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Continuation Passing Interpreter

A Trampoline Interpreter

An Imperativ

Exception

Thread:

# Part V: Continuation-Passing Interpreters

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Continuatio Passing Interpreter

Trampoline Interpreter

Interpreter

Eventions

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#### Continuation-Passing Interpreter

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- Environments establish the context in which each portion of a program is evaluated
- We shall now study the control context
- The control context dictates how a computation proceeds
- Think of a computation as divided in two parts
  - the evaluation of a function call for the value of an argument
  - the rest of the computation that uses the result obtained
- The control context is made explicit (just as environments)
- A continuation is an abstraction for the control context
- A continuation knows how to finish a computation after an intermediate value is computed
- We say that a continuation is applied to an intermediate value to finish the computation

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### Continuation-Passing Interpreters

Consider:

```
(define (add a b)
(if (= b 0)
a
    (+ 1 (add a (- b 1)))))
```

• Trace (add 3 3):

```
= (+ 1 (add 3 2))
= (+ 1 (+ 1 (add 3 1)))
= (+ 1 (+ 1 (+ 1 (add 3 0))))
```

- = (+ 1 (+ 1 (+ 1 3)))
- = (+ 1 (+ 1 4))
- = (+ 1 5)
- = 6
- Each recursive call comes with the promise that its result will be added to one (this is control: finish the recursive call then come back to add 1)
- The control context grows with every function call (i.e., more promises to remember)

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## Continuation-Passing Interpreters

Consider:

- Add iter is always invoked in the same control context
- Call at the tail-end means no promises to do anything (no need to return and do anything)
- No need to remember what to do with the result
- Only a constant amount of memory is needed regardless of the number of (recursive) calls: memory for a and for b

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```
(define (add a b)

(if (= b 0)

a

(+ 1 (add a (- b 1)))))
```

- Function is called in an operand position
- Requires remembering the context to finish evaluating the outer call later (i.e., add the 1)
- IT IS THE EVALUATION OF OPERANDS, NOT CALLING PROCEDURES, THAT REQUIRES THE CONTROL CONTEXT TO GROW

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- Goal: Learn to track and manipulate control contexts
- Continuations
  - An abstraction for th control context notion
  - Our interpreter will explicitly pass a continuation (i.e., do this when operand is evaluated)
  - Represents a procedure that takes the result of an operand expression and completes the computation
  - A continuation is a function!
  - We will need the ability, therefore, to apply continuations to values
- ;; apply-cont: continuation value → expval
   ;; Purpose: To apply the given continuation to the
   ;; given value and return the final answer
- A value may be anything that is computed by the program or that is computed to evaluate the program
- We shall discover the needed continuation constructors as we analyze the LETREC language interpreter

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### Continuation-Passing Interpreters

```
• ;; value-of-program : program → expval (define (value-of-program pgm) (cases program pgm (a-program (exp1) (value-of/k exp1 (init-env)))))
```

- The value of exp1 must be evaluated. What needs to be done with its value?
- We need a continuation that simply returns the value it is applied to

Semantics:

```
(apply-cont (end-cont) val)
```

= (begin (display "End of computation.\n") val)

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-----

```
    ;; value-of: expression environment → expval
(define (value-of exp env)
(cases expression exp
    (const-exp (num) (num-val num))
```

```
    The computation ends by returning a value
```

- In continuation-passing style, the continuation must finish the computation
- ;; expression environment continuation o expval

```
(define (value-of/k exp env k)
(cases expression exp
```

```
(const-exp (num) (apply-cont k (num-val num)))
```

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```
ullet ;; value-of : expression environment 	o expval
  (define (value-of exp env)
    (cases expression exp
      (true-exp () (bool-val #t))
      (false-exp () (bool-val #f))
```

- The computation ends by returning a value
- In continuation-passing style, the continuation must finish the computation
- ;; expression environment continuation  $\rightarrow$  expval (define (value-of/k exp env k) (cases expression exp

```
(true-exp () (apply-cont k (bool-val #t)))
(false-exp () (apply-cont k (bool-val #f)))
```

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```
    ;; value-of: expression environment → expval
(define (value-of exp env)
(cases expression exp
    (var-exp (var) (apply-env env var))
```

- The computation ends by returning a value
- In continuation-passing style, the continuation must finish the computation
- ;; expression environment continuation → expval (define (value-of/k exp env k) (cases expression exp

```
(var-exp (var) (apply-cont k (apply-env env var)))
```

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- The computation ends by returning a value
- In continuation-passing style, the continuation must finish the computation
- ;; expression environment continuation → expval (define (value-of/k exp env k) (cases expression exp

```
(proc-exp (params body)
  (apply-cont k (proc-val (procedure params body (vector env)))))
```

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- There is one non-tail call: evaluate exp1
- In continuation-passing style, the continuation must finish the computation
- ;; expression environment continuation → expval (define (value-of/k exp env k) (cases expression exp

- Save the given continuation, k, to use after value of exp1 is known to finish the computation
- Semantics

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### Continuation-Passing Interpreters

- There is one non-tail call: evaluate exp1
- To finish the computation exp2, exp3, and env must be remembered
- Since a concrete value is not returned, the continuation must be remembered to be used after evaluating exp2 or exp3
- ;; expression environment continuation  $\rightarrow$  expval (define (value-of/k exp env k) (cases expression exp

Semantics

```
(apply-cont (if-cont (exp2 exp3 env saved-cont) val)
= (if (expval2bool val)
    (value-of/k exp2 env saved-cont)
    (value-of/k exp3 env saved-cont)))
```

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### Continuation-Passing Interpreters

 ;; value-of: expression environment → expval (define (value-of exp env) (cases expression exp

```
(letrec-exp (names params bodies letrec-body)
  (value-of letrec-body (mk-letrec-env names params bodies env)))
```

- There is one non-tail call: Create a letrec-env
- To finish the computation letrec-body must be remembered to evaluate it after the environment is computed
- Since a concrete value is not returned, the continuation must be remembered to be used after evaluating letrec-body
- ;; expression environment continuation → expval (define (value-of/k exp env k) (cases expression exp

```
(letrec-exp (names params bodies letrec-body)
  (mk-letrec-env/k names params bodies env (letrec-cont letrec-body)
```

Semantics

```
(apply-cont (letrec-cont letrec-body saved-cont) val)
```

= (value-of/k letrec-body val saved-cont))

```
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```

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### Continuation-Passing Interpreters

