passing Variations

```
(call-exp (rator rands)
    (let [(proc (expval2proc (value-of rator env)))
          (args (map (lambda (rand) (value-of rand env)) rands))]
      (apply-procedure proc args)))
  apply-procedure must be called with a (listof ref)

    (call-exp (rator rands)

    (let [(proc (expval2proc (value-of rator env)))
          (args (map (lambda (rand) (value-of-rand rand env)) rands)
      (apply-procedure proc args)))
  value-of-rand returns a reference
• ;; value-of-rand : expression environment -> Ref
  ;; Purpose: For a var-exp return existing reference.
              Otherwise, return reference to a new cell.
  (define (value-of-rand exp env)
    (cases expression exp
      (var-exp (var) (apply-env env var))
      (else (newref (value-of exp env)))))
```

Mutable Pairs

Parameter Passing Variations

Parameter Passing Variations

Call by Reference

```
(check-equal? (eval "let a = 3
                     in let p = proc(x) set x = 4
                        in begin (p a); a end")
              (num-val 4))
(check-equal? (eval "let x = 0
                     in letrec f (x) = set x = +(x, 1)
                               g(a) = set x = +(x, 2)
                        in begin (f x);
                                  (g x);
                                 x
                           end")
              (num-val 3))
(check-equal?
 (eval "let swap = proc (a)
                    proc (b)
                      let t = a
                      in begin set a = b; set b = t end
        in let a = 33
           in let b = 44
              in begin ((swap a) b);
                       -(a, b)
                 end")
 (num-val 11))
```

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- Call-by-value and call-by-reference are eager
- Always find the value of each operand
- Lazy evaluation
- Operands not evaluated until needed
- ullet Never needed ightarrow never evaluated
- Is this useful?

Mutable Pain

Parameter Passing Variations

Parameter Passing Variations

Lazy Evaluation: Call by Name

```
• letrec compute-ints-from-n (n) = (compute-ints-from-n +(n, 1))
in let f = proc (k) 42
in (f (compute-ints-from-n 100))
```

- What should this program return?
- It should return 42, but does not. Why?
- Under lazy evaluation this program returns 42
 - #lang eopl (require rackunit "../eopl-extras.rkt") (define (ints-from n) (stream-cons n (ints-from (+ n 1)))) (define natnums (ints-from 0)) (define (nth-natnum n) (stream-ref natnums n)) (define (first-n-natnums n) (if (= n 0))(list (nth-natnum 0)) (cons (nth-natnum n) (first-n-natnums (- n 1))))) (check-equal? (first-n-natnums 10) '(10 9 8 7 6 5 4 3 2 1 0)) (check-equal? (first-n-natnums 15) '(15 14 13 12 11 10 9 8 7 6 5 4 3 2 1 0))

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Parameter Passing Variations

Parameter Passing Variations

```
#lang eopl
  (require rackunit "../eopl-extras.rkt")
  :: natnum --> natnum
  ;; Purpose: Return the kth Fibonacci number
  (define (fib k)
    (if (< k 2))
        (+ (fib (- k 1)) (fib (- k 2)))))
  (define (the-fibs n) (stream-cons (fib n) (the-fibs (+ n 1))))
  (define fibs (the-fibs 0))
  (define (nth-fib n) (stream-ref fibs n))
  (check-equal? (nth-fib 5) 8)
  (check-equal? (nth-fib 10) 89)
  (define the-doubles (stream-map (\lambda (n) (* 2 n)) natnums))
  (check-equal? (stream-ref the-doubles 10) 20)
  (check-equal? (stream-ref the-doubles 1287) 2574)
```

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State

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Parameter Passing Variations

Parameter Passing Variations

- An operand is not evaluated until needed
- A bound var is associated with unevaluated expression (frozen)
- When the value of the bound var is needed, then the expression is evaluated (thawed)
- What does this require?
- The env that exists when the expr is frozen
- (define-datatype thunk thunk? (a-thunk (exp1 expression?)
 (env environment?))
- The expr in a thunk is evaluated when a proc needs the value of bound var