- There are two non-tail calls: map and foldr
- To finish the computation body, vars, and env must be remembered
- The continuation remembered to use after evaluating body
- Save the given continuation, k, to use after value of body is known to finish the computation
  - Semantics

```
(apply-cont (let1-cont (vars body env saved-cont)) val)
= (create-let-lenv vars val env (let2-cont body saved-cont))
```

```
(apply-cont (let2-cont (body saved-cont)) val)
```

= (value-of/k body val saved-cont)



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### Continuation-Passing Interpreters

- There are two non-tail function calls evaluate exp1 and evaluate exp2
- To finish the computation after evaluating exp1, the value of exp2 and env must be remembered
- Since a concrete value is not returned, the continuation must be remembered to be used after evaluating exp1
- A continuation is needed to finish the computation when exp2 is evaluated
- Must remember the value of exp1 and the continuation to use after exp2 is evaluated

Semantics

```
(diff-cont1 (exp2 env saved-cont)
= (value-of/k exp2 env (diff-cont2 val saved-cont)))
(diff-cont2 (val1 saved-cont)
= (apply-cont saved-cont (num-val (- (expval2num val1)))
```

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### Continuation-Passing Interpreters

- There are two non-tail function calls:
  - Evaluate rator
  - Evaluate rands
- To finish the computation after evaluating rator, the value of rands and env must be remembered
- Since a concrete value is not returned, the continuation must be remembered to be used after evaluating rator
- (rator-cont (rands env saved-cont)
- (eval-rands/k rands env (rands-cont val saved-cont))
   The continuation is needed to finish computation after rands are evaluated
  - The continuation is needed to limish computation after rands a
- Must remember rator value to use after rands is evaluated
- Semantics

```
(rator-cont (rands env saved-cont)
```

= (eval-rands/k rands env (rands-cont val saved-cont)))

```
(rands-cont (rator saved-cont)
```

= (apply-procedure/k (expval2proc rator) val saved-cont)) = 🗸 🗸 🔾

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```
;; proc (listof expval) continuation \rightarrow expval
;; Purpose: Apply the given procedure to the given values
(define (apply-procedure/k f vals k)
  (cases proc f
    (procedure (params body envv)
                (let [(saved-env (vector-ref envv 0))]
                  (value-of/k body
                              (foldr (lambda (binding acc)
                                        (extend-env (car binding)
                                                     (cadr binding)
                                                     acc))
                                      saved-env
                                      (map (lambda (p v) (list p v))
                                           params
                                           vals))
                              k)))))
```

- Continuation input for call to value-of
- Create new env to evaluate the body assuming foldr and map do not grow the control context

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```
;; (listof symbol) (listof (listof symbol)) (listof expression)
:: environment
                   continuation
:: → environment
;; Purpose: Add the proc-vals for the given procedures in the given environment
(define (mk-letrec-env/k names params bodies env k)
 (let* [(temp-proc-vals (map (lambda (p b)
                                (proc-val (procedure p b (vector (empty-env)))))
                              params
                              bodies))
         (new-env (foldl (lambda (name proc env) (extend-env name proc env))
                         env
                         names
                         temp-proc-vals))]
    (begin
      (for-each (lambda (p)
                  (cases proc p
                    (procedure (p b ve) (vector-set! ve 0 new-env))))
                (map (lambda (p) (expval2proc p)) temp-proc-vals))
      (apply-cont k new-env))))
```

- Temporarily create incorrect proc-vals for the locally defined recursive functions assuming map does not grow the control context.
- Createa new env by adding incorrect procs to the given environment
- Correct the environment in each incorrect proc
- Finish the computation by applying the continuation to the correct new env

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- Two steps: evaluate the first argument and evaluate the rest of the arguments
- Evaluate the first argument using a continuation that evaluates the rest of the arguments
- If there are no more arguments to evaluate apply the given continuation to the empty list of evaluated arguments

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- Accumulate new bindings in the given environment
- If no more bindings to add, apply continuation to the given environment that stores all the bindings
- No new continuations are needed: all function calls in tail-position

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```
(define-datatype continuation cont?
  (end-cont)
  (zero?-cont (k cont?))
  (letrec-cont (letrec-body expression?)
               (saved-cont cont?))
  (let1-cont (vrs (list-of symbol?))
             (b expression?)
             (e environment?)
             (k cont?))
  (let2-cont (b expression?)
             (k cont?))
  (if-cont (e2 expression?)
           (e3 expression?)
           (e environment?)
           (k cont?))
  (diff-cont1 (e2 expression?)
              (e environment?)
              (k cont?))
  (diff-cont2 (v1 expval?)
              (k cont?))
  (rator-cont (rnds (list-of expression?))
              (e environment?)
              (k cont?))
  (rands-cont (operator expval?)
              (k cont?))
  (eval-rands-cont1 (rands (list-of expression?))
                     (e environment?)
                     (k cont?))
  (eval-rands-cont2 (farg expval?)
                     (k cont?)))
```

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### Continuation-Passing Interpreters

**Auxiliary Functions** 

```
    ;; continuation expval → expval

  ;; Purpose: Apply the given cont to the given value and return
              the final answer
  ;;
  (define (apply-cont k val)
   (cases continuation k
     (end-cont () val)
     (zero?-cont (cont)
       (if (zero? (expval2num val))
                   (apply-cont cont (bool-val #t))
                   (apply-cont cont (bool-val #f))))
     (let1-cont (vars body env saved-cont)
      (create-let-lenv vars val env (let2-cont body saved-cont)))
     (let2-cont (body saved-cont)
       (value-of/k body val saved-cont))
     (if-cont (exp2 exp3 env saved-cont)
       (if (expval2bool val)
           (value-of/k exp2 env saved-cont)
           (value-of/k exp3 env saved-cont)))
```

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### Continuation-Passing Interpreters

### **Auxiliary Functions**

```
    ;; continuation expval → expval

  ;; Purpose: Apply the given cont to the given value and return the
  (define (apply-cont k val)
    (cases continuation k
      (letrec-cont (letrec-body saved-cont)
       (value-of/k letrec-body val saved-cont))
      (diff-cont1 (exp2 env saved-cont)
       (value-of/k exp2 env (diff-cont2 val saved-cont)))
      (diff-cont2 (val1 saved-cont)
       (apply-cont saved-cont (num-val (- (expval2num val1)
                                           (expval2num val)))))
      (rator-cont (rands env saved-cont)
       (eval-rands/k rands env (rands-cont val saved-cont)))
      (rands-cont (rator saved-cont)
       (apply-procedure/k (expval2proc rator) val saved-cont))
      (eval-rands-cont1 (rands env saved-cont)
       (eval-rands/k rands env (eval-rands-cont2 val saved-cont)))
      (eval-rands-cont2 (first-rand k)
       (apply-cont k (cons first-rand val)))))
```

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Eventions

Thread:

- add sum-exp and mult-exp to the interpreter
- **5**.4, **5.9\*\***

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Exception

- We know will explore how to transform a continuation-passing interpreter to a regular PL
- By regular we mean no HOF
- Can use data structure representation of continutations
- More problematic:
  - Most PLs <u>always</u> grow the control context with every procedure call
  - Control context is usually a stack (that always grows with every procedure call)
- Why do most PLs always grow the control context?
- Almost all procedure calls occur at the RHS of an assignment statement: x = f(...)
  - The assignment is a delayed operation and requires growing the control context to track its pending excution
  - Environment info is also placed on the stack & removed

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Exceptions

- One solution for such languages is trampolining
- Break an unbounded chain of proc calls by having one of the procedures in the interpreter return a zero-argument proc
- When called, this proc continues the computation
- The computation bounces from one procedure call to the next
- This is controlled by a trampoline procedure
- What procedure calls?
- Those that are steps in the evaluator: value-of/k, apply-cont, apply-procedure/k, eval-rands/k, and mk-letrec-env/k
- Instead of calling one of them (and grow the control context), make calls to these functions the body of a zero-argument function that is given to the trampoline function

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```
· Let illustrate how this works
```

(trampoline (value-of-program (value-of/k -(3, 1) (empty-env) (end-cont))))

- = (trampoline (lambda () (value-of/k 3 (diff1-cont 1 (empty-env) (end-cont)))))
- = (trampoline (value-of/k 3 (diff1-cont 1 (empty-env) (end-cont))))
- = (trampoline (lambda () (apply-cont (diff1-cont 1 (empty-env) (end-cont)) 3)))
- = (trampoline (apply-cont (diff1-cont 1 (empty-env) (end-cont)) 3))
- = (trampoline (lambda () (value-of/k 1 (empty-env) (diff-cont2 3 (end-cont)))))
- = (trampoline (value-of/k 1 (empty-env) (diff-cont2 3 (end-cont))))
- = (trampoline (lambda () (apply-cont (diff-cont2 3 (end-cont)) 1)))
- = (trampoline (apply-cont (diff-cont2 3 (end-cont)) 1))
- = (trampoline (lambda () (apply-cont (end-cont) 2)))
- = (trampoline (apply-cont (end-cont) 2))
- = (trampoline (lambda () 2))
- = (trampoline 2)
- = :

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Exception

• Trampoline input value:

A bounce is either:

- 1. expval
- 2. A zero-input function
- Specification:
  - If input is an expval then return it (computation is done)
  - If input is a zero-input function then evaluate and call the trampoline
- Trampoline implementation:

```
;; trampoline : bounce → expval
(define (trampoline a-bounce)
    (if (expval? a-bounce)
        a-bounce
        (trampoline (a-bounce))))
```

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 Wrap every call to value-of/k, apply-cont, apply-procedure/k, eval-rands/k, and mk-letrec-env/k inside a lambda-expression and call trampoline

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Exception

- Wrap every call to value-of/k, apply-cont, apply-procedure/k, eval-rands/k, and mk-letrec-env/k inside a lambda-expression and call trampoline
- ;; proc (listof expval) continuation -> bounce ;; Purpose: Apply the given procedure to the given values (define (apply-procedure/k f vals k) (cases proc f (procedure (params body envv) (let [(saved-env (vector-ref envv 0))] (trampoline (lambda () (value-of/k body (foldr (lambda (binding acc) (extend-env (car binding) (cadr binding) acc)) saved-env (map (lambda (p v) (list p v)) params vals)) k)))))))

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Exceptions

- Wrap every call to value-of/k, apply-cont, apply-procedure/k, eval-rands/k, and mk-letrec-env/k inside a lambda-expression and call trampoline
- ;; (listof expression) environment continuation --> expval ;; Purpose: Evaluate the given list of exprs and apply the given condition (define (eval-rands/k rands env k) (if (null? rands) (trampoline (lambda () (apply-cont k '()))) (trampoline (lambda () (value-of/k (car rands) env (eval-rands-cont1 (cdr rands) env k))))))

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Exceptions

- Wrap every call to value-of/k, apply-cont, apply-procedure/k, eval-rands/k, and mk-letrec-env/k inside a lambda-expression and call trampoline

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Exceptions

- Wrap every call to value-of/k, apply-cont, apply-procedure/k, eval-rands/k, and mk-letrec-env/k inside a lambda-expression and call trampoline
- ;; (listof symbol) (listof (listof symbol)) (listof expression) environment continuation ;; Purpose: Add the proc-vals for the given procedures in the given environment (define (mk-letrec-env/k names params bodies env k) (let\* [(temp-proc-vals (map (lambda (p b) (proc-val (procedure p b (vector (empty-env))))) params bodies)) (new-env (foldl (lambda (name proc env) (extend-env name proc env)) env names temp-proc-vals))] (begin (for-each (lambda (p) (cases proc p (procedure (p b ve) (vector-set! ve 0 new-env)))) (map (lambda (p) (expval2proc p)) temp-proc-vals)) (trampoline (lambda () (apply-cont k new-eny))))))

```
    Wrap every call to value-of/k, apply-cont, apply-procedure/k, eval-rands/k, and

   Part V:
                         mk-letrec-env/k inside a lambda-expression and call trampoline
Continuation-
                      • ;; expression environment continuation -> bounce
   Passing
                         (define (value-of/k exp env k)
 Interpreters
                           (cases expression exp
                             (const-exp (num) (trampoline (lambda () (apply-cont k (num-val num)))))
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                             (true-exp () (trampoline (lambda () (apply-cont k (bool-val #t)))))
                             (false-exp () (trampoline (lambda () (apply-cont k (bool-val #f)))))
                             (var-exp (var) (trampoline (lambda () (apply-cont k (apply-env env var)))))
                             (proc-exp (params body)
                                       (trampoline
Trampolined
                                        (lambda ()
Interpreter
                                           (apply-cont k (proc-val (procedure params body (vector env))))))
                             (zero?-exp (exp1)
                                        (trampoline (lambda () (value-of/k exp1 env (zero?-cont k)))))
                             (diff-exp (exp1 exp2)
                                       (trampoline
                                        (lambda () (value-of/k exp1 env (diff-cont1 exp2 env k)))))
                             (if-exp (exp1 exp2 exp3)
                                      (trampoline
                                      (lambda () (value-of/k exp1 env (if-cont exp2 exp3 env k)))))
                             (let-exp (vars exps body)
                                      (trampoline
                                       (lambda () (eval-rands/k exps env (let1-cont vars body env k)))))
                             (call-exp (rator rands)
                                       (trampoline
                                        (lambda () (value-of/k rator env (rator-cont rands env k)))))
                             (letrec-exp (names params bodies letrec-body)
                                          (trampoline
                                           (lambda ()
                                             (mk-letrec-env/k names params bodies env (letrec-cont letrec-body k)))
```