Mutable Pai

Parameter Passing Variations

Parameter Passing Variations

- Language
 - \rightarrow let remains eager
 - → lazy evaluation of arguments
 - \rightarrow effects
- Values
 - \rightarrow expval = int + bool + proc
 - \rightarrow denval = ref(expval + thunk)
- New allocations policy
 - → var: pass its denotation (which is a reference; same as call-by-reference)
 - ightarrow not var: pass a ref to a new location storing a thunk for the unevaluated arg

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CLALA

Language with Explicit

Language wit Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

```
• ;; value-of-rand : expression environment -> Ref
;; Purpose: if the expression is a var-exp, then return the reference; otherwise, return a thunk for the given expression.

(define (value-of-rand exp env)

(cases expression exp

(var-exp (var) (apply-env env var))

(else

(newref (a-thunk exp env))))) ← not a var-exp create thunk
```

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Parameter Passing Variations

Parameter Passing Variations

- How do you evaluate a var-expr?
- $\frac{w = deref(\rho(v))}{(value-of (var-expv) \rho) = if (expval? w) then w else (value-of-thunk w)}$
- change to value-of

```
(var-exp (var)
  (let ((ref1 (apply-env env var)))
    (let ((w (deref ref1)))
        (if (expval? w)
        w
  (value-of-thunk w))))
```

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Parameter Passing Variations

Lazy Evaluation: Call by Name

Evaluating a thunk

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Parameter Passing Variations

Lazy Evaluation: Call by Name

Consider

- x is the thunk for (g 0)
- the first x forces the evaluation of the thunk \rightarrow 20
- the second x forces the evaluation of the thunk \rightarrow 20
- returns 40

Language wit

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Parameter Passing Variations

Parameter Passing Variations

- Evaluating the same thunk seems wasteful
- Solution: Evaluate it once and mutate it for its value
- Change in value-of

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

```
• let g = let counter = 10
in proc (d) *(2, counter)
in (proc (x) +(x, x) (g 0))
```

- x is the thunk for (g 0)
- the first x forces the evaluation of the thunk to 20
- mutates x to 20
- the second x (simply) returns its value of 20
- returns 40

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Language with Explicit References

Language with Implicit References

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- In the absence of side-effects, call-by-name and call-by-need always yield the same answer
- In the presence of side-effects, it is easy to distinguish them

- g returns the number of times it is called
- Thunk for (g 0) is passed as the argument to the function in the body of the let
- call-by-name
- the first reference to x: sets count to 1 & returns 1 as the value of (g 0)
- the second reference to x: sets count to 2 & returns 2 as the value of (g 0)
- +(1, 2) = 3
- · call-by-need
- the first reference to x forces: sets count to 1, returns 1 as the value of (g
 0), and stores 1 as the value of (g
 0)
- second reference to x: returns the stored 1
- +(1, 1) = 2



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Parameter Passing Variations

Parameter Passing Variations

- Lazy evaluation: in the absence of side-effects allows for a simple way to reason about programs
- The effect of a procedure call is modeled by:
 - → Replacing the call with the body of the procedure
 - $\rightarrow\,$ Every reference to a parameter in the body is replaced by the corresponding operand
 - $\rightarrow\,$ This evaluation strategy is the basis of the lambda calculus and is known as $\beta\text{-reduction}$
- β -reduction: $\lambda(x.e)x0 \rightarrow e\{x0/x\}$

```
\lambda(x.+(x, *(2, x)) - (5, -10))

\rightarrow +(-(5, -10) *(2, -(5, -10)))

\rightarrow +(15, *(2, -(5, -10)))

\rightarrow +(15, *(2, 15))

\rightarrow +(15, 30)

\rightarrow 45
```

Mutable Pair

Parameter Passing Variations

Parameter Passing Variations

- All the freezing and thawing can lead to considerable overhead
- Reducing the number of thunks created is important for efficiency
- Difficult to determine the order of evaluation which is essential for programs with side-effects
- You do not have to think operationally: you can reason equationally about your programs.—S. Doaitse Swierstra
- I prefer call by value to call by name because it is more predictable.—Mitchell Wand
- Popular with pure functional languages (i.e. with no side-effects) and rarely found elsewhere
- Haskell and Clean
- C# (deferred execution)

References

Language w

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Parameter Passing Variations

Parameter Passing Variations

• HOMEWORK: 4.31, 4.32, 4.39, 4.40, 4.42