Part V: Continuation-Passing Interpreters

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```
• ;; continuation expval --> bounce
   :: Purpose: Apply the given cont to the given value and return the final answer
   (define (apply-cont k val)
    (cases continuation k
       (end-cont () (trampoline (lambda () val)))
      (zero?-cont (cont)
       (if (zero? (expval2num val))
            (trampoline (lambda () (apply-cont cont (bool-val #t))))
            (trampoline (lambda () (apply-cont cont (bool-val #f))))))
       (let1-cont (vars body env saved-cont)
       (trampoline
         (lambda () (create-let-lenv vars val env (let2-cont body saved-cont)))))
       (let2-cont (body saved-cont)
        (trampoline (lambda () (value-of/k body val saved-cont))))
      (if-cont (exp2 exp3 env saved-cont)
       (if (expval2bool val)
            (trampoline (lambda () (value-of/k exp2 env saved-cont)))
            (trampoline (lambda () (value-of/k exp3 env saved-cont)))))
       (letrec-cont (letrec-body saved-cont)
        (trampoline (lambda () (value-of/k letrec-body val saved-cont))))
       (diff-cont1 (exp2 env saved-cont)
        (trampoline (lambda () (value-of/k exp2 env (diff-cont2 val saved-cont)))))
       (diff-cont2 (val1 saved-cont)
        (trampoline
         (lambda () (apply-cont saved-cont (num-val (- (expval2num val1) (expval2num val))))
       (rator-cont (rands env saved-cont)
        (trampoline
         (lambda () (eval-rands/k rands env (rands-cont val saved-cont)))))
       (rands-cont (rator saved-cont)
        (trampoline
         (lambda () (apply-procedure/k (expval2proc rator) val saved-cont))))
       (eval-rands-cont1 (rands env saved-cont)
        (trampoline
         (lambda () (eval-rands/k rands env (eval-rands-cont2 val saved-cont)))))
       (eval-rands-cont2 (first-rand k)
        (trampoline (lambda () (apply-cont k (cons first-rand val))))))
                                                   4 D > 4 A > 4 B > 4 B > B 9 9 9 9
```

Continuation Passing Interpreter

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Exceptions

- How do we implement a continuation-passing interpreter in procedural languages with assignment?
- Remember that assignment to shared variables may be used in place of a binding

```
Consider
   Part V:
                          letrec
Continuation-
   Passing
                            odd(x)
 Interpreters
                          in (odd 10)
  Marco T.
                          Trace
  Morazán
                          (odd 10)
                          = (even 9)
                             (odd
                             (even 7)
                             (odd
                            (even 5)
                             (even 1)
An Imperative
```

Interpreter

Exception

```
even(x) = if zero?(x) then 1 else (odd sub1(x))
           = if zero?(x) then 0 else (even sub1(x))
   (odd
          0)
Make x a shared variable
let x = 10
in letrec
       even() = if zero?(x) then 1 else let d = set x = sub1(x) in (odd)
       odd()
              = if zero?(x) then 0 else let d = set x = sub1(x) in (even)
in (odd)
The trace is the same!
(odd )
 (even)
 (bbo)
   (even)
   (odd)
   (even)
   (even)
   (odd)
```

An Imperative Interpreter

This means we can rewrite as in assembly using GOTOs and labels

```
x = 10:
goto odd;
even:
  if (x == 0) then return(1) else x = x-1; goto odd;
odd:
  if (x == 0) then return(0) else x = x-1; goto even;
```

PC trace is the same!

```
(odd)
```

- (even)
- (odd)
- (even)
- (odd)
- (even)
- (even)
- (odd)
- Why are all these traces the same?
- Control context does not grow when all function calls are in tail position
- This means a function call is the same as a jump

Continuation Passing Interpreter

A Trampolined Interpreter

Interpreter
An Imperative

Interpreter Exceptions

- Important lessons
- If a set of procs call each other using tail-calls we can rewrite them to use assignment instead of an env
- REMEMBER: Values in one function call do not need to be remembered after another call is made because all calls are tail calls (no delayed operations)
- The assignment-based program can be rewritten using GOTOs and labels
- We need to identify which procedures need to communicate values
- Use registers to hold those values
- Write an imperative interpreter

Part V: Continuation-Passing Interpreters

# Marco T. Morazán

Continuation Passing

A Trampoline Interpreter

An Imperative Interpreter

Throads

- Let's start with out continuation-passing interpreter (not the trampolined interpreter)
- Functions that need to share values via registers:
  - (value-of/k exp env cont)
  - (apply-cont cont val)
  - (apply-procedure/k proc1 val cont)
  - (eval-rands/k rands env cont)
    - (create-let-lenv vars vals env cont)
    - (mk-letrec-env/k names params bodies env cont)
- How many registers (i.e., state variables) do we need?
- 11 registers given all calls are tail calls
  - exp
  - env
  - cont
  - val
  - proc1
  - rands
  - rand
  - vars
  - vals
  - letrec-names
  - letrec-params
  - letrec-bodies



Continuation Passing Interpreter

A Trampolined Interpreter

An Imperative Interpreter

- How do 11 registers help us?
- Replace each function with a zero-argument proc
- A function call stores parameter values in the registers and then calls
- Three possible scenarios:
  - Register is unchanged then do nothing
  - Make sure field names in cases expression do not shadow a register. If so, rename local vars
  - If a register is used twice in a single call then carefully sequence assignments to have the right values in registers and/or use temporary vars
- This process is called registerization
- From here it is easily translatable into an imperative language (e.g. C)

Continuation Passing Interpreter

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Eventions

Threads

• ;;; The registers

```
(define exp
              (void))
              (void))
(define env
(define cont
              (void))
(define val
              (void))
(define proc1 (void))
(define rands (void))
(define vars
              (void))
(define vals
              (void))
(define letrec-names
                       (void))
(define letrec-params (void))
(define letrec-bodies (void))
```

Continuation Passing Interpreter

A Trampolined Interpreter

An Imperative Interpreter

Exceptions

Threads

(set! cont (end-cont))
(value-of/k))))

Continuation Passing

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An Imperative Interpreter

Exceptions

Threads

(apply-cont)))

(set! val (num-val num))

(const-exp (num)

(begin

Continuation Passing Interpreter

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Exceptions

```
;; expression environment continuation -> expval
  (define (value-of/k)
    (cases expression exp
      (true-exp ()
                (apply-cont k (bool-val #t)))
  Becomes
  ;; expression environment continuation -> expval
  (define (value-of/k)
    (cases expression exp
      (true-exp ()
                (begin
                  (set! val (bool-val #t))
                  (apply-cont)))
```

Passing Interpreter

A Trampolined Interpreter

An Imperative Interpreter

Exceptions

Continuation Passing

A Trampoline Interpreter

An Imperative Interpreter

Exceptions

Threads

(apply-cont)))

(set! val (apply-env env var))

(begin

Continuation Passing Interpreter

A Trampoline Interpreter

An Imperative Interpreter

Threads

(set! exp exp1)

(value-of/k)))

(set! cont (zero?-cont cont))

(begin

Continuation Passing Interpreter

A Trampolined Interpreter

An Imperative Interpreter

(set! cont (diff-cont1 exp2 env cont))

(set! exp exp1)

(value-of/k)))

(cases expression exp
(diff-exp (exp1 exp2)
(begin

Continuation Passing

A Trampolined Interpreter

An Imperative Interpreter

```
;; expression environment continuation -> expval
  (define (value-of/k)
    (cases expression exp
      (if-exp (exp1 exp2 exp3)
              (value-of/k exp1 env (if-cont exp2 exp3 env k)))

    Becomes

  ;; expression environment continuation -> expval
  (define (value-of/k)
    (cases expression exp
      (if-exp (exp1 exp2 exp3)
              (begin
                (set! exp exp1)
                 (set! cont (if-cont exp2 exp3 env cont))
```

(value-of/k)))

Continuation Passing Interpreter

A Trampolined Interpreter

An Imperative Interpreter

Exception

---

Becomes

Continuation Passing Interpreter

A Trampolined Interpreter

An Imperative Interpreter

Exceptions

```
;; expression environment continuation -> expval
  (define (value-of/k)
    (cases expression exp
      (call-exp (rator rands)
                (value-of/k rator env (rator-cont rands env k)))
  Becomes
  ;; expression environment continuation -> expval
  (define (value-of/k)
    (cases expression exp
      (call-exp (rator rands)
                (begin
                  (set! exp rator)
                  (set! cont (rator-cont rands env cont))
                  (value-of/k)))
```

Continuation Passing

A Trampolined Interpreter

Interpreter
An Imperative

Interpreter

Threads

(set! letrec-names names)
(set! letrec-params params)
(set! letrec-bodies bodies)

(mk-letrec-env/k)))

(set! cont (letrec-cont letrec-body cont))

Continuation Passing

A Trampoline Interpreter

An Imperative Interpreter

Exception

Thursday

```
(define (mk-letrec-env/k)
  (let* [...]
    (begin
      (for-each (lambda (p)
                  (cases proc p
                     (procedure (p b ve)
                                (vector-set! ve 0 new-env))))
                 (map (lambda (p) (expval2proc p))
                     temp-proc-vals))
      (apply-cont k new-env))))
Becomes
(define (mk-letrec-env/k)
  (let* [...]
    (begin
      (for-each (lambda (p)
                   (cases proc p
                     (procedure (p b ve)
                                (vector-set! ve 0 new-env))))
                 (map (lambda (p) (expval2proc p))
                     temp-proc-vals))
      (begin
        (set! val new-env)
        (apply-cont)))))
```

An Imperative

Interpreter

```
• (define (create-let-lenv)
    (if (empty? vars)
        (apply-cont k env)
        (create-let-lenv (cdr vars)
                          (cdr vals)
                          (extend-env (car vars) (car vals) env)
                          k)
  Becomes
```

```
(define (create-let-lenv)
  (if (empty? vars)
      (begin
        (set! val env)
        (apply-cont))
      (begin
        ;; beware of dependencies between registers
        (set! env (extend-env (car vars) (car vals) env))
        (set! vars (cdr vars))
        (set! vals (cdr vals))
        (create-let-lenv))))
```

An Imperative Interpreter

```
(define (eval-rands/k)
  (if (null? rands)
      (apply-cont k '())
      (value-of/k (car rands)
                  env
                  (eval-rands-cont1 (cdr rands) env k))
Becomes
(define (eval-rands/k)
```

(set! cont (eval-rands-cont1 (cdr rands) env cont))

(if (null? rands) (begin

(begin

(set! val '()) (apply-cont))

(value-of/k)))

(set! exp (car rands))

An Imperative

Interpreter

```
(define (apply-cont)
    (cases continuation cont
      (end-cont () val)
      (zero?-cont (saved-cont)
                  (if (zero? (expval2num val))
                       (apply-cont saved-cont (bool-val #t))
                       (apply-cont cont (bool-val #f))))
  Becomes
  (define (apply-cont)
    (cases continuation cont
      (end-cont () val) ;; no function call, no change
      (zero?-cont (saved-cont)
                   (if (zero? (expval2num val))
                       (begin
                         (set! val (bool-val #t))
                         (set! cont saved-cont)
                         (apply-cont))
                       (begin
                         (set! val (bool-val #f))
                         (set! cont saved-cont)
```

(apply-cont))))

Continuation Passing Interpreter

A Trampolined Interpreter

An Imperative Interpreter

Exceptions

```
• (define (apply-cont)
    (cases continuation cont
      (let1-cont (the-vars body saved-env saved-cont)
       (create-let-leny vars
                         val
                         saved-env
                         (let2-cont body saved-cont)))

    Becomes

  (define (apply-cont)
    (cases continuation cont
      (let1-cont (the-vars body saved-env saved-cont)
        (begin
          (set! vars the-vars)
          (set! vals val) ;; val is the list of evaluated RHSs
          (set! env saved-env)
          (set! cont (let2-cont body saved-cont))
          (create-let-lenv)))
```

Continuation Passing Interpreter

A Trampolined Interpreter

An Imperative Interpreter

Exceptions

```
• (define (apply-cont)
    (cases continuation cont
      (let2-cont (body saved-cont)
                  (value-of/k body val saved-cont))
  Becomes
  (define (apply-cont)
    (cases continuation cont
      (let2-cont (body saved-cont)
                  (begin
                    (set! exp body)
                    (set! env val) ;; val is an env
                    (set! cont saved-cont)
                    (value-of/k)))
```

Continuation Passing

A Trampoline Interpreter

An Imperative

Interpreter

Threads

(define (apply-cont) (cases continuation cont (if-cont (exp2 exp3 saved-env saved-cont) (if (expval2bool val) (value-of/k exp2 saved-env saved-cont) (value-of/k exp3 env saved-cont))) Becomes (define (apply-cont) (cases continuation cont (if-cont (exp2 exp3 saved-env saved-cont) (if (expval2bool val) (begin (set! exp exp2) (set! env saved-env) (set! cont saved-cont) (value-of/k)) (begin (set! exp exp3) (set! cont saved-cont) (value-of/k)))

Continuation Passing Interpreter

A Trampolined Interpreter

An Imperative Interpreter

Eventions

```
• (define (apply-cont)
    (cases continuation cont
      (letrec-cont (letrec-body saved-cont)
                    (value-of/k letrec-body val saved-cont))
  Becomes
  (define (apply-cont)
    (cases continuation cont
      (letrec-cont (letrec-body saved-cont)
                    (begin
                      (set! exp letrec-body)
                      (set! env val) ;; val is an env
                      (set! cont saved-cont)
                      (value-of/k)))
```

Continuation Passing Interpreter

A Trampolined Interpreter

An Imperative Interpreter

Exceptions

```
• (define (apply-cont)
    (cases continuation cont
      (diff-cont1 (exp2 saved-env saved-cont)
        (value-of/k exp2 saved-env (diff-cont2 val saved-cont)))

    Becomes

  (define (apply-cont)
    (cases continuation cont
      (diff-cont1 (exp2 saved-env saved-cont)
                   (begin
                     (set! exp exp2)
                     (set! env saved-env)
                     (set! cont (diff-cont2 val saved-cont))
                     (value-of/k)))
```

Continuation Passing Interpreter

A Trampolined Interpreter

An Imperative Interpreter

Exception

```
(define (apply-cont)
    (cases continuation cont
      (diff-cont2 (val1 saved-cont)
       (apply-cont saved-cont (num-val (- (expval2num val1)
                                           (expval2num val)))))
  Becomes
  (define (apply-cont)
    (cases continuation cont
      (diff-cont2 (val1 saved-cont)
                  (begin
                    (set! cont saved-cont)
                    (set! val (num-val (- (expval2num val1)
                                           (expval2num val))))
                    (apply-cont)))
```

Continuation Passing Interpreter

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Exceptions

Threads

(set! rands saved-rands)
(set! env saved-env)

(eval-rands/k)))

(set! cont (rands-cont val saved-cont))

Continuation Passing Interpreter

Trampoline Interpreter

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Interpreter

Threads

(set! vals val) ;; val is the list of evaluated args

(set! proc1 (expval2proc rator))

(set! cont saved-cont)
(apply-procedure/k)))

Continuation Passing Interpreter

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Thursda

Becomes

```
(define (apply-cont)
  (cases continuation cont

  (eval-rands-cont1 (saved-rands saved-env saved-cont)
     (begin
          (set! rands saved-rands)
          (set! env saved-env)
          (set! cont (eval-rands-cont2 val saved-cont))
          (eval-rands/k)))
```

Continuation Passing Interpreter

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An Imperative Interpreter

Thursday

```
    (define (apply-cont)

    (cases continuation cont
      (eval-rands-cont2 (first-rand saved-cont)
        (apply-cont saved-cont (cons first-rand val))

    Becomes

  (define (apply-cont)
    (cases continuation cont
      (eval-rands-cont2 (first-rand saved-cont)
                         (begin
                           (set! cont saved-cont)
                           (set! val (cons first-rand val))
                           (apply-cont)))
```

Part V: Continuation-Passing Interpreters

> Marco T. Morazán

Continuation Passing Interpreter

Trampoline Interpreter

An Imperative Interpreter

merpreter

- Add mult-exp and add-exp to the imperative interpreter
- 5.29

Continuation Passing Interpreter

Trampolined Interpreter

Exceptions

- Remember exceptions (or throwing errors)?
- Manage ordinary control flow
- Alter the control context
- Continuations may be used for these
- Two new type of expressions in our language
- ullet expression ightarrow try expression catch (identifier) expression
- Evaluate first expression and if it returns normally then its value is the value of the try-expression and the handler expression is ignored
- expression → raise expression
- Evaluate the expression and send that value to the most recent exception handler

Continuation Passing

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An Imperati

Exceptions

Threads

# Syntax

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Exceptions

```
(eval
"let f = proc (n)    ;; function to return n if not 0
        if zero?(n)
        then raise -1
        else n
   in try (f 0) catch (i) -(i, 1)") ;; handler subs 1 from its input
```

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Exceptions

Threads

- ullet expression ightarrow try expression catch (identifier) expression
- Need a continuation for what to do after evaluating the first expression (define-datatype continuation cont? : : (try-cont (var symbol?) (handler-exp expression?); use if abnormal evaluation end
- ullet expression o raise expression

(env environment?)
(cont continuation?))

- Need a continuation for what to do after evaluating the expression
- (define-datatype continuation cont?

```
:
(try-cont
  (var symbol?)
  (handler-exp expression?) ;; use if abnormal evaluation end
  (env environment?)
  (cont cont?))
(raise1-cont (saved-cont cont?))
;; save current cont to find handler (saved in a try-cont)
```

Continuation-Passing Interpreter

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An Imperativ

Exceptions

\_\_\_\_\_

```
(define (value-of/k exp env k)
    (cases expression exp
:
    (try-exp (exp1 var handler)
        (value-of/k exp1 env (try-cont var handler env k)))
(raise-exp (exp1)
    (value-of/k exp1 env (raise1-cont k)))
```

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Exceptions

Throade

Continuation Passing

A Trampoline

An Imperati

Exceptions

Lxceptioi

```
• ;; apply-handler: expval cont → Final Answer
(define (apply-handler val cont)
(cases continuation cont
(try-cont (var handler-exp saved-env saved-cont)
(value-of/k
handler-exp;; evaluate handler
(extend-env var val saved-env);; binding for exception value
saved-cont))
(end-cont () (report-uncaught-exception));; no handler
(else (apply-handler val saved-cont))));; keep searching
```

Part V: Continuation-Passing Interpreters

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Continuation Passing Interpreter

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Exceptions



Continuation Passing Interpreter

Trampoline Interpreter

An Imperation

Exceptions

- One may want to have multiple computations at the same time in the same address space
- Text editor: Spell checker, Back-up, Grammar check, etc.
- Same address space and same process: threads
- Interpreter will simulate the execution of multiple threads
- Each thread is a computation in progress
- Threads communicate through shared memory using assignment

Continuation Passing

A Trampolined Interpreter

Evention

Threads

Big picture (much from your OS course)

Pool of threads

• Each thread: running, runnable, blocked

In our system, only one thread running at a time

• Ready Queue: contains the runnable threads

· Scheduler chooses which thread to run

• Preemptive scheduling (quantum or time slice)

Start with IMPLICIT-REFS Language

spawn: creates a new thread

takes one arg that should evaluate to a proc

When a thread is run an argument is passed to this proc

• Does not run immediately....put in the ready queue

spawn is executed for effect; don't care return value

```
Part V:
Continuation-
   Passing
 Interpreters
  Marco T
  Morazán
Threads
```

```
Non-cooperating threads
letrec
 noisy (1) = if null?(1)
             then 0
             else begin
                    print(car(1));
                    (noisy cdr(1))
                  end
in begin
    spawn(proc (d) (noisy [1, 2, 3, 4, 5]);
    spawn(proc (d) (noisy [6, 7, 8, 9, 10]);
    print(100);
    33
  end
A trace
100
    main
    first thread
2
3
6
    second thread
8
4
    first thread
5
9
    second thread
10
returns 33 (when threads are done)
```

Part V: Continuation-Passing Interpreters Marco T Morazán

Cooperating threads examples

Threads

let buffer = 0 one element buffer shared in let producer = proc (n) input: a buffer element n letrec wait(k) = if zero?(k) then set buffer = n else begin print(-(k,-200)); (wait -(k,1)) end in (wait 5) execute wait loop 5 times ignores input, loops while buffer is 0 printing the timer in let consumer = proc (d) letrec busywait (k) = if zero?(buffer) then begin print(-(k,-100)); (busywait -(k,-1)) end else buffer in (busywait 0) in begin spawn(proc (d) (producer 44)); print(300); (consumer 86) end Trace 300 100 consumer runs for a while 101 205 producer runs for a while 204 203 102 consumer runs for a while 103 202 producer runs for a while 201 104 consumer runs for a while 105 producer sets buffer to 44 and stops consumer returns 44

- Implementation
- Continuation-passing IMPLICIT-REFS: Store + continuations
- Add a scheduler

Continuation
Passing
Interpreter

A Trampolined Interpreter

Exception

- Scheduler
- Internal State
  - Ready queue
  - Final answer value of main thread when done
  - Max time slice max steps a thread can run
  - Time remaining steps left for the running thread
- Scheduler Interface
  - init-scheduler: int → void
  - place-on-ready-queue!: thread  $\rightarrow$  void
  - run-next-thread: () → FinalAnswer, runs next thread or if none returns the final answer
  - set-final-answer!: expval → void
  - time-expired?: ()  $\rightarrow$  Bool
  - decrement-timer!: () → void

Continuation Passing Interpreter

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An Imperati Interpreter

Exception

 ${\sf Threads}$ 

```
    Queue Interface

  (define (empty-queue) '())
  (define null? null?)
  (define (enqueue q val) (append q (list val)))
  (define (dequeue q f) (f (car q) (cdr q)))

    f updates the state of the scheduler and runs the first thread

  State variables (registers)
  (define the-ready-queue
                                'uninitialized)
  (define the-final-answer
                                'uninitialized)
  (define the-max-time-slice 'uninitialized)
  (define the-time-remaining 'uninitialized)
```

Part V: Continuation-Passing Interpreters

# Marco T. Morazán

Continuation Passing

A Trampoline

An Impera

- ...

Threads

Scheduler Implementation

```
:: natnum>0 → void
   :: Purpose: Initialize the scheduler
   (define (initialize-scheduler! ticks)
    (begin
       (set! the-ready-queue (empty-queue))
       (set! the-final-answer 'uninitialized)
       (set! the-max-time-slice ticks)
      (set! the-time-remaining the-max-time-slice)))
:: thread → (void)
   ;; Purpose: Place given thread in the ready queue
   (define (place-on-ready-queue! th)
    (set! the-ready-queue (enqueue the-ready-queue th)))
:: expval → (void)
   ;; Purpose: Set the final answer register
   (define (set-final-answer! val) (set! the-final-answer val))
  :: → Bool
   ;; Purpose: Determine if time slice has ended
   (define (time-expired?) (zero? the-time-remaining))
:: → (void)
   ;; Purpose: Decrement the time slice
   (define (decrement-timer!)
    (set! the-time-remaining (- the-time-remaining 1)))
 ;; → expval
   ;; Purpose: Run the next thread in the rady queue
   (define (run-next-thread)
    (if (empty-queue? the-ready-queue)
        the-final-answer
        (dequeue the-ready-queue
                 (lambda (first-ready-thread other-ready-threads)
                    (set! the-ready-queue other-ready-threads)
                    (set! the-time-remaining the-max-time-slice)
                    (first-ready-thread)))))
```

Continuatio Passing Interpreter

A Trampoline Interpreter

An Imperati

Exceptions

- Threads
- thread = ()  $\rightarrow$  expval
- a procedure with no args that returns an expval

Continuation-Passing

A Trampolined Interpreter

Interprete

Exception

- Interpreter
- IMPLICIT-REFS refactored to be a continuation-passing interpreter (as we did for LETREC)
- (spawn-exp (exp) (value-of/k exp env (spawn-cont k)))
- apply-cont

Continuation Passing Interpreter

A Trampolined Interpreter

Evention

Threads

# Interpreter

- What continuation should each thread be run in?
- Main thread
- · record the value of the final answer
- run any remaining threads
- apply-cont

- Other subthreads
- ignore its value
- runs remaining threads
- apply-cont

```
(end-subthread-cont ()
  (run-next-thread))
```

Continuation Passing

A Trampolined Interpreter

Interpreter

Exception

Threads

- To evaluate a program:
- initialize the store
- initialize the scheduler
- evaluate expression in the end-main-thread-cont

• The wrapper function (eval)
(define TIMESLICE 5)

```
;; string → ExpVal
;; Purpose: Evaluate the given extended LC-program
(define (eval string)
  (value-of-program TIMESLICE (parse string)))
```

Continuation Passing Interpreter

A Trampolined Interpreter

\_

- Applying a continuation
- If time has expired then place thread on ready queue interrupting the continuation application and run the next thread
- If time has not expired then decrement the timer and apply the given continuation to the given value

```
(eval "let x = 0
   Part V:
                                      in let mut = mutex()
Continuation-
                                         in let incr_x = proc (id) proc (dummy)
   Passing
                                                                      begin set x = -(x, -1):
 Interpreters
                                                                            print(x)
                                                                      end
  Marco T
                                             in begin spawn((incr_x 100));
  Morazán
                                                      spawn((incr_x 200));
                                                      spawn((incr_x 300))
                                                end")
                      • What is the value of x when the program ends?
                         set x = -(x, -1);
                               LDR1 x
                               I.DR2 -1
                               SUR
                               SET X R3

    Trace

                               T1 runs and sets x to 1
                               T2 runs and sets x to 2
                               T3 runs and sets x to 3
                         x is 3 after all threads run

    Trace

Threads
                               T1 LDR1 x Loads 0 as the value of x
                                  I.DR2 -1
                                  T1 is interrupted
                                            Loads 0 as the value of x
                               T2 I.DR1 x
                                  LDR2 -1
                                  SUB
                                  SET X R2 mutates x to 1
                               T2 LDR1 x
                                            Loads 1 as the value of x
                                  I.DR2 -1
                                  SUB
                                  SET X R3 mutates x to 2
                               T1 Restores 0 to R1 and -1 to R2
                                  SUB
                                  SET X R3 mutates x to 1
```

v is 1 after all threads run

Shared variables for communication are dangerous: assignment > < 🗗 > < 📱 > < 📱 >

Passing Interpreter

A Trampolined Interpreter

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Threads

# • How do we avoid such interferences between processes?

- Synchronization mechanism is needed
- Binary semaphore or mutex: used to control access to shared variables and avoid busy waiting
- Mutex
  - is open or closed
  - has a queue of threads waiting for the mutex to become open

Continuation
Passing
Interpreter

A Trampoline Interpreter

Exception

Threads

Mutex interface

mutex

no args

creates an open mutex

wait

one argument

used to indicate access to a mutex

ullet open mutex o mutex becomes closed and thread runs

closed mutex → thread put in the mutex's queue

returns void

signal

• single mutex argument

used to release a mutex

mutex closed and empty queue → mutex open and thread continues

 mutex closed and non-empty queue → one thread put in ready queue, queue remains closed, and thread continues executing

returns no value

Mutex guarantees

 only one thread has access to shared vars between wait and signal calls

 region where shared vars are accessed is called a critical region/section

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Interpreter

Evention

```
(eval
   "let x = 0
    in let mut = mutex()
       in let incr_x =
                proc (id)
                  proc (dummy)
                    begin
                      wait(mut);
                      set x = -(x, -1); critical section
                      print(x);
                      signal(mut)
                    end
          in begin
               spawn((incr_x 100));
               spawn((incr_x 200));
               spawn((incr_x 300))
             end")
```

```
Part V:
Continuation-
Passing
Interpreters
```

Continuation Passing Interpreter

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An Imperat Interpreter

Exception

Threads

Implementation

```
(define-datatype mutex mutex?
    (a-mutex
     (ref-to-closed? reference?) ;; ref to bool closed or open
     (ref-to-wait-queue reference?))) ;; ref to (listof thread)

    Mutexes are expressed values

  (define-datatype expval expval?
    (num-val
     (value number?))
    (bool-val
     (boolean boolean?))
    (proc-val
     (proc proc?))
    (mutex-val
     (mutex mutex?)))
  (define expval2mutex
    (lambda (v)
      (cases expval v
        (mutex-val (m) m)
        (else (expval-extractor-error 'mutex v)))))
  In value-of/k
  (mutex-exp () (apply-cont k (mutex-val (new-mutex))))
  (define (new-mutex) (a-mutex (newref #f) (newref '())))
```

Continuation Passing Interpreter

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Interpreter

Exceptions

```
wait
  In value-of/k
  (wait-exp (exp) (value-of/k exp env (wait-cont k)))

    In apply-cont

  (wait-cont (saved-cont)
    (wait-for-mutex
      (expval2mutex val)
      (lambda () (apply-cont saved-cont (num-val 52)))))
signal

    In value-of/k

  (signal-exp (exp) (value-of/k exp env (signal-cont k)))

    In apply-cont

  (signal-cont (saved-cont)
    (signal-mutex (expval2mutex val)
                   (lambda ()
                     (apply-cont saved-cont (num-val 53)))))
```

Continuation Passing

A Trampoline Interpreter

Interpreter

Exception

Continuation Passing

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Exception

```
;; mutex thread → expval
  ;; Purpose: To signal given mutex and run a waiting thread if any
  (define (signal-mutex m th)
   (cases mutex m
    (a-mutex (ref-to-closed? ref-to-wait-queue)
     (let [(closed? (deref ref-to-closed?))
           (wait-queue (deref ref-to-wait-queue))]
      (if closed?
          (begin
           (if (empty? wait-queue)
               (setref! ref-to-closed? #f)
               (dequeue
                 wait-queue
                 (lambda (first-waiting-th other-waiting-ths)
                  (begin
                   (place-on-ready-queue! first-waiting-th)
                   (setref! ref-to-wait-queue other-waiting-ths)))))
           (th)) ;;error in book: Page 190, Fig 5.22
          (th))))))
```

Part V: Continuation-Passing Interpreters

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Passing Interpreter

A Trampoline Interpreter

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Eventions

Threads

• 5.45, 5.47, 5.58 (outline the algorithm!)